







Article

The globular cluster system of the Auriga simulations

Q1: [Copyeditor to Author]
[Permissions: Permission to reproduce any third party material in your paper should have been obtained prior to acceptance. If your paper contains figures or text that require permission to reproduce, please confirm that you have obtained all relevant permissions and that the correct permission text has been used as required by the copyright holders.]

Please contact
jnls.author.support@oup.com if you have any questions regarding permissions.] **Q2: [Copyeditor to Author]**
[Please ensure that all queries are answered, as otherwise publication will be delayed as we will be unable to complete the next stage of the production process. Please note that proofs will not be sent back for further editing.]

Timo L. R. Halbesma^{1,★} , Robert J. J. Grand¹ , Facundo A. Gómez^{2,3}, Federico Marinacci⁴ , Rüdiger Pakmor¹ , Wilma H. Trick¹, Philipp Busch¹  and Simon D. M. White¹ 

¹Max-Planck-Institut für Astrophysik, Karl-Schwarzschild-Str. 1, [D-85741 Garching, Germany](#)

Q3: [Copyeditor to Author][To check that we have your surnames correctly identified and tagged (e.g. for indexing), we have coloured green the names that we have assumed are surnames. If any of these are wrong, please let us know so that we can amend the tagging.])

²Instituto de Investigación Multidisciplinar en Ciencia y Tecnología, Universidad de La Serena, Raúl Bitrán 1305, La Serena, [Chile](#)

³Departamento de Física y Astronomía, Universidad de La Serena, Av. Juan Cisternas 1200 N, La Serena, [Chile](#)

⁴Department of Physics ~~and~~ Astronomy, University of Bologna, via Gobetti 93/2, [I-40129 Bologna, Italy](#)

★E-mail: halbesma@mpa-garching.mpg.de **Q4:** [Copyeditor to Author][Please supply email addresses for between one and three authors who are willing to correspond with readers and for their email address to be included in the article.])

Accepted: [2020 May 15](#); Revised: [2020 May 14](#); Received: [2019 September 05](#)

ABSTRACT

We investigate whether the **Q5:** [Copy Editor Aptara to Author] Please note that it is journal style to refer to ‘our’ Galaxy with a capital ‘G’ (e.g. in case of Galaxy, Galactic Centre or Galactocentric) and to other galaxies with a lowercase ‘g’. Please check that all the notations in this paper are correct.] galaxy and star formation model used for the Auriga simulations can produce a realistic globular cluster (GC) population. We compare statistics of GC candidate star particles in the Auriga haloes with catalogues of the Milky Way (MW) and Andromeda (M31) GC populations. We find that the Auriga simulations do produce sufficient stellar mass for GC candidates at radii and metallicities that are typical for the MW GC system (GCS). We also find varying ~~mass ratios~~ ~~mass ratios~~ of the simulated GC candidates relative to the observed mass in the MW and M31 ~~GC systems~~ ~~GCSs~~ for different bins of galactocentric ~~radius-metallicity~~ ~~radius metallicity~~ (r_{gal} — $[\text{Fe}/\text{H}]$). Overall, the Auriga simulations produce GC candidates with higher metallicities than the MW and M31 GCS and they are found at larger radii than observed. The Auriga simulations would require bound cluster formation efficiencies higher than ~~ten~~ ~~10~~ per cent for the metal-poor GC candidates, and those within the Solar radius should experience negligible destruction rates to be consistent with observations. GC candidates in the outer halo, on the other hand, should either have low formation

efficiencies, or experience high ~~mass-loss-mass-loss~~ for the Auriga simulations to produce a GCS that is consistent with that of the MW or M31. Finally, the scatter in the metallicity as well as in the radial distribution between different Auriga runs is considerably smaller than the differences between that of the MW and M31 GCSs. The Auriga model is unlikely to give rise to a GCS that can be consistent with both galaxies. **Q6:** [Copyeditor to Author][If you refer to any data bases in your paper, please note the journal policy for properly crediting those responsible for compiling the data base. Rather than citing only a URL, if at all possible please also cite a reference (and include it in the reference list), or if a reference is not available then the names of those who compiled the data base. Note that some data bases do provide guidelines on how they should be cited - please check for these and follow them in your paper where appropriate.]]

Key words:

galaxies: formation; galaxies: star clusters: general **Q7:** [Copyeditor to Author][The MNRAS list of approved key words has been revised and updated. The new list is appended to these proofs. If you had previously selected key words from the old list, please now check them carefully against the new list in case they need to be changed, or there are new ones that you would like to add. If you had not previously selected key words from the MNRAS approved list, please now choose up to six from the new list.]]

1 INTRODUCTION

Globular star clusters (~~GCs~~~~GCSs~~) are old, bright, and ubiquitous. Various properties of GC systems (~~GCS~~~~GCSs~~) show correlations with their host galaxies. GCSs are believed to retain information about the galactic (gas) conditions at their times of formation. Thus they could offer a unique insight into the (chemodynamical) evolution of their parent galaxies, if the formation and evolution of GCs ~~and GC systems~~ ~~GCSs~~ themselves is adequately understood. However, despite decades of research (e.g. Harris 1991; ~~Harris~~, 2001; West et al. 2004; Brodie & Strader 2006; Gratton, Carretta & Bragaglia 2012; Kruijssen 2014; Forbes et al. 2018), consensus on an exhaustive picture of the formation of GCs is yet to be reached. Most galaxies host a GCS with a bimodal colour distribution that may reflect a bimodal metallicity distribution, which is argued to arise from two distinct formation channels (Brodie & Strader 2006). GCs are typically referred to as ‘blue’ or ‘red’ (e.g. Zinn 1985; Gebhardt & Kissler-Patig 1999; Larsen et al. 2001) where the former class is more metal-poor, more radially extended, and showing little to no rotation, whereas the latter is more metal-rich, radially concentrated, and rotating with the galaxy.

The literature offers a wealth of formation scenarios, many of which focus on the distinct characteristics of the blue or red subpopulation. Peebles & Dicke (1968) and Peebles (1984) argue that GCs form as the earliest bound structures in the Universe **Q8:** [Copy Editor Aptara to Author] Please note that it is journal style to refer to ‘our’ Universe with a capital ‘U’ and to model universes with a lowercase ‘u’. Please check that all the notations in this paper are correct. (i.e. prior to formation of the main galaxy), noting that

the Jeans length and mass shortly after recombination is consistent with typical GC masses and sizes. Diemand, Madau & Moore (2005) and Boley et al. (2009) argue that the blue, metal-poor GCs ($[\text{Fe}/\text{H}] < -1$) form in radially biased dark matter (DM) haloes at high redshift. Other recent hypotheses of GC formation prior to collapse of the proto-galaxy include formation in colliding supershells (Recchi et al. 2017), in supersonically induced gaseous objects (Chiou et al. 2019), or in high-speed collisions of ~~dark matter-DM~~ subhaloes (Madau et al. 2019). Boylan-Kolchin (2017) suggests that (the blue subpopulation of) GCs could form in ~~high-density-high-density~~ regions along the cosmic filament before or during collapse.

Other models also date GCs formation during formation of the proto-galaxy itself, for example, as a result of thermal instabilities in hot gas-rich haloes (Fall & Rees 1985, also see the discussions in Kang et al. 1990). Alternative formation triggers are also explored, such as (other causes of) shock compression, or ~~cloud-cloud-cloud-cloud~~ collisions (e.g. Gunn 1980; Murray & Lin 1992; Harris & Pudritz 1994; Vietri & Pesce 1995; Larson 1996; Cen 2001).

Yet another hypothesis is that star cluster formation traces periods of high-intensity star formation, which can be triggered by major gas-rich (spiral) galaxy mergers (Schweizer 1987; Ashman & Zepf 1992). Such a scenario is naturally expected within the framework of hierarchical assembly and predicts formation of young clusters in interacting and merging galaxies, which has been observed and are found to show remarkable similarities with GCs in the Milky Way (~~-MW~~) (~~e.g. MW~~; e.g. Whitmore & Schweizer 1995; Holtzman et al. 1996; ~~Zepf-Whitmore~~ et al. 1999; ~~Whitmore-Zepf~~ et al. 1999). Moreover, modelling efforts of this framework yield GC (sub)populations consistent with various observables (e.g. Muratov & Gnedin 2010; Choksi, Gnedin & Li 2018), and the recent numerical simulation of an isolated ~~dwarf-dwarf-dwarf-dwarf~~ merger executed at very high resolution (baryonic mass $m_b \sim 4 M_\odot$; softening $\epsilon = 0.1$ pc) produces star clusters that could be GC progenitors (Lahén et al. 2019).

As for the formation timeline, the scenarios (and flavours thereof) of Fall & Rees (1985) and Ashman & Zepf (1992) are intertwined because accretion and mergers continually occur during the hierarchical build-up of galaxies. Various (other) hierarchical formation channels thus combine different aspects of the aforementioned paradigms, such as GC formation in (small) galactic ~~disks-discs~~ before they are accreted on to an assembling galaxy (e.g. Côté et al. 2000; Beasley et al. 2002; Côté, West & Marzke 2002; ~~Beasley et al. 2002~~; Gnedin 2003). We refer to Gnedin, Lahav & Rees (2001) for a scoreboard of GC formation models compared to observations of the MW GCSs.

An idea that has recently been studied extensively is the hypothesis that the formation mechanisms of young massive clusters (~~-YMCs, YMCs~~; see Portegies Zwart, McMillan & Gieles 2010, for a review) and GCs are the same. The proximity of YMCs in the local Universe allows to study these processes with a level of detail that cannot be achieved for GCs at high redshifts. In this framework, differences between the two classes of objects are caused by nearly a Hubble time of (dynamical) evolution (e.g. Spitzer 1987). This picture is based on observed similarities between YMCs and GCs (e.g. Holtzman et al. 1992; Whitmore et al. 1999) and strengthened by observations of gravitationally lensed objects at high redshifts ($z = 2$ —6). These sources have properties reminiscent of (local) YMCs and may be GC progenitors at times of formation (~~-Vanzella-Johnson~~ et al. 2017; ~~Johnson-Vanzella~~ et al. 2017). The modelling work

by Kruijssen et al. (2011), Kruijssen et al. (2012), and Kruijssen (2015) is now incorporated into cosmological zoom simulations and shows promising results (Pfeffer et al. 2018; Kruijssen et al. 2019).

The (mass) resolution of cosmological zoom simulations has reached the mass range populated by GCs, and the gravitational force softening can be as low as several parsec. A number of groups can thus incorporate formation of (globular) star clusters into their high-resolution hydrodynamical simulations. Ricotti, Parry & Gnedin (2016) ran ~~parsec-scale~~ parsec-scale simulations of the high-redshift universe prior to reionization (the simulations stop at $z = 9$), Li et al. (2017) implement a new subgrid model for star (cluster) formation and run simulations that reach $z = 3.3$, and the run of Renaud, Agertz & Gieles (2017) reaches $z = 0.5$. Kim et al. (2018) find that mergers can push gas to high density ~~that, which~~ quickly forms clustered stars that end up tightly bound by the end of the simulation. A somewhat different approach couples semi-analytical models to DM-only simulations (Muratov & Gnedin 2010; Li & Gnedin 2014; Choksi et al. 2018; Choksi & Gnedin 2019b, a2019a,b), also done in the work by El-Badry et al. (2019).

