

Towards Causal Reinforcement Learning (CRL)

Elias Bareinboim
Causal Artificial Intelligence Lab
Columbia University
( @eliasbareinboim)

Slides: <https://crl.causalai.net>
ICML, 2020

JOINT WORK WITH CAUSAL AI LAB & COLLABORATORS



Yotam Alexander (Columbia)

Juan Correa (Columbia)

Kai-Zhan Lee (Columbia)

Sanghack Lee (Columbia)

Adele Ribeiro (Columbia)

Kevin Xia (Columbia)

Junzhe Zhang (Columbia)

Amin Jaber (Purdue)

Chris Jeong (Purdue)

Yonghan Jung (Purdue)

Daniel Kumor (Purdue)

Judea Pearl (UCLA)

Carlos Cinelli (UCLA)

Andrew Forney (UCLA)

Brian Chen (Brex)

Jin Tian (Iowa State)

Duligur Ibeling (Stanford)

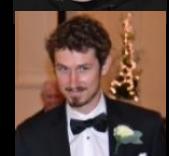
Thomas Icard (Stanford)

Murat Kocaoglu (IBM)

Karthikeyan Shanmugam (IBM)

Jiji Zhang (Lingnan University)

Paul Hünermund (Copenhagen)

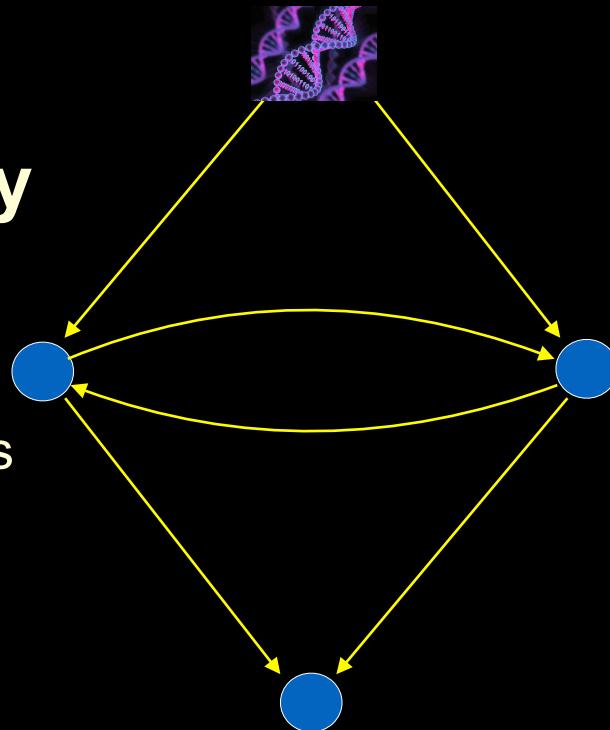


CausalAI Lab

Structural Causal Models

1. Explainability

(Effect identification and decomposition, Bias Analysis and Fairness, Robustness and Generalizability)



2. Decision-Making

(Reinforcement Learning, Randomized Controlled Trials, Personalized Decision-Making)

3. Applications, Education, Software

Data Science:

Principled (“scientific”) inferences from large data collections.

AI-ML:

Principles and tools for designing robust and adaptable learning systems.

What is Causal RL?

- Reinforcement Learning (RL) is awesome at handling sample complexity and credit assignment.
- Causal Inference (CI) is great at leveraging structural invariances across settings and conditions.
- Can we have the best of both worlds? Yes!

Simple solution:

$$\text{Causal RL} = \text{CI} + \text{RL}$$

Our goal: Provide a cohesive framework that takes advantage of the capabilities of both formalisms (from first principles), and that allows us to develop the next generation of AI systems.

Outline

- Part 1. Foundations of CRL (60')
 - Intro to Structural Causal Models, Pearl Causal Hierarchy (PCH), Causal Hierarchy Theorem (CHT)
 - Current RL & CI methods through CRL Lens
- Part 2. New Challenges and Opportunities of Causal Reinforcement Learning (60')

Goal: Introduce the main ideas, principles, and tasks.
Not focused on the implementation details.

For a more detailed discussion, see: NeurIPS'15,
PNAS'16, ICML'17, IJCAI'17, NeurIPS-18, AAAI-19,
UAI-19, NeurIPS-19, ICML-20 ... + new CRL survey.

Resources: <https://crl.causalai.net>

PRELUDE: REINFORCEMENT LEARNING

What's Reinforcement Learning?

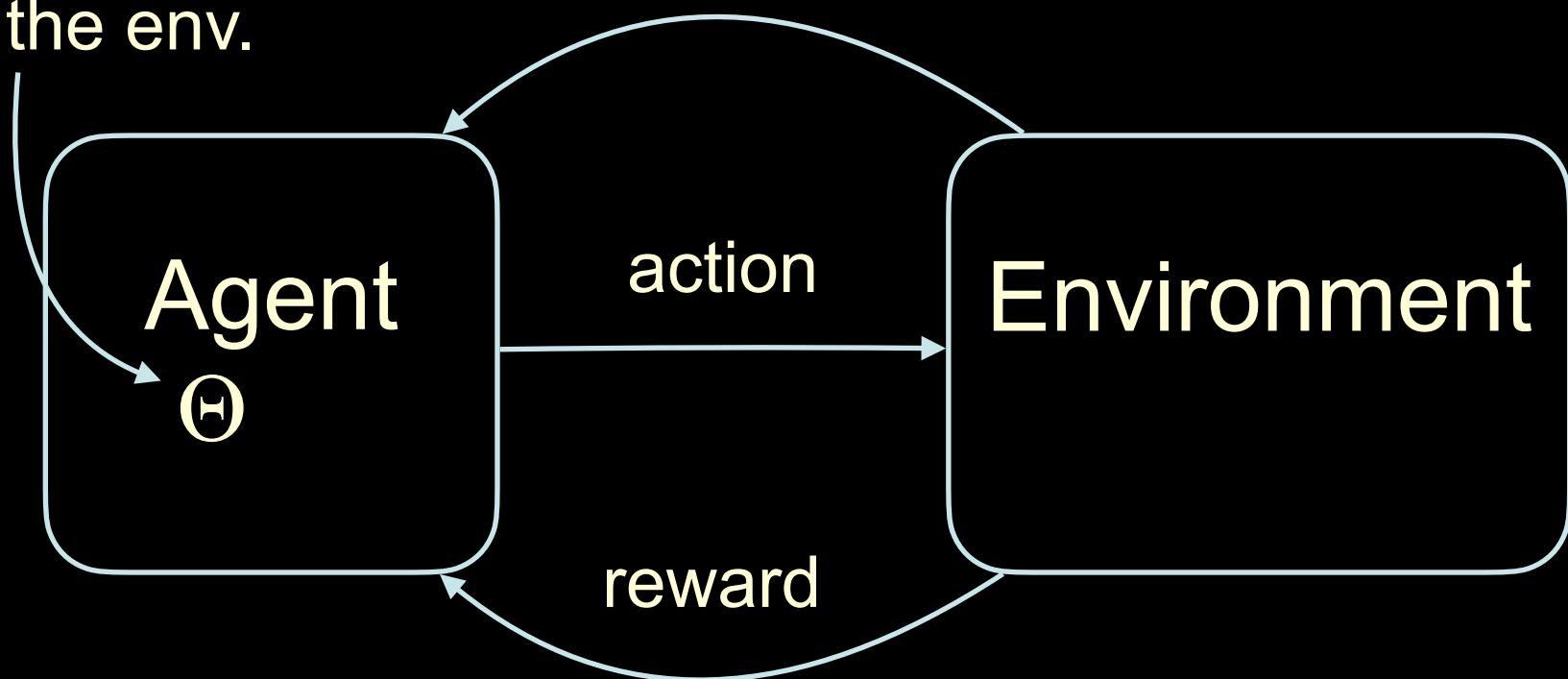
- Goal-oriented learning -- how to maximize a numerical reward signal.
- Learning about, from, and while interacting with an external environment.
- Adaptive learning -- each action is tailored for the evolving covariates and actions' history.

(Learning without having a full specification of the system; versus planning/programming)

RL - Big Picture

Parameters
about the env.

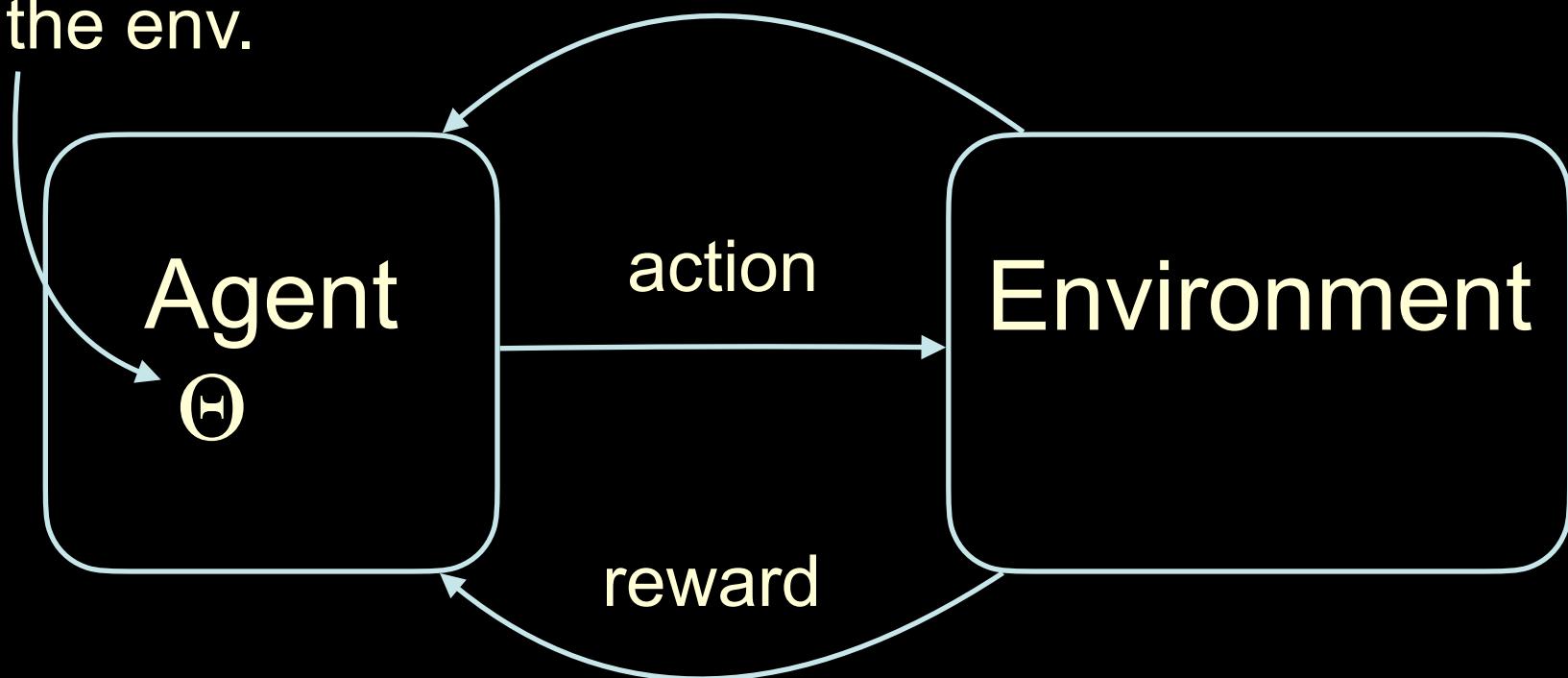
context / state



RL - Big Picture

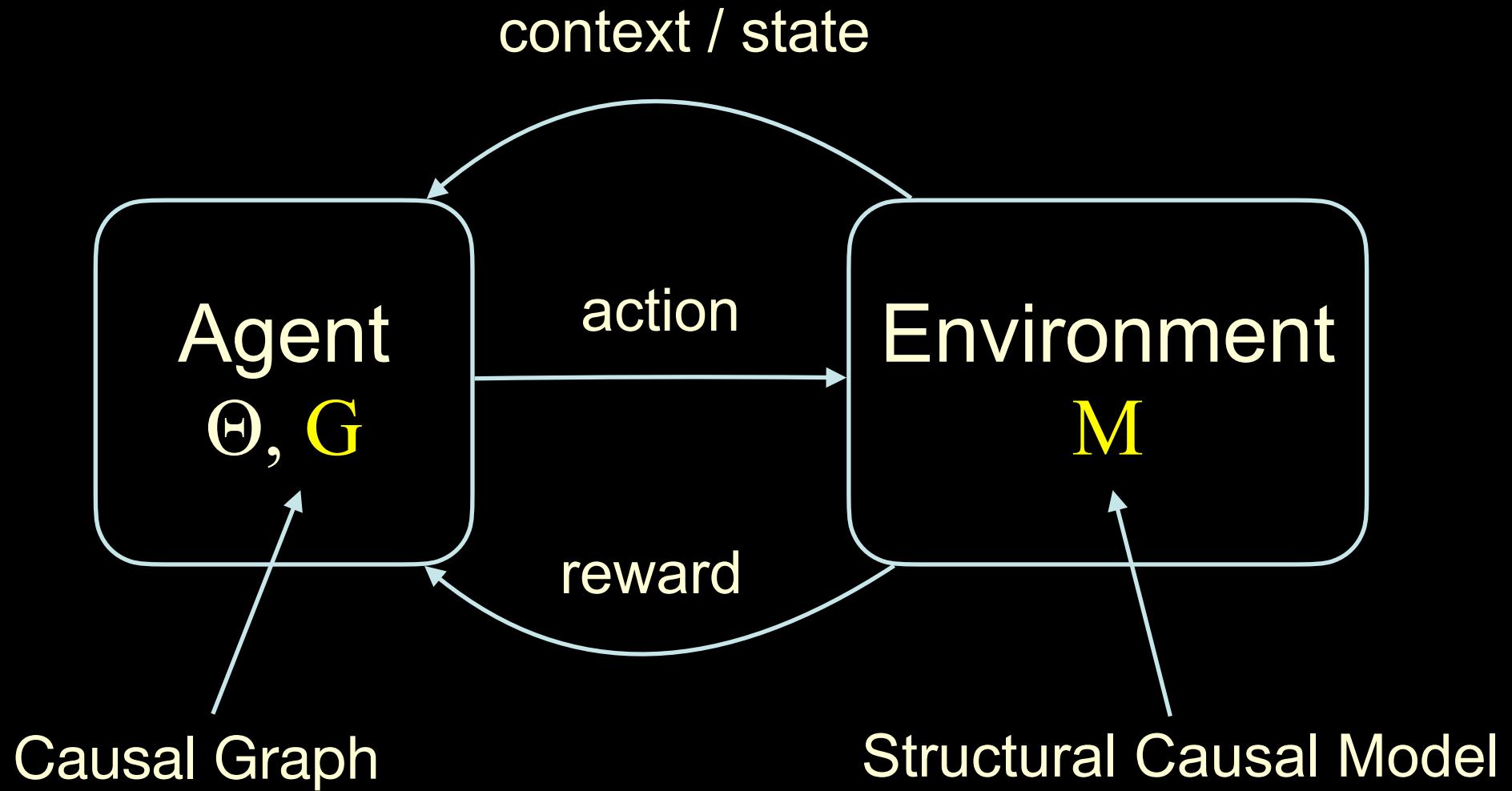
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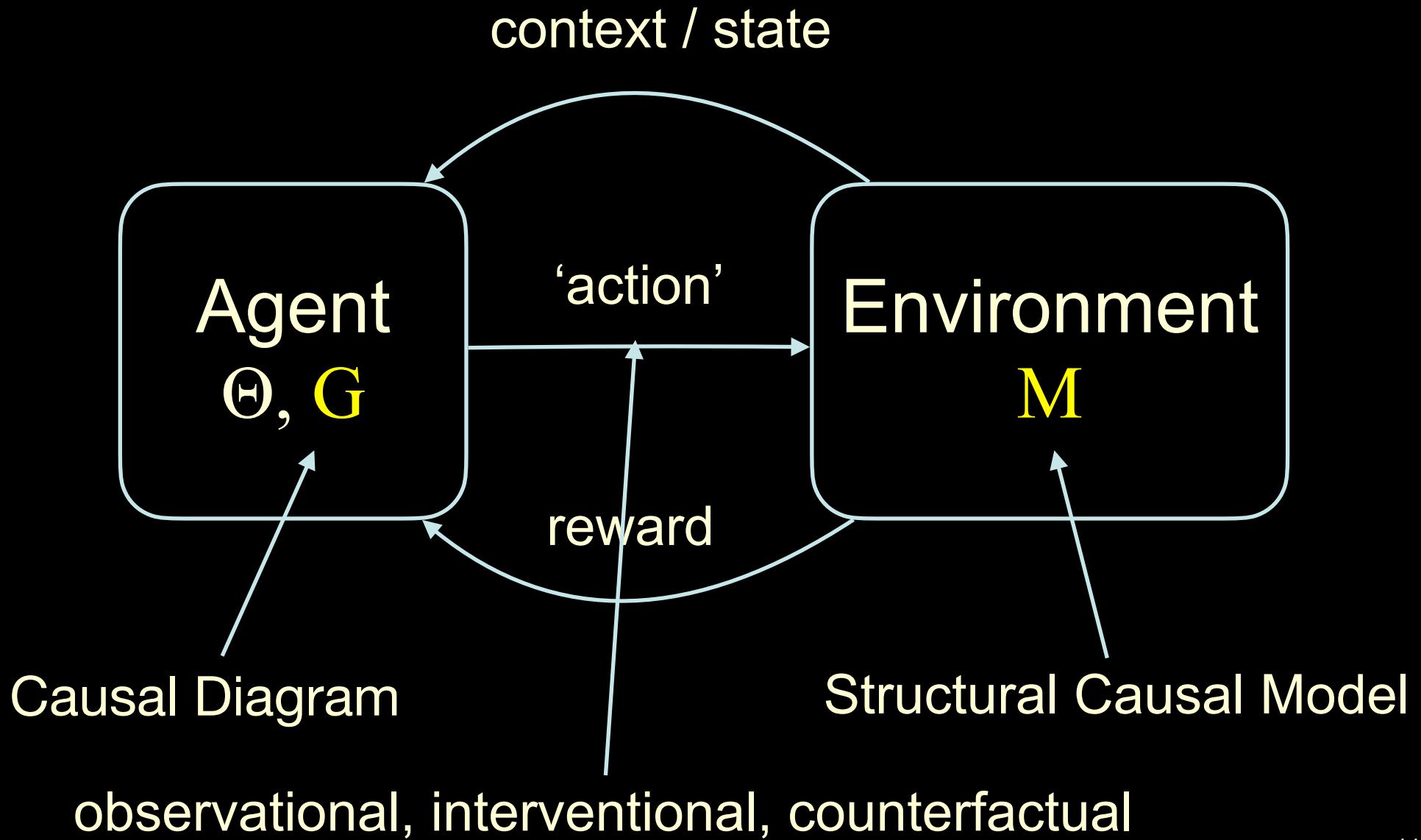


- Receive feedback in the form of **rewards**.
- Agent's utility is defined by the reward function.
- Must (learn to) act so as to **maximize expected rewards**.

Causal RL - Big Picture

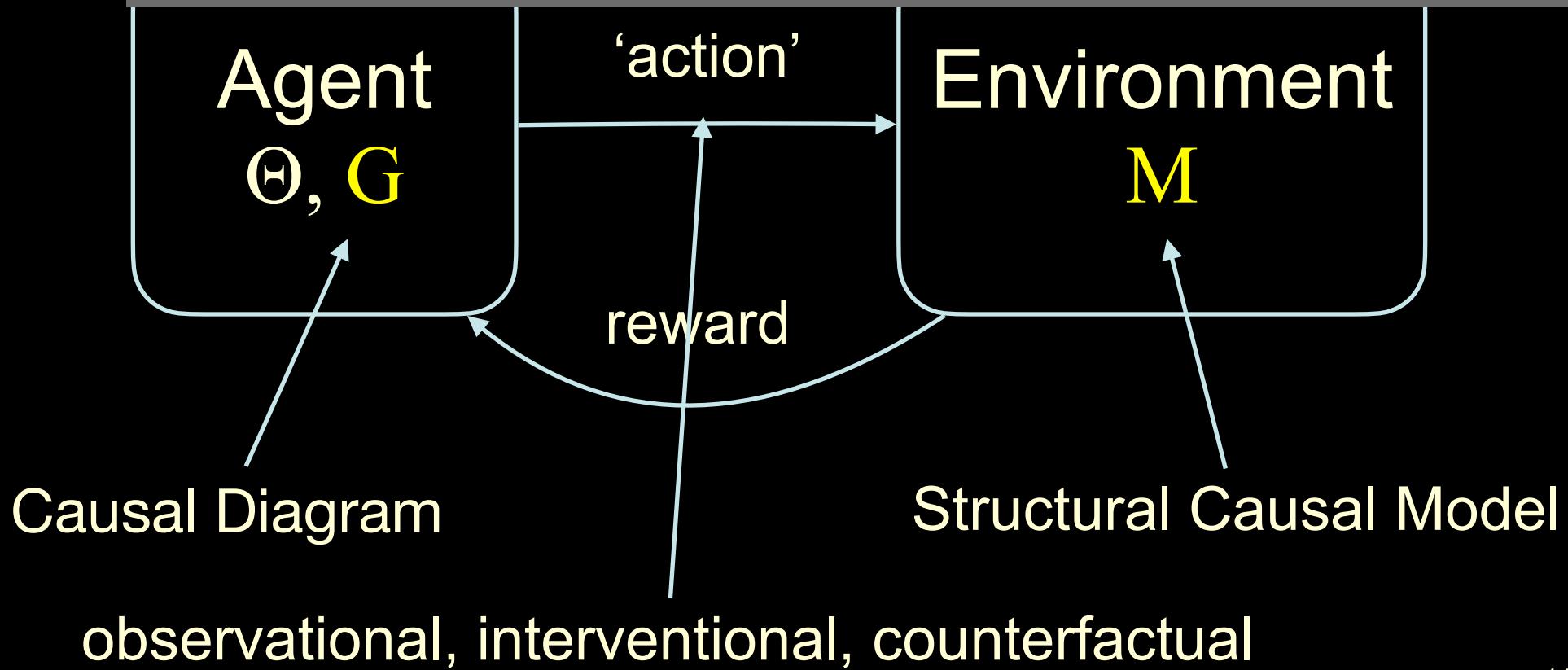


Causal RL - Big Picture



Two key observations (RL \rightarrow CRL):

1. The environment and the agent will be tied thr. the pair SCM M & causal graph G.
2. We'll define different types of "actions", or interactions, to avoid ambiguity (PCH).



Two key observations (RL \rightarrow CRL):

1. The environment and the agent will be tied thr. the pair **SCM M & causal graph G**.
2. We'll define different types of “actions”, or interactions, to avoid ambiguity (PCH).

Let's define and understand
(1) the pair $\langle M, G \rangle$, and (2) the PCH.



STRUCTURAL CAUSAL MODELS & CAUSAL GRAPHS



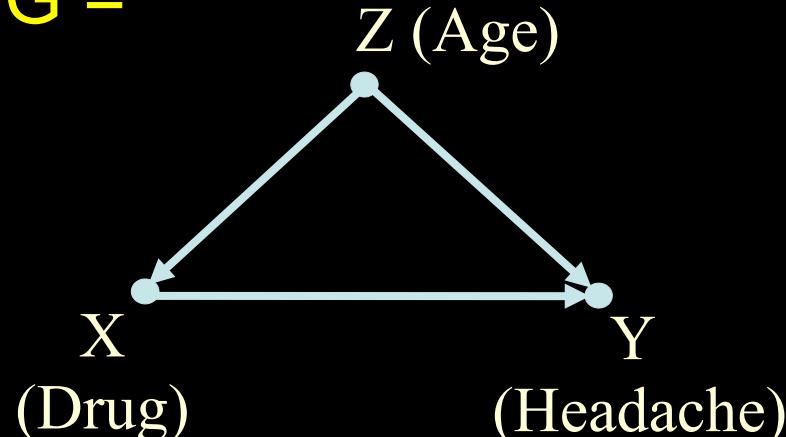
SCM -- REPRESENTING THE DATA GENERATING MODEL

- Processes

$$\text{Drug} \leftarrow f_D(\text{Age}, U_D)$$

$$\text{Headache} \leftarrow f_H(\text{Drug}, \text{Age}, U_H)$$

G =



$P(Z, X, Y)$
(observational)

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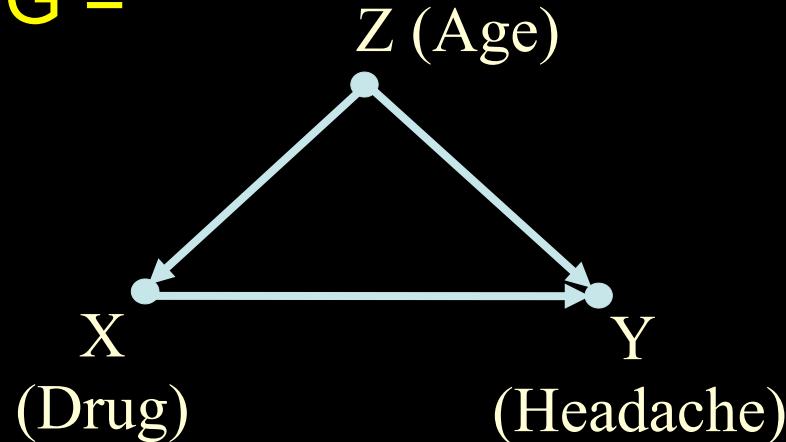
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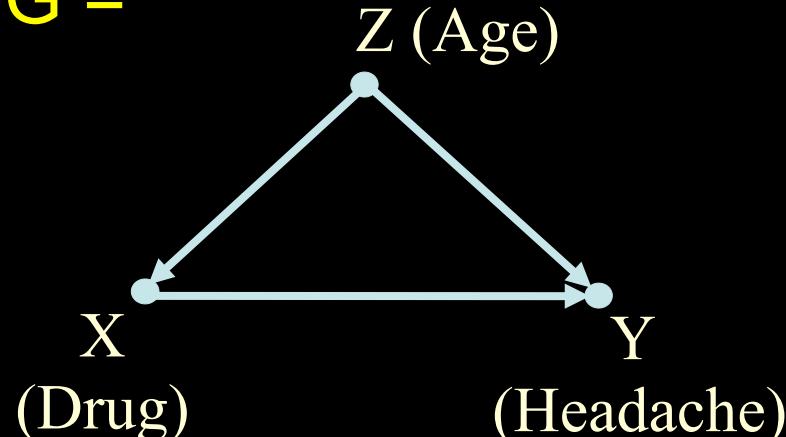
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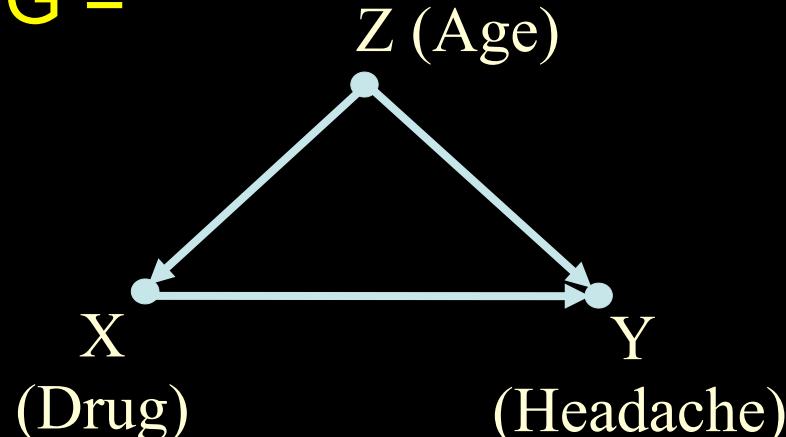
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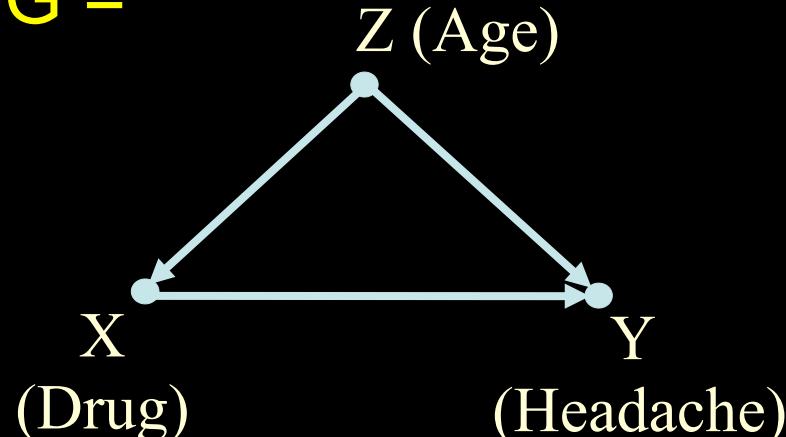
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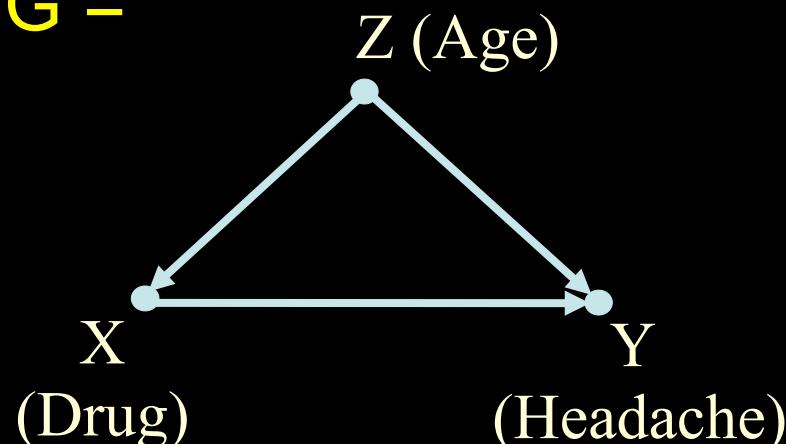
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σ -calculus (Correa
& Bareinboim 2020)

