

MIS-64018-004 Assign_Module_2 The LP Model

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1. Back Savers Production Tradeoff Problem

- a. The decision variables are: X_1 as the number of Collegiate backpack produced and X_2 as the number of the Mini backpack produced.
- b. The objective function is to maximize the total profit from the backpack production as
Max Profit = $32X_1 + 24X_2$
- c. There are three constraints as the following:
 - Total nylon available per week: $3X_1 + 2X_2 \leq 5,000$
 - Total hours available from all labor per week: $45/60X_1 + 40/60X_2 \leq 35 \text{ laborers} \times 40 \text{ hours/labor/week}$
 - Total sold per week: $X_1 \leq 1,000$, $X_2 \leq 1,200$
- d. Full mathematical formulation
Max Profit = $32X_1 + 24X_2$
Subject to
 $3X_1 + 2X_2 \leq 5,000$
 $45/60X_1 + 40/60X_2 \leq 35 \times 40$
 $X_1 \leq 1,000$, $X_2 \leq 1,200$

2. The Weigelt Corp. Capacity Allocation Problem

- a. Decision variables:
 - L_1 : number of units of large products produced in Plant 1
 - L_2 : number of units of large products produced in Plant 2
 - L_3 : number of units of large products produced in Plant 3
 - M_1 : number of units of medium products produced in Plant 1
 - M_2 : number of units of medium products produced in Plant 2
 - M_3 : number of units of medium products produced in Plant 3
 - S_1 : number of units of small products produced in Plant 1
 - S_2 : number of units of small products produced in Plant 2
 - S_3 : number of units of small products produced in Plant 3

b. LP model:

The objective function is to max profit

$$\text{Max } Z = 420 \times (L_1 + L_2 + L_3) + 360 \times (M_1 + M_2 + M_3) + 300 \times (S_1 + S_2 + S_3)$$

Subject to:

Capacity constraint:

$$L_1 + M_1 + S_1 \leq 750$$

$$L_2 + M_2 + S_2 \leq 900$$

$$L_3 + M_3 + S_3 \leq 450$$

Storage constraint:

$$20 * L_1 + 15 * M_1 + 12 * S_1 \leq 13,000$$

$$20 * L_2 + 15 * M_2 + 12 * S_2 \leq 12,000$$

$$20 * L_3 + 15 * M_3 + 12 * S_3 \leq 5,000$$

Sale constraint:

$$L_1 + L_2 + L_3 \geq 900$$

$$M_1 + M_2 + M_3 \geq 1,200$$

$$S_1 + S_2 + S_3 \geq 750$$

Same percentage in excess capacity production:

$$(L_1 + M_1 + S_1) : (L_2 + M_2 + S_2) : (L_3 + M_3 + S_3) = 750 : 900 : 450$$

Non-negativity:

$$L_1, L_2, L_3, M_1, M_2, M_3, S_1, S_2, S_3 \geq 0$$