In this work, we use ~~state-of-the-art~~ state-of-the-art simulations that produce realistic spiral galaxies (MW analogues) at redshift zero for which several global properties are consistent with the observations. The question thus naturally arises whether the star formation histories of the simulations could give rise to a GCS similar to the MW and/or Andromeda (M31) GCSs. In particular, we use the Auriga simulations (Grand et al. 2017, hereafter G17), further described in Section 2. We investigate whether the star formation model implemented produces metallicity, radial, and ~~metallicity-radial~~ metallicity-radial distributions that are consistent with the MW and/or M31 GCSs, and whether the model produces enough stellar mass with the right properties. Moreover, the simulations provide us with the history of the star particles, which allows us to investigate the differences between these properties for ~~sub-populations~~ subpopulations that have formed *in situ* versus those that have been accreted. We focus on the metallicity and radial distributions because observations of the red and blue GCs show distinct differences between these properties.

The plan of ~~the this~~ paper is as follows. We ~~summarise~~ summarize the relevant characteristics of the Auriga simulations in Section 2, followed by a summary of the observations of the MW and M31 GCSs in Section 3 that we compare our simulations to in Section 4. We discuss our findings in Section 5 to come to our conclusions in Section 6.

2 THE AURIGA SIMULATIONS

We use the Auriga simulations (G17), a suite of high-resolution cosmological zoom simulations of MW analogues. The MW-mass selected initial conditions in the range ~~1–2–(1–2)~~ $\times 10^{12} M_{\odot}$ were selected from the EAGLE DM-only box; see G17 for details. The simulations are performed with the Q9: [Copy Editor Aptara to Author] Please note that computer software/programming languages must be styled in {\sc small capital letters}, according to journal style. Please check and correct this paper accordingly. AREPO code (Springel 2010; Pakmor et al. 2016) that solves the magnetohydrodynamical equations on a moving mesh.

The galaxy formation model includes primordial and metal-line cooling with self-shielding corrections. Reionization is completed at redshift 6 by a time-varying spatially uniform ~~UV~~ ultraviolet background (Faucher-Giguère et al. 2009; Vogelsberger et al. 2013). The interstellar medium (ISM) is

described by an equation of state for a two-phase medium in pressure equilibrium (Springel & Hernquist 2003): cold clouds embedded in a hot ambient medium, whose mass and energy densities are described by processes important for star formation, such as the condensation of cold clouds and the photoevaporation of clouds. Stars form stochastically in thermally unstable gas with a density threshold of $n = 0.13 \text{ cm}^{-3}$, and consecutive stellar evolution is accounted for. The channel for energetic stellar feedback is from non-local ~~type~~ Type II supernovae (~~SN~~ SNe II), which is modelled with wind particles (Marinacci, Pakmor & Springel 2014–; G17). Galactic winds enrich the ISM with metals from ~~SNII~~ SNIa, ~~SNII~~ SNIa, and asymptotic giant branch stars (Vogelsberger et al. 2013). Supermassive black holes grow via ~~Bondi–Hoyle–Lyttleton~~ Bondi–Hoyle–Lyttleton accretion (Bondi & Hoyle 1944; Bondi 1952), and feedback from the active galactic nuclei has a low-accretion and high-accretion mode (radio and quasar) (Springel, Di Matteo & Hernquist 2005; Marinacci et al. 2014–; G17). Finally, the simulations follow the evolution of a magnetic field of 10^{-14} (comoving) G seeded at $z = 127$ (Pakmor & Springel 2013; Pakmor, Marinacci & Springel 2014).

This model was tailored to the AREPO code and calibrated to reproduce key observables of galaxies, such as the history of the cosmic star formation rate density, the stellar mass to halo mass relation, and galaxy luminosity functions. The galaxy formation model produces realistic spiral galaxies at redshift zero that match observations such as sizes, morphologies (G17), ~~HH~~ H I disc properties (Marinacci et al. 2017), and the diversity of accreted stellar halo properties (Monachesi et al. 2019). Furthermore, the simulations are able to reproduce major Galactic components, such as the chemical thin/thick disc dichotomy (Grand et al. 2018) and the recently discovered *Gaia* Sausage (Fattahi et al. 2019). They are thus a large set of detailed simulations similar enough to the Galaxy to make predictions for the GC population properties of the MW and M31.

The Auriga suite has a fiducial baryonic mass resolution $m_b = 5 \times 10^4 M_\odot$, with gravitational softening of collisionless particles $\epsilon = 369 \text{ pc}$. Simulations at this resolution are referred to as level 4 (L4). Selected initial condition runs are ~~accompanied~~ accompanied by the lower (higher) resolution level L5 (L3). The resolution for these levels is $m_b = 4 \times 10^5 M_\odot$ with $\epsilon = 738 \text{ pc}$, and $m_b = 6 \times 10^3 M_\odot$ with $\epsilon = 184 \text{ pc}$, respectively. The mass resolution of the Auriga simulations is thus close, i.e. $10^5 M_\odot$, to the characteristic peak mass of the lognormal GC mass distribution (Harris 1991), although the gravitational softening is two orders of magnitudes larger than typical GC radii of several parsec. High-density gaseous regions are thus not expected to produce surviving stellar clumps with masses and radii consistent with GCs because such objects would numerically disperse, even in the ~~highest-resolution~~ highest resolution runs. On the other hand, we can investigate (statistical) properties of age-selected GC candidates because each star particle represents a single stellar population with a total mass that could be consistent with one GC. This means that their formation sites could be consistent with those of real-world GCs.

3 OBSERVATIONAL DATA

We describe observations of the MW GCS in Section 3.1 for these clusters, and of the M31 GCS in Section 3.2. We discuss ~~age estimates~~ age estimates in Section 3.3, their distribution of galactocentric radius in Section 3.4, and their total mass in ~~2D~~ two-dimensional bins of metallicity-galactocentric radius

in Section 3.5. We focus on both metallicity and galactocentric radius because these data are available in the observations and in the Auriga simulations.

3.1 Milky Way

Harris (1996, 2010 edition; hereafter H96e10) provides a catalogue¹ of the MW GCS that contains properties of 157 GCs. The authors initially estimated the number of GCs in the MW GCS to be 180 ± 10 , thus, their catalogue to be ~ 85 per cent complete. However, an additional 59 GC candidates have been discovered more recently by various authors. The total number of GCs in the MW might thus be 216 with recent estimates now anticipating an additional 30 GCs yet to be discovered (e.g. Ryu & Lee 2018, and references therein). We still use data from the Harris catalogue, but caution that it may (only) be ~~50~~ 70 per cent complete. Specifically, the relevant data fields that we use from H96e10 are the metallicity [Fe/H], the Galactic distance components X , Y , and Z (in kpc),² and absolute magnitude in the V band, M_V . We use the V -band magnitude to calculate ~~mass-estimates~~ mass estimates by assuming $M_{V,\odot} = 4.83$ and a ~~mass-to-light~~ mass-to-light ratio $M/L_V = 1.7 M_\odot/L_\odot$, the mean for MW clusters (McLaughlin & van der Marel 2005). We supplement the catalogue with ~~age-estimates~~ age estimates from isochrone fits to stars near the main-sequence turnoff in 55 GCs (VandenBerg et al. 2013, hereafter V13).

3.2 Andromeda

Caldwell et al. (2011, hereafter C11) and Caldwell & ~~Romano-wsky~~ Romanowsky (2016, hereafter CR16) present a uniform set of spectroscopic observations of the inner ~~4.6°-1.6°~~ 4.6°-1.6° (~ 21) kpc of M31 that is believed to be 94 per cent complete. In addition, the outer stellar halo of M31 up to $r_{\text{proj}} \sim 150$ kpc is observed in the Pan-Andromeda Archaeological Survey (~~PAndAS~~, PAndAS; Huxor et al. 2014, hereafter H14; Veljanoski et al. 2014; Mackey et al. 2019, hereafter H14). In fact, the work of H14 is incorporated in the latest public release³ of the C11 and CR16 data sets. Therefore, we use the latest data set of CR16 because it is the most recent aggregated ~~dataset~~ data set of M31's GCS that contains GCs in the inner region and in the outer halo. The relevant fields in the CR16 ~~dataset~~ data set that we use are the age, metallicity, and the ~~mass-estimate~~ mass estimate.⁴ We calculate the galactocentric radii from the observed positions RA and ~~DEC~~ Dec., as further discussed in Section 3.4.

3.3 ~~Age-estimates~~ Age estimates

The top panel of Fig. 1 shows a histogram of the ~~age-estimates~~ age estimates of the 55 MW GCs in V13 and 88 GCs in M31 for which ~~age-estimates~~ age estimates are available in CR16. The mean age of the MW GCs in this data set is 11.9 Gyr and the standard deviation is 0.8 Gyr. Furthermore, only 1 of the 55 GC ~~age-estimates~~ age estimates is below 10 Gyr. The M31 GCS has a mean age of 11.0 Gyr with a standard deviation of 2.2 Gyr, and 24 GCs have ~~age-estimates~~ age estimates below 10 Gyr with a minimum age of 4.8 Gyr. Based on these data, we find that the age distributions of the MW and M31 GCSs are not statistically consistent. The MW appears to host a GCS that is somewhat older than that of M31. This is somewhat surprising, given that M31 is generally considered to be earlier type than the MW so that an older stellar population would naively be expected. On the other hand, the MW could be an outlier as it may have formed and assembled most of its mass earlier than galaxies with a similar mass (e.g. Snaith et al. 2014, 2015; Mackereth et al. 2018). In addition, we caution that both data sets are

incomplete and the age measurements have large uncertainties (of 1–2 Gyr). On the other hand, the magnitude of the uncertainty is insufficient to explain the low-age tail in M31.

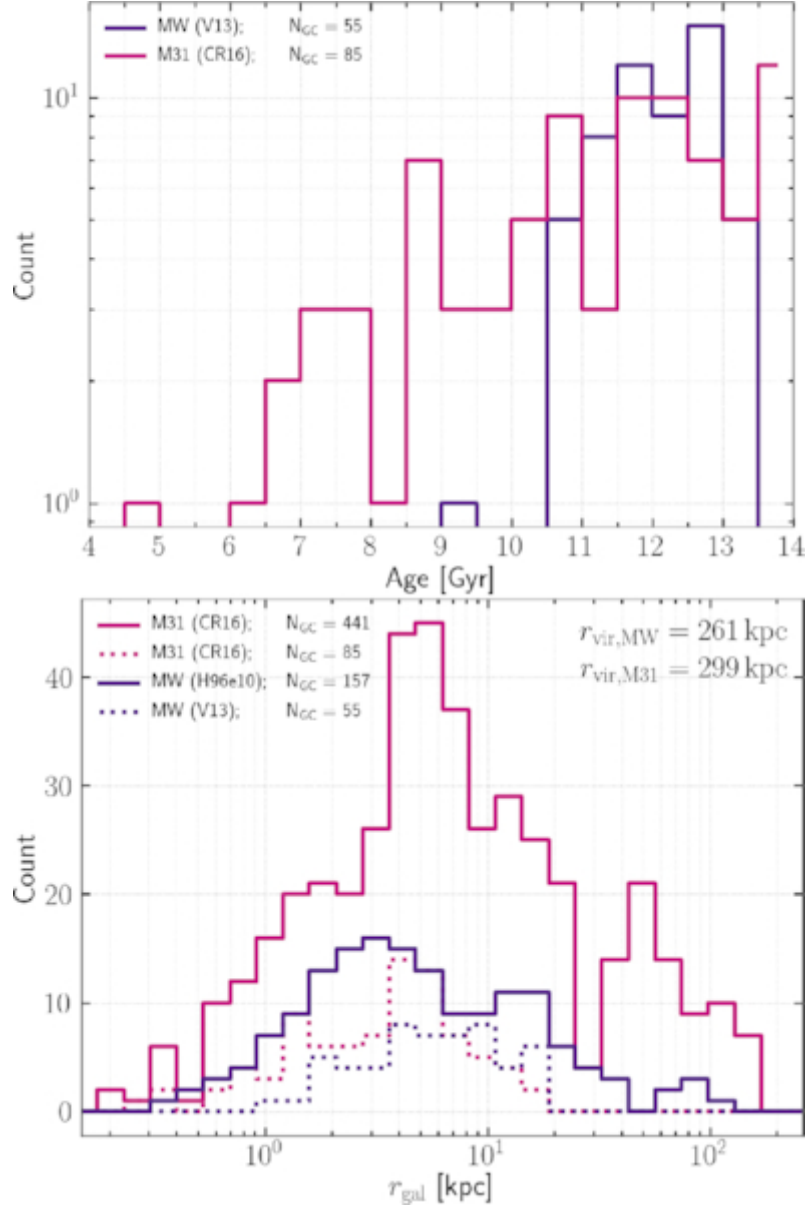


Figure 1. Top panel: Age-age distribution of 55 GCs in the MW (data from VandenBerg et al. 2013) and 88 GCs in M31 (data from Caldwell & Romanowsky 2016). Bottom panel: Distribution distribution of galactocentric radius in the MW and M31. The dotted lines show the subset of data that also have age measurements (i.e. the same sample as in the top panel). We divide the radii of M31 by $r_{\text{vir, M31}} = 299$ kpc and multiply by $r_{\text{vir, MW}} = 261$ kpc (Patel et al. 2017) to compensate for the different intrinsic sizes of both galaxies. Q10: [Copyeditor to Author][Please check the figures in the PDF proof carefully.]