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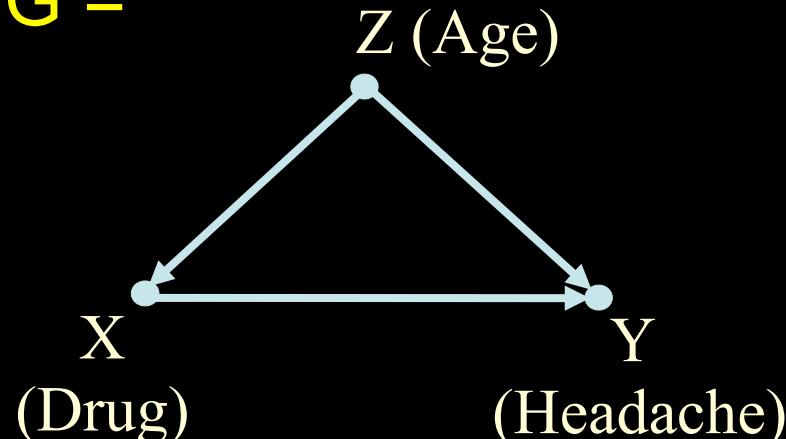
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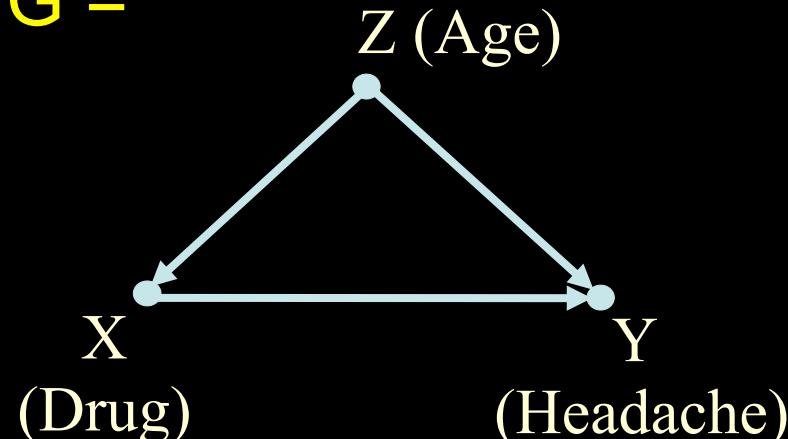
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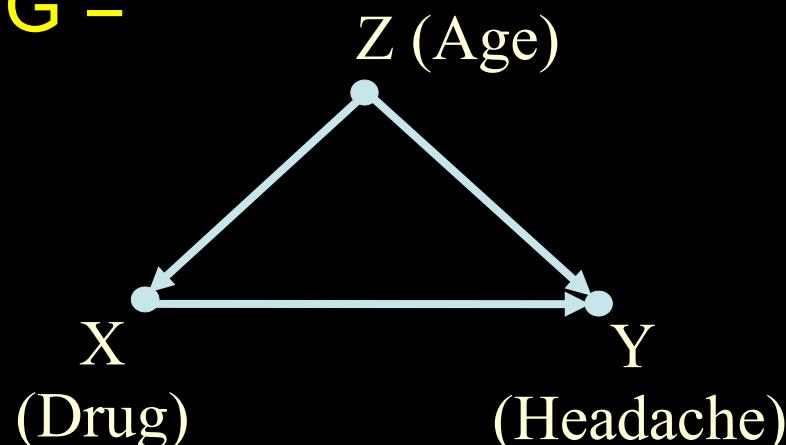
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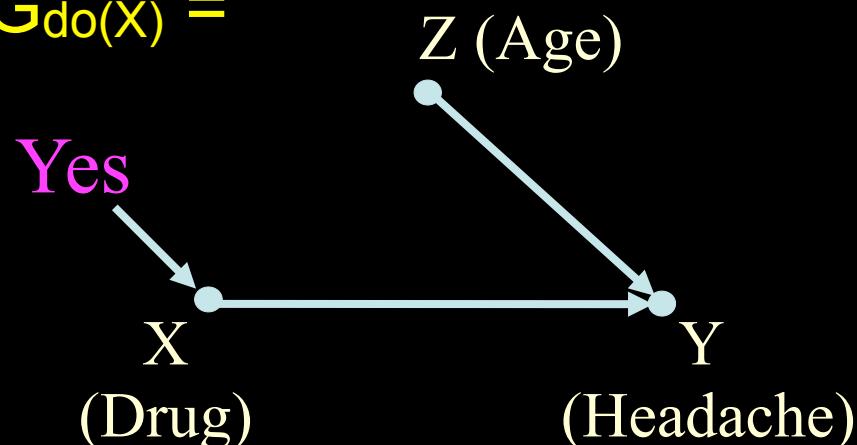
$G =$



$$P(Z, X, Y)$$

(observational)

$G_{do(X)} =$



$$P(Z_{x=\text{yes}}, Y_{x=\text{yes}}) = P(Z, Y | do(X = \text{Yes}))$$

(counterfactuals) (interventional)

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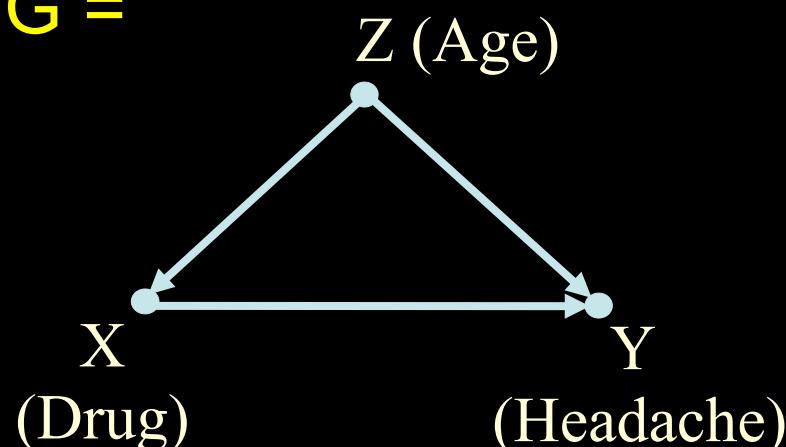
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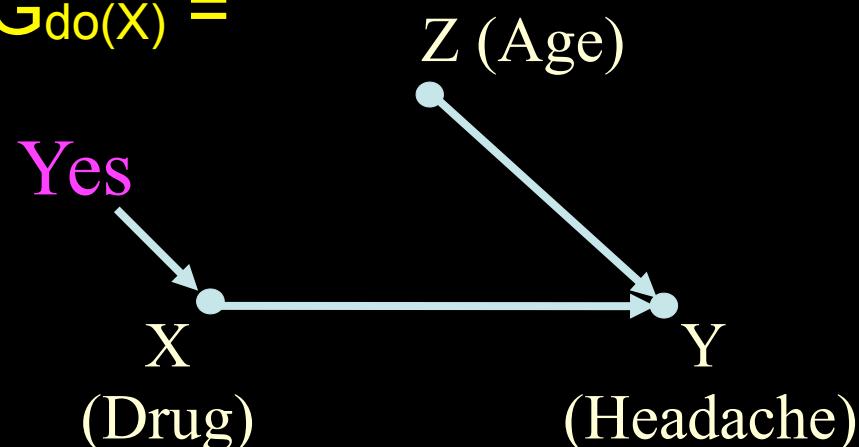
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(interventional)

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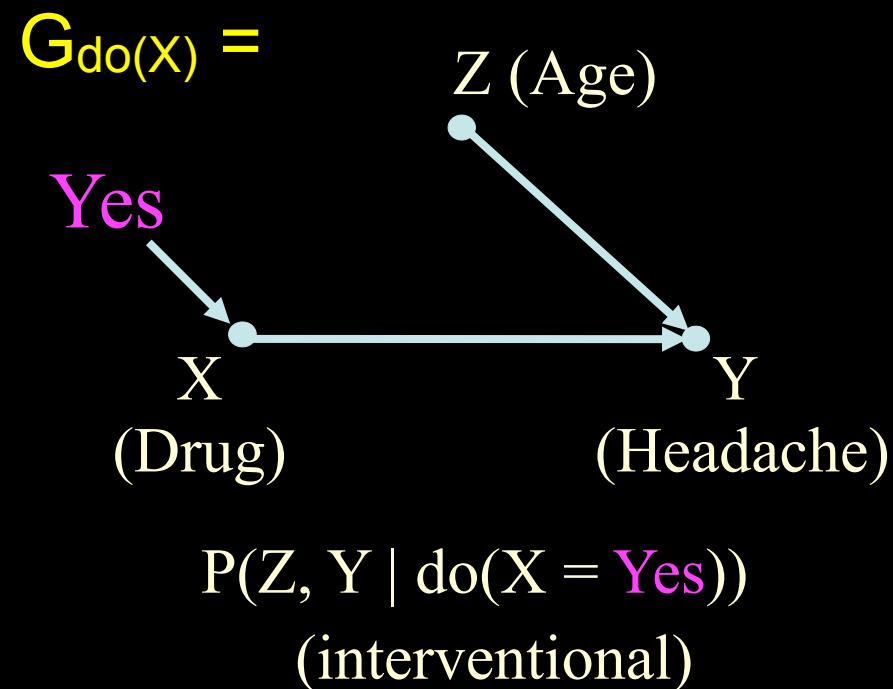
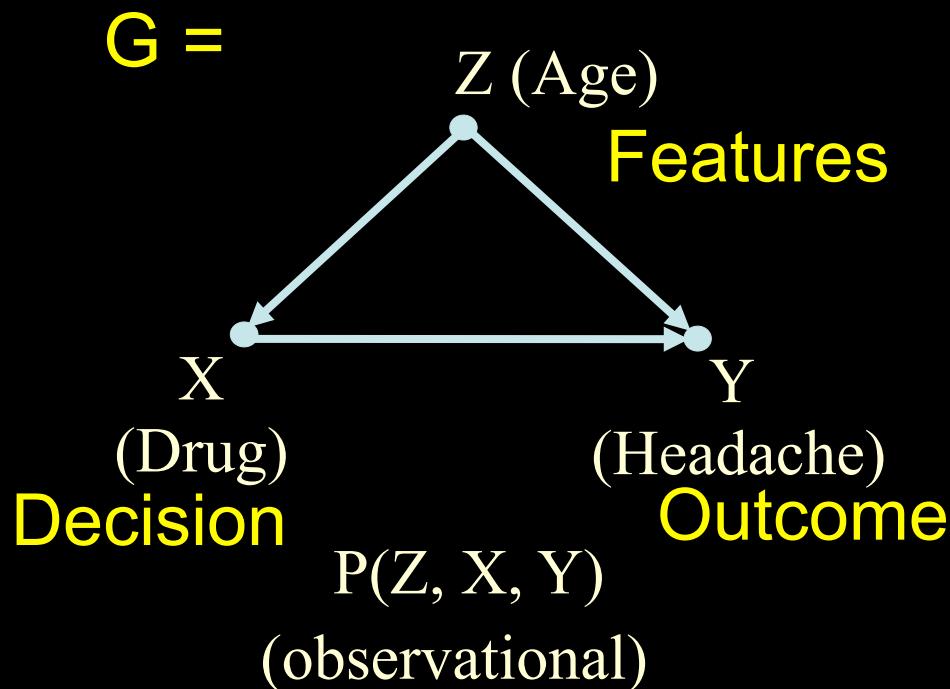
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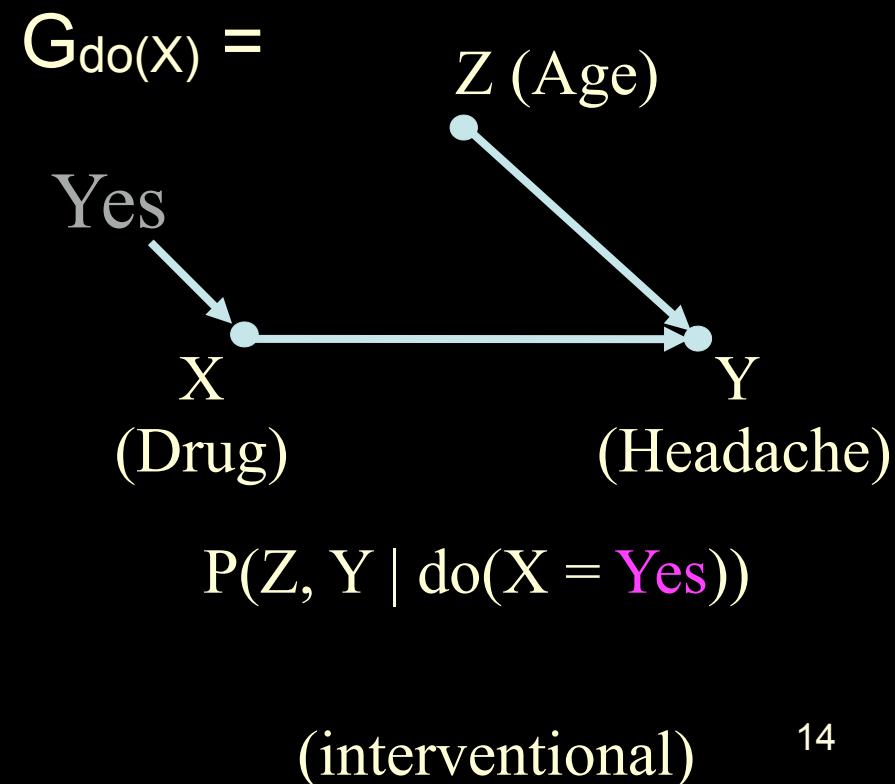
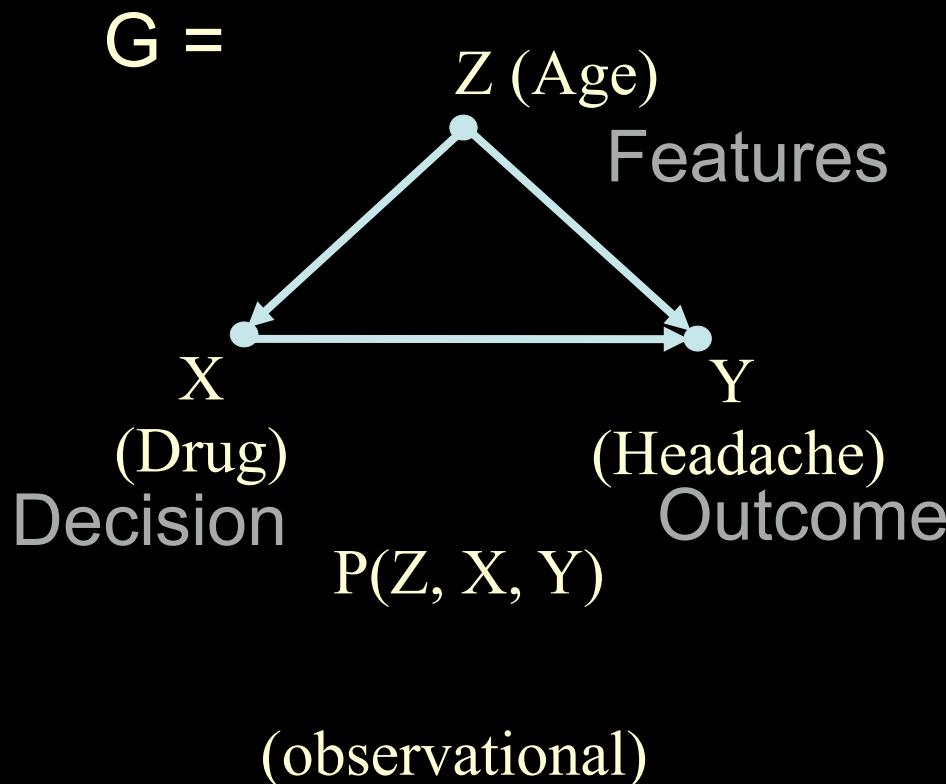
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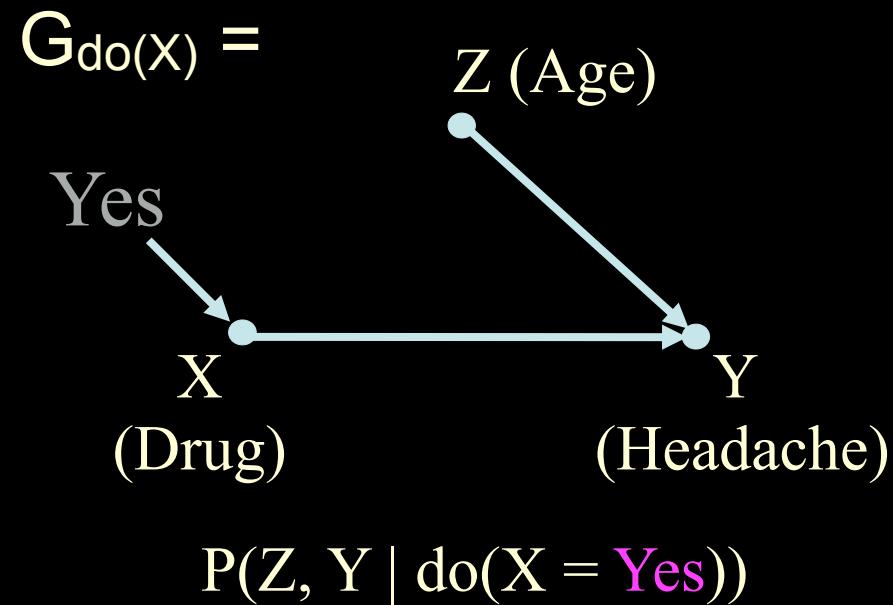
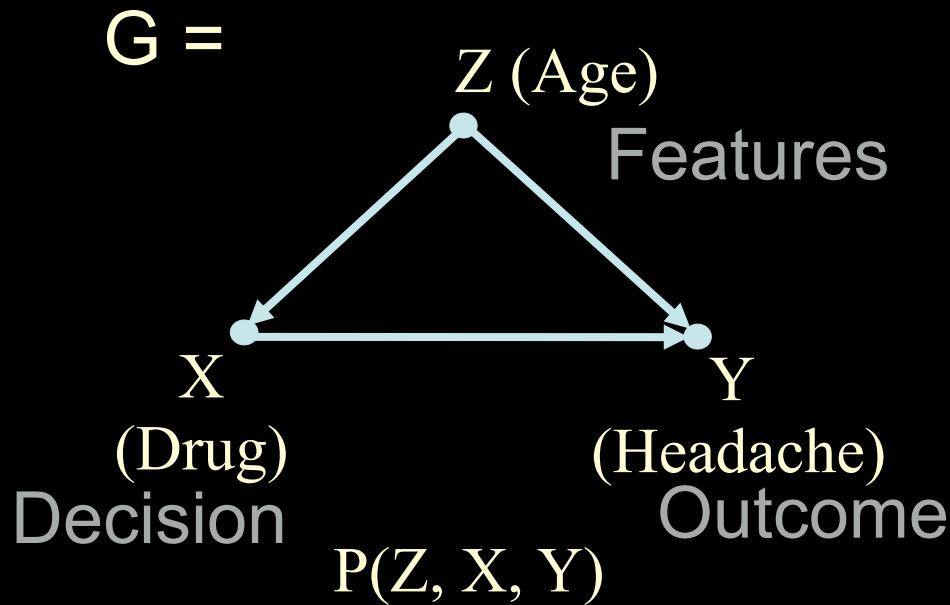
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Seeing



Doing

STRUCTURAL CAUSAL MODELS

Definition: A **structural causal model M** (or, data generating model) is a tuple $(V, U, F, P(u))$, where

- $V = \{V_1, \dots, V_n\}$ are endogenous variables,
- $U = \{U_1, \dots, U_m\}$ are exogenous variables,
- $F = \{f_1, \dots, f_n\}$ are functions determining V ,
for each $V_i, V_i \leftarrow f_i(Pa_i, U_i)$, where $Pa_i \subset V, U_i \subset U$.
- $P(u)$ is a distribution over U .

(Axiomatic characterization [Halpern, Galles, Pearl, 1998].)

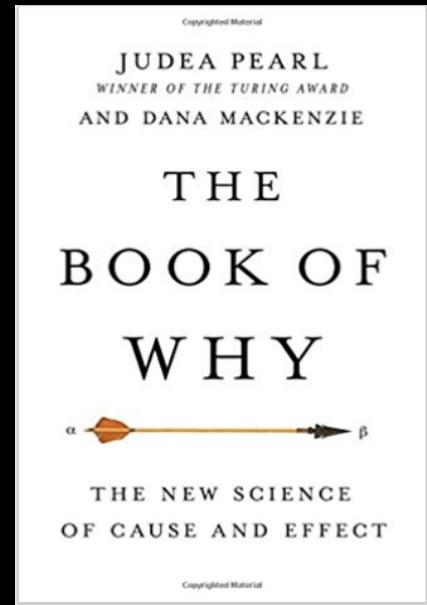
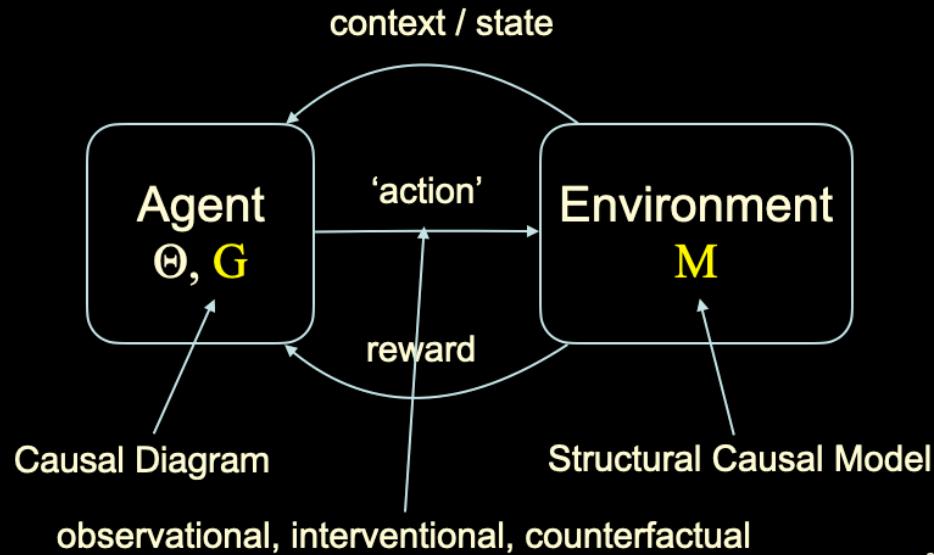
Prop. SCM M implies Pearl Causal Hierarchy (PCH).

PEARL CAUSAL HIERARCHY (PCH)

PEARL CAUSAL HIERARCHY (PCH)

(LADDER OF CAUSATION)

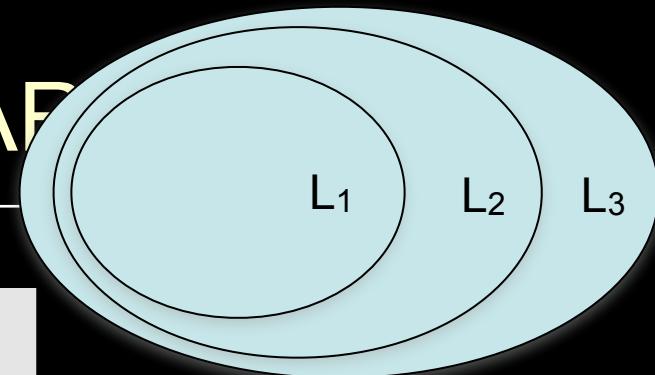
Causal RL - Big Picture



SCM → PEARL CAUSAL HIERARCHY (PCH)

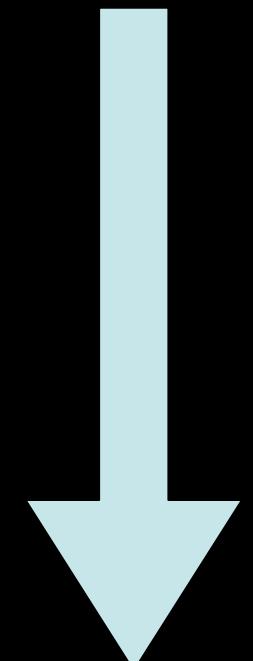
Layer (Symbol)	Typical Activity	Typical Question	Examples
L ₁  Associational P(y x)	Seeing ML - (Un)Supervised DT, Bayes net, Regression, NN	What is? How would seeing X change my belief in Y?	What does a symptom tell us about the disease?
L ₂  Interventional P(y do(x), c)	Doing ML - Reinforcement Causal BN, MDP	What if? What if I do X?	What if I take aspirin, will my headache be cured?
L ₃  Counterfactual P(y _x x', y')	Imagination, Introspection Structural Causal Model	Why? What if I had acted differently?	Was it the aspirin that stopped my headache?

SCM → PEARL CAUSAL HIERARCHY



Layer (Symbol)	Typical Activity	Typical Question
L ₁ Associational $P(y x)$	Seeing ML - (Un)Supervised DT, Bayes net, Regression, NN	What is? How would seeing X char my belief in Y'
L ₂ Interventional $P(y \text{do}(x), c)$	Doing ML - Reinforcement Causal BN, MDP	What if? What if I do X'
L ₃ Counterfactual $P(y_x x', y')$	Imagination, Introspection Structural Causal Model	Why? What if I had acted different

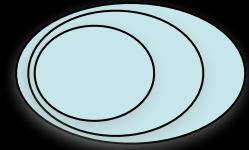
less detailed



more detailed

description of environment

CAUSAL HIERARCHY THEOREM



[Bareinboim, Correa, Ibeling, Icard, 2020]

Given that an SCM $M \rightarrow PCH$, we can show the following:

Theorem (CHT). With respect to Lebesgue measure over (a suitable encoding of L_3 -equivalence classes of) SCMs, the subset in which any PCH ‘collapse’ is measure zero.

Informally, for almost any SCM (i.e., almost any possible environment), the PCH does not collapse, i.e., the layers of the hierarchy remains distinct.



Corollary. To answer question at Layer i (about a certain interaction), one needs knowledge at layer i or higher.

