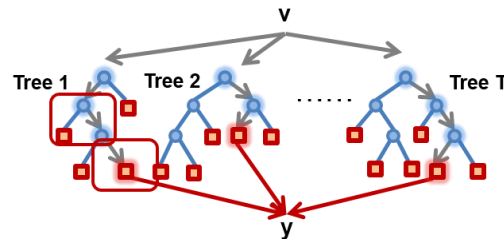


# CS485 *Machine Learning for Computer Vision*

**Coursework1** -part 1 on Manifold Learning, Online Learning, Discriminant Analysis, Ensemble Learning, Randomised Forests [40% mark]



**Release on 10 Oct 2024, the report due on 08 Nov 2024 (midnight)**

The coursework requires Python or Matlab programming.

## Submission instructions:

One joint report by each pair

Page limit: 4 or 5 A4 pages per report with 10 font size (use the IEEE standard double column format, either in MS word or latex).

<https://cvpr2023.thecvf.com/Conferences/2023/AuthorGuidelines>

Explain physical meanings and discuss with insights behind your answers, within the scope of lectures. **Quality and completeness of discussions within the page limit** will be marked.

Source code is not mandatory, unless specified. Optionally, this can go to appendices, which do not count for the page limit.

General principles for writing technical reports are expected to be known and adhered to. Similarly, for practices in conducting experiments, some are as listed below:

- Select/discuss relevant results that support the points you want to make rather than everything that the program code gives.
- The important results should be in the report, not just in the appendix.
- Use clear and tidy presentation style, consistent across the report e.g. figures, tables.
- The experiments should be described such that there is no ambiguity in the settings, protocol and metrics used.
- The main points are made clear, identifying the best and the worst case results or other important observations.
- Do not copy standard formulas from lecture notes, explain algorithms in detail, or copy figures from other sources. References to lecture slides or publications/webpages are

enough in such cases, however short explanations of the terms or parameters referred to are needed.

- Find and demonstrate the parameters that lead to optimal performance and validate it by presenting supporting results.
- Include formulas only where appropriate, results presented in figures, and their discussions. Try to visualise any interesting observations to support your answers.

Submit the report **in pdf** through the KLMS system. No hard copy is needed. Write your full names and school ID numbers on the first page.

If you have questions, please contact

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## Experiment with face dataset

Use the provided face data (face.mat), which stores raster-scanned face images (46x56 pixels) in columns. In all questions, you can use any existing toolbox/code, if needed.

### Q1.

#### [10] Eigenfaces

- Partition the provided face data into your training and testing data, e.g. 8 images and 2 other images of each face identity for training and testing respectively. Apply PCA to your training data, by computing the eigenvectors and eigenvalues of the covariance matrix  $S=(1/N)AA^T$  directly. Show and discuss the results, including: the eigenvectors, the eigenvalues, and the mean image, how many eigenvectors with non-zero eigenvalues are obtained and how many eigenvectors are to be used for face recognition. Give insights and reasons behind your answers.
- Apply PCA to your training data, using the eigenvectors and eigenvalues of  $(1/N)A^TA$ . Show and discuss the results in comparison to the above, including: if the eigenvectors and eigenvalues obtained are identical, what are the pros/cons of each method. Show respective measurements for your answers.

>> Hereinafter, we use the low-dimensional PCA technique, wherever needed.

#### [15] Application of Eigenfaces

Use the data partition, which you used in Q1, into training and testing.

- Perform the face image reconstruction using the PCA bases learnt. Show and discuss the results, while varying the number of bases to use, including: if the reconstruction error (or

the distortion measure) obtained is same as in the theory, how good the reconstruction results are for at least 3 images of your choice (e.g. from both the training and testing dataset).

- b. Perform the PCA-based face recognition by either the **NN classification method or alternative method learnt in the PCA lecture**. Report and discuss, including: the recognition **accuracy** (success rates), **example** success and failure cases, the **confusion matrices**, **time/memory** (and any other aspects you observe), **by varying the parameter values/experimental settings** you used. Give insights and reasons behind your answers.