3.4 Radial distribution

The bottom panel of Fig. 1 shows the radial distribution of the MW and M31 GCS. We divide the radii of M31 by its virial radius⁵ $r_{\text{vir, M31}} = 299$ kpc and multiply by $r_{\text{vir, MW}} = 261$ kpc to account for the different intrinsic sizes of the two galaxies, adopting the values and cosmology from Patel, Besla & Sohn (2017). Values for r_{gal} are readily available in H96e10 (assuming $r_{\odot} = 8.0$ kpc), but the galactocentric radius of GCs in M31 is not available in CR16. Therefore, we follow Wang, Ma & Liu (2019, section 4.1) to calculate the projected radius r_{proj} from the observed positions, adopting M31’s central

position from the NASA Extragalactic Database ~~$(\alpha_0, \delta_0) = (0^{\text{h}}42^{\text{m}}44.35^{\text{s}}, +41^{\circ}16'08.63'')$~~ ⁶
 ~~$(\alpha_0, \delta_0) = (0^{\text{h}}42^{\text{m}}44.35, +41^{\circ}16'08.63)$~~ and the distance $D_{\text{M31}} = 780$ kpc (McConnachie et al. 2005; Conn
 et al. 2012). We estimate r_{gal} as ‘average deprojected distance’ $r_{\text{gal}} = r_{\text{proj}} \times (4/\pi)$.

The solid lines show the distributions using all available data (because the sky coordinates are known for each GC), while the subset for which ~~age-estimates~~ age estimates are available is indicated using dotted lines. The latter shows a narrower range of radii than the full data set: it appears that few ~~age-estimates~~ age estimates are available for the innermost (<1 kpc) GCs, and none for those beyond roughly 20 kpc (the halo GCs). We compare the two distributions of the full data set (solid lines) and find that the MW has more GCs in the range 1–4 kpc than M31 when accounting for the larger number of total GCs in M31. Interestingly, the two distributions show a similar trend for $r_{\text{gal}} > 4$ kpc and host a subpopulation of halo GCs. Our naive expectation would be that the spiral galaxies in the Local Group host similar ~~GC systems~~ GCSs. However, based on a two-sample KS test, we find that the radial distributions of the GCS of the MW and M31 are not statistically consistent with being drawn from the same underlying distribution due to substantial differences at intermediate radii.

3.5 Total GC mass in ~~metallicity-radius~~ the metallicity-radius space

We show the two-dimensional mass-weighted ~~metallicity-radius~~ metallicity-radius distribution of the MW and the M31 GCS in the top and bottom panel of Fig. 2, respectively. Note that the number of GCs is different than in Fig. 1 because here we plot $[\text{Fe}/\text{H}]$ between -2.5 and 0 and r_{gal} between 1 and 250 kpc, whereas Fig. 1 shows the full range of metallicities and radii.

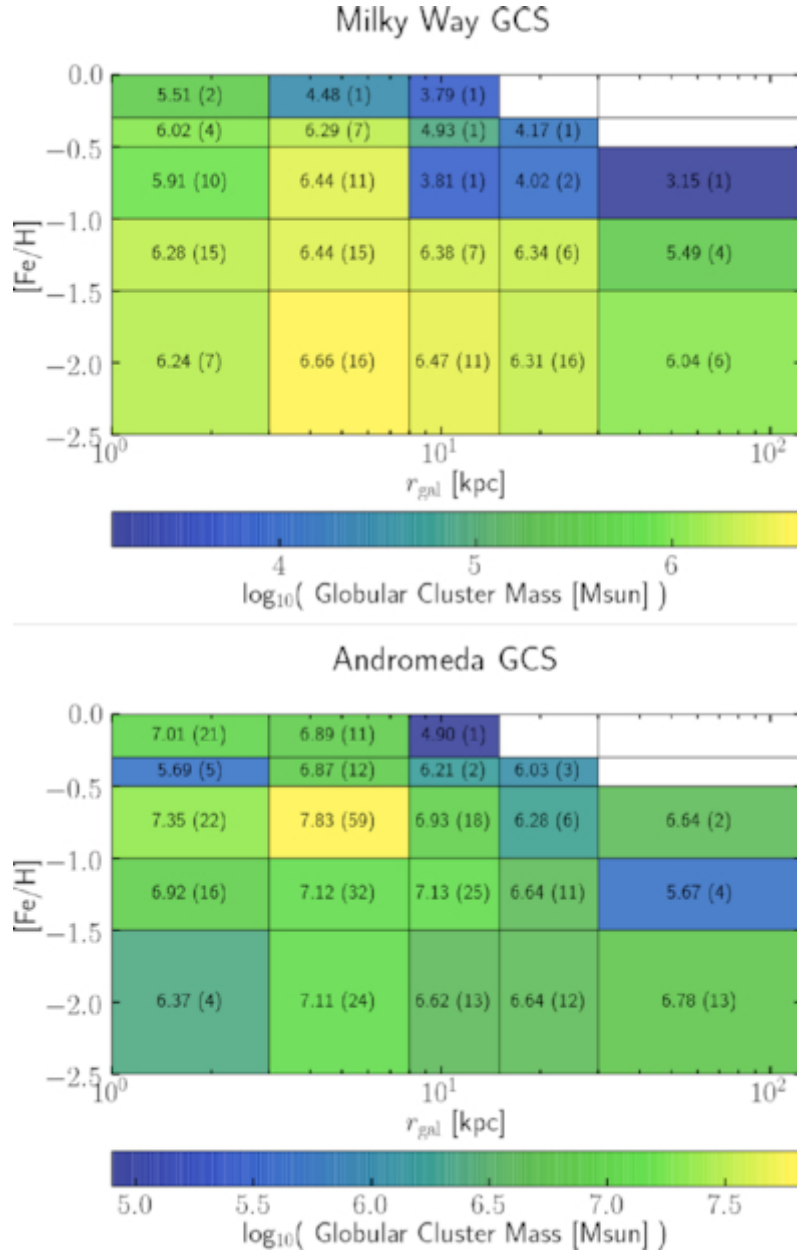


Figure 2. Top panel: ~~Mass-weighted-mass-weighted~~ r_{gal} — $[Fe/H]$ distribution of 151 GCs in the MW (data from ~~1996Harris, 2010 ed.)~~ H96e10), colour-coded by the median (values also shown in each bin). The numbers in parenthesis show how many star particles fall within the bin. Bottom panel: ~~Same same~~ for M31, showing the 366 GCs in CR16 (data from Caldwell & Romanowsky 2016). Radii of M31 are again divided by $r_{vir, M31}$ and multiplied by $r_{vir, MW}$. Note that the range of the ~~colourmap-colour map~~ differs in both figures,.

The observations indicate very few GCs with high metallicities at large radii (the three bins in the upper ~~right-right-hand~~ corner, both for MW and for M31), and relatively few GCs at large radii in general ($r_{gal} > 30$ kpc; ~~right-right-hand~~ column: 11 GCs or 7.3 per cent in the MW and 17 or 4.6 per cent in M31). Moreover, M31 hosts more metal-rich ($[Fe/H] > -1$) GCs in each radial bin in comparison to the MW after accounting for the fact that M31 hosts a larger GCS. Finally, given that the marginalized (i.e. the metallicity and radial) distributions are not statistically consistent between the two galaxies, we find that the two-dimensional distributions are also not consistent. More generally, the GCS of the MW differs significantly from that of M31, not only in the number of clusters but also in their distribution over radius and metallicity. We compare these observations to the Auriga simulations in Section 4.3.

4 RESULTS

We define GC candidates in the Auriga simulations as all star particles older than 10 Gyr based on the age distribution of the MW GCS (top panel of Fig. 1), adopting the definition of a GC from Portegies Zwart et al. (2010) and following the method of Renaud et al. (2017). However, we caution that this definition, although statistically consistent with the estimated ages of all GCs in the MW, is not consistent with the tail of younger clusters as stated in Section 3.3, and further discussed in Section 5.3.

Throughout our analysis, we compare distributions of age-selected GC candidates (age > 10 Gyr) with those of all star particles (i.e. with no age cut). The mean number of star particles in the Auriga L4 simulations that we select as GC candidates is 3.1×10^5 (with a mean total mass of $1.15 \times 10^{10} M_{\odot}$), and the mean number of all star particles is 1.93×10^6 ($7.3 \times 10^{10} M_{\odot}$). The subset of GC candidates is thus around 15 per cent of all the stars in the galaxy when averaged over all Auriga L4 haloes. We further split the GC candidates into an *in situ* subset (defined as GC candidates that are bound to the ~~most massive~~ most massive halo/subhalo in the first snapshot that the particle was recorded), and an accreted subpopulation (those that have formed *ex situ* but are bound to the ~~most massive~~ most massive halo/subhalo at $z = 0$). A GC candidate either formed *in situ* or it was accreted. We consider the metallicity distribution in Section 4.1, the distribution of galactocentric radii in Section 4.2, and the combination of the two in Section 4.3.

4.1 Metallicity distribution

We investigate whether the star formation model implemented in Auriga produces metallicity distributions consistent with the MW and M31 GCSs, and whether the simulations generate sufficient total mass at metallicities typical for the MW and M31 GCSs. To visually inspect the former, we show the normalized metallicity distribution of three specific Auriga galaxies in Fig. 3 in comparison to the MW and M31 [Fe/H] distributions.