WHY IS CAUSAL INFERENCE “NON-TRIVIAL”? SCMs ARE ALMOST NEVER OBSERVED

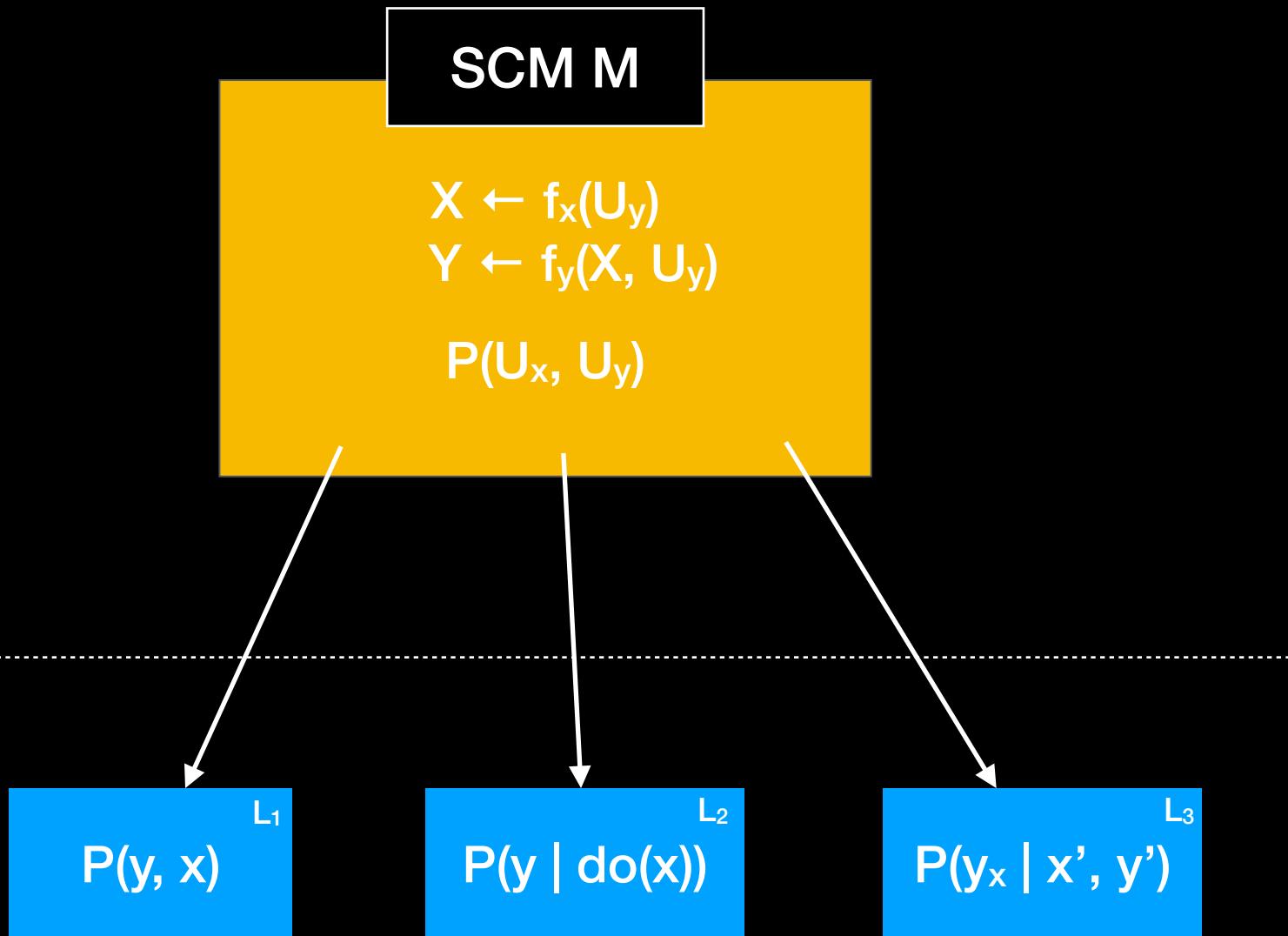
SCM M

$$X \leftarrow f_X(U_y)$$

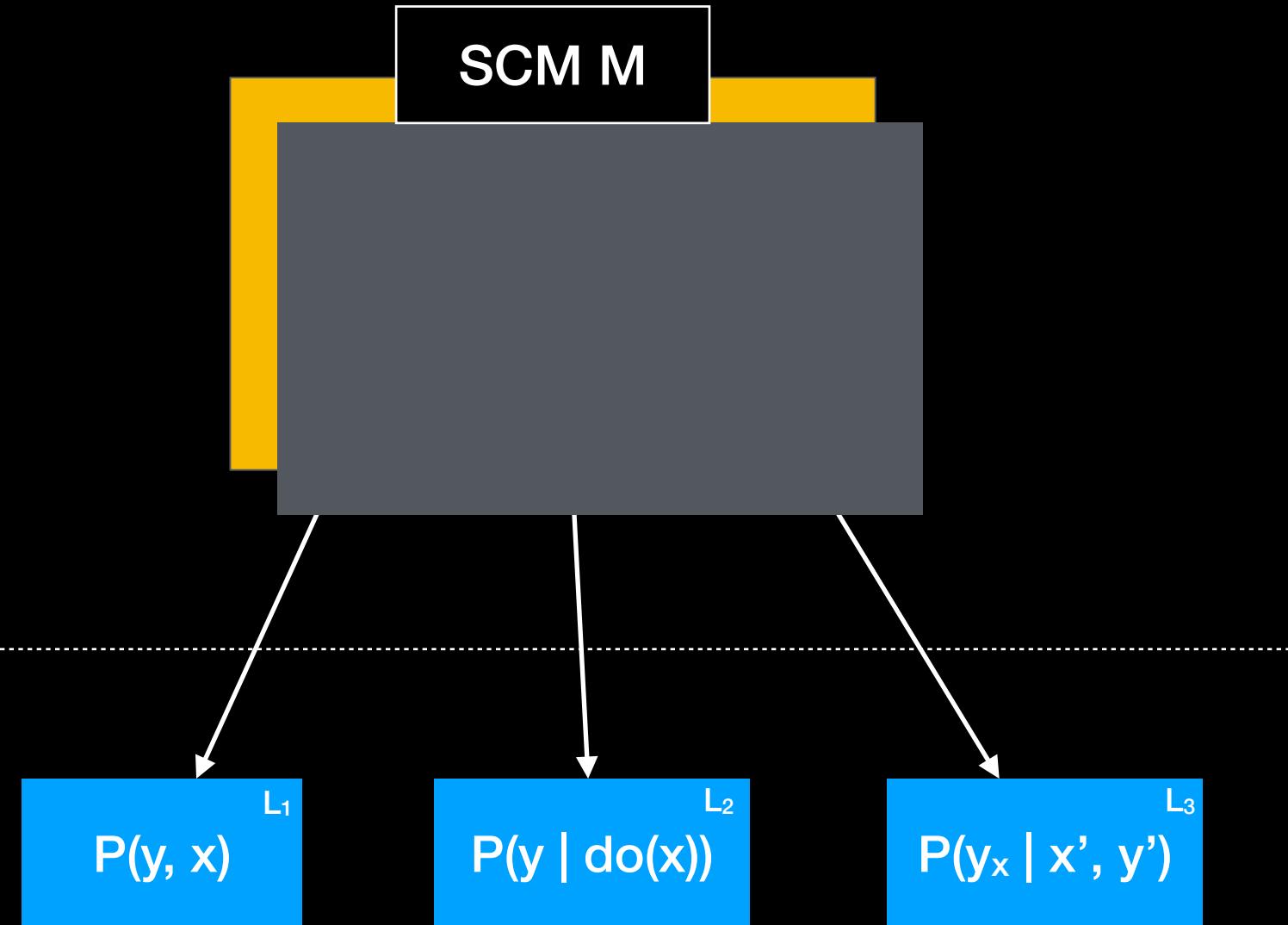
$$Y \leftarrow f_y(X, U_y)$$

$$P(U_x, U_y)$$

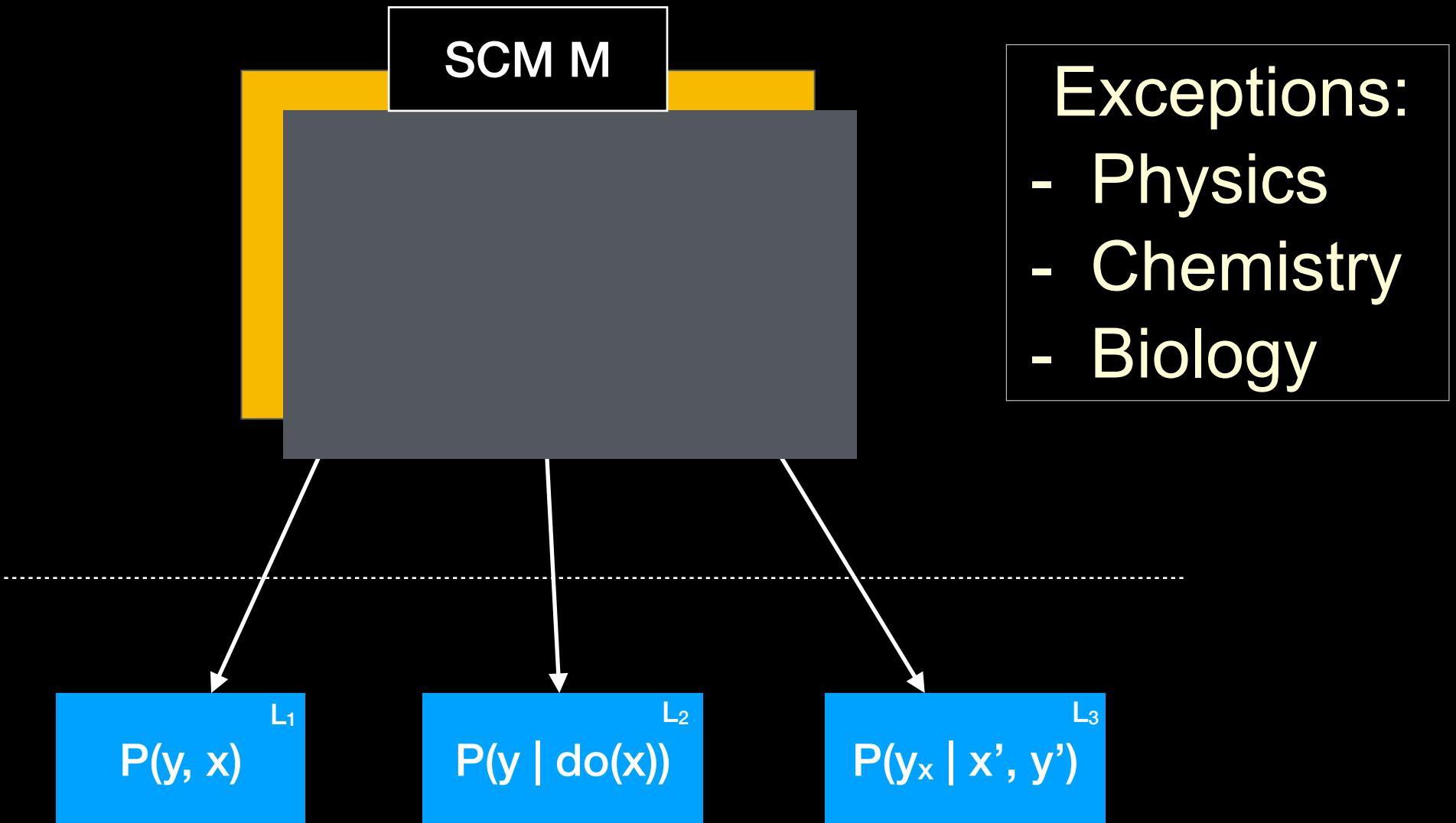
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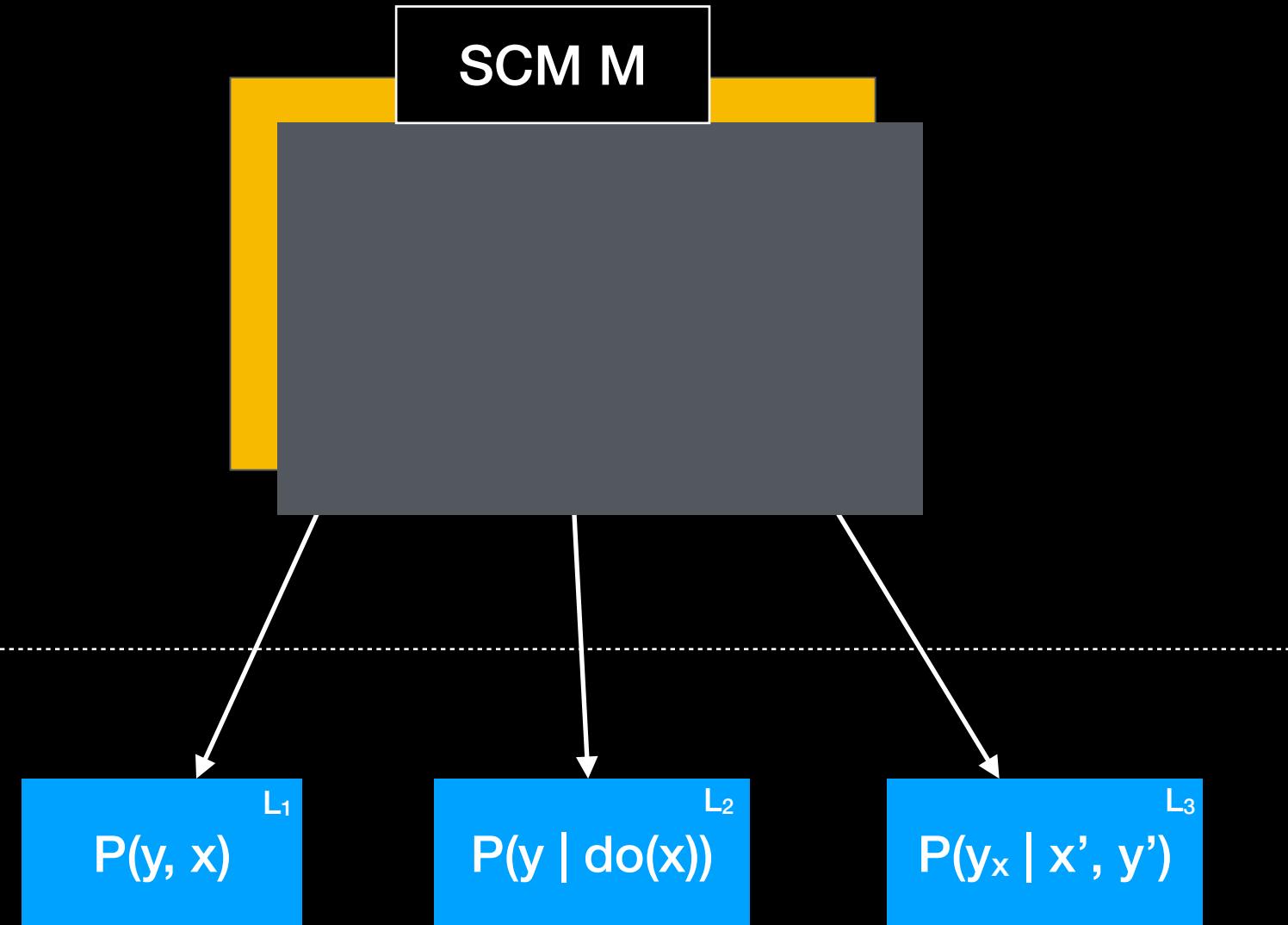
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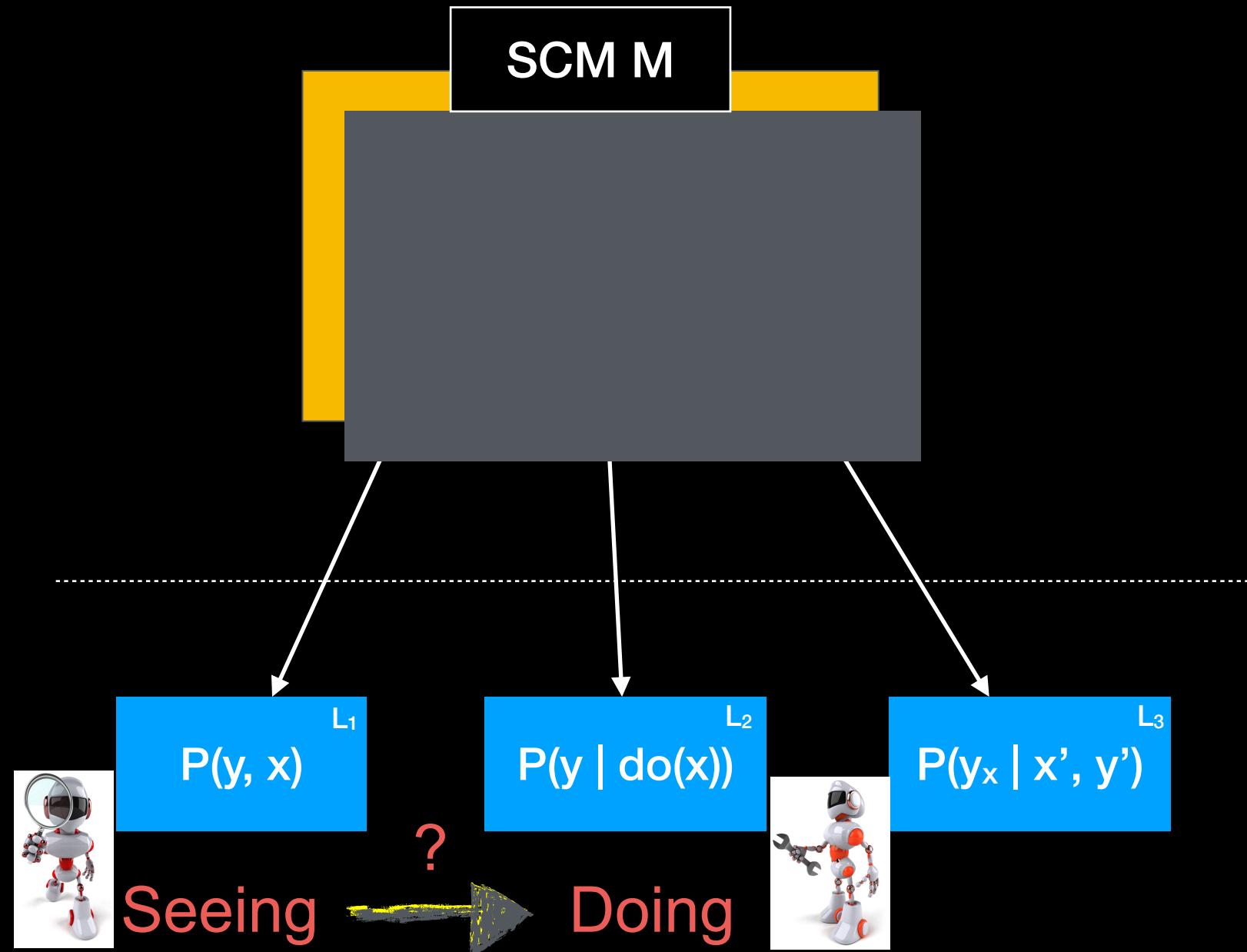
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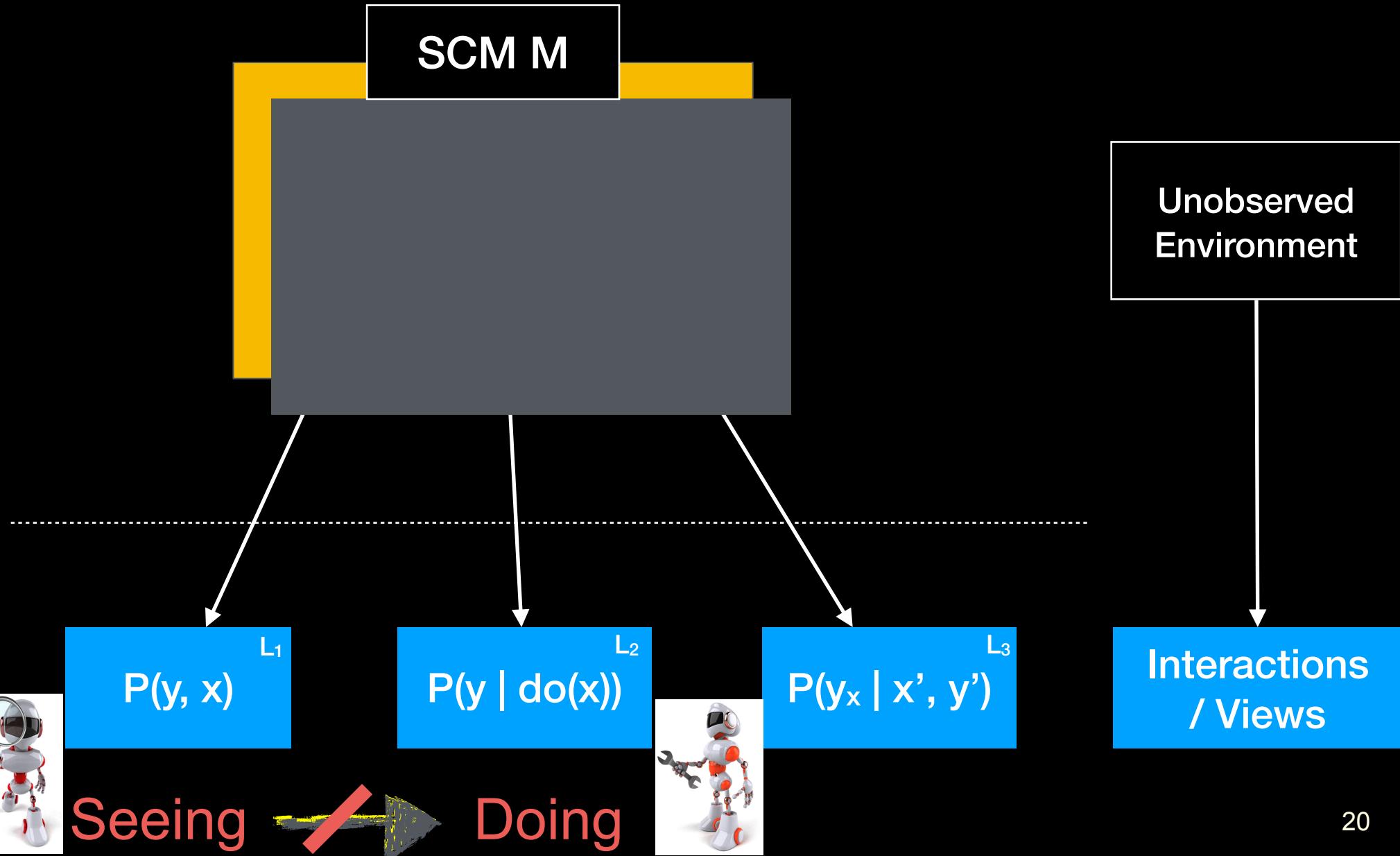
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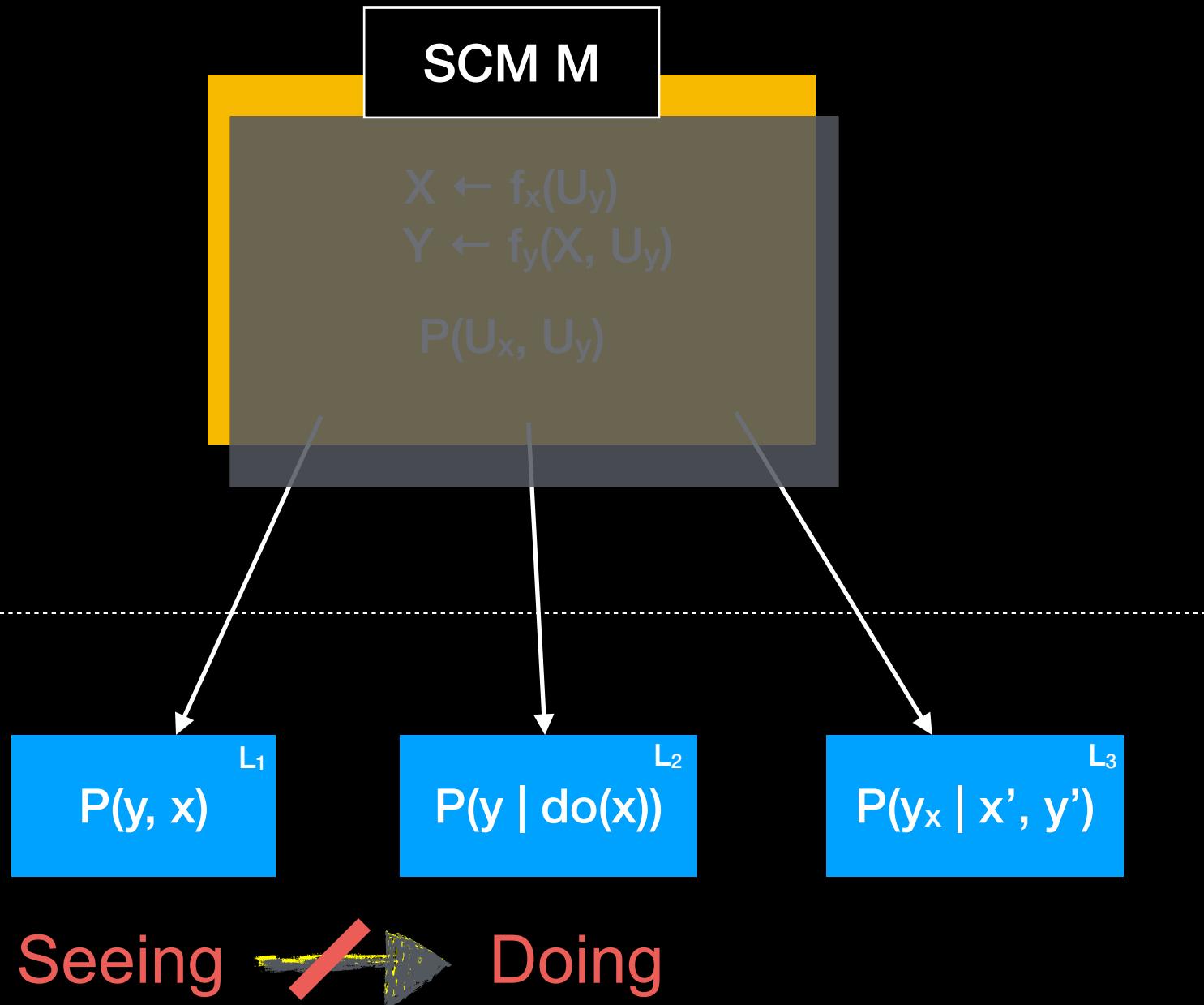
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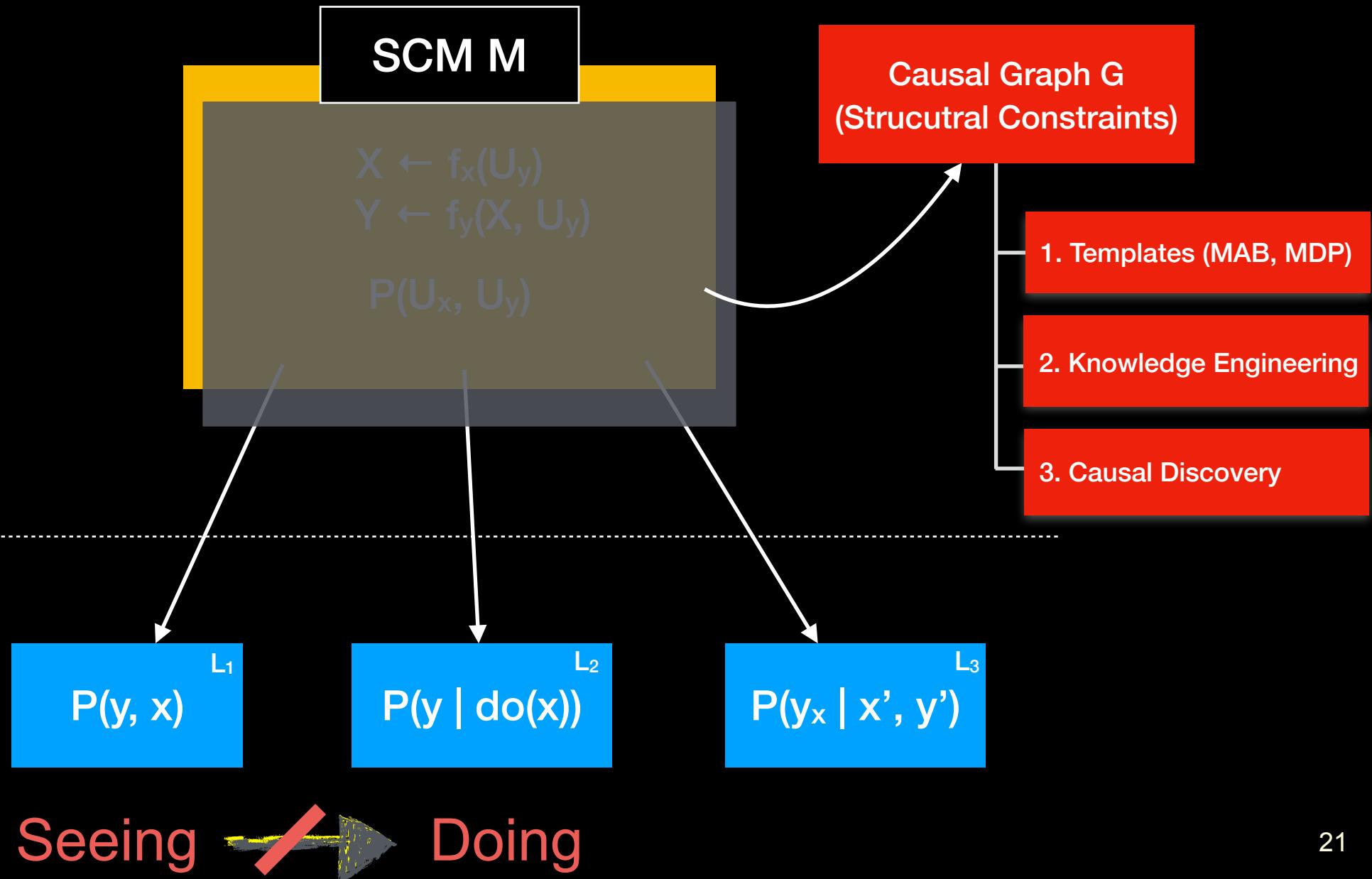
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ENCODING STRUCTURAL CONSTRAINTS — CLASSES OF CAUSAL GRAPHS



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KEY POINTS (SO FAR)

- The environment (mechanisms) can be modeled as an SCM
 - SCM M (specific environment) is rarely observable
- Still, each SCM M can be probed through qualitatively different types of interactions (distributions) -- the PCH -- i.e.:
 - L_1 : Observational
 - L_2 : Interventional
 - L_3 : Counterfactual
- CHT (Causal Hierarchy Thm.): For almost any SCM, lower layers (say, L_i) underdetermines higher layers (L_{i+1}).
 - This delimits what an agent can infer based on the different types of interactions (and data) it has with the environment;
 - For instance, from passively observing the environment (L_1), it cannot infer how to act (L_2).
 - From intervening in the environment (L_2), it can't infer how things would have been had she acted differently (L_3).
- Causal Graph G is a surrogate of the invariances of the SCM M.

CURRENT METHODS IN RL & CI THROUGH CRL LENS

REINFORCEMENT LEARNING AND CAUSAL INFERENCE

Goal: Learn a policy Π s.t. sequence of actions $\Pi(\cdot) = (X_1, X_2, \dots, X_n)$ maximizes reward $E_{\Pi}[Y | \text{do}(X)]$.

Current strategies found in the literature (circa 2020):

1. Online learning

- Agent performs experiments herself
- Input: experiments $\{(do(X_i), Y_i)\}$; Learned: $P(Y | \text{do}(X))$

2. Off-policy learning

- Agent learns from other agents' actions
- Input: samples $\{(do(X_i), Y_i)\}$; Learned: $P(Y | \text{do}(X))$

3. Do-calculus learning

- Agent observes other agents acting
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3. Do-calculus learning ($\text{👀} \rightarrow \text{💪}$)

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- Agent performs experiments herself
- Input: experiments $\{(do(X_i), Y_i)\}$; Learned: $P(Y | \text{do}(X))$

2. Off-policy learning ($\text{do}(x) \rightarrow \text{do}(x)$)

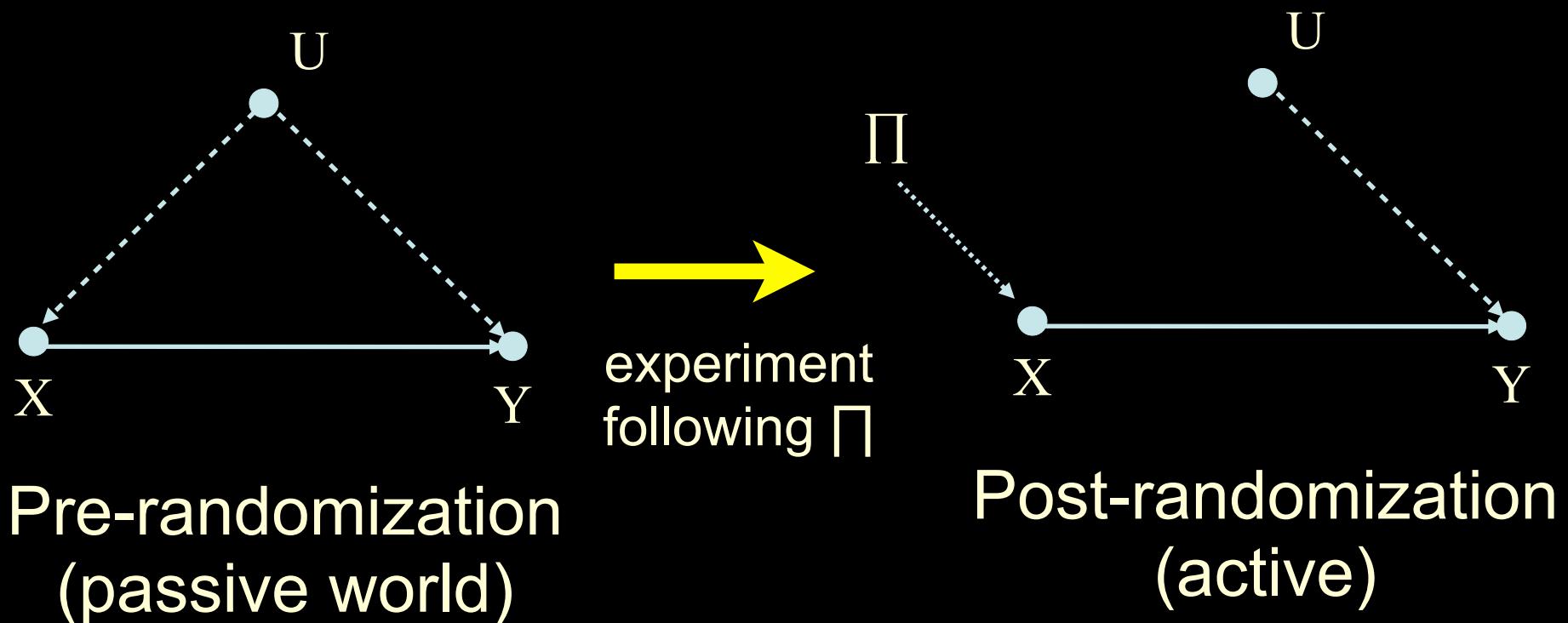
- Agent learns from other agents' actions
- Input: samples $\{(do(X_i), Y_i)\}$; Learned: $P(Y | \text{do}(X))$

3. Do-calculus learning ($\text{see}(v) \rightarrow \text{do}(x)$)

- Agent observes other agents acting
- Input: samples $\{(X_i, Y_i)\}$, G ; Learned: $P(Y | \text{do}(X))$

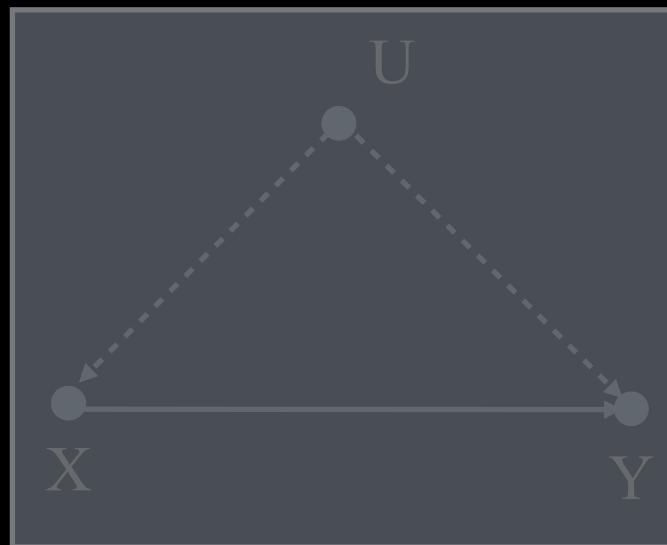
1. ONLINE LEARNING

- Finding x^* is immediate once $E[Y | \text{do}(X)]$ is learned.
- $E[Y | \text{do}(X)]$ can be estimated through randomized experiments or adaptive strategies.
 - Pros: Robust against unobserved confounders (UCs)
 - Cons: Experiments can be expensive or impossible