## **Q2. [20] Incremental PCA**

Use the same data partition into training and testing as in Q1. Further divide the training data equally into **four subsets, each with 104 images** (i.e. two images per person). Starting with the first subset, **keep adding a more subset into your training**.

Perform Incremental PCA, and compare it with the counterpart i.e. batch PCA, and PCA trained only by the first subset, in terms of \*training time, reconstruction error, face recognition accuracy (using NN classification).

Show and discuss, including: how accurate your incremental method is, what important parameters in the method are (and how they are set). Provide your own discussions and measurements to support.

\*Note: You might ignore all other computations e.g. constructing covariance matrices, orthonormalization, matrix products, (**which can be accelerated by proper implementations**) than eigen-decompositions.

## **Q3. [25] LDA Ensemble for Face Recognition**

Use the provided face data, and the same data partition into training and testing as in Q1.

**Try PCA-LDA and its ensemble learning**, along with the **NN classifier**. Compare and discuss face recognition results.

### **PCA-LDA**

Perform the PCA-LDA based face recognition with the NN classifier. Report and discuss, including:

- recognition accuracies by varying the parameter values,  $M_{pca}$  and  $M_{lda}$
- ranks of the scatter matrices,
- the confusion matrix, example success and failure cases

Explain your observations and reasons, and discuss the results in comparison to those of **Q1**.

## PCA-LDA Ensemble

Show, measure and discuss the results, including:

- randomisation in feature space
- randomisation on data samples (i.e. bagging)
- the number of base models, the randomness parameter,
- the error of the committee machine vs the average error of individual models
- fusion rules
- recognition accuracy and confusion matrix

Observe and discuss the above by varying the parameter values/architectures you used. Give insights and reasons behind all your answers.

### Q4. [15] Generative and Discriminative Subspace Learning

PCA is a generative model, by which input images or data can be reconstructed. LDA is a discriminative model, which **extracts better features for classification**. Say we are interested in subspace learning that fulfils both aspects or controls a balance between the two aspects.

Mathematically formulate the problem (i.e. the objective or goal function to optimise) that learns the subspace for reconstruction and discriminative features at the same time.

And mathematically derive the solution that optimises the defined problem. If needed, you may use Lagrange multiplier formulation, gradient-based optimization, eigenvector-eigenvalues, and/or generalized eigenvector-eigenvalues.

Discuss foreseeable behaviours, and pros and cons, of your method. **No programming is needed.**

### Q5. [15] RF classifier

Train and test **Random Forest** using the training and testing data set as in Q1. Change the RF parameters (including the number of trees, the depth of trees, the degree of randomness parameter, the type of weak-learners: e.g. axis-aligned, two-pixel test, or any other features you can think of), and show and discuss the results:

- recognition accuracy, confusion matrix,
- example success/failures,
- time-efficiency of training/testing,
- impact of the different types of weak-learners

Discuss the results in comparison to those of **Q1, Q3**.

### Q6. (optional) Multi-class SVM for Face Recognition

(This part carries no mark, should go to an appendix of your report.)

Use the provided face data, and the same data partition into training and testing as in Q1.

Feature vectors  $\mathbf{x}$  are the raw-intensity vectors (obtained by raster-scanning pixel values of face images) or PCA coefficients. Try both and compare the results below.

Train and test multi-class SVM using the feature vectors  $\mathbf{x}$ . You can use any existing toolbox for two-class (or binary-class) SVMs. Note, write your own lines of code for the multi-class extensions of SVM (both one-versus-the-rest and one-versus-one), and provide your code in an appendix of your report. Compare the results of the two multi-class extensions of SVM.

Show, measure and discuss the results, including:

- setting the SVM parameters, i.e. kernel type, kernel parameters,  $C$  (underfitting/overfitting),
- recognition accuracy and confusion matrix
- time-efficiency of SVM training/testing
- examples of support vectors and success/failure images
- margin etc.

Discuss the results in comparison to those of **Q1, Q3, Q5**.  
Give insights and reasons behind all your answers.