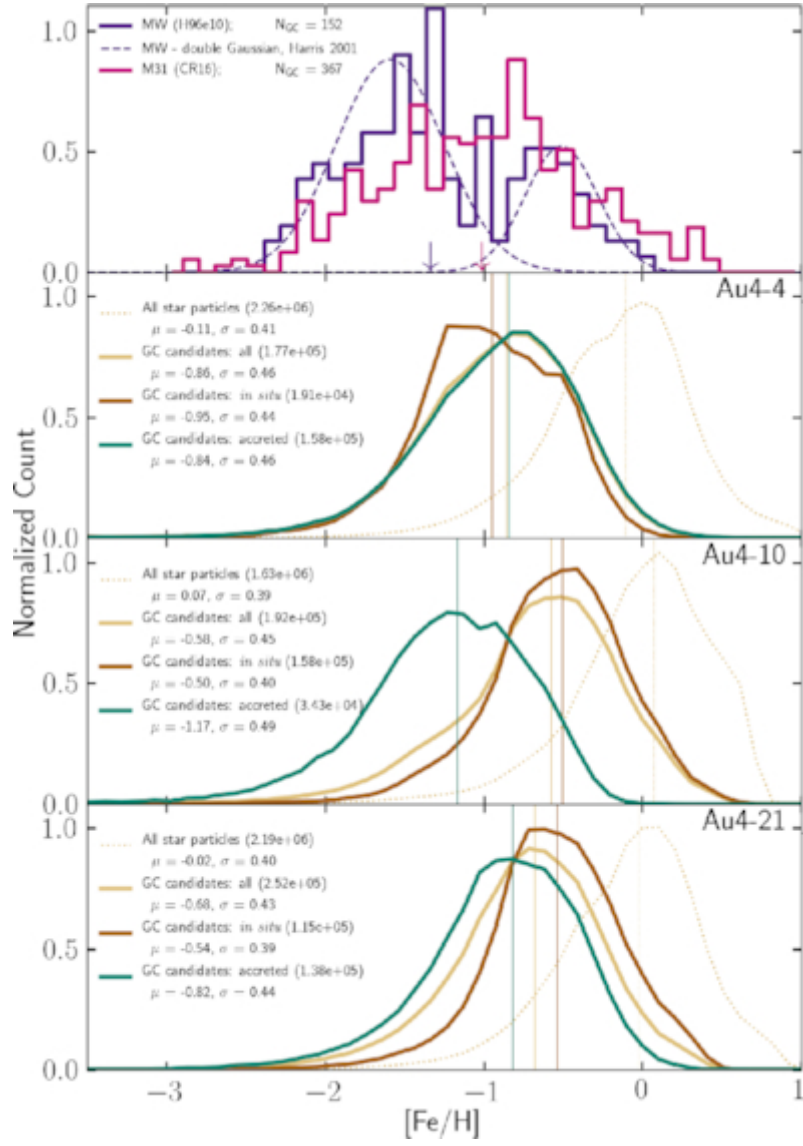


Figure 3. Top panel: ~~Metallicity-metallicity~~ distribution of the MW and M31 GCS. The solid purple (magenta) line shows the GCSs of the MW (M31), and we indicate the mean value with an arrow at the bottom of the ~~x-axis-x-axis~~. We overplot a double Gaussian for the MW GCS using purple dotted lines, taking the mean and dispersion from (Harris 2001). Other panels: three selected Auriga haloes as indicated in the upper ~~right-right-hand~~ corner. In each of these three panels, we show the GC candidates in beige, and use a beige dotted line for all star particles. We split the GC candidates up into two subpopulations, those that have formed *in situ* (brown), and those that have been accreted (teal). The numbers in parenthesis show how many star particles are included in the subset.

We select Au4-10,⁷ Au4-21, and Au4-4 to show the distributions of three individual simulation runs that we consider representative for specific behaviour, and to highlight that different runs give rise to different distributions. We show the age-selected GC candidates as well as the accreted and *in situ* subsets. The top panel of Fig. 3 shows the MW and M31 GCSs, where we overplot a double Gaussian for the MW GCS by adopting literature values of the mean μ and standard deviation σ of the metal-rich and metal-poor subpopulations (Harris 2001).

We find that the age cut, on average, lowers the mean metallicity $\langle [Fe/H] \rangle$ from 0.0 to -0.6 . This reflects the enrichment history of the galaxy because the age cut removes the more metal-rich stellar population, which shifts the mean metallicity towards lower values. Furthermore, accreted GC candidates generally have lower mean metallicities than the *in situ* subset with differences of roughly ~ 0.3 dex for the majority of the simulation runs. This behaviour can be seen in Au4-21, while a slightly

larger difference of ~ 0.5 dex is seen for Au4-10 (as plotted), Au4-16, Au4-17, Au4-18, and Au4-22. However, this trend is reversed for Au4-1 and Au4-4 for which the *in situ* subset has a lower mean metallicity instead. Au4-1 is undergoing a major merger at redshift zero and we find a mean metallicity in this simulation $\mu = -1.51$ (-0.74) for the *in situ* (accreted) GC candidates, although the former consists of only 1019 particles (1.3 per cent of all GC candidates, and with a total mass of $5 \times 10^7 M_{\odot}$). For Au4-4, only 10.8 per cent of the GC candidates is classified as *in situ* (compared to *in situ* fractions of 40–80 per cent for other haloes). We note that Au4-4 has undergone a major merger around 2–Gyr lookback time, which is probably why the accreted population is more metal-rich. After inspection of the same figure for every one of the 30 Auriga L4 haloes, we find that the simulations produce (sub)populations of GC candidates that are more metal-rich than the MW and M31 GCSs. Moreover, none of the simulations produces GC candidates with a bimodal metallicity distribution.

We show the mean metallicity and standard deviation of all 30 Auriga L4 haloes in Fig. 4 to illustrate the individual behaviour for the full set of Auriga galaxies. The beige crosses are to be compared to the purple and magenta crosses, which show the mean value of all MW and M31 GCs, respectively. In addition, we show the metal-rich population of the MW GCS using a solid dot, and the metal-poor population with an open dot. We caution that these literature values result from individual Gaussian fits to subsets of the observational data cut at $[\text{Fe}/\text{H}] = -1$. We do not include corresponding data points calculated using such an artificial cut for the simulated star particles. It is interesting that the mean metallicities of the *in situ* GC candidates appear roughly consistent with that of the metal-rich population of the MW despite the lack of such a metallicity cut, although the simulations show larger dispersions. The latter could simply be caused by the hard separation of the MW data into two groups, which means the range is smaller and the resulting dispersion lower. With regard to the M31 GCS, so far no definitive consensus has been reached in the literature concerning ~~uni-bi-uni~~, ~~bi~~, or trimodality in the $[\text{Fe}/\text{H}]$ distribution, but CR16 argues that the data, after removal of younger objects due to improved age classification, hints at three populations separated at $[\text{Fe}/\text{H}] = -0.4$ and $[\text{Fe}/\text{H}] = -1.5$. None of the Auriga subsets has a mean value that offers much hope of reconciling the simulated distribution with the lowest metallicity group in the M31 GCS. This is also true for the metal-poor population of the MW with a mean value of -1.6 . The main result of this figure is that all Auriga L4 galaxies have metallicity distributions with (much) larger mean values than observed for the MW and M31 GCS, and that we systematically find lower mean metallicities for the accreted GC candidates than for those that have formed *in situ*.

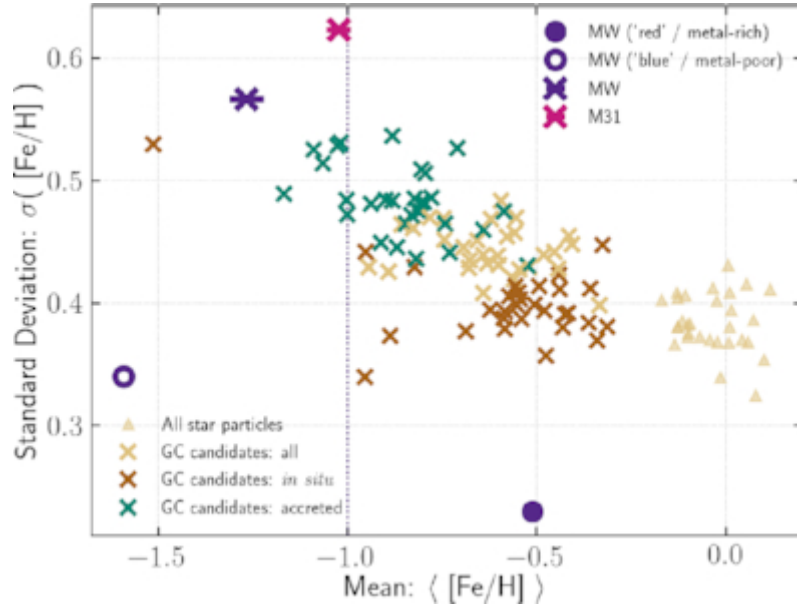


Figure 4. First versus second central moment of the Auriga L4 metallicity distributions. Each cross (for a given colour) represents one simulation. The beige (brown) [teal] crosses show the values calculated using all (only *in situ*) [only accreted] GC candidates. Beige triangles indicate that all stars were used. The purple (magenta) cross denotes our calculation using all MW (M31) observations (which would be appropriate for a unimodal distribution). The purple solid (open) dots indicate the literature values of a bimodal Gaussian fit to the data (values from Ashman & Zepf 1998, page 38), showing the metal-rich (metal-poor) component of the MW (separated at $[Fe/H] = -1$ as indicated by the purple dotted vertical line).

We now turn to our second goal, which is to see whether sufficient total mass in GC candidates is produced by the Auriga simulations. To answer this question, we plot a mass-weighted metallicity distribution in Fig. 5. We show the median over all the 30 Auriga L4 haloes and the 25–75 ~~percentile~~ percentile range as shaded regions, which shows the scatter between runs that have different initial conditions, thus, have varying merger histories. We chose to aggregate the data to indicate general trends that we find when the GC candidates are split up into the accreted and *in situ* subsets, rather than selecting typical examples of individual (simulated) galaxies. Once again we notice that the peak metallicity shifts down from $[Fe/H] = 0$ to ~~[Fe/H] =~~ -0.6 for GC candidates compared to all stars, and we find that the mass at the peak lowers by roughly ~~one~~ 1 dex. The mass budget of the GC candidates is dominated by the *in situ* subpopulation above $[Fe/H] = -1$, and by the accreted subset below this value. We show the MW GCS in purple and that of M31 in magenta, and notice that the difference between the MW and M31 distributions is substantially larger than the scatter between different Auriga galaxies, particularly around $[Fe/H] = -1$. In addition, M31 does host (a handful of) GCs with $[Fe/H] < -2.5$ as well as GCs with $[Fe/H] > 0$ while the MW does not.