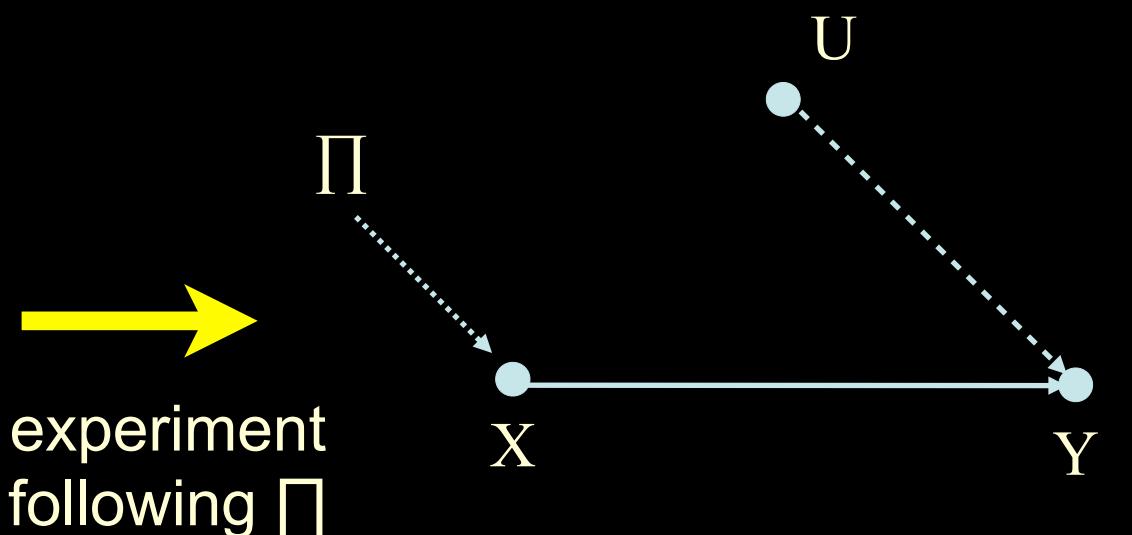


1. ONLINE LEARNING

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Pre-randomization
(passive world)

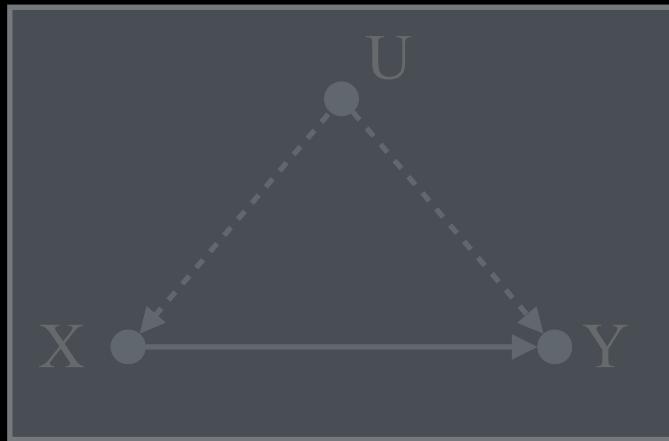


Post-randomization
(active)

* More details: [Fisher, 1936; Auer et al., 2002; Jaksch et al., 2010; Lattimore et al., 2016]. 25

1. ONLINE LEARNING

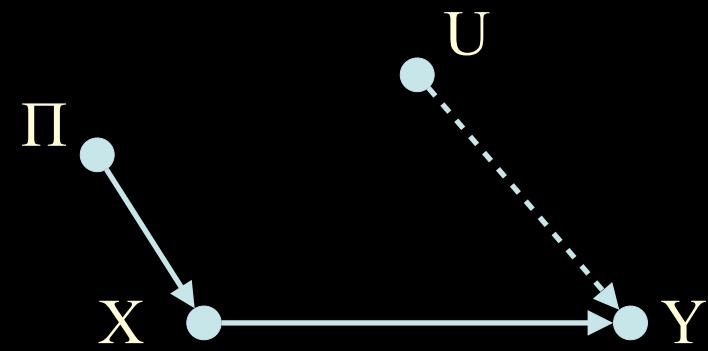
(interventional learning)



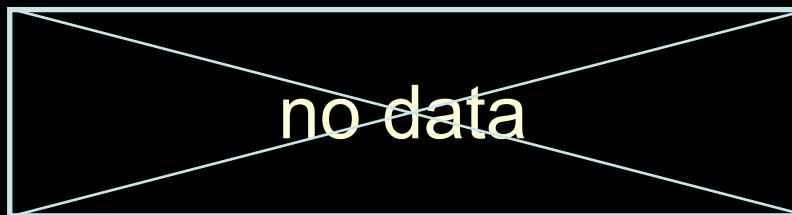
Pre-randomization
world (passive)



experiment
following Π



under $\text{do}(X)$

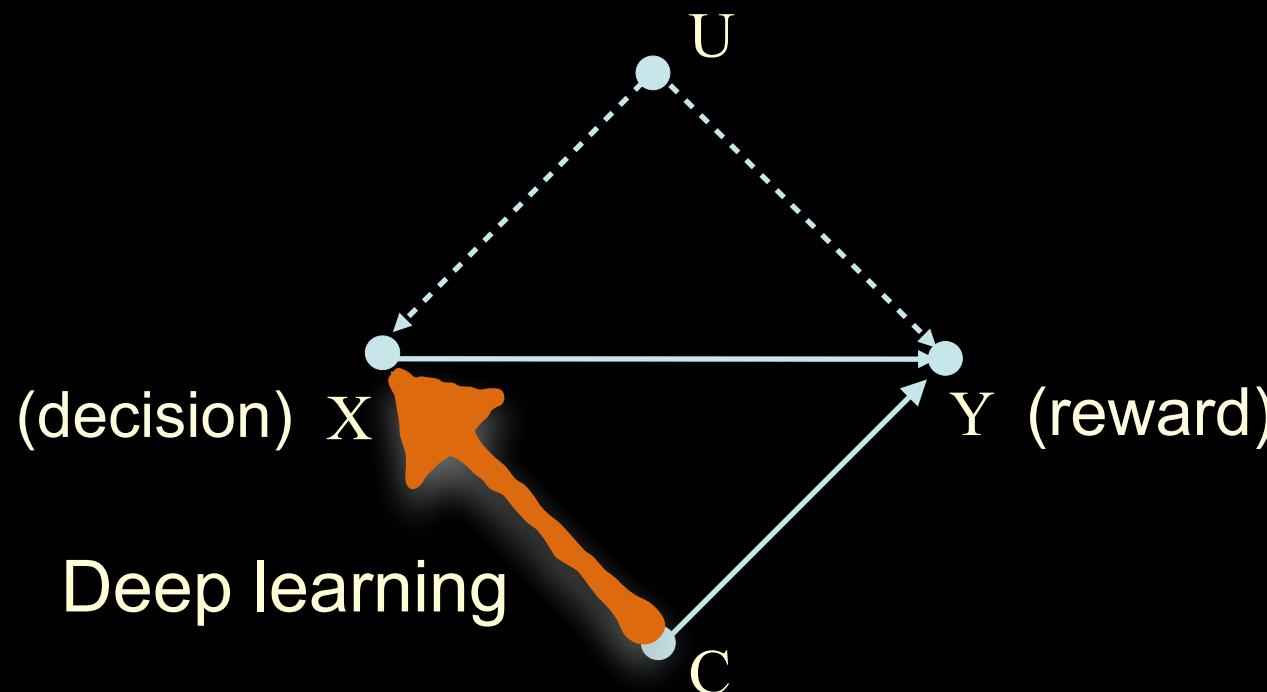


$\text{do}(x_0) \text{ do}(x_1) \dots \text{ do}(x_0)$

* Online learning can be improved thr. causal machinery [ZB, ICML'20].

NOTE: COVARIATE-SPECIFIC CAUSAL EFFECTS (CONTEXTUAL)

- Model can be augmented to accommodate set of observed covariates C (also known as context); U is the set of (remaining) unobserved confounders (UCs).

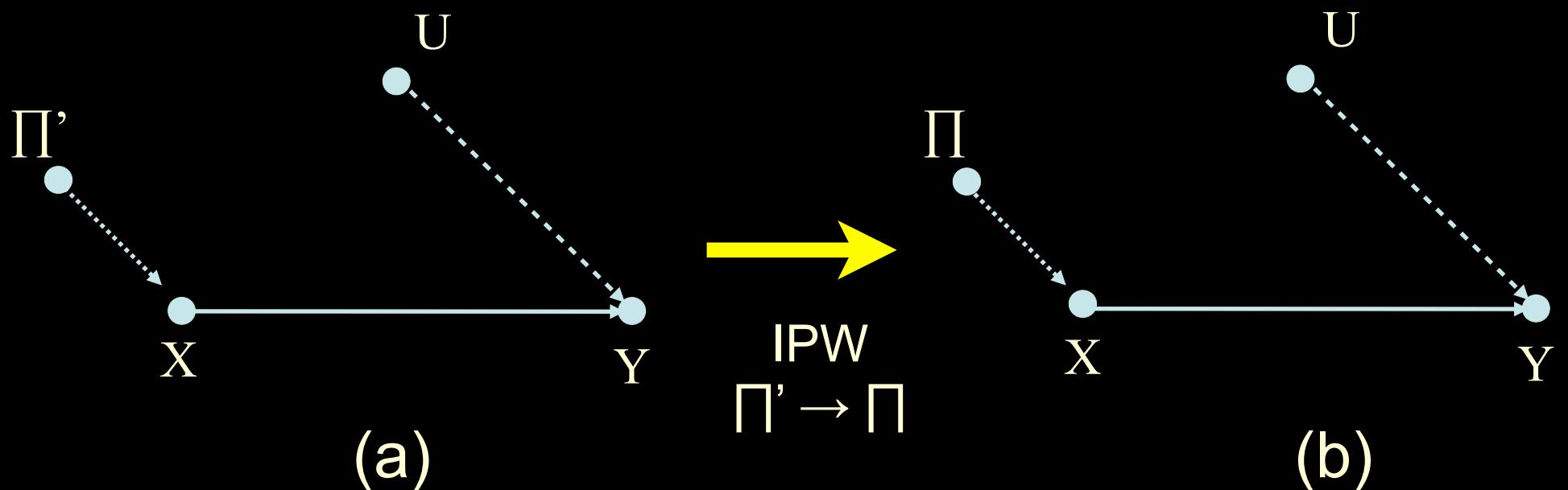


» Challenge:
high-dimensional C

- Goal: learn a policy $\Pi(c)$ so as to optimize based on the c -specific causal effect, $P(Y | \text{do}(X), C = c)$.

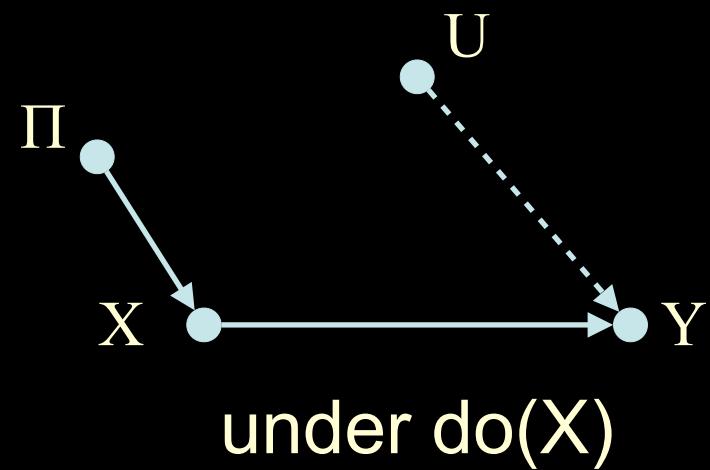
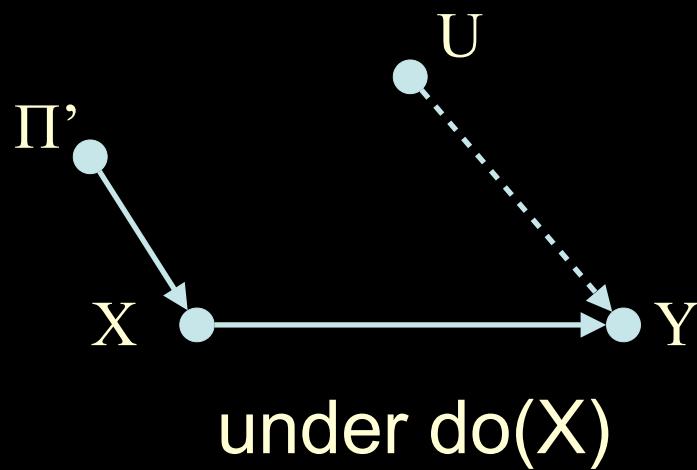
2. OFF-POLICY LEARNING

- $E[Y | \text{do}(X)]$ can be estimated through experiments conducted by other agents and different policies.
 - **Pros:** no experiments need to be conducted
 - **Cons:** rely on assumptions that (a₁) same variables were randomized and (a₂) context matches (e.g., $C = \{\}$).



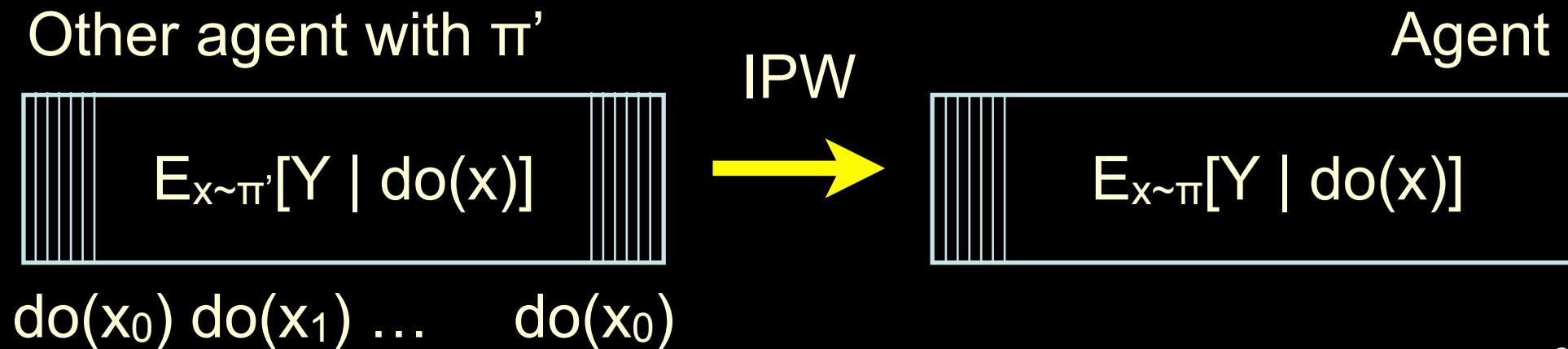
* More details: [Watkins & Dayan, 1992; Dudik et al., 2011; Jiang & Li, 2016].

2. OFF-POLICY LEARNING



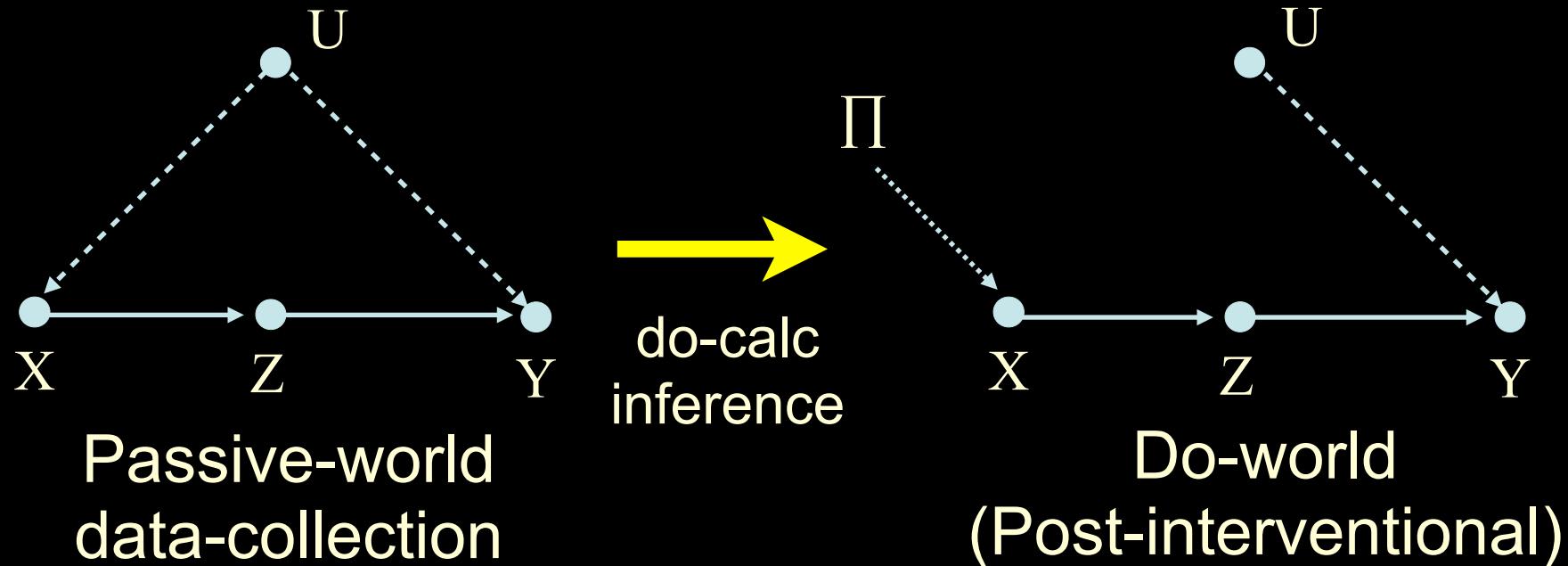
$$P_{\Pi}(y \mid do(x)) = \sum_{x,c} P_{\Pi'}(y, x, c) \frac{P_{\Pi}(x \mid c)}{P_{\Pi'}(x \mid c)}$$

A lot of work here
since the variance
may blow up...



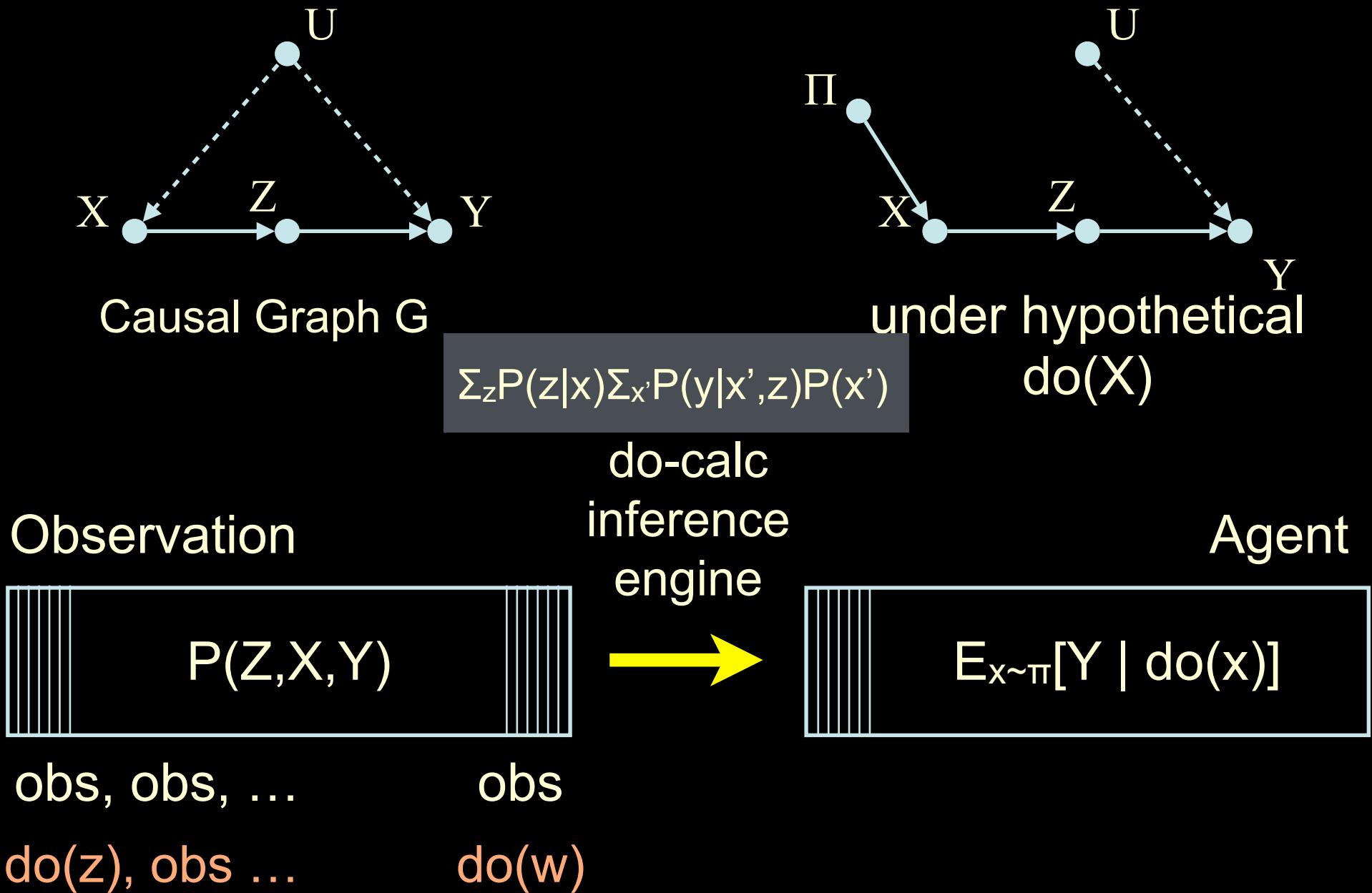
3. DO-CALCULUS LEARNING*

- $E[Y | \text{do}(X)]$ can be estimated from non-experimental data (also called *natural / behavioral regime*)
 - **Pros:** estimation is feasible even when context is unknown and experimental variables do not match (i.e., off-policy assumptions are violated).
 - **Cons:** Results are contingent on the model; for weak models, effect is not uniquely computable (not ID).



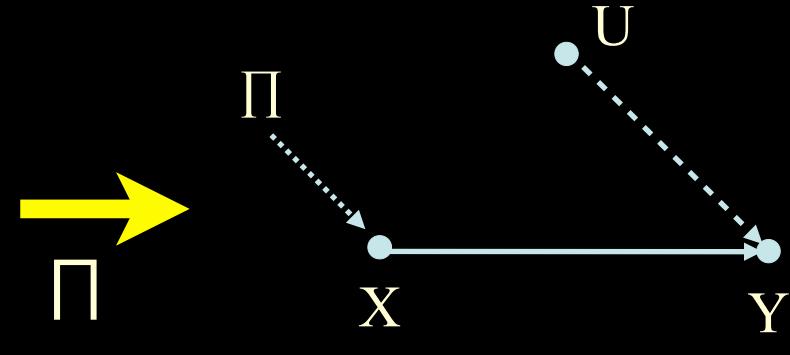
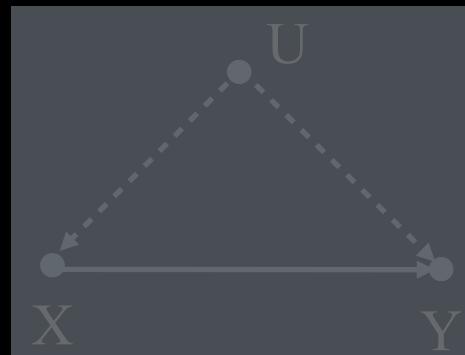
* For details, see data-fusion survey [Bareinboim & Pearl, PNAS'2016].

3. DO-CALCULUS LEARNING

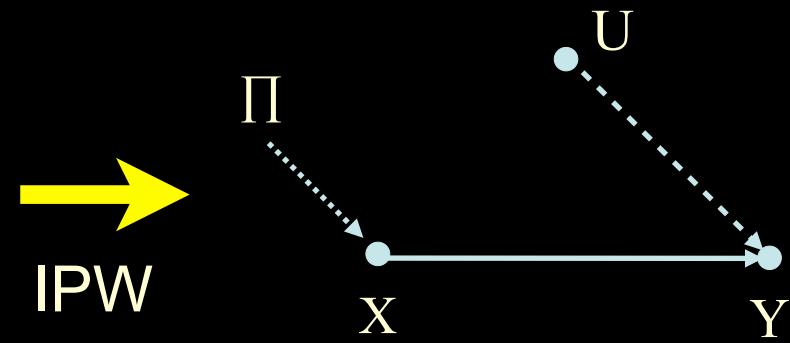
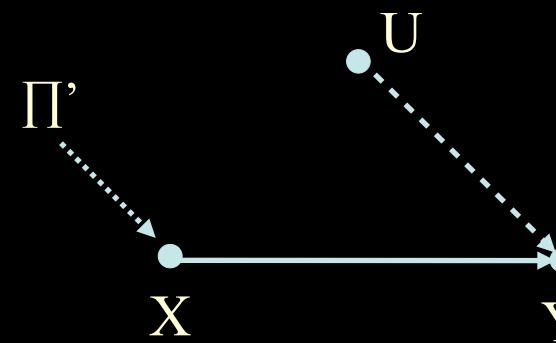


SUMMARY RL-CAUSAL (CIRCA 2020)

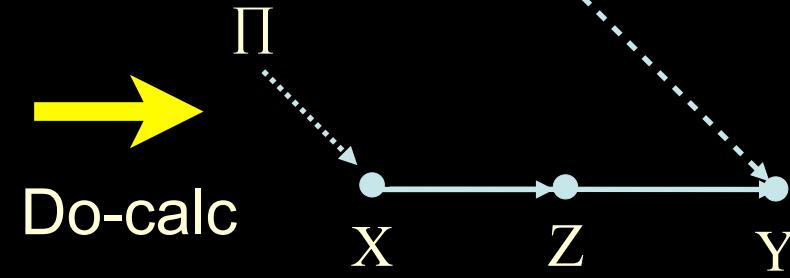
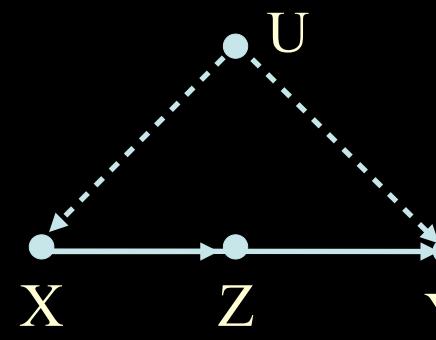
1. Online
 $(\rightarrow \text{do}_{\Pi}(x))$



2. Off-policy
 $(\text{do}_{\Pi'}(x) \rightarrow \text{do}_{\Pi}(x))$



3. Do-calculus
 $(\text{see}(\cdot) \rightarrow \text{do}_{\Pi}(x))$



Do these strategies always work?



IS LEARNING IN INTERACTIVE
SYSTEMS ESSENTIALLY DONE?

IF NOT, WHAT IS MISSING?

TOWARDS CAUSAL REINFORCEMENT LEARNING



CRL NEW CHALLENGES & LEARNING OPPORTUNITIES (I)

Task 1 (IJCAI'17, NeurIPS'19, ICML'20)

Generalized Policy Learning
(combining online + offline learning)

Task 2 (NeurIPS'18, AAAI'19)

When and where to intervene?
(refining the policy space)

Task 3 (NeurIPS'15, ICML'17)

Counterfactual Decision-Making
(changing optimization function based on
intentionality, free will, and autonomy)

CRL NEW CHALLENGES & LEARNING OPPORTUNITIES (II)

Task 4

(NeurIPS'14, PNAS'16, UAI'19, AAAI'20)

Generalizability & robustness of causal claims
(transportability & structural invariances)

Task 5

(NeurIPS'17, ICML'18, NeurIPS'19)

Learning causal model by combining
observations (L_1) and experiments (L_2)

Task 6

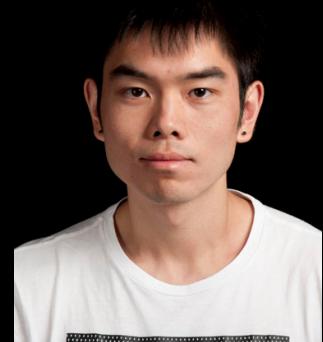
(R-66 @CausalAI)

Causal Imitation Learning

TASK 1.
GENERALIZED POLICY LEARNING
(Combining Online and Offline Learning)

TASK 1.
GENERALIZED POLICY LEARNING
(Combining Online and Offline Learning)

Junzhe Zhang



CRL-TASK 1. GENERALIZED POLICY LEARNING (GPL)

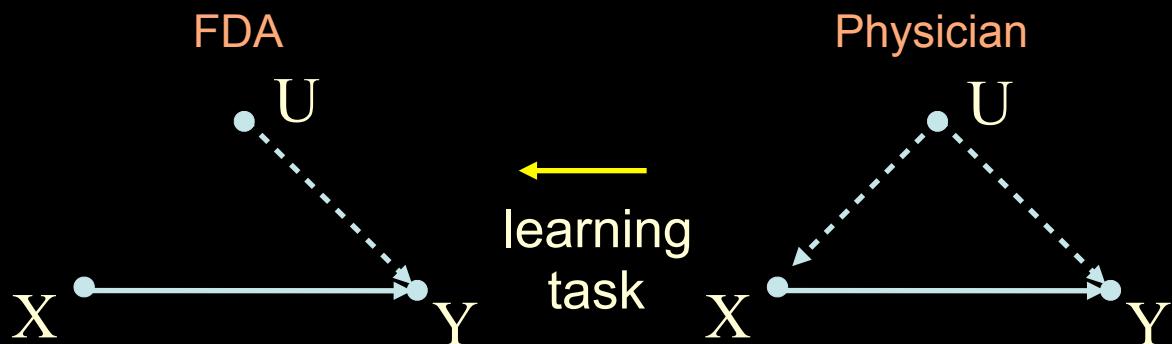
- Online learning is usually undesirable due to financial, technical, or ethical constraints. In general, one wants to leverage data collected under different conditions to speed up learning, without having to start from scratch.
- On the other hand, the conditions required by offline learning are not always satisfied in many practical, real world settings.
- In this task, we move towards realistic learning scenarios where these modalities come together, including when the most traditional, and provably necessary, assumptions do not hold.

GENERALIZED POLICY LEARNING

Task 1. Input: $P(x, y)$, learn: $P(y | \text{do}(x))$.

- Robotics: learning by demonstration when the teacher can observe a richer context (e.g., more accurate sensors).
- Medical: optimal experimental design from observational data.

- Off-policy a_2 X
- Do-calc ID X
- Online ?

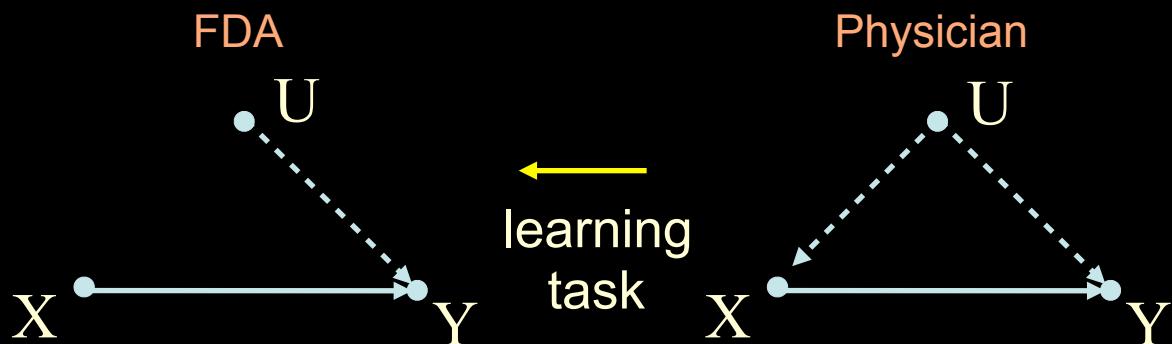


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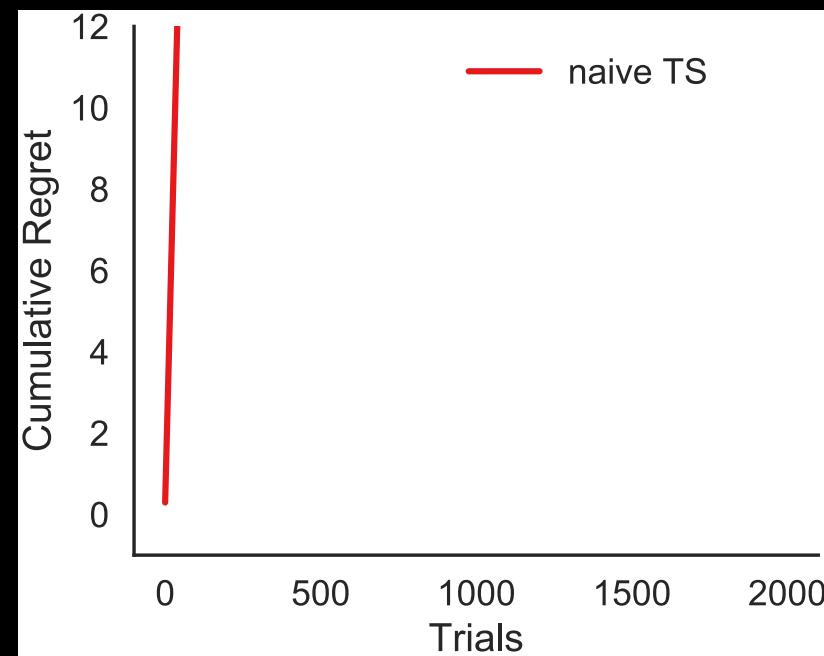
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Let's ignore their differences, and pretend that physician and FDA are exchangeable — call “naive TS”.

In other words, “naive TS” attempts to use observational data as prior.

Traditional TS means ignoring the observational data.

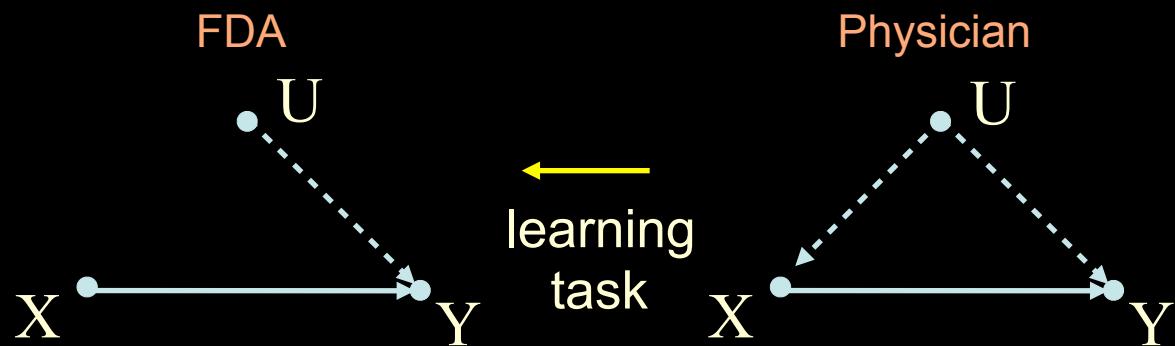


GENERALIZED POLICY LEARNING

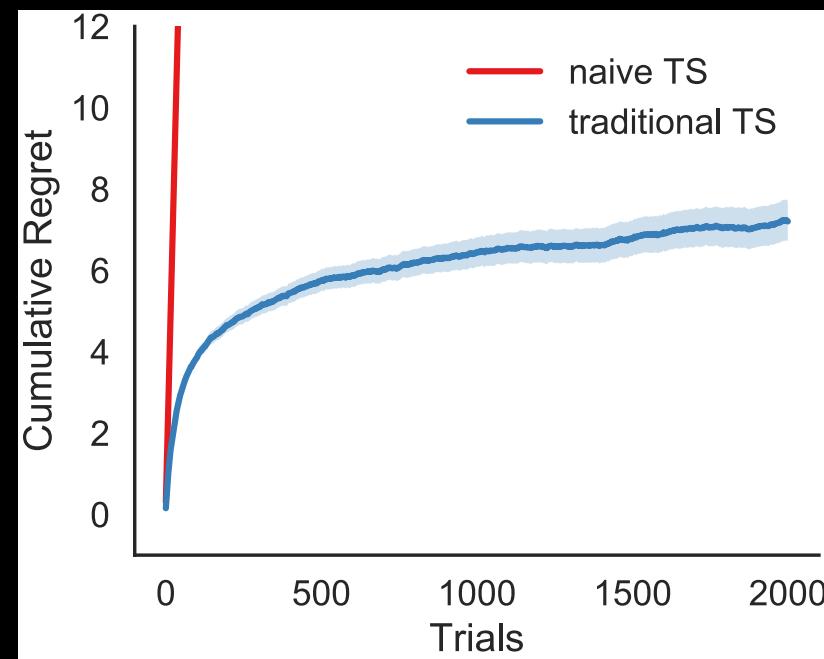
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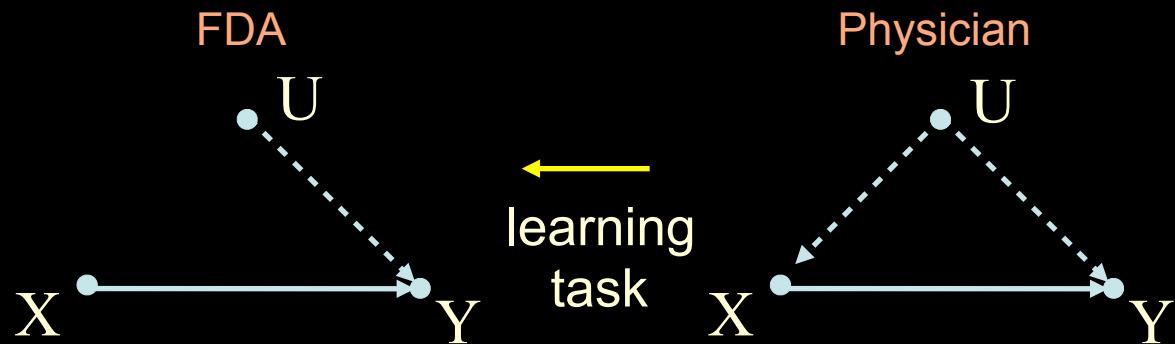
How could this be happening?!
Could more data be hurting?

GENERALIZED POLICY LEARNING

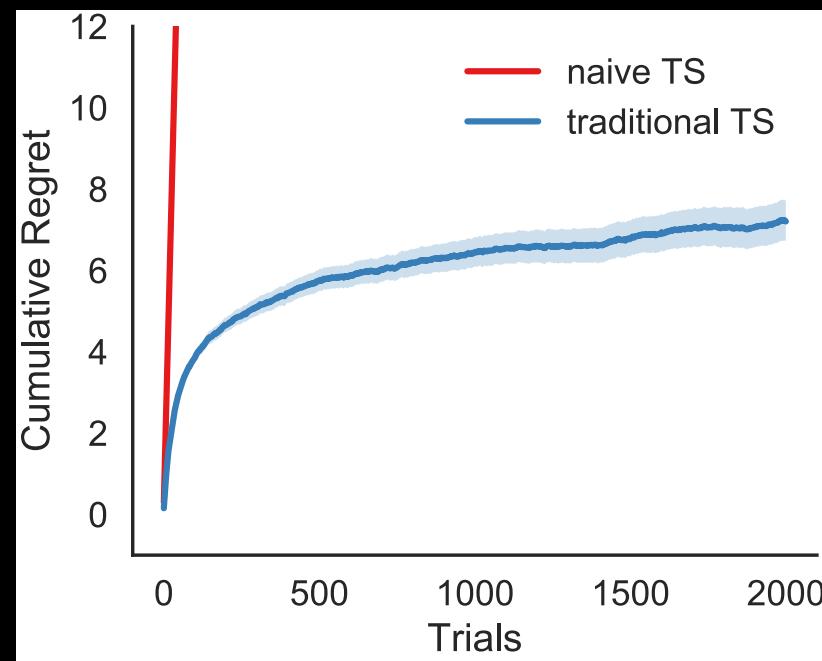
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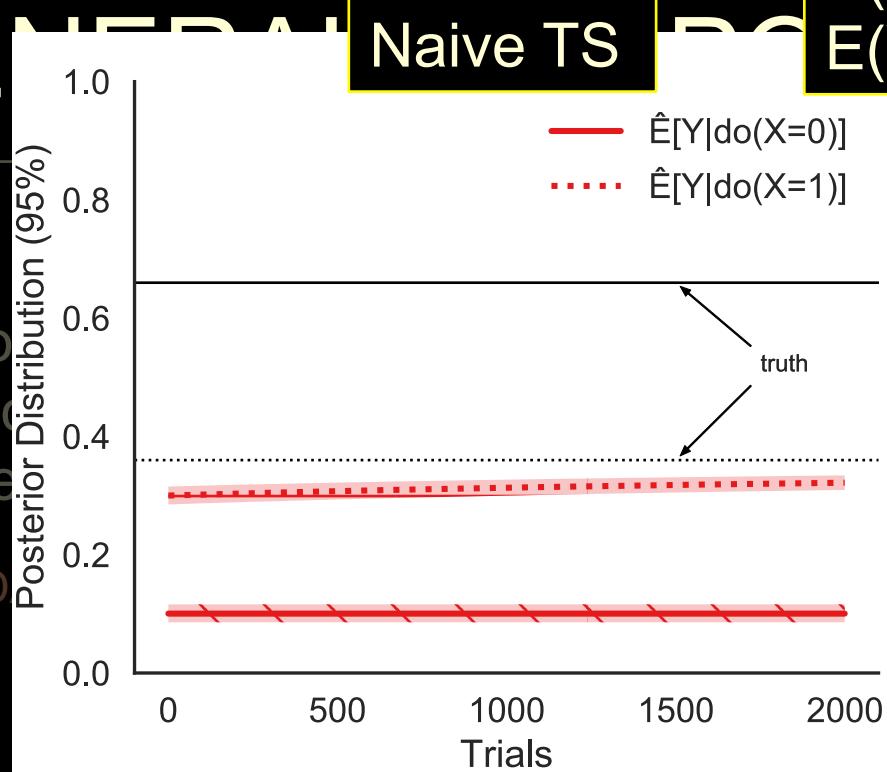
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GENERALIZING

Task

- Root
- Mean

FD



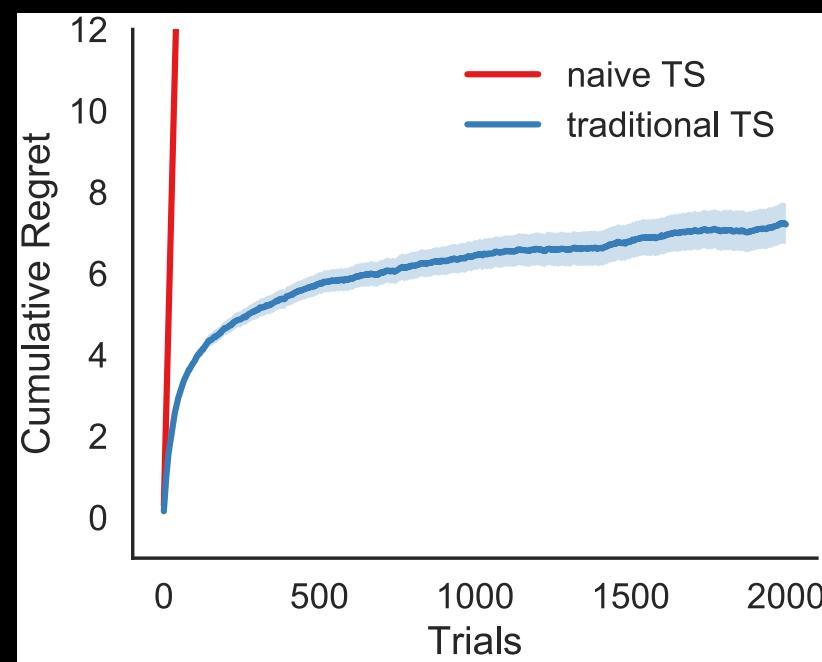
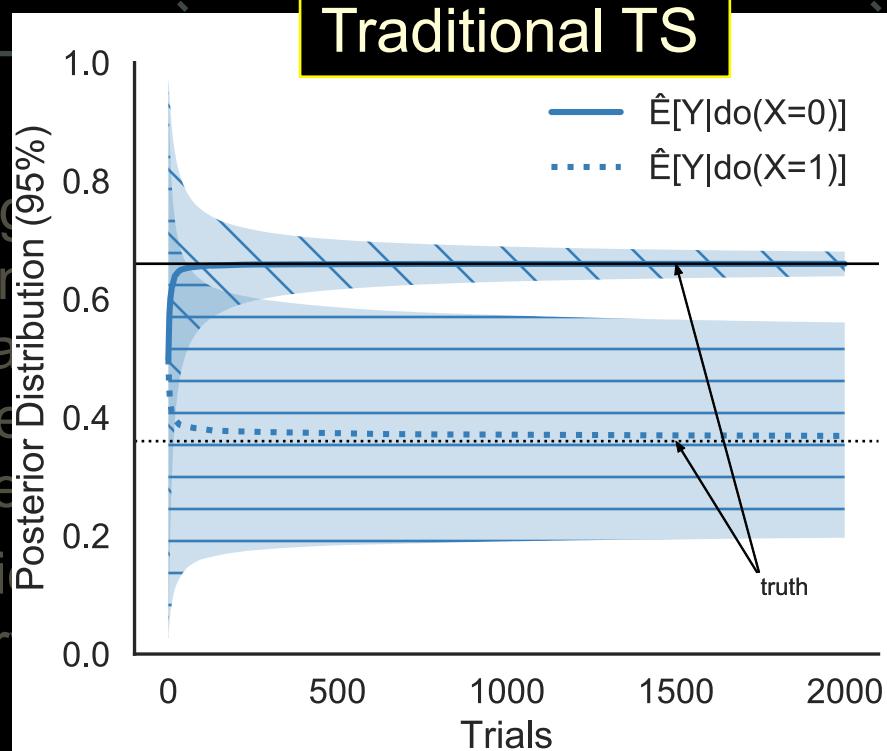
$$\begin{aligned} E(Y | X = 0) &< E(Y | X = 1) \\ E(Y | do(X = 0)) &> E(Y | do(X = 1)) \end{aligned}$$

Why is naive-TS doing so badly?

X

Let's ignore
preterm
exchange
In other
to use
Traditional
observers

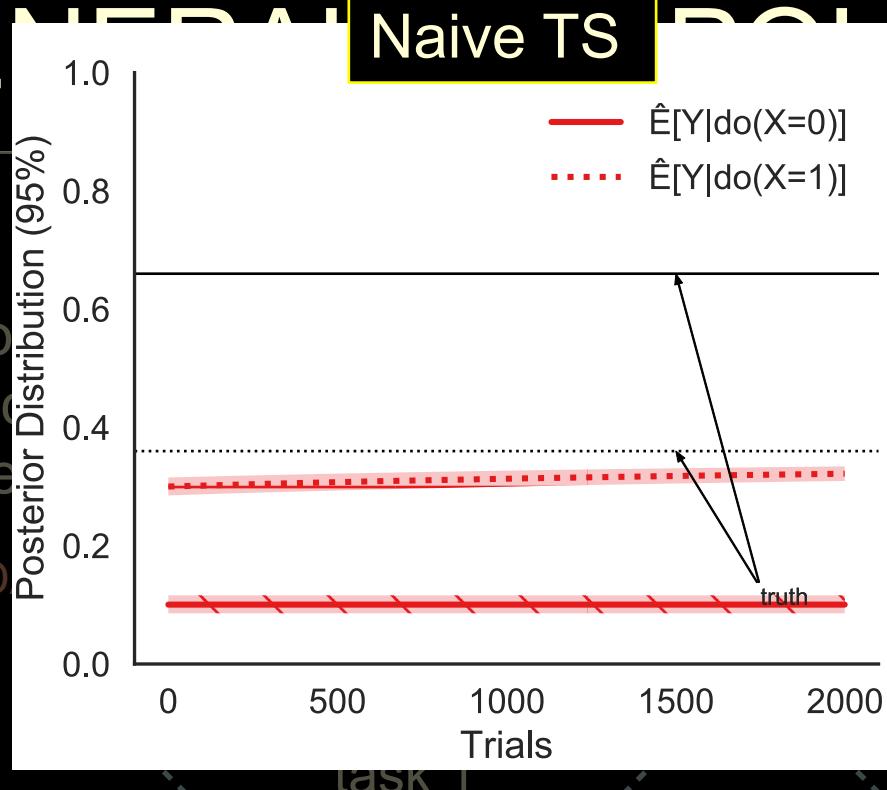
Y



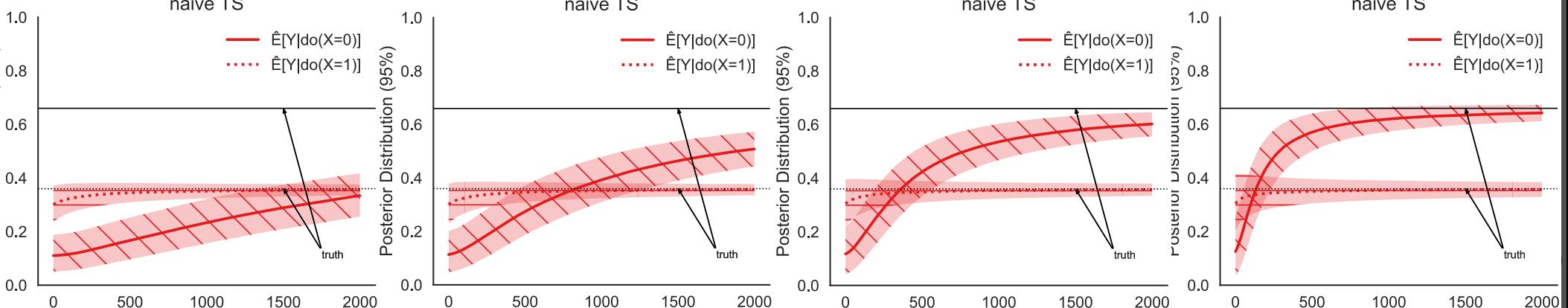
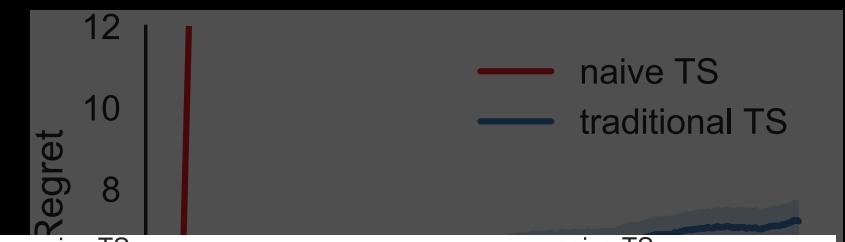
How could this be happening?!
Could more data be hurting?

GENERAL POLICY LEARNING

Task
- Rot
- Me
FD



Why is naive-TS doing so badly?



$n = 250$

200

150

100

Structural Explanation for Naive-TS's behavior

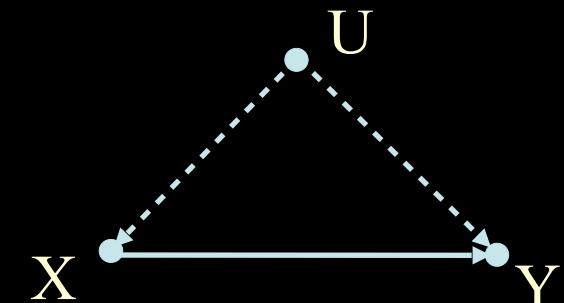
-- The Challenge of Non-Identifiability

- SCM M (Unobserved)

$X=U$
 $P(U=0)=0.3$

$P[Y X,U]$	$U=0$	$U=1$
$X=0$	0.1	0.9
$X=1$	0.5	0.3

- Causal Graph G



- Distributions



$$\begin{aligned} E(Y | X = 0) &< E(Y | X = 1) \\ E(Y | \text{do}(X = 0)) &> E(Y | \text{do}(X = 1)) \end{aligned}$$

	$E[Y \text{do}(X)]$	$E[Y X]$
$X=0$	0.66	0.1
$X=1$	0.36	0.3

L_2

L_1

Structural Explanation for Naive-TS's behavior

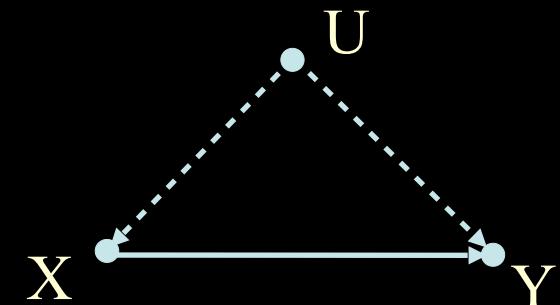
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		$E[Y \text{do}(X)]$		$E[Y X]$
$X=0$		0.66		0.1
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L_2

L_1

Structural Explanation for Naive-TS's behavior

-- The Challenge of Non-Identifiability

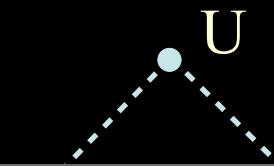
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$P[Y X,U]$	$U=0$	$U=1$
$X=0$	0.1	0.9
$X=1$		

- Causal Graph G



X=1 is looking quite good, should I do() it?

- Distributions



$$\begin{aligned} E(Y | X = 0) &< E(Y | X = 1) \\ E(Y | \text{do}(X = 0)) &> E(Y | \text{do}(X = 1)) \end{aligned}$$

		$E[Y \text{do}(X)]$		$E[Y X]$
$X=0$		0.66		0.1
$X=1$		0.36		0.3

L_2

L_1

Structural Explanation for Naive-TS's behavior

-- The Challenge of Non-Identifiability

- SCM M (Unobserved)



- Causal Graph G



Questions (more general):

1. How do I know this pattern is not present in my data? **Don't know :(**
2. Does this then imply that I should throw away all the data not collected by me (the agent) and learn from scratch? **Hopefully not...**
3. After all, is there any useful information in the obs. data? **Yes!**

Let's try to understand how to leverage confounded data...

X=0		0.66		0.1
X=1		0.36		0.39

L_2 L_1

Step 1. Extracting Causal Information from Confounded Observations

Solution: Bounding $E[Y | \text{do}(x)]$ from observations $P(x,y)$.

Theorem. Given observations coming from any distribution $P(x,y)$, the average causal effect $E[Y | \text{do}(x)]$ is bounded in $[l_x, h_x]$, where

$$l_x = E[Y | x] P(x) \quad \text{and} \quad h_x = l_x + 1 - P(x).$$

- Linear Program formulation in other causal graphs (non-parametric SCMs): [Balke & Pearl, 1996; Zhang and Bareinboim, IJCAI'17]
- Incorporating parametric knowledge: [Kallus & Zhou, 2018; Namkoong et al., 2020]
- Sequential treatments in longitudinal settings: [Zhang & Bareinboim, NeurIPS'19; ICML'20]

Step 2. Incorporating Bounds into Learning (e.g., Causal Thompson Sampling)

Input: prior parameters α, β ,
causal bounds $[l_x, h_x]$ for each arm x . /* $[l_x, h_x]$ are

Initialization: $S_x=0, F_x=0$ for each arm x

For $t = 1, \dots, T$ do

 For each x do

 Repeat

 Draw $\theta_x \sim \text{Beta}(S_x + \alpha, F_x + \beta)$.

 Until $\theta_x \in [l_x, h_x]$

 End

 Play $d(x_t)$ where $X_t = \operatorname{argmax}_x \theta_x$.

 Observed Y_t and update F_{xt} and S_{xt} .

End

computed from
confounded
observations */

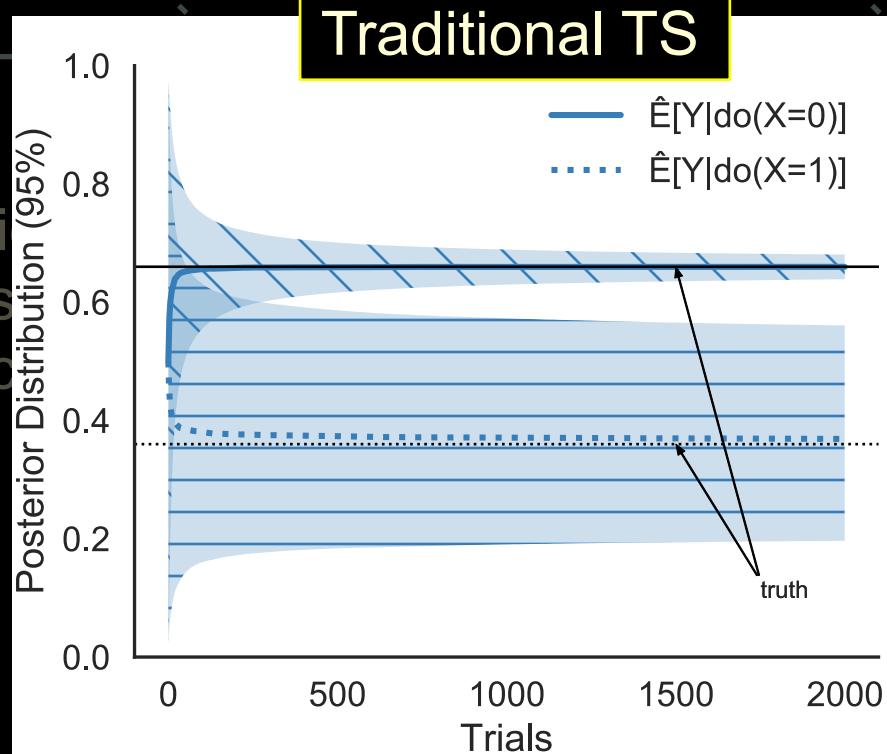
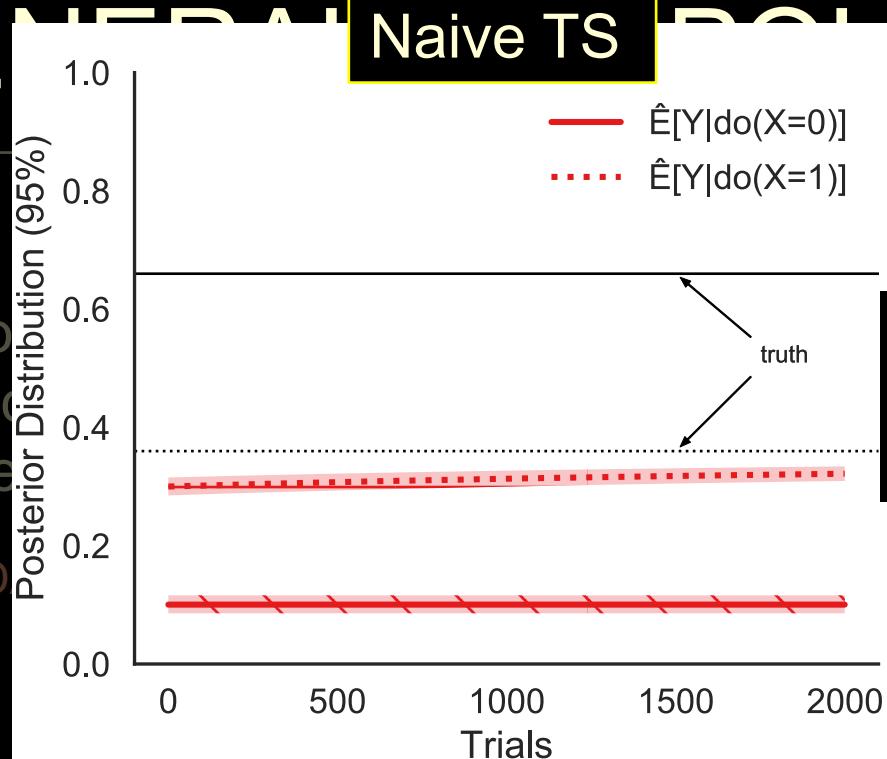
/* Causal
bounds are
ascertained thr.
a rejection
procedure. */

GENERAL POLICY LEARNING

Task

- Rollout
- Merge

FD



X

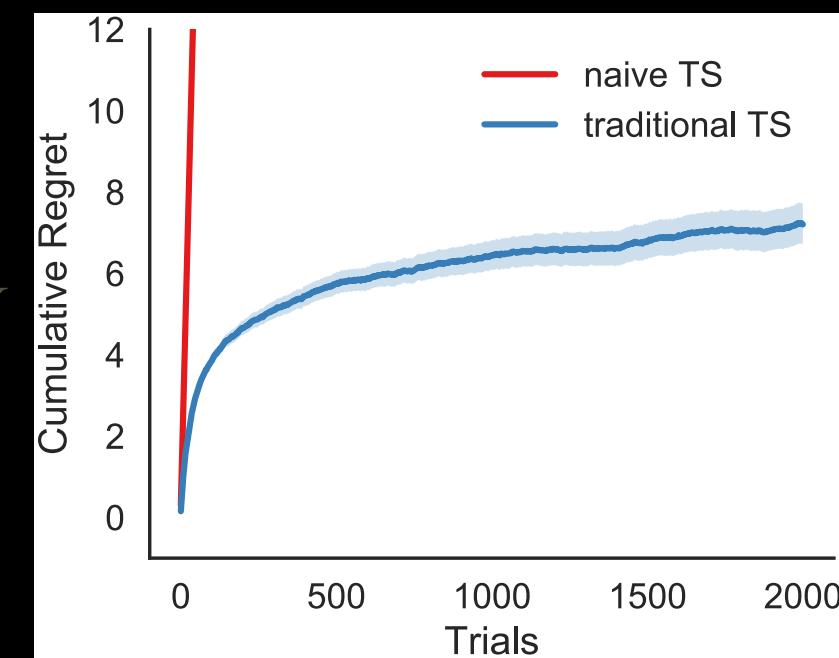
Let's ignore
that some
interactions

GENERAL POLICY LEARNING

$do(x))$.