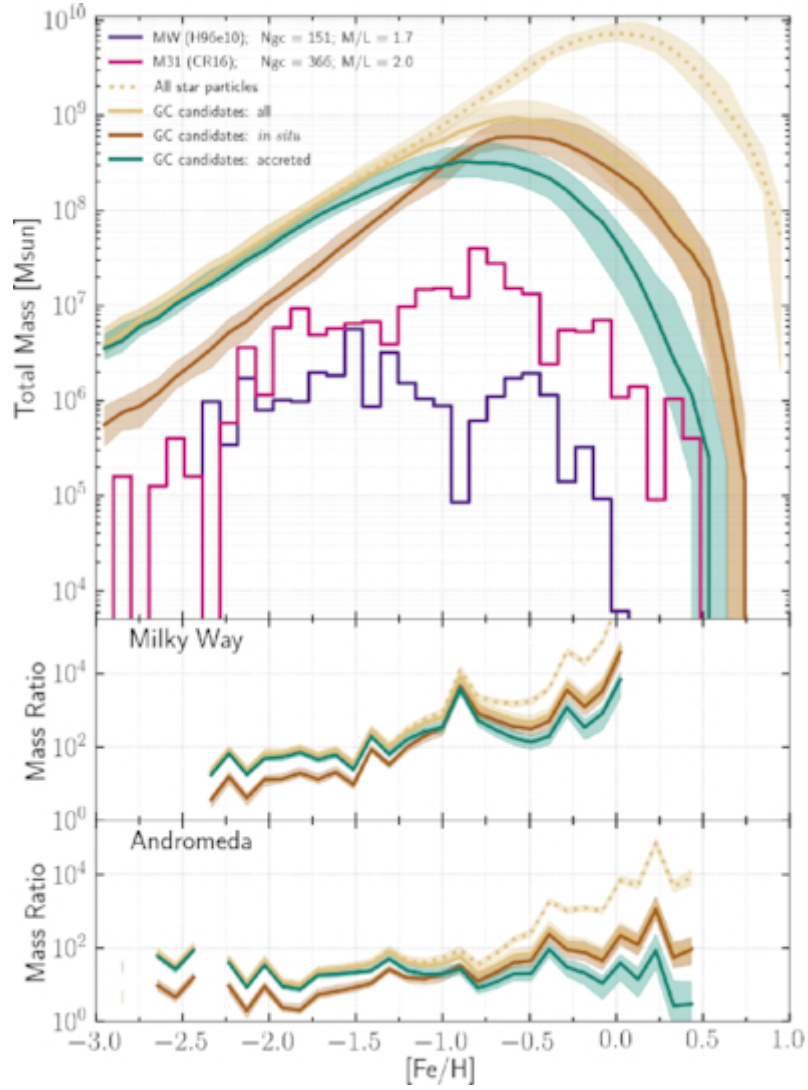


Figure 5. Mass-weighted metallicity distribution of star particles in the Auriga L4 simulations. We show the median value of all Auriga haloes for all stars (beige dotted) and GC candidates (i.e. stars with age > 10 Gyr; beige solid). The latter subset is further split up between stars that formed *in situ* (brown solid), and those that were accreted (teal solid). Shaded regions indicate the 25–75 percentile–percentile range. The MW (M31) GCS is shown in purple (magenta). The middle (bottom) panel shows the ratio of the simulated mass to the mass in the MW (M31) GCS.

We show the ratio of the simulated to the observed profiles in the middle and bottom panels. This mass excess can be thought of the ‘mass budget’ that the Auriga GC candidates can ‘afford to lose’ (due to a combination of smaller than unity bound cluster formation efficiencies combined with a Hubble time of dynamical evolution), while still producing sufficient mass at the right metallicities. In particular, the combined efficiency would have to increase with decreasing metallicity for Auriga GC candidates to produce a population of GC candidates that is consistent with the MW. For the GC candidates in M31, we find a constant mass ratio up to $[\text{Fe}/\text{H}] = -0.9$, above which the simulations produce a higher mass ratio with increasing metallicity. If dynamical evolution is not expected to more efficiently disrupt GCs of higher metallicity, then we would find that the efficiency to form bound star clusters would have to decrease with increasing metallicity. This trend could be consistent with the cluster formation efficiency model of Kruijssen (2012) as lower metallicity star particles formed at earlier times when the bound cluster formation efficiencies are higher due to higher pressure birth environments.

4.2 Radial distribution

We repeat the analysis of the previous subsection for the distribution of galactocentric radius instead of metallicity. We divide the Auriga radii by $r_{\text{vir, Au}}$ and multiply by $r_{\text{vir, MW}}$ to compensate for the different intrinsic sizes of the Auriga galaxies. We look for general trends present in all Auriga L4 galaxies. Fig. 6 shows the median and standard deviation of $\log_{10}(r_{\text{gal}})$ of star particles in all Auriga L4 simulations, respectively. The purple and magenta cross show the median of the MW and M31 GCs, which are to be compared to the beige crosses. The solid dot now shows our calculation of the median value of the ‘red’ metal-rich population, and the open dot that of the ‘blue’ metal-poor population. We split the radii up into the metal-rich/metal-poor groups by taking a metallicity cut at $[\text{Fe}/\text{H}] = -1$ as is done in the literature.

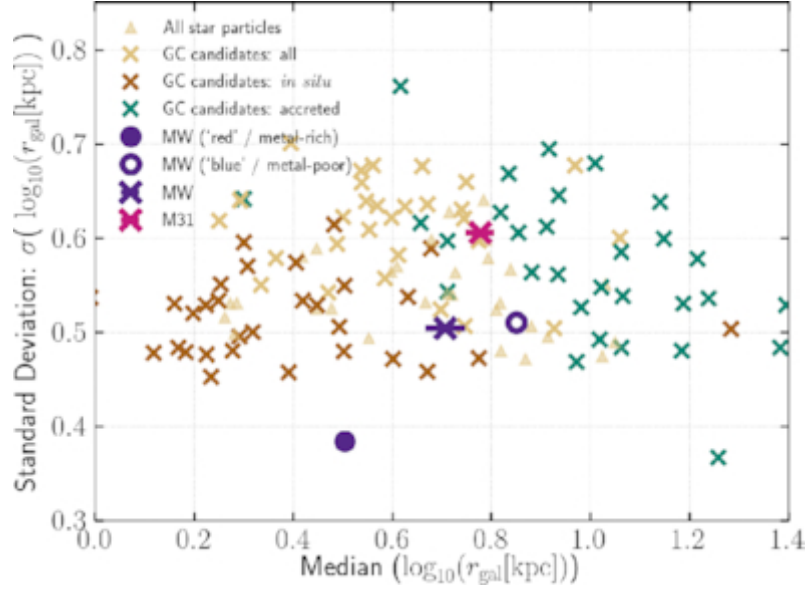


Figure 6. Median and standard deviation of the logarithm of radial distribution of star particles in each of the 30 Auriga L4 haloes compared to the MW (M31) GCS shown in purple (magenta). The Auriga (M31) radii are divided by $r_{\text{vir, Au}}$ ($r_{\text{vir, M31}}$) and multiplied by $r_{\text{vir, MW}}$ to compensate for different intrinsic sizes of the galaxies.

We notice that the *in situ* GC candidates are more centrally distributed, whereas the accreted subsets have a larger radial extent. This is not surprising because the classification of *in situ* requires star particles to have formed within the virial radius—; thus, they could naturally be expected to end up at small galactocentric radii. Accreted star particles, on the other hand, have formed in another (sub)halo beyond the virial radius—; thus, they would first have to migrate inwards in order to populate the innermost radii. Moreover, we find that the simulations have a wider dispersion in $\log(r_{\text{gal}})$ than the MW GCS, while the dispersion of M31 seems to lie within the range of dispersions found in the Auriga galaxies. Furthermore, the median of the MW GCS lies roughly within the range of values produced by the Auriga simulations, whereas the median of M31 is somewhat larger and slightly closer to typical median values of the accreted GC candidates in the Auriga simulations. The larger radial extent of the M31 GCS is generally believed to hint at a more accretion-dominated origin of the GCS, and may reflect a richer accretion history of M31 in comparison to the MW.

Fig. 7 shows the mass-weighted radial distribution of the Auriga L4 haloes. We notice a subtle peak around 10 kpc for all star particles—that, which—is not present for the GC candidates, indicating that the stellar disc is no longer present when applying the latter selection criterion. Furthermore, we find that the dominant contribution to the total mass in GC candidates changes from those formed *in situ* to the accreted population around 10 kpc. Again, we show the mass ratio of the simulations compared to the

MW and M31 GCS. We find a decreasing mass ratio with increasing radius in the range 0.2 to ~ 5 kpc, followed by an increase attributed to the accreted subpopulation. For the MW, we notice that significantly fewer GCs are found beyond 40 kpc than for M31, and that accreted GC candidates contribute mostly to the Auriga GCS at these radii. We further investigate a breakdown of the total mass in Auriga GC candidates into bins of both metallicity and radius in the following section.

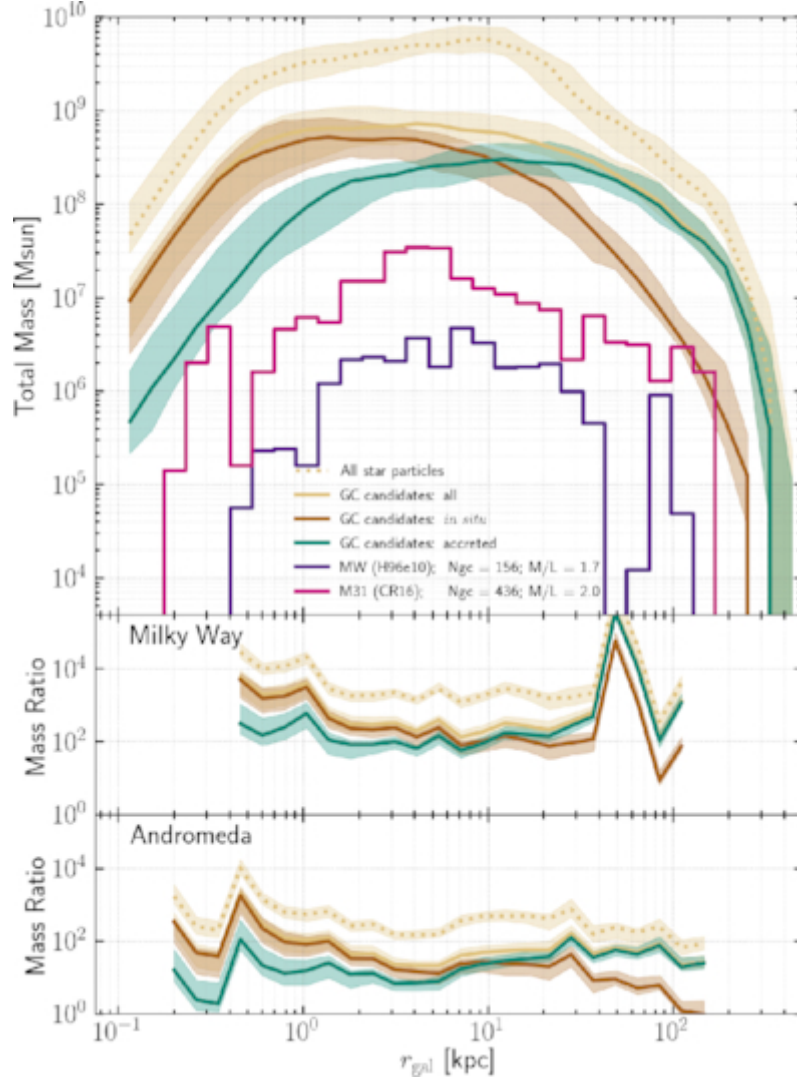


Figure 7. Mass-weighted radial distribution of star particles in the Auriga L4 simulations, where the Auriga (M31) radii are again divided by r_{vir} , Au (r_{vir} , M31) and multiplied by r_{vir} , MW. We show the median value of all Auriga haloes for all stars (beige dotted) and GC candidates (i.e. stars with age > 10 Gyr; beige solid). The latter subset is further split up between stars that formed *in situ* (brown solid), and those that were accreted (teal solid). Shaded regions indicate the 25–75 percentile–percentile range. The MW (M31) GCS is shown in purple (magenta). The middle (bottom) panel shows the ratio of the simulated mass to the mass in the MW (M31) GCS.

4.3 Total mass in ~~metallicity–radial–metallicity–radial~~ space

We investigate whether the Auriga simulations still produce sufficient mass when the GC candidates are two-dimensionally binned in $[\text{Fe}/\text{H}]$ and r_{gal} . First, we sum the total mass of GC candidates in each bin (for an individual Auriga simulation), then we calculate the median total mass in each bin over all 30 Auriga L4 haloes. The result is shown in Fig. 8, which can be compared to the observed total GC mass shown in Fig. 2. We notice that the simulations produce relatively little mass in metal-poor GC

candidates at small radii and in metal-rich GC candidates at large radii. However, there is still few times $10^7 M_{\odot}$ produced by the simulations in the uppermost 3 bins where no observed GCs are found.

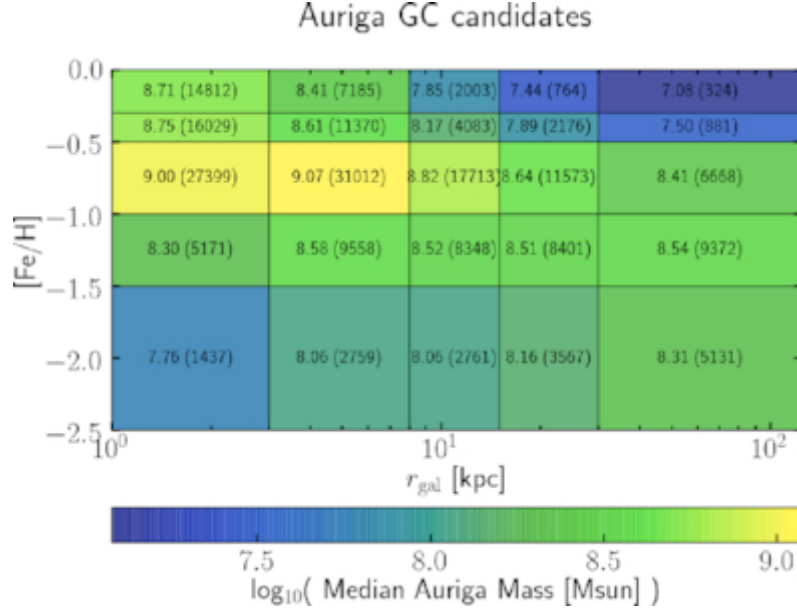


Figure 8. Mass-weighted $[\text{Fe}/\text{H}]-r_{\text{gal}}$ distribution of all 30 Auriga L4 haloes. Here we consider only the GC candidates and colour-code by the median mass (values also shown in each bin). The numbers in parenthesis show how many star particles fall within the bin. Note that the range of the colourmap differs from both panels in Fig. 2 (for improved contrast within the plot).

To ease this comparison between the simulations and observations we take the ratio of the total mass of GC candidates in Auriga to the total GC mass in the observations. We use a diverging colour map ~~centered-centred~~ around the overall median of the mass ratio (i.e. we subtract the median of these 25 bins from the value in each bin). We show this in the top and bottom panel of Fig. 9 for the MW and M31, respectively. Note that the ~~3-three~~ bins in the top right ~~hand side~~ are empty (white) because the mass ratio cannot be calculated due to zero mass in the observations. If the product of the bound cluster formation efficiency and consecutive GC disruption over a Hubble time would be constant, then the value in each bin would be zero. The red and blue bins indicate deviations from such a scenario and indicate a higher and lower than average mass excess in the simulations. The median value used to shift the mass ratio is 2.68 and 1.69 dex for the MW and M31, respectively. This means that the median ‘mass budget’ that the simulations ‘can afford to lose’ is roughly a factor ~~of~~ 480 and 50 for the MW and M31, respectively. The lowest mass surplus for both galaxies is the bin with metallicities in the range $[\text{Fe}/\text{H}] \in [-2.5, -1.5]$ and galactocentric radius $r_{\text{gal}} \in [3, 8]$ kpc, for which the simulations produce a factor ~~of~~ 10 $2.68/10^{1.33} \approx 22$ and $10^{1.69}/10^{0.75} \approx 9$ more mass in GC candidates than is observed in the MW and M31, respectively. The highest factor for the MW is 2.1×10^5 , and 1.1×10^3 for M31.

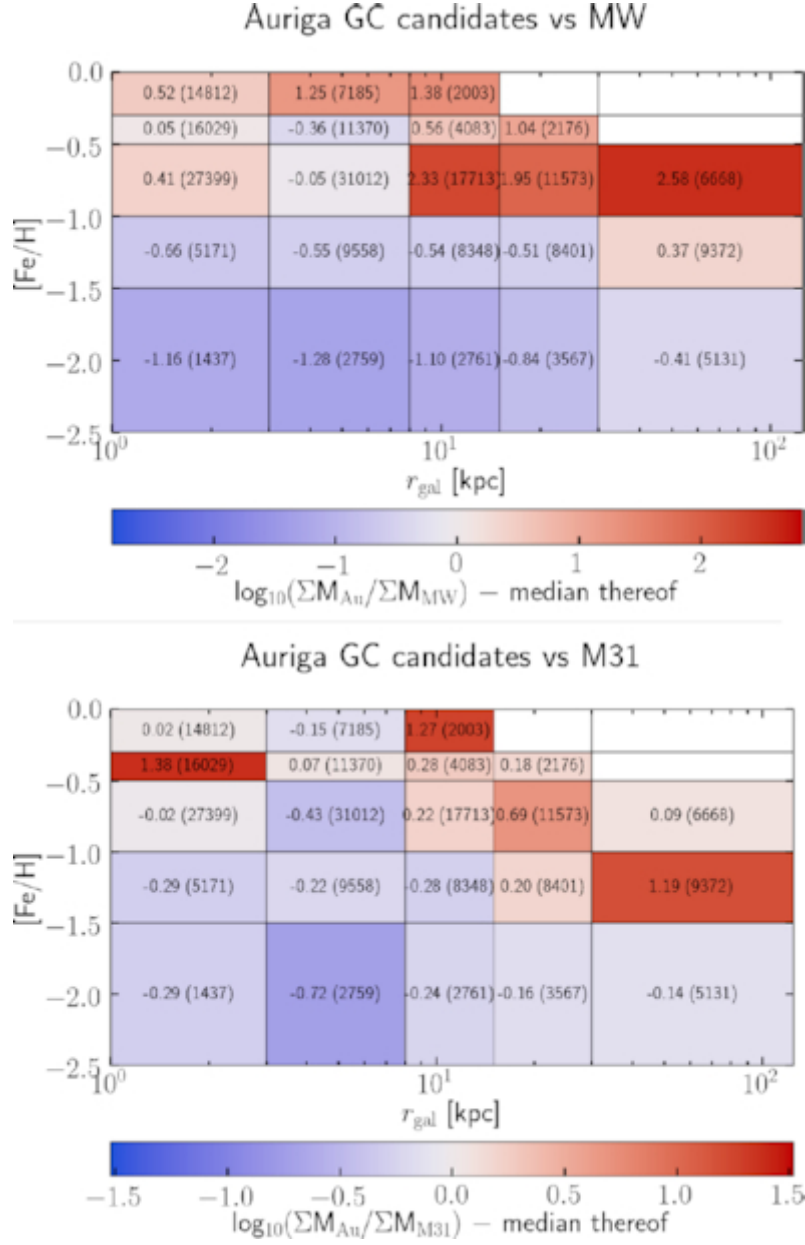


Figure 9. The top (bottom) panel shows the logarithm of the ratio of simulated mass to mass in the MW (M31) GCs, i.e. the logarithm of the mass ratio, minus the median value of these 25 bins. The values are 2.68 and 1.69 dex for the MW and M31, respectively. Red (blue) indicates a higher (lower) overall mass excess. The number in each bin shows the colour-coded value that is plotted, and the (median) star particle count is given in parenthesis. Note that the three bins in the upper right corner are white because the observations have zero mass there.

We now focus on four quadrants of this diagram, split at $[\text{Fe}/\text{H}] = -1$ (metal-poor or metal-rich) and $r_{\text{gal}} = 8$ kpc (inside or outside the Solar radius). The majority of the mass in Auriga GC candidates is produced in metal-rich star particles inside the Solar radius. The total mass is dominated by the *in situ* component, for $[\text{Fe}/\text{H}]$ as well as for r_{gal} as can be seen in Figs 5 and 7. The total mass excess in this region increases with decreasing metallicity for the MW and M31, and there is a weak trend of decreasing ~~over-production~~ overproduction with increasing radius for the *in situ* subsets but no trend with radius for the accreted GC candidates. As for the metal-rich GC candidates outside the Solar radius, we find that the mass excess with respect to the median is largest in this corner for the MW and M31. The main reason for this trend are the lower GC counts in the observations, whereas the Auriga simulations efficiently form metal-rich GC candidates and have no problem to produce them at large radii. The

opposite is true for the metal-poor GC candidates inside the Solar radius, where the mass surplus with respect to the median is smallest for both galaxies. However, the disruption rates are expected to be particularly high for GCs in the inner regions of galaxies which must have orbits with pericentres close to the galactic bulge or bar. In addition, ~~disk-disc~~ crossings in this region will cause spikes in the tidal tensor due to steep density gradients that could be highly disruptive to the GCs. The bins with the lowest ‘mass budget’ are in this region (a factor of 9 for the MW and 22 for M31). The bound cluster formation efficiency has to exceed 10 per cent, and none of the GC candidates in this region can experience significant ~~mass-loss-mass-loss~~ in order for Auriga to produce sufficient mass in this quadrant. Finally, the metal-poor GC candidates outside the Solar radius have lower than average mass ratios, which is not surprising, given that the Auriga simulations overall underproduce low-metallicity stars particles.

5 DISCUSSION

5.1 Metallicity distribution

GCs are ~ 0.5 dex more metal-poor than spheroid stars observed at the same radius for almost all galaxies (Harris 1991). Our selection function (age cut) does lower the mean metallicity of GC candidates by 0.5 dex with respect to all star particles, but we still find that the GC candidates in the Auriga simulations are more metal-rich than the MW and M31 GCSs. Although the (old) star particles represent single stellar populations with a mass consistent with that of GCs, they are, in fact, statistical tracers of the stellar population of the galaxy as a whole. Therefore only a (small) fraction of the star particles may represent plausible formation sites of GCs, whereas the majority represents (halo) field stars — ~~the disk-disc~~ component effectively falls outside our selection of star particles due to the age cut. It is implausible that all halo stars come from disrupted GCs because the total mass in GCSs at redshift zero is generally a few orders of magnitude lower than the total mass of stellar haloes of galaxies. If stellar haloes solely consist of disrupted GCs, then the GC disruption rate would have to be considerably higher than expected from theoretical models. Moreover, disrupted dwarf galaxies are more likely to contribute to the ~~build-up-build-up~~ of the stellar halo than GCs (e.g. Deason, Belokurov & Weisz 2015; Conroy et al. 2019). Overall, our set of GC candidates most likely contains an overabundance of regular stars. It could be that the resulting metallicity distribution is then biased towards higher values than observed for real GCs. An alternative explanation could overmixing of metals at early times.

In general, the colour (metallicity) distribution of most GCSs appears to be bimodal with typical separating value $[\text{Fe}/\text{H}] \sim -1$ (Zinn 1985; Gebhardt & Kissler-Patig 1999; Larsen et al. 2001; Peng et al. 2006). Indeed, Ashman & Zepf (1998) and Harris (2001) find that the MW GCS has a bimodal $[\text{Fe}/\text{H}]$ distribution. Observations of GCs in M31, however, may be best split into three distinct metallicity groups (Caldwell & Romanowsky 2016). The numerical simulation of Renaud et al. (2017) does yield a bimodal metallicity distribution where the metal-poor population is dominated by accreted star particles and the metal-rich population by *in situ* stars.