- do-calc ID

Can we do better using
the causal bounds?

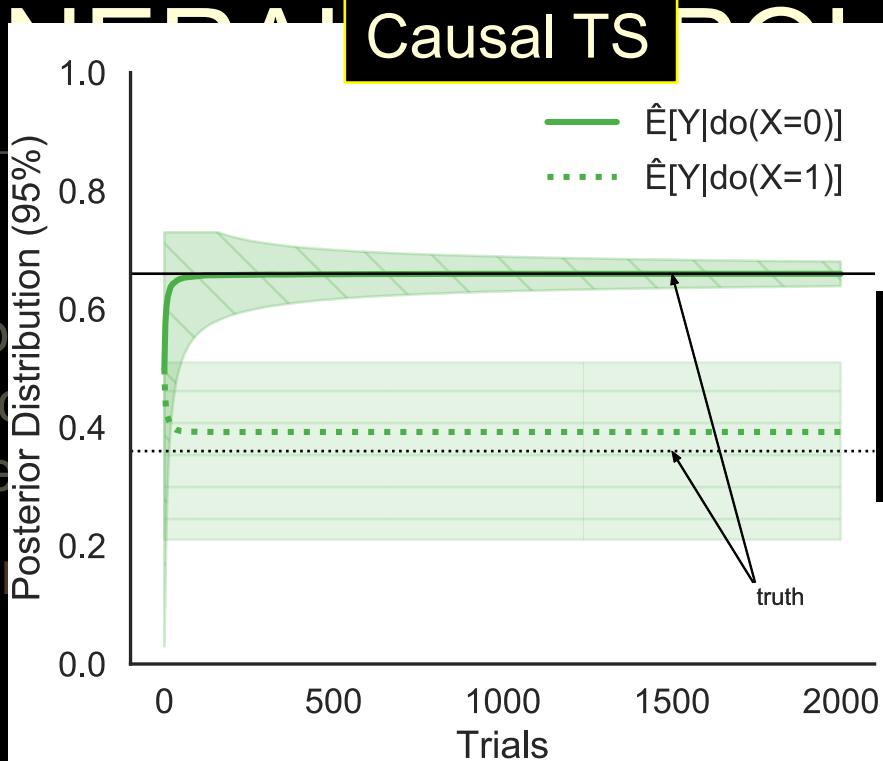


happening?!
be hurting?

GENERAL POLICY LEARNING

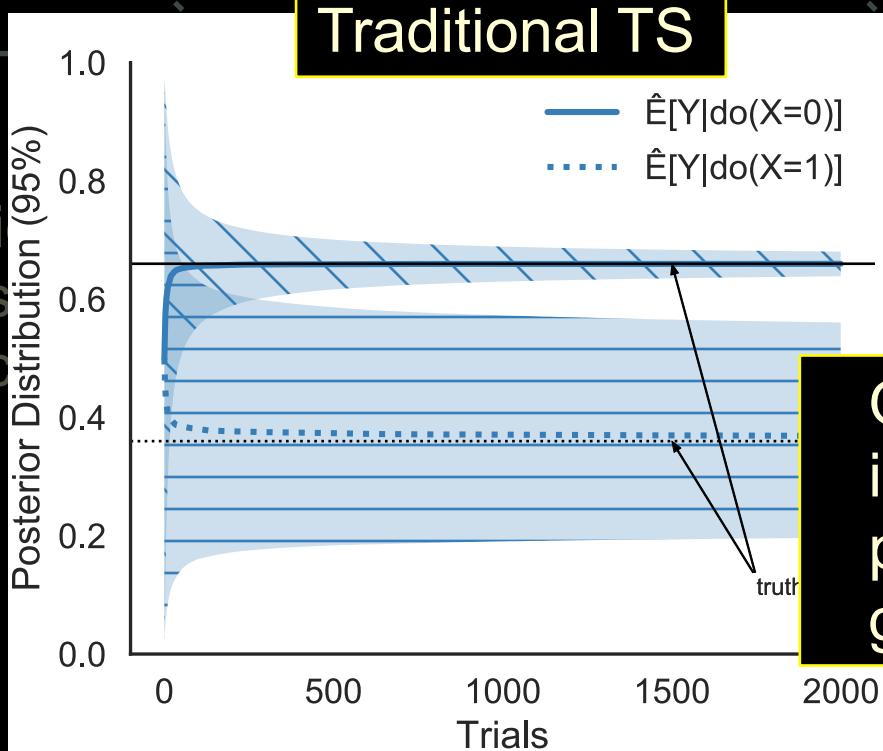
Task

- Rotation
- Mean



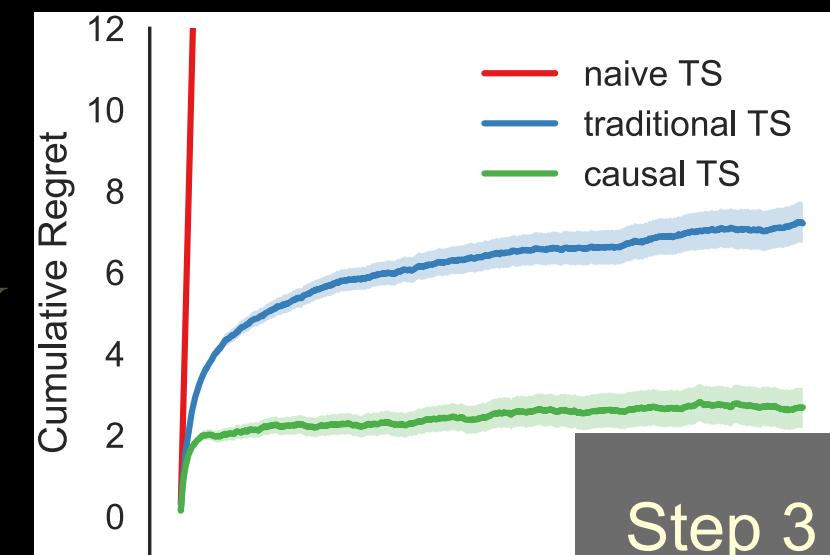
X

Let's ignore
that some
interactions



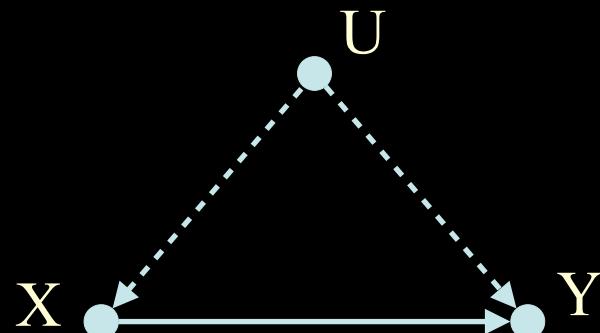
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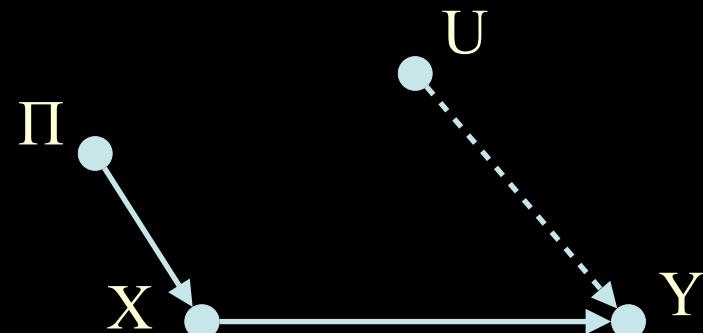


Orders of magnitude
improvement can be achieved in
practice, and can be proved in
general settings (ZB, IJCAI'17).

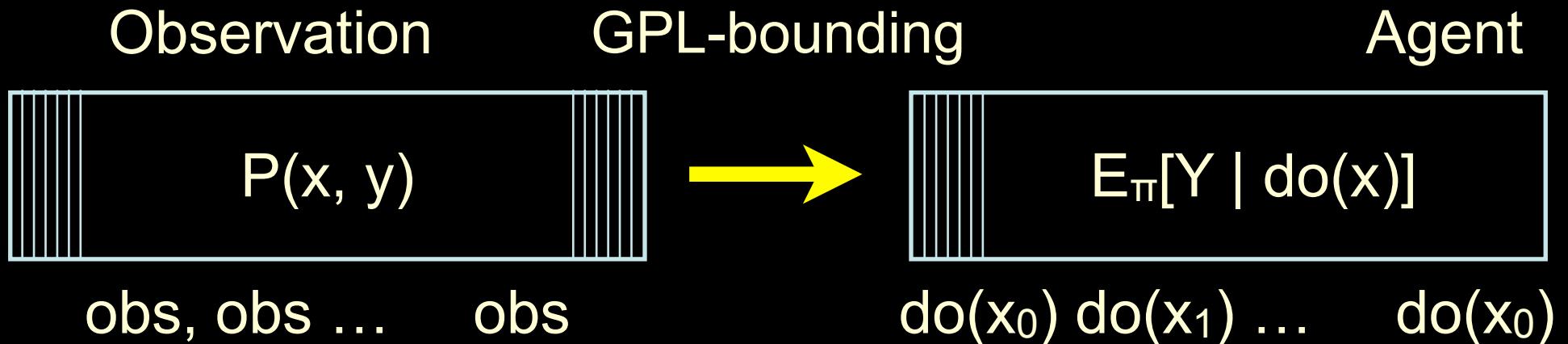
GENERALIZED POLICY LEARNING -- BIG PICTURE



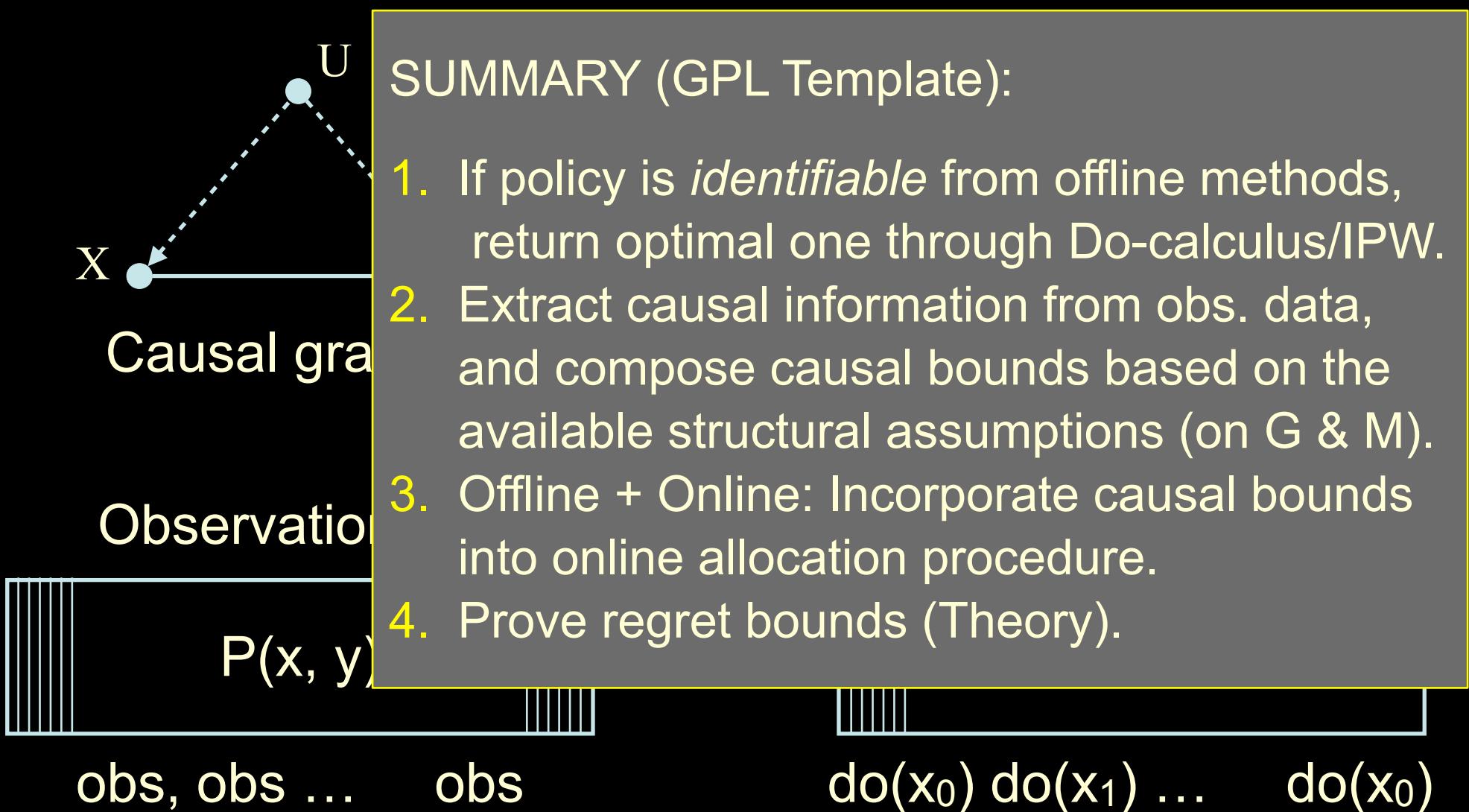
Causal graph G



under $\text{do}(X)$

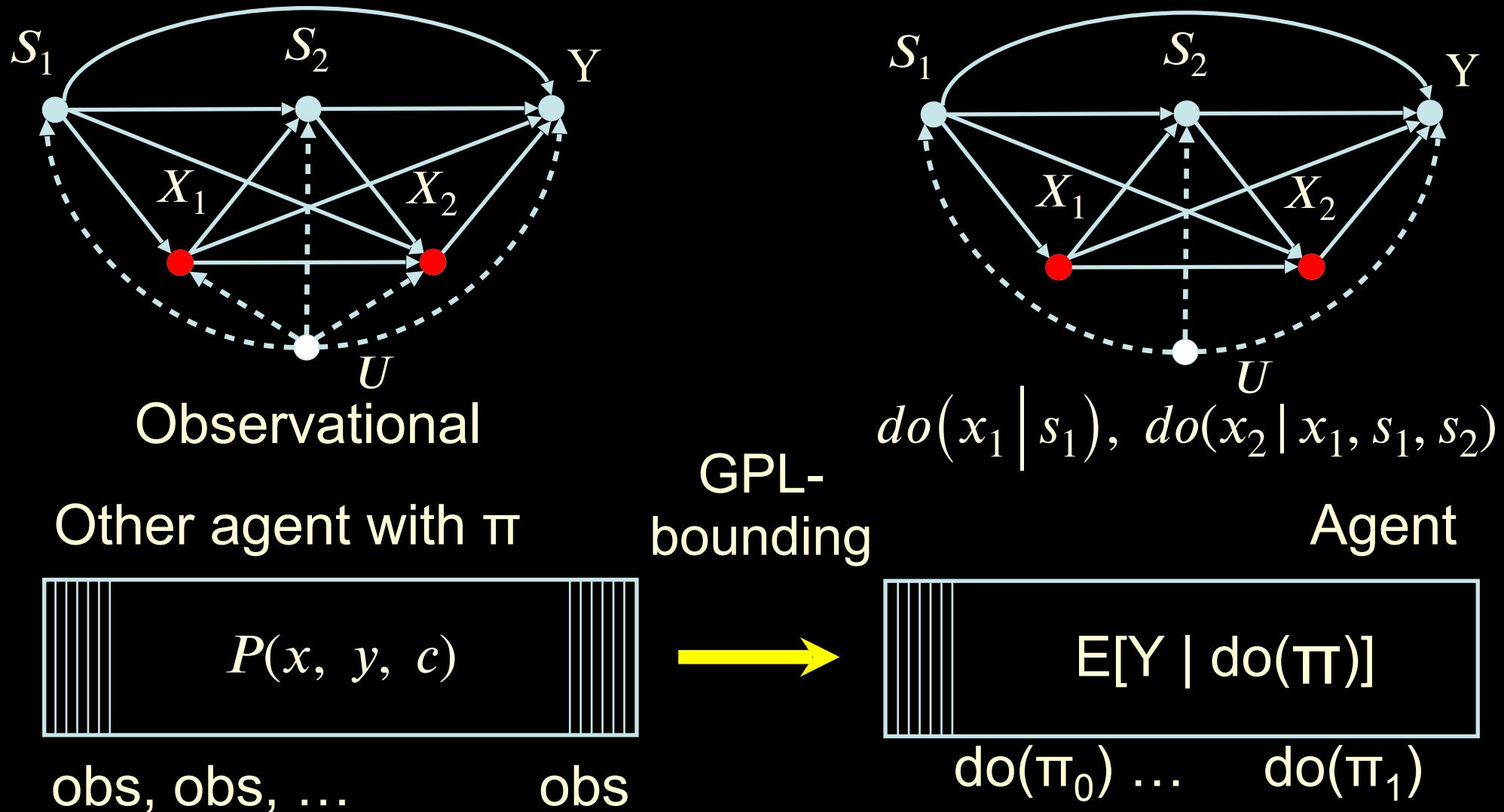


GENERALIZED POLICY LEARNING -- BIG PICTURE



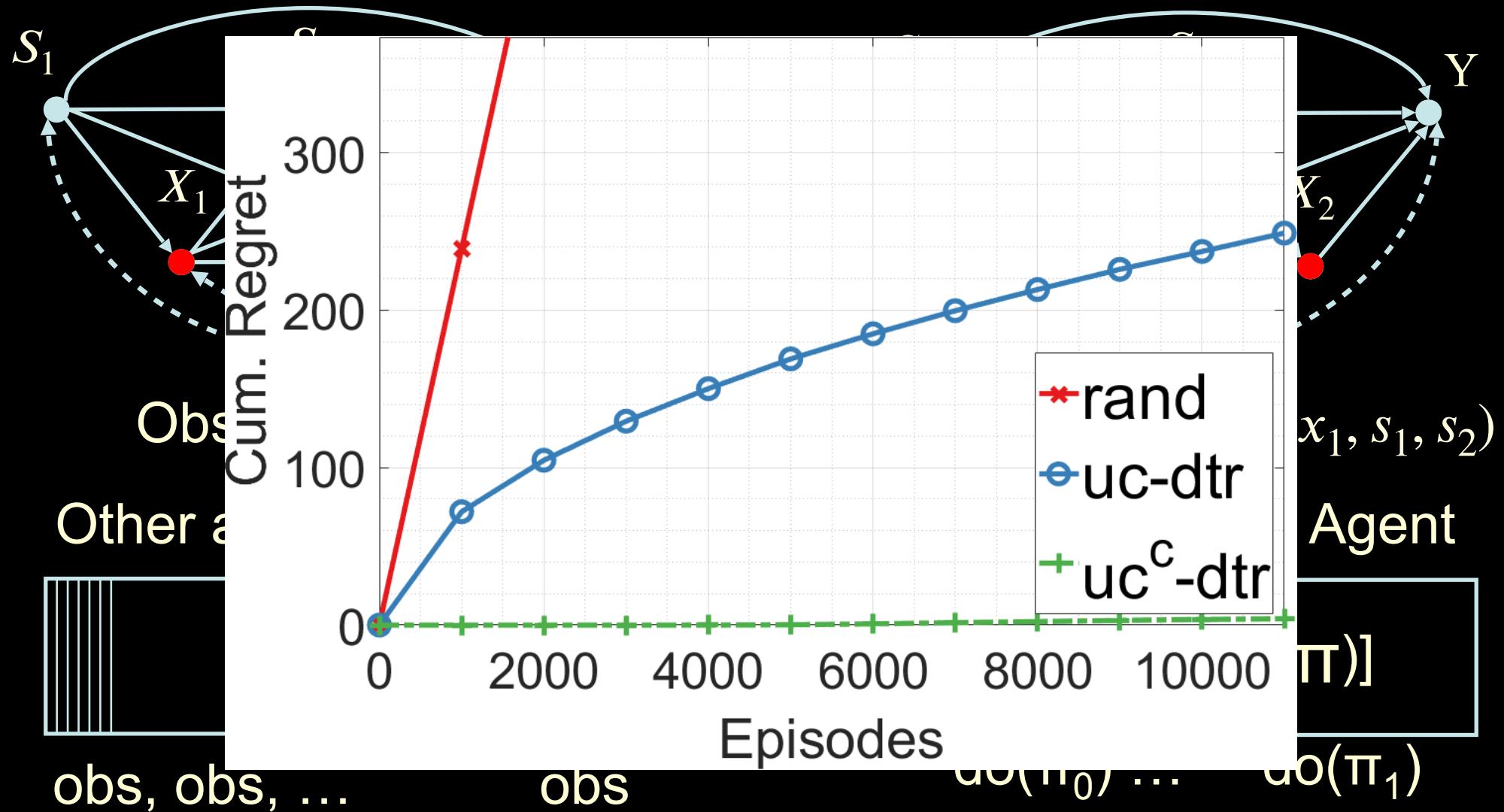
NEW RESULT: GPL FOR DYNAMIC TREATMENT REGIMES

- DTRs is a popular model for sequential treatment in **medical domains** [Murphy, 2003; Moodie et al., 2007]:



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- DTRs is a popular model for sequential treatment in **medical domains** [Murphy, 2003; Moodie et al., 2007]:



* For details, see [Zhang & Bareinboim, NeurIPS'19; ICML'20].

TASK 2. WHEN AND WHERE TO INTERVENE? (Refining the policy space)

Sanghack Lee

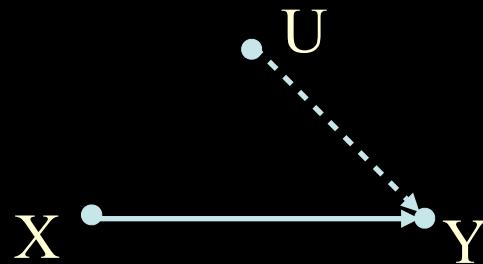


CRL-TASK 2. WHEN AND WHERE TO INTERVENE?

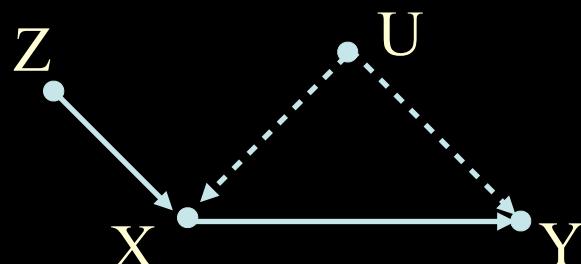
- In general, it's assumed throughout the literature a policy space such that actions are fixed *a priori* (e.g., a set $X = \{X_1, \dots, X_k\}$), and intervening is usually assumed to lead to positive outcomes.
- Our goal here is to understand when interventions are required, or if they may lead to unintended consequences (e.g., side effects). when
/ if
- In the case interventions may be needed, we would like to understand what should be changed in the underlying environment so as to bring a desired state of affairs about (e.g., maybe $do(X_1, X_3, X_7)$ instead of $do(X_1, X_2, X_3, \dots, X_7)$). where

UNDERSTANDING THE POLICY SPACE

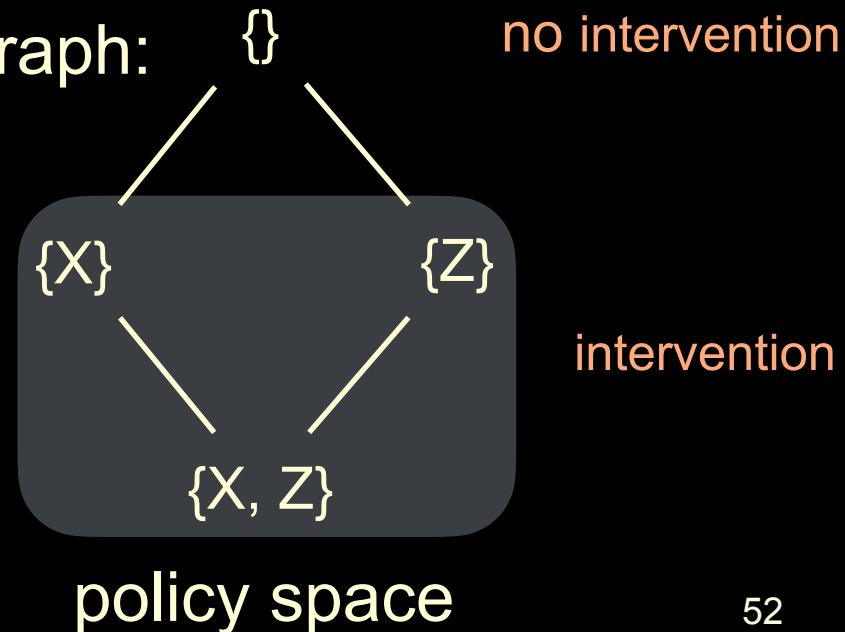
- Consider the causal graph of a bandit model:



- Our goal is to optimize Y (e.g., keep it high as much as possible), and we are not a priori committed to intervening on any specific variable, or intervening at all.
- Consider now the 3-var causal graph:



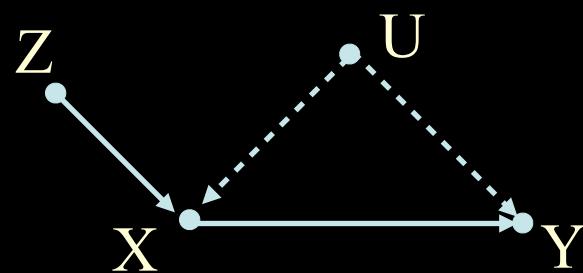
causal graph G



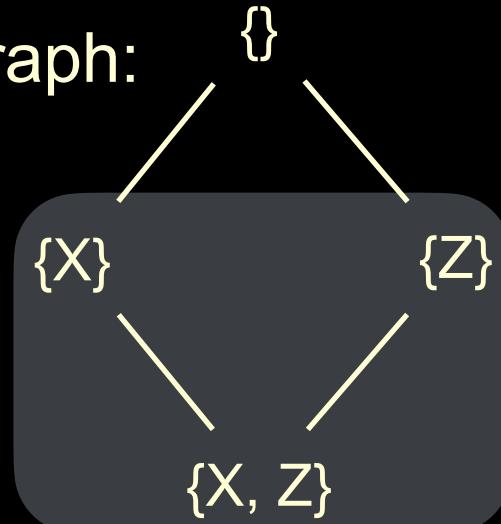
policy space

UNDERSTANDING THE POLICY SPACE

- Our goal is to optimize Y (e.g., keep it high as much as possible), and we are not a priori committed to intervening on any specific variable, or intervening at all.
- Consider now the 3-var causal graph:



causal graph G



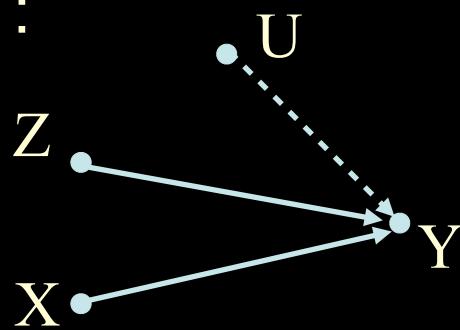
policy space

- Causal-insensitive strategy: Ignore the causal structure G, take $\{X, Z\}$ as one larger variable, and search based on

$$\operatorname{argmax}_{xz} E[Y \mid \text{do}(X = x, Z = z)]$$

Agent's model:

G' :

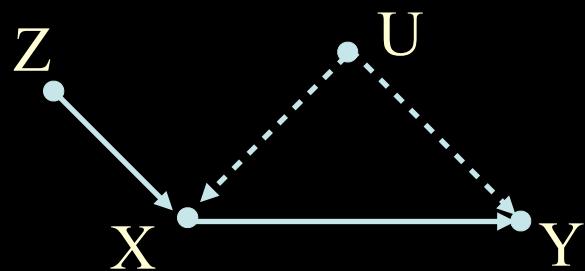


UNDERSTANDING THE POLICY SPACE

Key observations:

1. Note that the implicit causal graph in the agent's mind (G'), which follows from standard optimization procedure, is different than G .

2. The true causal model G encodes constraints of the underlying environment (SCM M).



causal graph G

- Causal-insensitive strategy: take $\{X, Z\}$ as one larger variable

$$\operatorname{argmax}_{xz} E[Y \mid \text{do}(X = x, Z = z)]$$

Question -- Despite what is in the agent's mind (or optimization function), it's still the case that it will be evaluated by the SCM M. Is then being oblivious to the pair $\langle G, M \rangle$ okay? Can't we just do more interventions? Meaning, more $\text{do}(X=x, Z=z)$, and things will eventually converge?

THE CAUSAL STRUCTURE CANNOT BE DISMISSED

- SCM M (Unobserved)

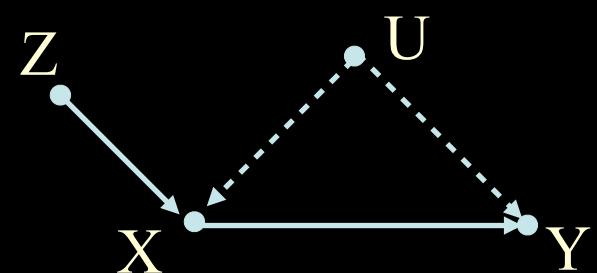
$$Z \leftarrow U_z$$

$$X \leftarrow Z \oplus U$$

$$Y \leftarrow X \oplus U$$

$$P(U=1) = P(U_z=1) = 0.5$$

- Causal Graph G



THE CAUSAL STRUCTURE CANNOT BE DISMISSED

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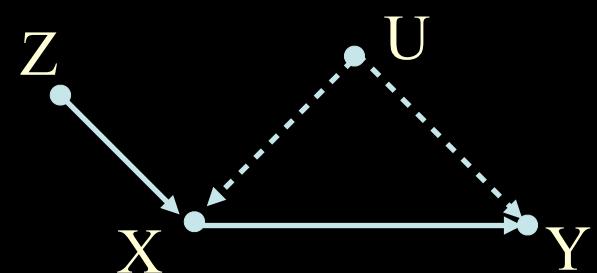
$$E[Y | do(X)] = E[Y | do(X, Z)] = 0.5$$

$$E[Y | do(Z)] = (Z \oplus U) \oplus U = Z$$

So, if $do(Z=1)$,

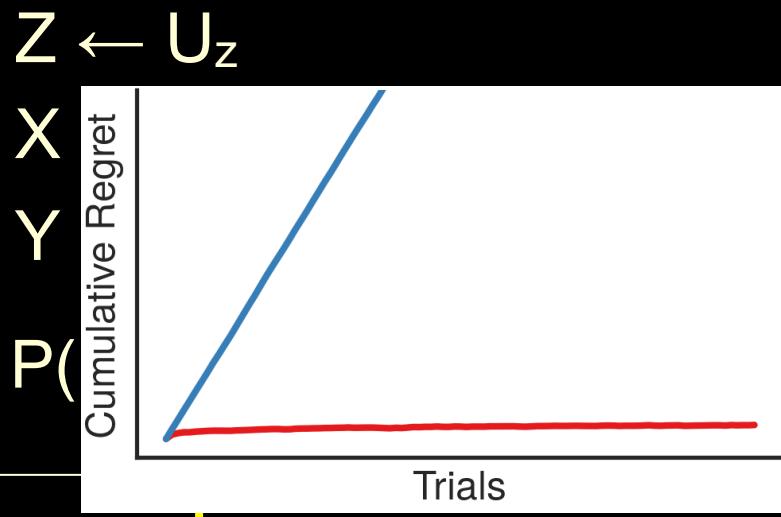
$$E[Y | do(Z = 1)] = 1$$

- Causal Graph G

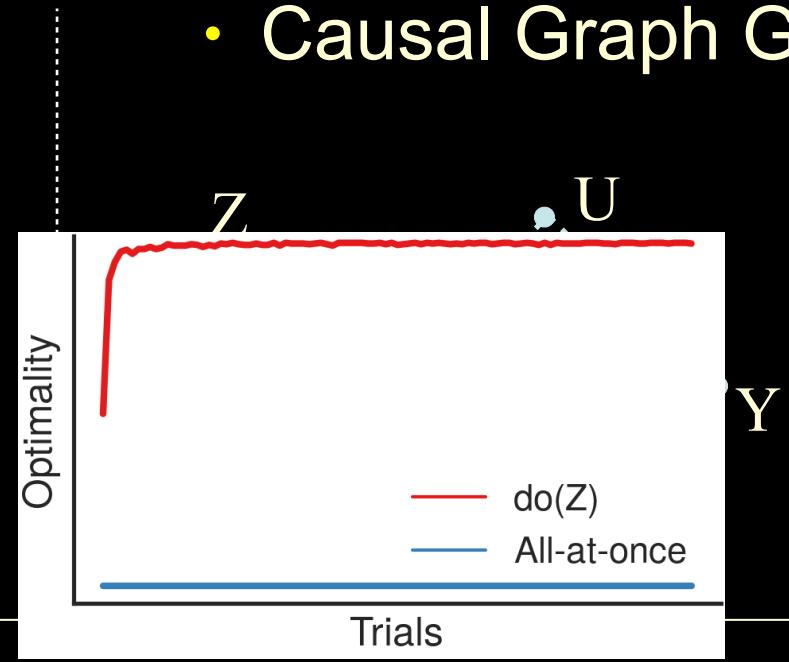


THE CAUSAL STRUCTURE CANNOT BE DISMISSED

- SCM M (Unobserved)



- Causal Graph G



$E[Y]$

$E[Y]$

So, if $\text{do}(Z=1)$,

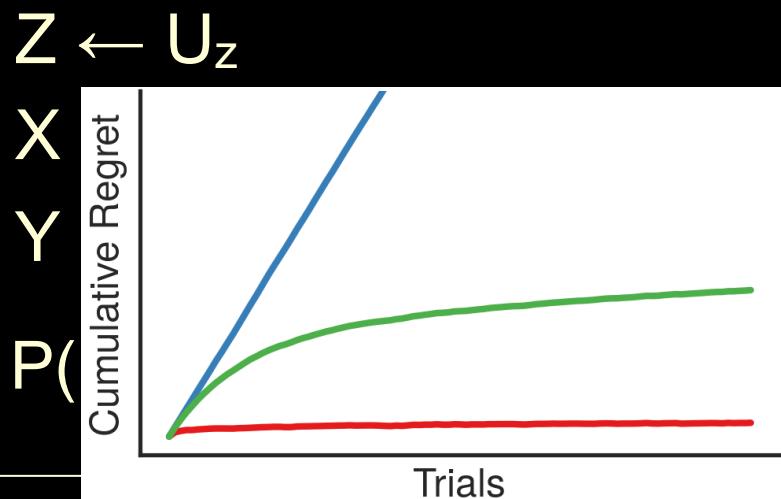
$$E[Y | \text{do}(Z = 1)] = 1$$

- A causal insensitive strategy (i.e., “all-at-once”, $\text{do}(X,Z)$) will not pick up the $\text{do}(Z)$ -intervention, and will never converge!
- A naive, “all-subsets” strategy works since it includes $\text{do}(Z=1)$

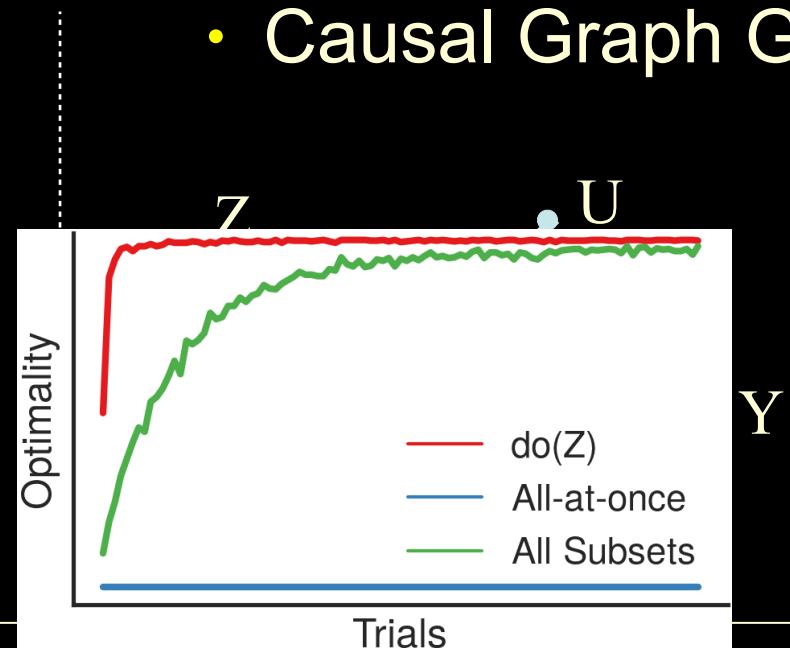


THE CAUSAL STRUCTURE CANNOT BE DISMISSED

- SCM M (Unobserved)



- Causal Graph G



$E[Y]$

$E[Y]$

So, if $\text{do}(Z=1)$,

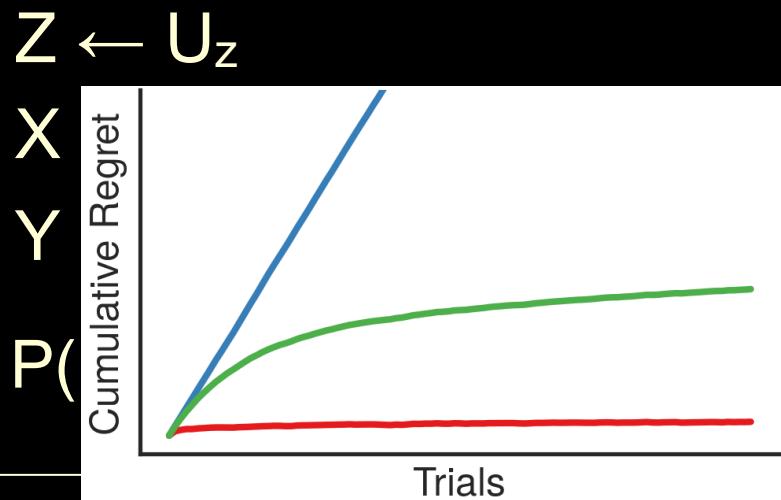
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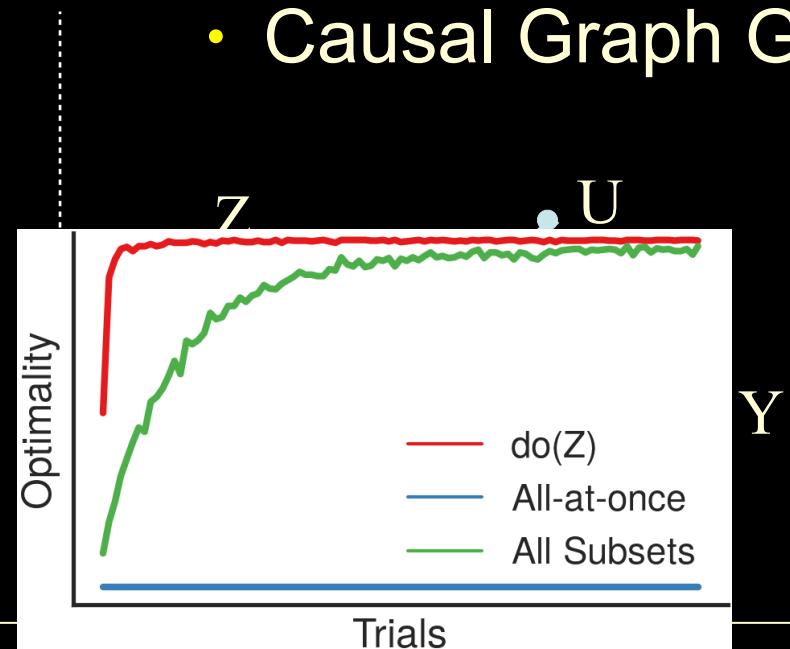


THE CAUSAL STRUCTURE CANNOT BE DISMISSED

- SCM M (Unobserved)



- Causal Graph G



$E[Y]$

$E[Y]$

So,
 $E[Y]$

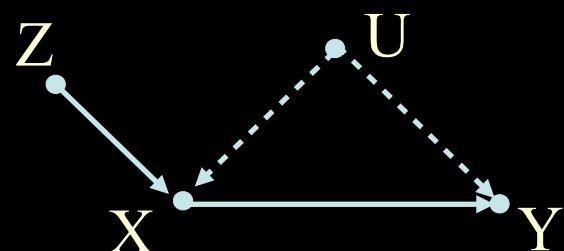
Can we do better than these two naive strategies?



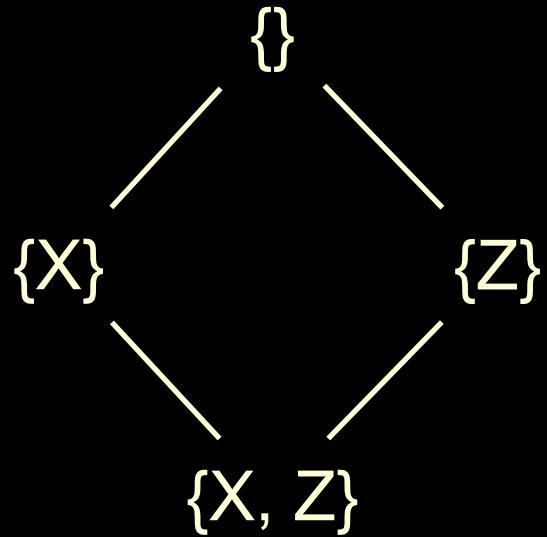
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POLICY SPACE (EXAMPLE)

Causal graph G



Policy space

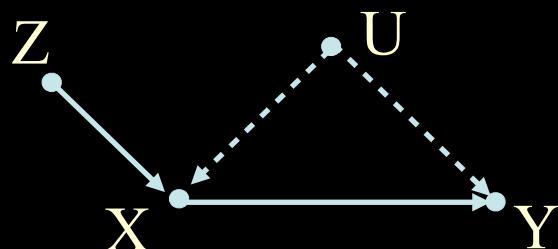


Intervention Sets (IS)

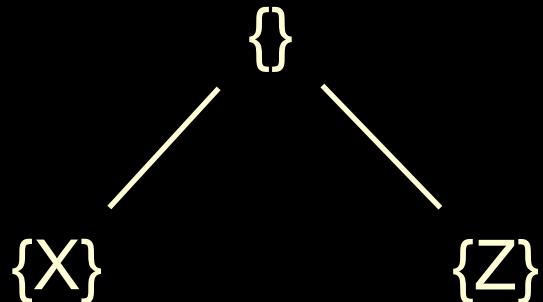
Intervention Sets (IS)	Actions
{}	do()
do(X)	do(X=0) do(X=1)
do(Z)	do(Z=0) do(Z=1)
do(X,Z)	do(X=0,Z=0) do(X=0,Z=1) do(X=1,Z=0) do(X=1,Z=1)

POLICY SPACE (EXAMPLE)

Causal graph G



Policy space



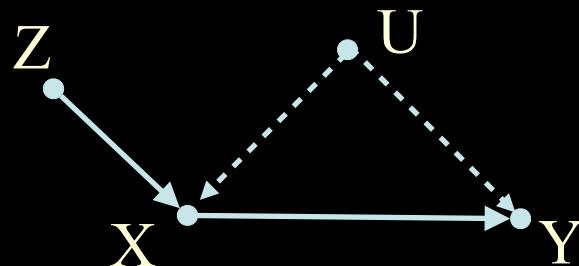
Intervention Sets (IS)

Actions

Intervention Sets (IS)	Actions
{}	do()
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We'll study properties of the policy space with respect to the topological constraints imposed by M in G.

PROPERTY 1: INTERVENTIONAL EQUIVALENCE



$$E[Y | \text{do}(x, z)] = E[Y | \text{do}(x)]$$

$\because (Y \perp\!\!\!\perp Z | X)$ in $G_{\overline{X}, \overline{Z}}$ (Rule 3 of do-calculus)

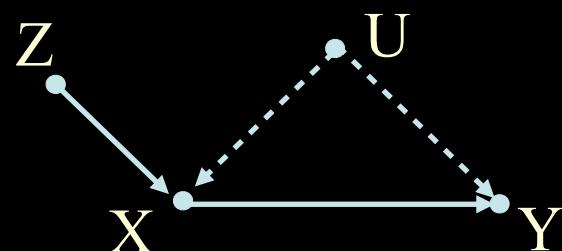
Implication: prefer playing $\text{do}(X)$ to playing $\text{do}(X, Z)$.

Definition (Minimal Intervention Set, MIS)

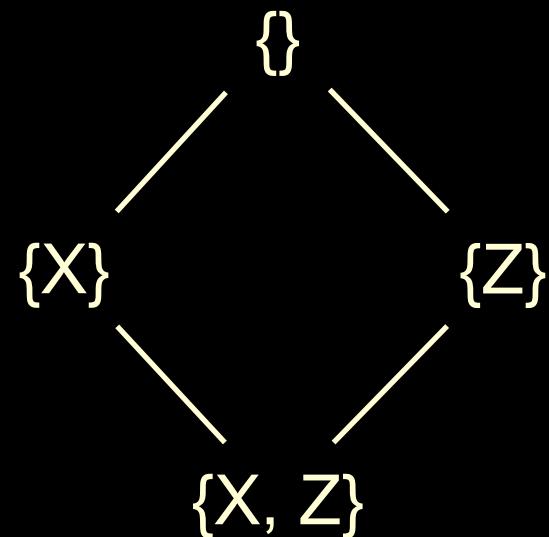
Given $\langle G, Y \rangle$, a set of variables $X \subseteq V \setminus \{Y\}$ is said to be a *minimal intervention set* if there is no $X' \subset X$ such that $E[Y | \text{do}(x')] = E[Y | \text{do}(x)]$ for every SCM conforming to G where x' is consistent with x .

PROPERTY 1: MIS (EXAMPLE)

Causal graph G



Policy space

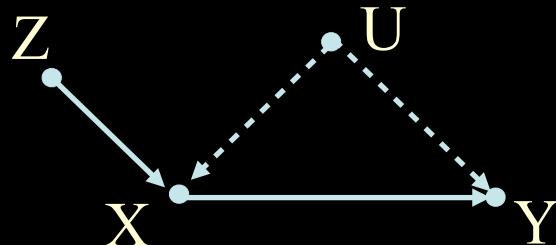


Intervention Sets (IS)	Actions	MIS
{}	do()	
do(X)	do(X=0) do(X=1)	
do(Z)	do(Z=0) do(Z=1)	
do(X,Z)	do(X=0,Z=0) do(X=0,Z=1) do(X=1,Z=0) do(X=1,Z=1)	

PROPERTY 1: MIS (EXAMPLE)

Causal graph G	Intervention Sets (IS)	Actions	MIS
	{}	do()	✓
Policy space 	do(X)	do(X=0) do(X=1)	✓
	do(Z)	do(Z=0) do(Z=1)	✓
	do(X,Z)	do(X=0,Z=0) do(X=0,Z=1) do(X=1,Z=0) do(X=1,Z=1)	✗

PROPERTY 2: PARTIAL-ORDEREDNESS



$$\begin{aligned} E[Y] &= \sum_z E[Y|do(z)] P(z) \\ &\leq \sum_z E[Y|do(z^*)] P(z) \\ &= E[Y|do(z^*)] \quad z^* \equiv \operatorname{argmax}_z E[Y|do(z)] \end{aligned}$$

$\therefore E[Y] \leq E[Y|do(z^*)]$

Implication: playing $do(Z)$ should be preferred to playing $do()$.

Definition (Possibly-Optimal MIS, POMIS)

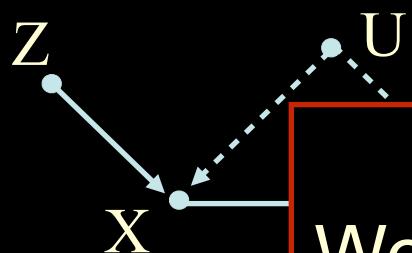
Given $\langle G, Y \rangle$, let $\mathbf{X} \in \text{MISs}$. \mathbf{X} is said to be a possibly-optimal MIS if there exists a SCM M conforming to G such that

$$\max_{\mathbf{x}} E[Y | do(\mathbf{X}=\mathbf{x})] > \max_{\mathbf{W} \in \text{MIS} \setminus \{\mathbf{X}\}} E[Y | do(\mathbf{W}=\mathbf{w})]$$

PROPERTY 2: PARTIAL-ORDEREDNESS

$$E[Y] = \sum_z E[Y|do(z)] P(z)$$

$$\leq \sum_z E[Y|do(z^*)] P(z)$$



$E[Y|do(z)]$

We provide a complete characterization of POMIS & algorithm that enumerates all POMISs given a causal graph G .

ng do().

Definition (Possibly-Optimal MIS, POMIS)

Given $\langle G, Y \rangle$, let $\mathbf{X} \in \text{MISs}$. \mathbf{X} is said to be a possibly-optimal MIS if there exists a SCM M conforming to G such that

$$\max_{\mathbf{x}} E[Y | do(\mathbf{X}=\mathbf{x})] > \max_{\mathbf{W} \in \text{MIS} \setminus \{\mathbf{X}\}} E[Y | do(\mathbf{W}=\mathbf{w})]$$

PROPERTY 2: POMIS (EXAMPLE)

Causal graph G

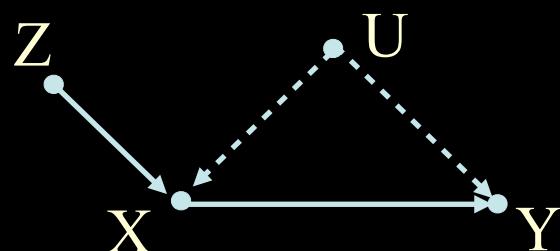
intervention sets

	actions	MIS	POMIS
{}	do()	✓	
do(X)	do(X=0) do(X=1)	✓	
do(Z)	do(Z=0) do(Z=1)	✓	
do(X,Z)	do(X=0,Z=0) do(X=0,Z=1) do(X=1,Z=0) do(X=1,Z=1)	✗	

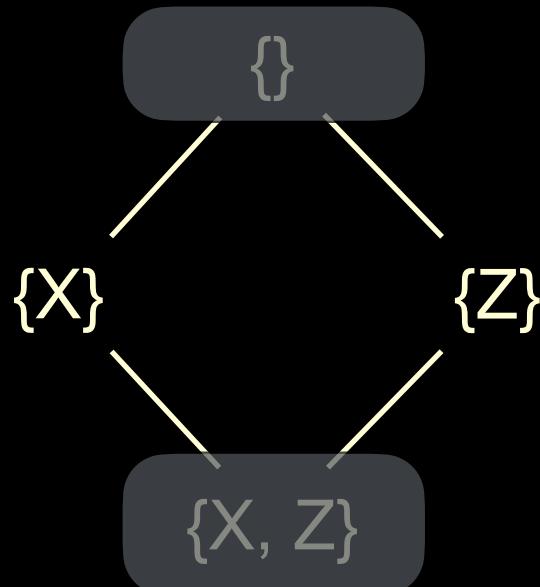
Policy space

PROPERTY 2: POMIS (EXAMPLE)

Causal graph G



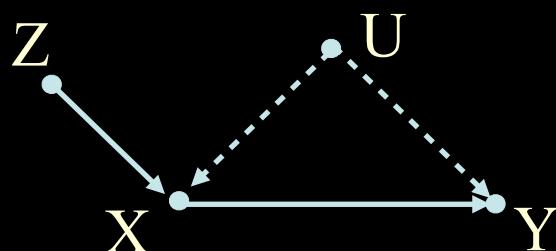
Policy space



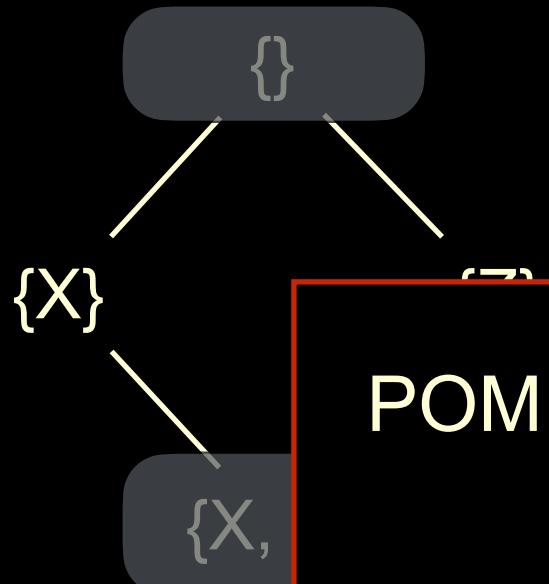
intervention sets	actions	MIS	POMIS
{}	do()	✓	✗
do(X)	do(X=0) do(X=1)	✓	✓
do(Z)	do(Z=0) do(Z=1)	✓	✓
do(X,Z)	do(X=0,Z=0) do(X=0,Z=1) do(X=1,Z=0) do(X=1,Z=1)	✗	✗

PROPERTY 2: POMIS (EXAMPLE)

Causal graph G



Policy space



intervention sets	actions	MIS	POMIS
{}	do()	✓	✗
do(X)	do(X=0) do(X=1)	✓	✓
do(Z)	do(Z=0) do(Z=1)	✓	✓
do(X, Z)	do(X=0, Z=0)		

PROPERTY 3: ARMS' QUANTITATIVE RELATIONSHIPS

- Goal: infer an arm's expected reward from other arms' data,

$$P(y|do(\mathbf{x})) \leftarrow \{ P(V | do(Z)) \}_{Z \in \text{POMIS} \setminus \{\mathbf{x}\}}$$

- New ID algorithm (z^2ID) to find a matching POMIS, that can borrow some additional data.

- Example

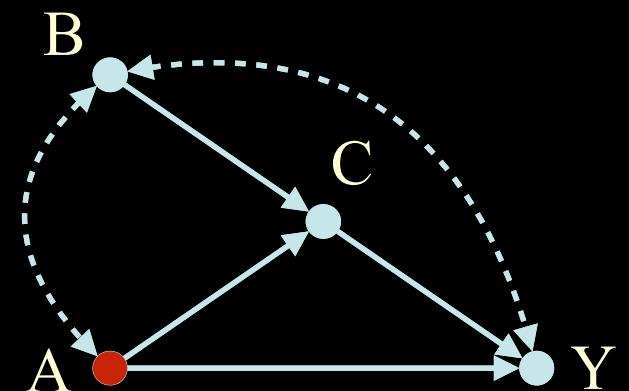
Given POMISs $\{\}$, $\{B\}$, and $\{C\}$:

$$P(y) = \sum_{a,b,c} P_b(c|a)P_c(a, b, y)$$

$$P_b(y) = \sum_{a,c} P(c|a, b) \sum_{b'} P(y|a, b', c)P(a, b')$$

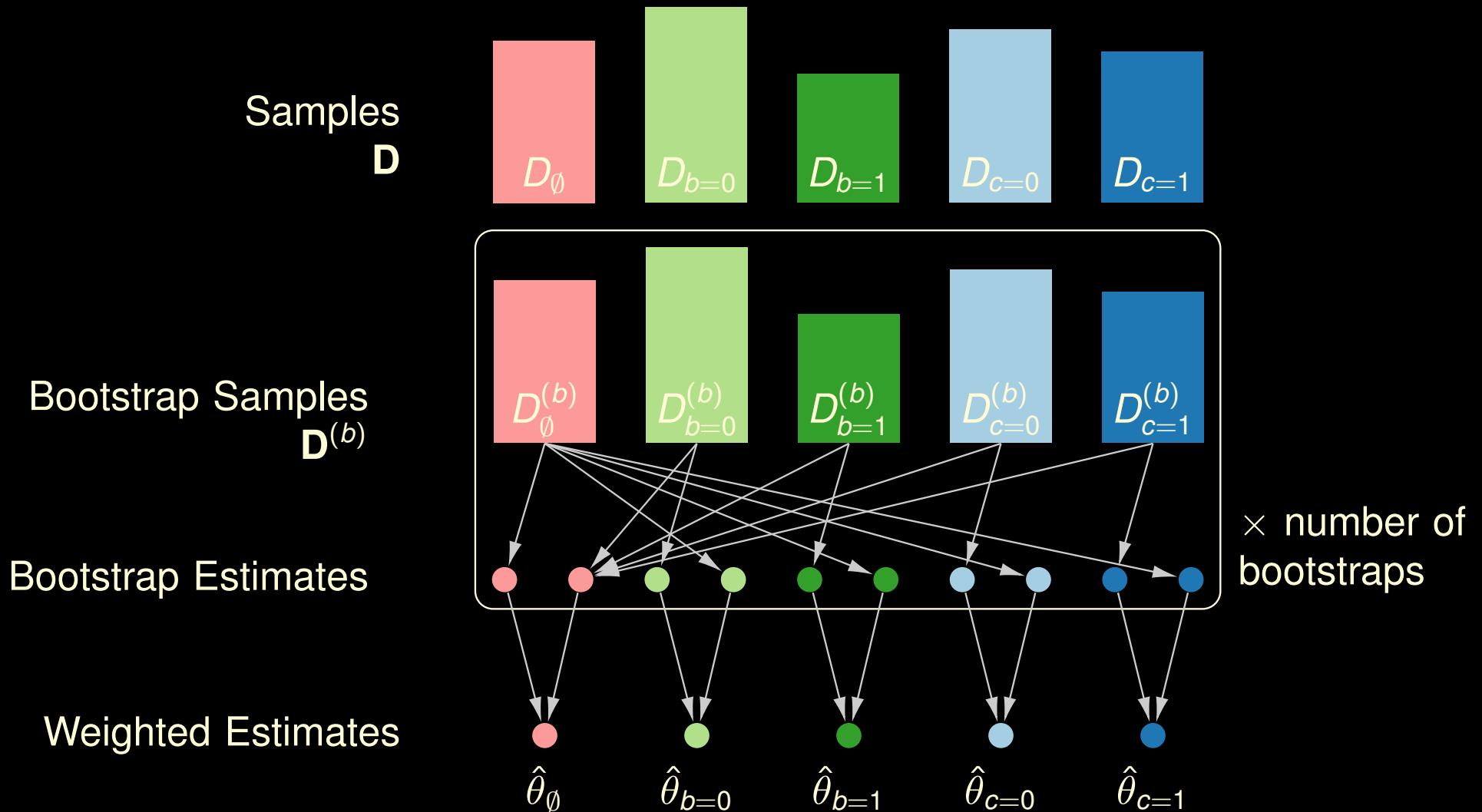
$$P_c(y) = \sum_{a,b} P(y|a, b, c)P(a, b)$$

$$P_c(y) = \sum_a P_b(y|a, c)P_b(a)$$



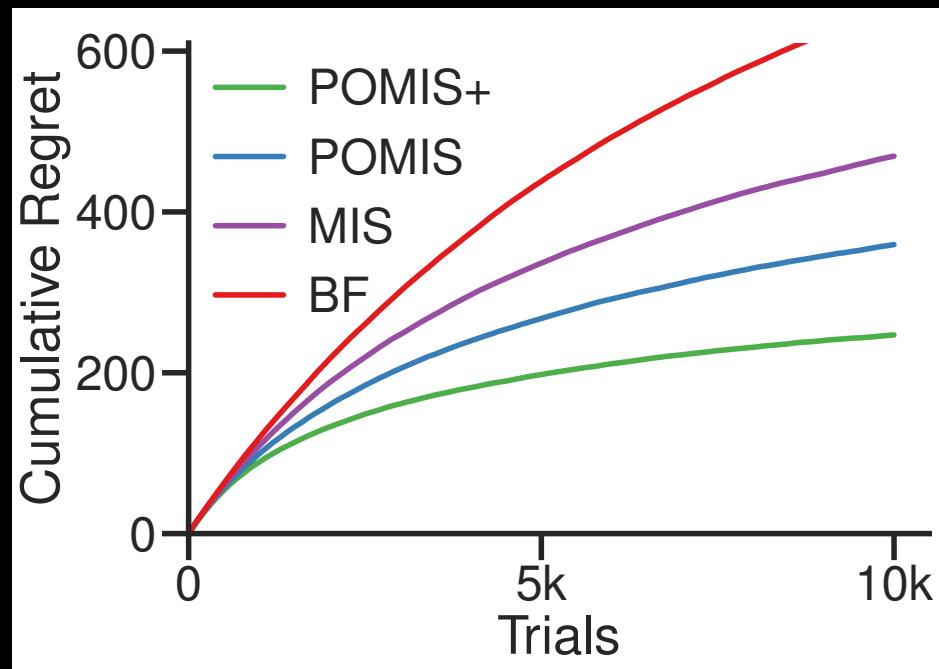
PROPERTY 3: ARMS' QUANTITATIVE RELATIONSHIPS

- Make the most of data — Minimum Variance Weighting

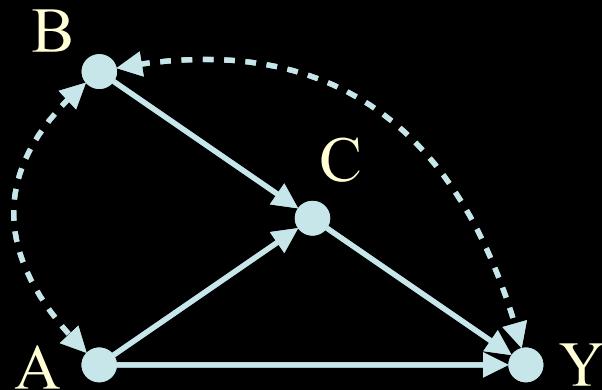


WHEN AND WHERE TO INTERVENE -- ALGORITHMS & EXPERIMENTS

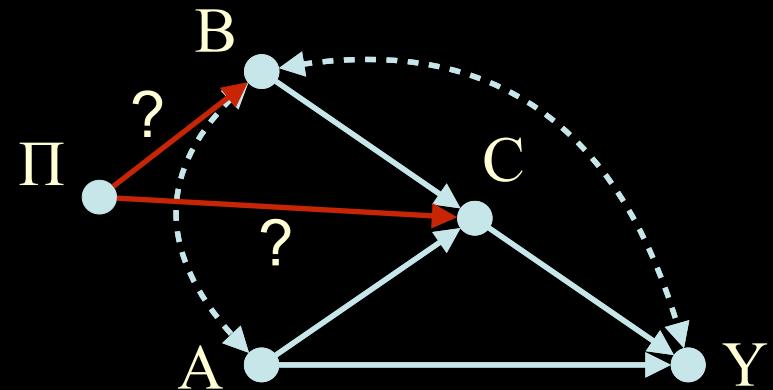
- We embed these results into TS/UCB solvers:
 - z^2 -TS: posterior distributions for expected rewards → adjust ‘posterior distributions’ reflecting all used data
 - z^2 -kl-UCB: upper confidence bounds for expected rewards → adjust ‘upper bounds’ by taking account samples from other arms
- Performance: **POMIS+** \geq **POMIS** \geq **MIS** \geq **Brute-force**