However, we find that none of the Auriga simulations produces a bimodal metallicity distribution for age-selected GC candidates. Interestingly, the cross-over point above (below) which the mass-weighted metallicity distribution of GC candidates is dominated by those that have formed *in situ* (were accreted) does coincide with the separation between the metal-rich and metal-poor populations of GCSs at $[\text{Fe}/\text{H}] = -1$, as for the MW. Moreover, we do find that the mean metallicity shifts when we split the

GC candidates according to birth location (accreted or *in situ*). In particular, the mean values of the *in situ* GC candidates are roughly consistent with the metal-rich MW GCs. On the other hand, we also notice that most of the simulations have a similar mean value for all GC candidates, and the simulated *in situ* GC candidates have larger dispersions than is claimed for metal-rich GCs in the MW. Moreover, the offset between the means of the metal-rich and metal-poor populations in the MW is 1 dex, a factor ~~2~~^{2–3} larger than the offset that we find between the *in situ* and accreted populations. However, we caution that Kruijssen et al. (2019) suggests to reserve the ‘*ex situ*’ classification for accretion after $z = 2$, when the central galaxy has formed and accretion unambiguously contributes to the radially extended halo GC population. In fact, our classification might not hold for Au4-1.

Finally, we note that Brodie & Strader (2006) compares the number of metal-poor GCs to the stellar halo mass and find⁸ $T_{\text{blue}}^n \sim 100$, while the number of metal-rich GCs compared to the bulge mass yields $T_{\text{red}}^n \sim 5$, and therefore conclude that the formation efficiency of metal-poor GCs is 20 times higher than the metal-rich GCs with respect to field stars. We find that a gradual increase in formation efficiency of GCs with respect to field stars would be required with decreasing metallicity for the GC candidates in the Auriga simulations to yield sufficient total mass to be consistent with the MW or M31 GCS. In addition, the metal-poor GC candidates would have to experience low ~~mass-loss-mass-~~^{loss} rates, especially those within the Solar radius.

5.2 Radial distribution

The M31 GCS has a factor ~~2~~^{2–3} more GCs at large radii compared to the MW GCS, which may indicate that M31 has a richer merger history than the MW (Caldwell & Romanowsky 2016). In the Auriga simulations, we find that the GC candidates at radii larger than ~ 20 kpc are indeed dominated by accreted star particles. However, we select star particles that are bound to the main halo and main subhalo, which means that we include particles up to the virial radius r_{200} . The Auriga simulations have no problem populating the stellar halo up to the virial radius, even with our additional age cut. On the other hand, the MW and M31 have fewer GCs at large radii. We expect tidal disruption to be less efficient at larger radii, thus, the formation efficiencies of the accreted GC candidates would have to be lower. Alternatively, the fraction of old star particles in our subset of GC candidates may contain considerably more star particles that represent stars in the old stellar halo that have been accreted during hierarchical ~~buildup-build-up~~ of the galaxy. Our classification of GC candidates could be improved for the accreted subset in particular. For example, we could select only a subset of the accreted star particles as GC candidates where the number of GCs would be determined by the satellite halo mass, given the $M_{\text{vir}} \propto N_{\text{gal}}$ correlation found by Burkert & Forbes (2019). However, we did not include such an analysis in this study.

5.3 Lower age cut in the GC selection function

Our method is sensitive to the definition that we adopt to classify GC candidates (e.g. Forbes et al. 2018). Therefore, we explore how our results change if we include all star particles older than 8 Gyr, and if we further lower the age cut to 6 Gyr. The average fraction of GC candidates that we select from the all the star particles increases to 35 ~~per-cent~~^{per cent} and 55 per cent for an age cut of 8 and 6 Gyr, respectively.

We find that including more recently formed star particles in our subset of GC candidates shifts the mean metallicity to higher values. Moreover, the total mass in metal-rich ($[\text{Fe}/\text{H}] > \text{--}1$) GC candidates

increases for a lower age threshold and moves closer to the dotted line that shows the distribution of all star particles in Fig. 5. However, we notice that the Auriga simulations, on average, do not form new stars with a metallicity below $[\text{Fe}/\text{H}] = -1$ more recent than 6 Gyr ago: ~~the~~ The behaviour of Fig. 5 does not change for metallicities below $[\text{Fe}/\text{H}] = -1$ when we change the age cut to 8 or 6 Gyr, and the slope of the mass ratio for metallicities above $[\text{Fe}/\text{H}] = -1$ is slightly steeper. In addition, we still find that the accreted GC candidates are more metal-poor than those that have formed *in situ*.

The qualitative behaviour of the median distribution of galactocentric radii (Fig. 7) is unaffected by lowering the age cut other than including more star particles (more ~~mass~~ mass), which leads to a higher normalization and a higher mass ratio with respect to the observed ~~GC systems~~ GCSs of the MW and M31. The qualitative behaviour presented in Fig. 9 does not change when the age cut is lowered to 8 or 6 Gyr. Overall, reducing the age cut worsens the agreement between the observed GCSs and the candidate GCs in the Auriga galaxies.

6 SUMMARY AND CONCLUSIONS

We investigate statistics of age-selected (> 10 Gyr) GC candidates in the Auriga simulations and compare the simulations to the MW and M31 GCSs to test whether the star formation model implemented for the Auriga simulations could give rise to metallicity and radial distributions that are consistent with these two observed ~~GC systems~~ GCSs. Based on our analysis, we draw the following conclusions:

- (i) The star formation model implemented in the Auriga simulations produces metallicity distributions that are more metal-rich than the MW and M31 GCSs. For most of the Auriga simulations we find that the subset of accreted GC candidates has a lower mean metallicity than the *in situ* subpopulation. However, the accreted subsets are still more metal-rich than the MW and M31 GCSs. Moreover, none of the simulated subsets has a mean metallicity as low as the mean of the ‘blue’ metal-poor component of the MW GCS.
- (ii) We find that the difference between the metallicity distributions of the MW and M31 GCSs is big compared to the scatter in the Auriga GC candidates of different Auriga runs. The radial distributions of the MW and M31 GCSs are somewhat more similar, but they are not consistent with being drawn from the same distribution. The scatter between the radial distributions of different Auriga simulations is smaller than the difference between the MW and M31 GCSs.
- (iii) GC candidates in the Auriga simulations may be found out to r_{200} , given that our selection function of star particles selects all stars bound to the main subhalo of the halo. The total mass of GC candidates is dominated by accreted star particles at radii beyond 20 kpc. The GCs in the MW and M31, on the other hand, have a much smaller radial extent.
- (iv) Tidal forces are larger in the inner regions of galaxies than in the outer halo. Therefore, we expect dynamical evolution to more strongly affect GC candidates at small radii than at large radii. However, we find that the Auriga simulations produce more mass in GC candidates with high metallicities at large radii than with low metallicities at small radii. The cluster formation efficiency would have to increase with decreasing metallicity for GC candidates in the Auriga simulations to be consistent with the MW GCS. This trend of ~~over-production~~ overproduction of old star particles that are metal-rich and at large radii compared to observed GCs is less clear for the M31 GCS.

- (v) Overall, we conclude that the metallicity and radial distribution of age-selected star particles in the Auriga simulations are not consistent with ~~globular cluster system~~ **GCS** of the Milky Way or with that of the Andromeda galaxy.

Footnotes

¹See https://www.physics.mcmaster.ca/Fac_Harris/mwgc.dat.

²In a ~~Sun-centered~~ **Sun-centred** coordinate system⁺, X points toward Galactic ~~center~~ **Centre**, Y in direction of Galactic rotation, and Z toward the ~~North-north~~ Galactic **Pole-pole**. We calculate the galactocentric radius $r_{\text{gal}} = \sqrt{(X - r_{\odot})^2 + Y^2 + Z^2}$, assuming the solar radius $r_{\odot} = 8$ kpc.

³Last revised ~~23 Sep~~ 2015, **September 23**; see https://www.cfa.harvard.edu/oir/eg/m31clusters/M31_Hectospec.html.

⁴The authors assumed $M/L_V = 2$ independent of $[\text{Fe/H}]$.

⁵ r_{vir} is the radius in a spherical ‘top-hat’ perturbation model at which the average density reaches an overdensity of $\Delta_{\text{vir}} = 357$ times the background density.

⁶<https://ned.ipac.caltech.edu/> <https://ned.ipac.caltech.edu/>.

⁷The nomenclature is ‘Au’ for Auriga, followed by the resolution level 4 and halo number 10, indicating which set of initial conditions was used.

⁸The specific frequency T is the number of GCs per $10^9 M_{\odot}$ of galaxy stellar mass.

ACKNOWLEDGEMENTS

Q11: [Copy Editor Aptara to Author] In order to validate your funding information prior to publication, please check and confirm whether the name of the funding body given in your manuscript is complete and correct. If any edits are required please mark them on the text. Please also expand any acronyms used in this section. If multiple grants are cited, please ensure the text of your funding statement clearly indicates which grant applies to which funding body. We thank the anonymous referee for a thoughtful and elaborate report. TLRH acknowledges support from the International Max-Planck Research School (IMPRS) on Astrophysics. TLRH thanks the Max Planck Computing and Data Facility for maintaining the Freya compute cluster, where the simulations were post-processed. FM is supported by the program ‘Rita Levi Montalcini’ of the Italian MIUR. FAG acknowledges financial support from **CONICYT** through the project **FONDECYT** Regular Nr. **1181264**, and funding from the **Max Planck Society** through a Partner Group grant. This work has been supported by the **European Research Council** under ERC-StG grant ~~EXAGAL-308037~~ **EXAGAL-308037**. Part of the simulations of this paper used the SuperMUC system at the Leibniz Computing Centre, Garching, under the project PR85JE of the Gauss Centre for Supercomputing. This work used the DiRAC Data Centric system at Durham University, operated by the Institute for Computational Cosmology on behalf of the **STFC** DiRAC HPC Facility ~~‘~~ (www.dirac.ac.uk⁺). This equipment was funded by **BIS** National E-infrastructure capital grant **ST/K00042X/1**, **STFC** capital grant **ST/H008519/1** and **STFC** DiRAC Operations grant **ST/K003267/1**, and **Durham University**. DiRAC is part of the UK National E-Infrastructure.

The analysis in this work was performed using the ~~PYTHON~~ **PYTHON** (van Rossum & de Boer 1991) programming language, the ~~IPYTHON~~ **IPYTHON** (Perez & Granger 2007) environment, the ~~NUMPY~~ **NUMPY** (van der Walt, Colbert & Varoquaux 2011), ~~SCIPY~~ **SCIPY** (Jones et al. 2001), and ~~ASTROPY~~ **ASTROPY** (Astropy Collaboration et al. 2013) packages. Plots were created with ~~MATPLOTLIB~~ **MATPLOTLIB** (Hunter 2007), using the perceptually uniform colour maps from Kovesi (2015) for two-dimensional plots. This research has made use of NASA’s Astrophysics Data System Bibliographic Services.

REFERENCES

Ashman K. M., Zepf S. E., 1992, *ApJ*, **384**, 50

Ashman K. M., Zepf S. E., 1998, *Globular Cluster Systems*. **Q12:** [Copy Editor Aptara to Author] Please provide the publisher name and location for this reference.

Astropy Collaboration et al., 2013, *A&A*, **558**, A33

Beasley M. A., Baugh C. M., Forbes D. A., Sharples R. M., Frenk C. S., 2002, *MNRAS*, **333**, 383

Boley A. C., Lake G., Read J., Teyssier R., 2009, *ApJ*, **706**, L192

Bondi H., 1952, *MNRAS*, **112**, 195

Bondi H., Hoyle F., 1944, *MNRAS*, **104**, 273

Boylan-Kolchin M., 2017, *MNRAS*, **472**, 3120

Brodie J. P., Strader J., 2006, *ARA&A*, **44**, 193

Burkert A., Forbes D., 2019, preprint ([arXiv:e-print](#)) **Q13:** [Copy Editor Aptara to Author] Please update this reference, if possible, with full details to be added to the references list.

Caldwell N., Romanowsky A. J., 2016, *ApJ*, **824**, 42_([CR16](#))

Caldwell N., Schiavon R., Morrison H., Rose J. A., Harding P., 2011, *AJ*, **141**, 61_([C11](#))

Cen R., 2001, *ApJ*, **560**, 592

Chiou Y. S., Naoz S., Burkhart B., Marinacci F., Vogelsberger M., 2019, preprint ([arXiv:e-print](#)) **Q14:** [Copy Editor Aptara to Author] Please update this reference, if possible, with full details to be added to the references list.

Choksi N., Gnedin O. Y., 2019a, preprint ([arXiv:e-print](#)) **Q15:** [Copy Editor Aptara to Author] Please update this reference, if possible, with full details to be added to the references list.

Choksi N., Gnedin O. Y., 2019b, *MNRAS*, **486**, 331

Choksi N., Gnedin O. Y., Li H., 2018, *MNRAS*, **480**, 2343

Conn A. R. et al., 2012, *ApJ*, **758**, 11

Conroy C., Naidu R. P., Zaritsky D., Bonaca A., Cargile P., Johnson B. D., Caldwell N., 2019, *ApJ*, **887**, 237

Côté P., Marzke R. O., West M. J., Minniti D., 2000, *ApJ*, **533**, 869

Côté P., West M. J., Marzke R. O., 2002, *ApJ*, **567**, 853

Deason A. J., Belokurov V., Weisz D. R., 2015, *MNRAS*, **448**, L77

Diemand J., Madau P., Moore B., 2005, *MNRAS*, **364**, 367

El-Badry K., Quataert E., Weisz D. R., Choksi N., Boylan-Kolchin M., 2019, *MNRAS*, **482**, 4528

Fall S. M., Rees M. J., 1985, *ApJ*, **298**, 18

Fattahi A. et al., 2019, *MNRAS*, **484**, 4471

Faucher-Giguère C.-A., Lidz A., Zaldarriaga M., Hernquist L., 2009, *ApJ*, **703**, 1416

Forbes D. A. et al., 2018, ~~*Proceedings of the Royal Society of London Series Proc. R. Soc. A*~~, **474**, 20170616

Gebhardt K., Kissler-Patig M., 1999, *AJ*, **118**, 1526

Gnedin O. Y., 2003, in ~~Kissler-Patig M., ed., Extragalactic Globular Cluster Systems . p. 224~~preprint (astro-ph/0210556)Extragalactic Globular Cluster Systems. Springer-Verlag, Berlin

Gnedin O. Y., Lahav O., Rees M. J., 2001, preprint (arXiv:e-print) **Q16:** [Copy Editor Aptara to Author] Please update this reference, if possible, with full details to be added to the references list.

Grand R. J. J. et al., 2017, *MNRAS*, **467**, 179.(G17)

Grand R. J. J. et al., 2018, *MNRAS*, **474**, 3629

Gratton R. G., Carretta E., Bragaglia A., 2012, *A&A Rev.* AR, **20**, 50

Gunn J. E., 1980, in ~~Hanes D., Madore B., eds, Globular Clusters . p. 304~~Globular Clusters. Cambridge Univ. Press, Cambridge

Harris W. E., 1991, *ARA&A*, **29**, 543

Harris W. E., 1996, *AJ*, **112**, 1487.(H96e10)

Harris W. E., 2001, *Globular Cluster Systems*. Springer, Berlin, ~~Heidelberg~~, p. 223

Harris W. E., Pudritz R. E., 1994, *ApJ*, **429**, 177

Holtzman J. A. et al., 1992, *AJ*, **103**, 691

Holtzman J. A. et al., 1996, *AJ*, **112**, 416

Hunter J. D., 2007, ~~Computing in Science and Engineering~~Comput. Sci. Eng., **9**, 90

Huxor A. P. et al., 2014, *MNRAS*, **442**, 2165.(H14)

Johnson T. L. et al., 2017, *ApJ*, **843**, L21

Jones E., ~~Oliphant T., Peterson P.~~ et al., 2001, ~~SciPy: Open source scientific tools for Python, SciPy: Open Source Scientific Tools for Python~~, <http://www.scipy.org/> **Q17:** [Copy Editor Aptara to Author] Please provide the publisher name and location for this reference. Also, list all authors if eight or fewer.

Kang H., Shapiro P. R., Fall S. M., Rees M. J., 1990, *ApJ*, **363**, 488

Kim J.-h. et al., 2018, *MNRAS*, **474**, 4232

Kovesi P., 2015, preprint (arXiv:1509.03700) **Q18:** [Copy Editor Aptara to Author] Please update this reference, if possible, with full details to be added to the references list.

Kruijssen J. M. D., 2012, *MNRAS*, **426**, 3008

Kruijssen J. M. D., 2014, ~~Classical and Class.~~ *Quantum Gravity*, **31**, 244006

Kruijssen J. M. D., 2015, *MNRAS*, **454**, 1658

Kruijssen J. M. D., Pelupessy F. I., Lamers H. J. G. L. M., Portegies Zwart S. F., Icke V., 2011, *MNRAS*, **414**, 1339

Kruijssen J. M. D., Pelupessy F. I., Lamers H. J. G. L. M., Portegies Zwart S. F., Bastian N., Icke V., 2012, *MNRAS*, **421**, 1927

Kruijssen J. M. D., Pfeffer J. L., Crain R. A., Bastian N., 2019, *MNRAS*, **486**, 3134

Lahén N., Naab T., Johansson P. H., Elmegreen B., Hu C.-Y., Walch S., 2019, preprint (arXiv:e-print) **Q19:** [Copy Editor Aptara to Author] Please update this reference, if possible, with full details to be

added to the references list.

Larsen S. S., Brodie J. P., Huchra J. P., Forbes D. A., Grillmair C. J., 2001, *AJ*, **121**, 2974

Larson R. B., 1996, in Morrison H. L., Sarajedini A., eds, *ASP Conf. Ser. Vol. 92, Formation of the Galactic Halo...Inside and Out*. Astron. Soc. Pac., San Francisco, eds, p. ~~Astronomical Society of the Pacific Conference Series Vol. 92, Formation of the Galactic Halo...Inside and Out~~. p. 241

Li H., Gnedin O. Y., 2014, *ApJ*, **796**, 10

Li H., Gnedin O. Y., Gnedin N. Y., Meng X., Semenov V. A., Kravtsov A. V., 2017, *ApJ*, **834**, 69

McConnachie A. W., Irwin M. J., Ferguson A. M. N., Ibata R. A., Lewis G. F., Tanvir N., 2005, *MNRAS*, **356**, 979

McLaughlin D. E., van der Marel R. P., 2005, *ApJS*, **161**, 304

Mackereth J. T., Crain R. A., Schiavon R. P., Schaye J., Theuns T., Schaller M., 2018, *MNRAS*, **477**, 5072

Mackey A. D. et al., 2019, *MNRAS*, **484**, 1756

Madau P., Lupi A., Diemand J., Burkert A., Lin D. N. C., 2019, preprint ([arXiv:e-print](#)) **Q20:** [Copy Editor Aptara to Author] Please update this reference, if possible, with full details to be added to the references list.

Marinacci F., Pakmor R., Springel V., 2014, *MNRAS*, **437**, 1750

Marinacci F., Grand R. J. J., Pakmor R., Springel V., Gómez F. A., Frenk C. S., White S. D. M., 2017, *MNRAS*, **466**, 3859

Monachesi A. et al., 2019, *MNRAS*, **485**, 2589

Muratov A. L., Gnedin O. Y., 2010, *ApJ*, **718**, 1266

Murray S. D., Lin D. N. C., 1992, *ApJ*, **400**, 265

Pakmor R., Springel V., 2013, *MNRAS*, **432**, 176

Pakmor R., Marinacci F., Springel V., 2014, *ApJ*, **783**, L20

Pakmor R., Springel V., Bauer A., Mocz P., Munoz D. J., Ohlmann S. T., Schaal K., Zhu C., 2016, *MNRAS*, **455**, 1134

Patel E., Besla G., Sohn S. T., 2017, *MNRAS*, **464**, 3825

Peebles P. J. E., 1984, *ApJ*, **277**, 470

Peebles P. J. E., Dicke R. H., 1968, *ApJ*, **154**, 891

Peng E. W. et al., 2006, *ApJ*, **639**, 95

Perez F., Granger B. E., 2007, ~~Computing in Science and Engineering~~ *Comput. Sci. Eng.*, **9**, 21

Pfeffer J., Kruijssen J. M. D., Crain R. A., Bastian N., 2018, *MNRAS*, **475**, 4309

Portegies Zwart S. F., McMillan S. L. W., Gieles M., 2010, *ARA&A*, **48**, 431

Recchi S., Wünsch R., Palouš J., Dinnbier F., 2017, *Ap&SS*, **362**, 183

Renaud F., Agertz O., Gieles M., 2017, *MNRAS*, **465**, 3622

Ricotti M., Parry O. H., Gnedin N. Y., 2016, *ApJ*, **831**, 204

Ryu J., Lee M. G., 2018, *ApJ*, **863**, L38

Schweizer F., 1987, ~~in Faber S. M., ed., *Nearly Normal Galaxies. From the Planck Time to the Present*. p. 18~~*Nearly Normal Galaxies: From the Planck Time to the Present*. Springer-Verlag, New York

Snaith O. N., Haywood M., Di Matteo P., Lehnert M. D., Combes F., Katz D., Gómez A., 2014, *ApJ*, **781**, L31

Snaith O., Haywood M., Di Matteo P., Lehnert M. D., Combes F., Katz D., Gómez A., 2015, *A&A*, **578**, A87

Spitzer L., 1987, ~~*Dynamical evolution of globular clusters*, *Dynamical Evolution of Globular Clusters*~~ **Q21:** [Copy Editor Aptara to Author] Please provide the publisher name and location for this reference.

Springel V., 2010, *MNRAS*, **401**, 791

Springel V., Hernquist L., 2003, *MNRAS*, **339**, 289

Springel V., Di Matteo T., Hernquist L., 2005, *MNRAS*, **361**, 776

van der Walt S., Colbert S. C., Varoquaux G., 2011, ~~*Computing in Science and Engineering*~~*Comput. Sci. Eng.*, **13**, 22

van Rossum G., de Boer J., 1991, *CWI Quarterly Q.*, **4**, 283

VandenBerg D. A., Brogaard K., Leaman R., Casagrande L., 2013, *ApJ*, **775**, 134

Vanzella E. et al., 2017, *MNRAS*, **467**, 4304

Veljanoski J. et al., 2014, *MNRAS*, **442**, 2929

Vietri M., Pesce E., 1995, *ApJ*, **442**, 618

Vogelsberger M., Genel S., Sijacki D., Torrey P., Springel V., Hernquist L., 2013, *MNRAS*, **436**, 3031, [\(V13\)](#)

Wang S., Ma J., Liu J., 2019, preprint ([arXiv:e-print](#)) **Q22:** [Copy Editor Aptara to Author] Please update this reference, if possible, with full details to be added to the references list.

West M. J., Côté P., Marzke R. O., Jordán A., 2004, *Nature*, **427**, 31

Whitmore B. C., Schweizer F., 1995, *AJ*, **109**, 960

Whitmore B. C., Zhang Q., Leitherer C., Fall S. M., Schweizer F., Miller B. W., 1999, *AJ*, **118**, 1551

Zepf S. E., Ashman K. M., English J., Freeman K. C., Sharples R. M., 1999, *AJ*, **118**, 752

Zinn R., 1985, *ApJ*, **293**, 424