WHEN & WHERE TO INTERVENE -- BIG PICTURE

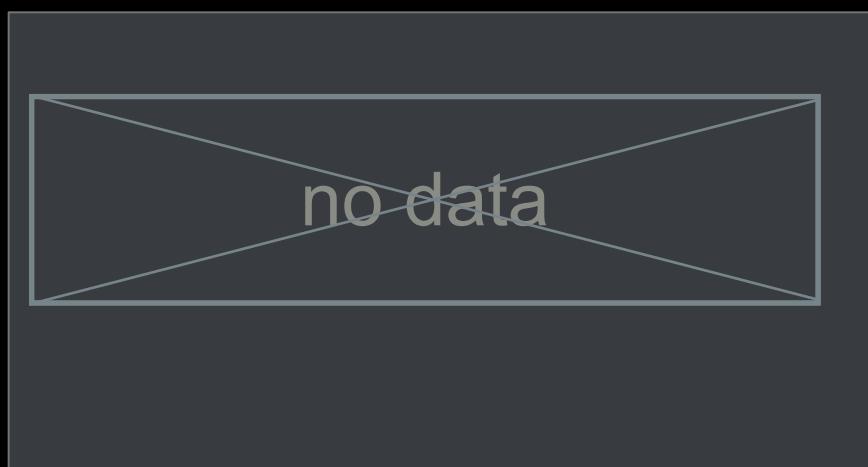


Causal Graph G



under $\text{do}(x)$

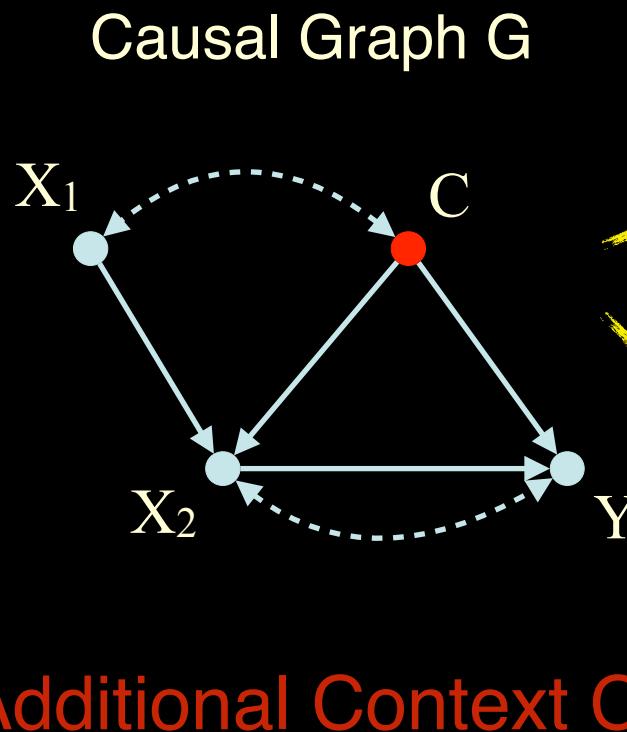
POMIS,
formulas



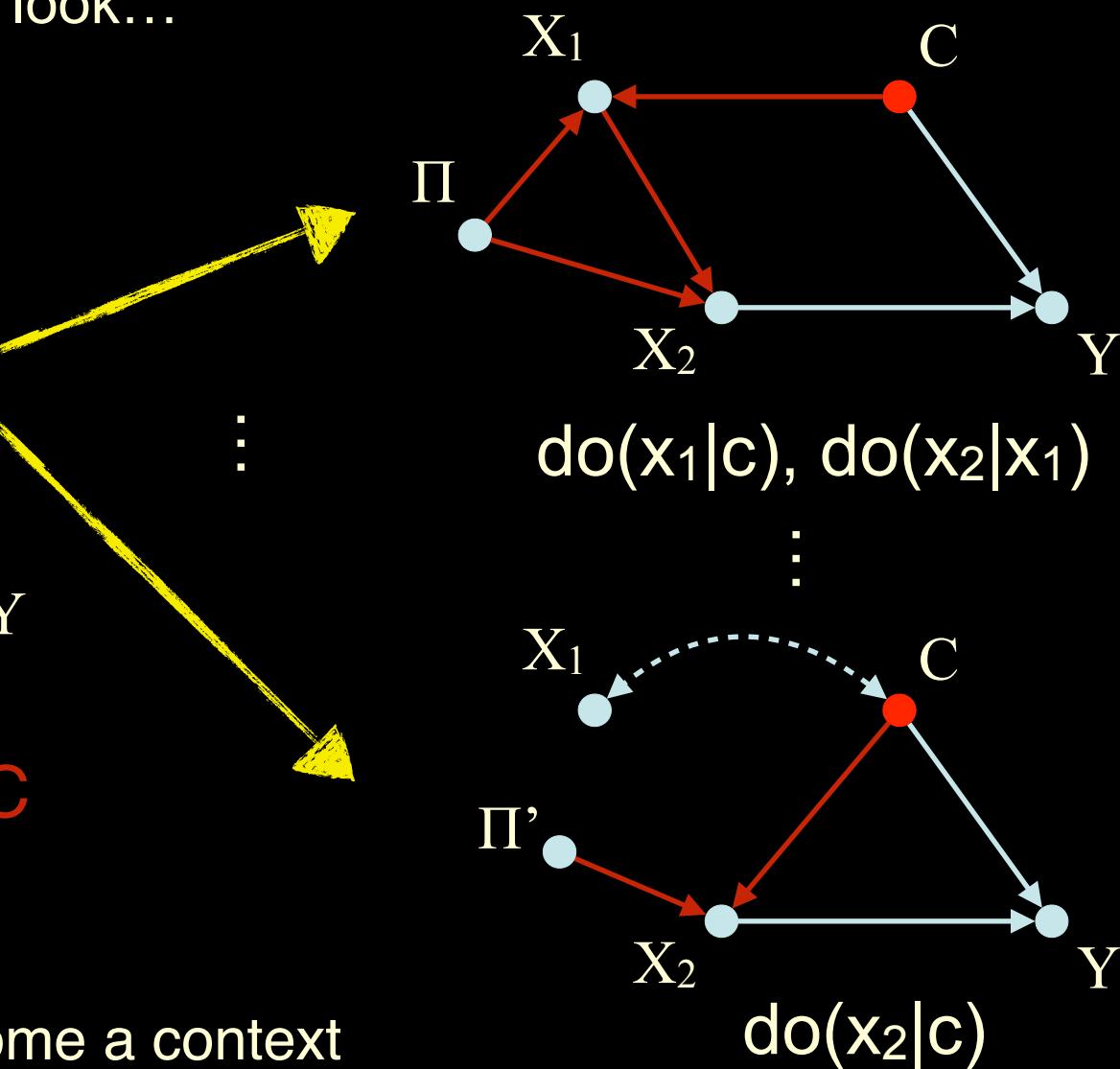
$\text{obs}()$, $\text{do}(b)$, ... $\text{do}(c)$

NEW RESULT: WHERE TO INTERVENE & WHAT TO SEE

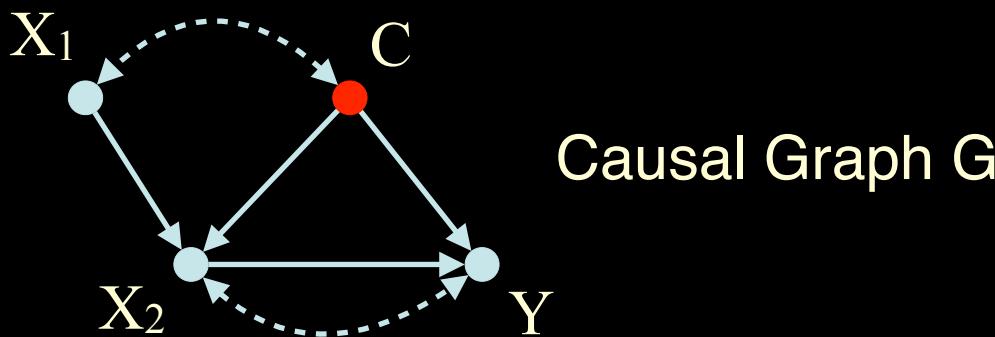
- In addition to deciding where to intervene, agents also need to decide where to look...



* both C and X₁ can become a context

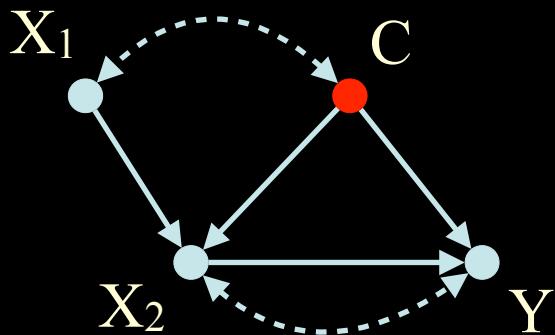


WHERE TO INTERVENE & WHAT TO SEE — POLICY SPACE



$\{\}$	$\{X_2\}$			
$do()$	$do(x_2)$	$do(x_2 c)$	$do(x_2 x_1)$	$do(x_2 c,x_1)$
$\{X_1\}$	$\{X_1, X_2\}$			
$do(x_1)$	$do(x_1),$ $do(x_2)$	$do(x_1),$ $do(x_2 c)$	$do(x_1),$ $do(x_2 x_1)$	$do(x_1),$ $do(x_2 c,x_1)$
$do(x_1 c)$	$do(x_1 c),$ $do(x_2)$	$do(x_1 c),$ $do(x_2 c)$	$do(x_1 c),$ $do(x_2 x_1)$	$do(x_1 c),$ $do(x_2 c,x_1)$

WHERE TO INTERVENE & WHAT TO SEE — POLICY SPACE



Policies with the same maximum expected rewards

do()

do(x_1)

do(x_2)

do(x_1),
do(x_2)

do($x_1|c$),
do(x_2)

do(x_1),
do($x_2|x_1$)

do($x_2|x_1$)

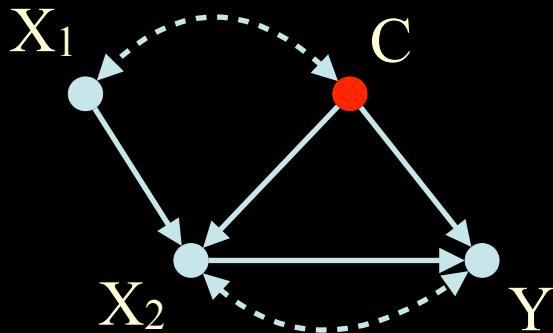
do($x_2|c$) do($x_2|c,x_1$)

do(x_1),
do($x_2|c$) do(x_1),
do($x_2|c,x_1$)

do($x_1|c$),
do($x_2|x_1$)

do($x_1|c$),
do($x_2|c$) do($x_1|c$),
do($x_2|c,x_1$)

WHERE TO INTERVENE & WHAT TO SEE — POLICY SPACE



1. minimal policy among reward-equivalent policies

do()

do(x_1)

do(x_2)

do(x_1),
do(x_2)

do($x_1|c$),
do(x_2)

do(x_1),
do($x_2|x_1$)

do($x_2|x_1$)

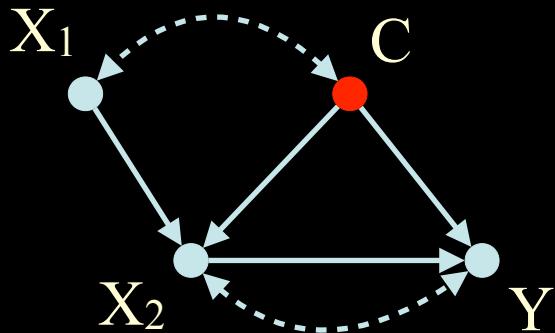
do($x_2|c$) do($x_2|c,x_1$)

do(x_1),
do($x_2|c$) do(x_1),
do($x_2|c,x_1$)

do($x_1|c$),
do($x_2|x_1$)

do($x_1|c$),
do($x_2|c$) do($x_1|c$),
do($x_2|c,x_1$)

WHERE TO INTERVENE & WHAT TO SEE — POLICY SPACE



1. minimal policy among

Partial-orders among policies wrt
maximum expected rewards

$\text{do}()$

$\text{do}(x_1)$

$\text{do}(x_2)$

$\text{do}(x_1),$
 $\text{do}(x_2)$

$\text{do}(x_1|c),$
 $\text{do}(x_2)$

$\text{do}(x_1),$
 $\text{do}(x_2|x_1)$

\leq

$\text{do}(x_2|x_1)$

$\text{do}(x_1|c),$
 $\text{do}(x_2|x_1)$

$\text{do}(x_2|c)$

$\text{do}(x_1),$
 $\text{do}(x_2|c)$

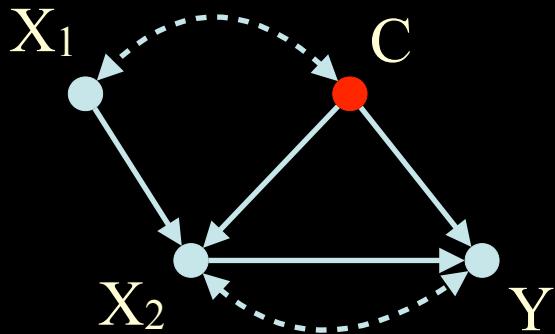
$\text{do}(x_2|c,x_1)$

$\text{do}(x_1),$
 $\text{do}(x_2|c,x_1)$

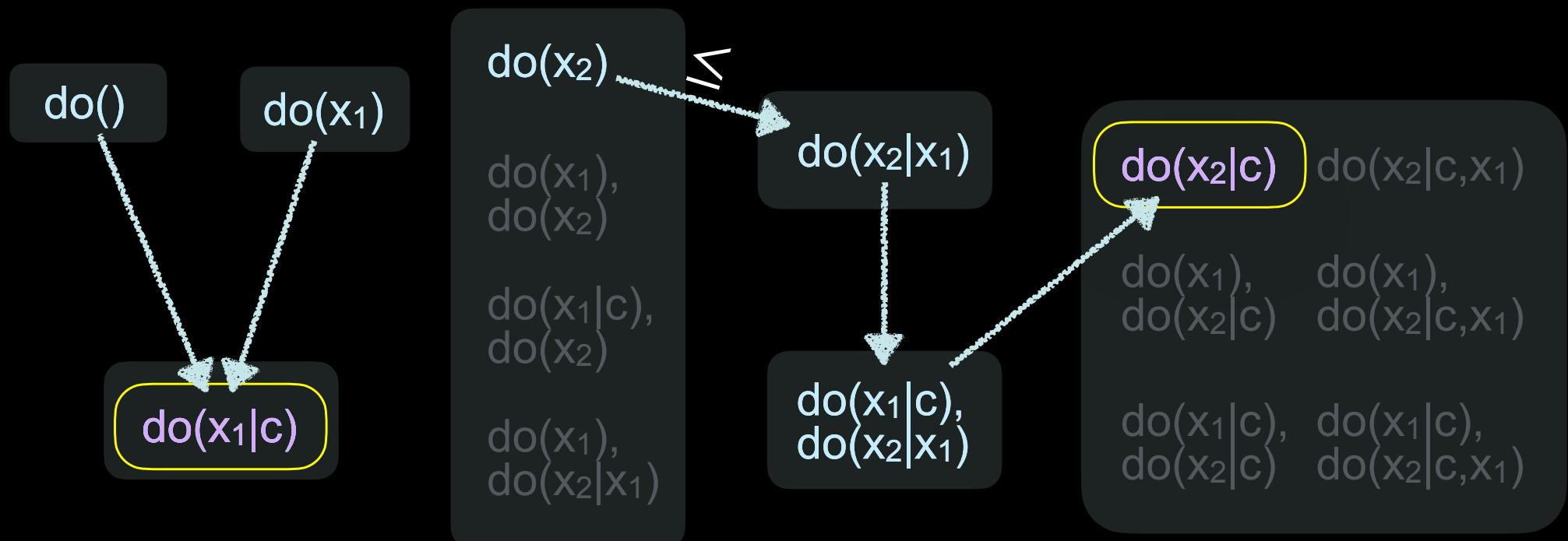
$\text{do}(x_1|c),$
 $\text{do}(x_2|c)$

$\text{do}(x_1|c),$
 $\text{do}(x_2|c,x_1)$

WHERE TO INTERVENE & WHAT TO SEE — POLICY SPACE



1. minimal policy among reward-equivalent policies
2. possibly-optimal policies among min. policies.



* For details, see [R-63 @CausalAI].

TASK 3.

COUNTERFACTUAL DECISION-MAKING

(Intentionality, Free Will, Autonomy)

Andrew Forney



Judea Pearl



CRL-TASK 3.

COUNTERFACTUAL DECISION-MAKING

- Agents act in a reflexive manner, without considering the reasons (or causes) for behaving in a particular way. Whenever this is the case, they can be exploited without never realizing.
- This is a general phenomenon in online learning whenever the agent optimizes by Fisherian rand./ the do-distribution (incl. all known RL settings).
- Our goal is to endow agents with the capability of performing counterfactual reasoning (taking their own intent into account), which leads to a more refined notion of regret & a new OPT function.

COUNTERFACTUAL DECISION-MAKING

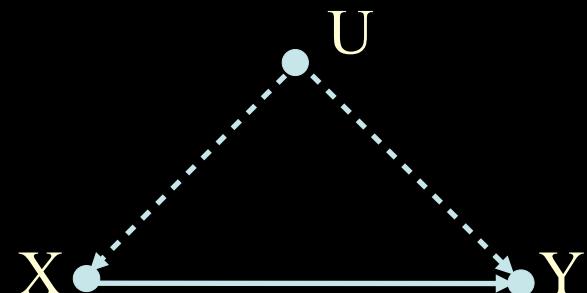
Question:

How should one **select the treatment (x^*)** to a particular unit $U=u$ so as to **maximize expected reward (Y)**?

What if we have observational data? Experimental data?

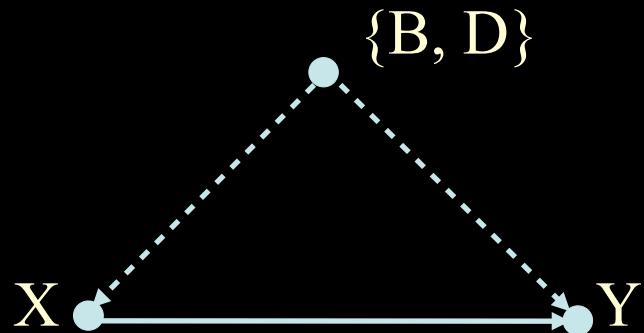
Applications:

- » Robotics
- » Medical Treatment
- » Job Training Program



GREEDY CASINO. INDIVIDUAL VERSUS POPULATION-LEVEL DECISIONS

Goal: Find a strategy (Π) so as to minimize cumulative regret.



X = type of the machine (x_0, x_1)
Y = reward (y_0, y_1)
B = blinking machine (b_0, b_1)
D = drunkenness level (d_0, d_1)

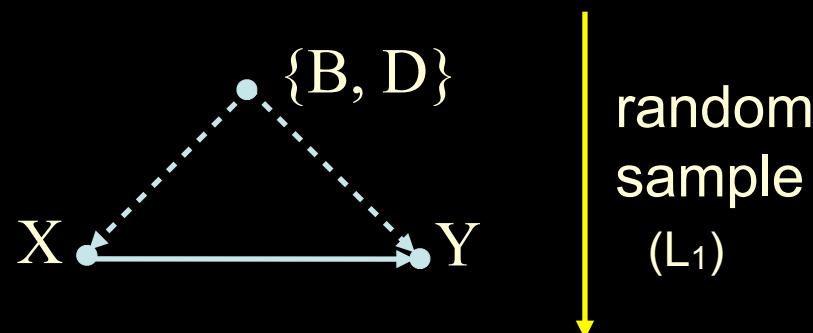
- Regulations: payout has to be ≥ 0.3 .
- Casino learns how customers operates and decides to set the payout structure as follows (using ML):

$E[y_1 $ $X, B, D]$	$D = 0$		$D = 1$	
	$B = 0$	$B = 1$	$B = 0$	$B = 1$
$X = x_1$	0.10	0.50	0.40	0.20
$X = x_0$	0.50	0.10	0.20	0.40

GREEDY CASINO. INDIVIDUAL VERSUS POPULATION-LEVEL DECISIONS

- Casino's model: $f_X(B, D)$, $P(B)$, $P(D)$,

$E[y_1 X, B, D]$	$D = 0$		$D = 1$	
	$B = 0$	$B = 1$	$B = 0$	$B = 1$
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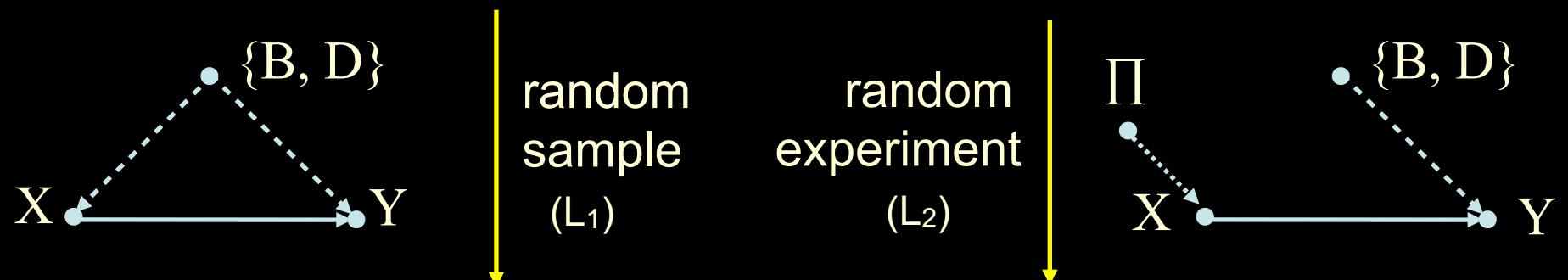
$D_1 \quad E(y_1 | X = x_0) = 0.15$
 $E(y_1 | X = x_1) = 0.15$

GREEDY CASINO.

INDIVIDUAL VERSUS POPULATION-LEVEL DECISIONS

- Casino's model: $f_X(B, D)$, $P(B)$, $P(D)$,

$E[y_1 X, B, D]$	$D = 0$		$D = 1$	
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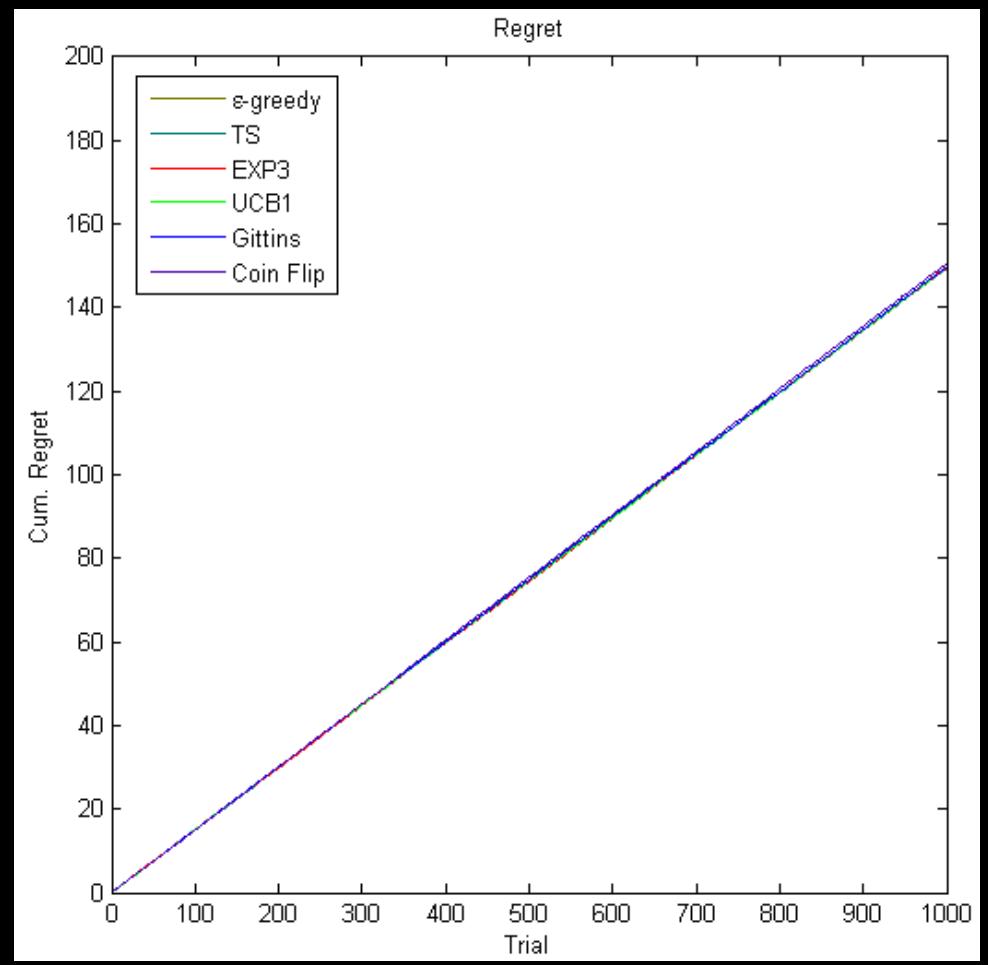
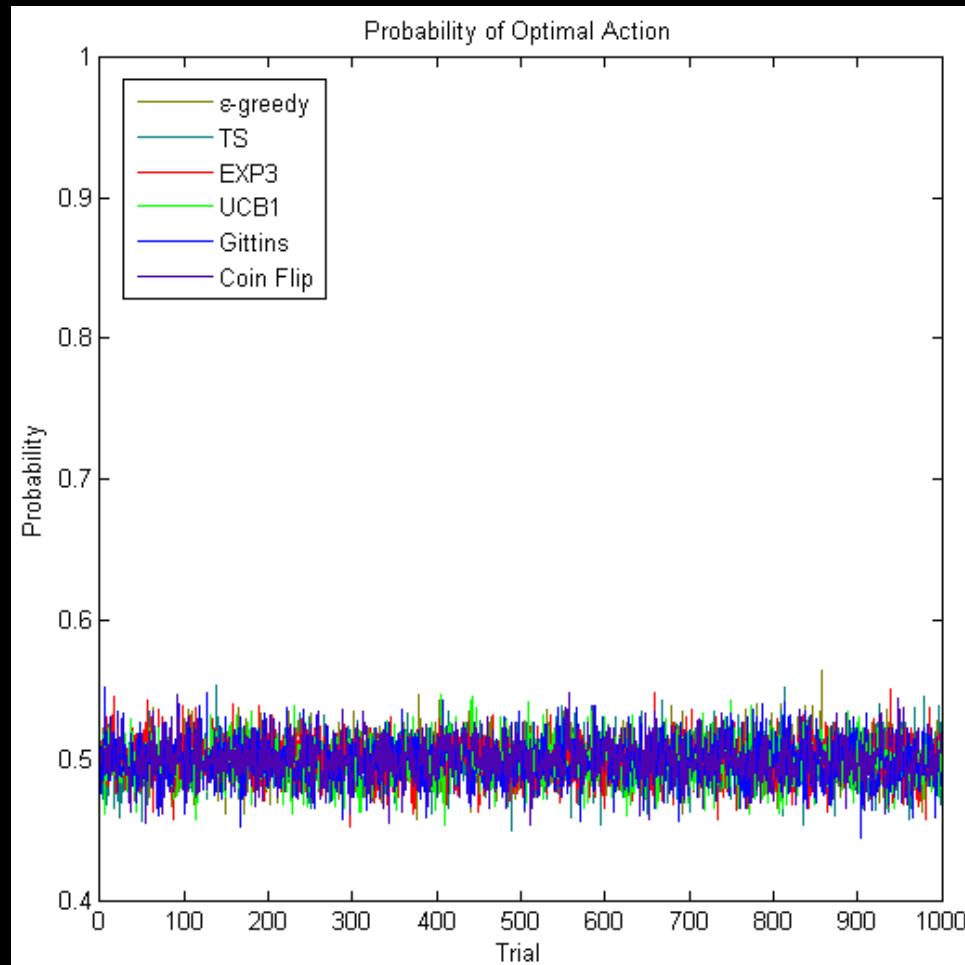


$D_1 \quad E(y_1 | X = x_0) = 0.15$
 $E(y_1 | X = x_1) = 0.15$

$D_2 \quad E(y_1 | do(X = x_0)) = 0.30$
 $E(y_1 | do(X = x_1)) = 0.30$

GREEDY CASINO. INDIVIDUAL VERSUS POPULATION-LEVEL DECISIONS

- Attempt 1. ML (ϵ -greedy, Thompson Sampling, EXP3, UCB, Gittins).



* Bandits minimize short-term regret based on the $\text{do}()$ -distribution.

GREEDY CASINO: CAN WE DO BETTER?

GREEDY CASINO: CAN WE DO BETTER?

- Attempt 2. Counterfactual randomization
- RDC (Regret Decision Criterion):

$$X^* = \arg \max_x E(Y_{X=x_1} | X=x_0)$$

$$X^* = \arg \max_x E(Y | \text{do}(X=x))$$

- This should be read as the counterfactual sentence:
“Expected value of Y had X been x_1 , given that $X = x_0$? ”
(Also known as Effect of Treatment on the Treated.)

GREEDY CASINO: CAN WE DO BETTER?

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$$X^* = \arg \max_x E(Y | \text{do}(X = x)) = E(Y_{X=x})$$
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- This should be read as the counterfactual sentence:
“Expected value of Y had X been x_1 , given that $X = x_0$? ”
(Also known as Effect of Treatment on the Treated.)
- General counterfactuals are difficult (or impossible) to evaluate from data (even experimentally), except for some special conditions (e.g., binary treatment, backdoor admissibility, unconfoundedness) (Pearl, 2000, Ch. 9).

COUNTERFACTUAL DECISION-MAKING

- RDC (Regret Decision Criterion):

$$X^* = \operatorname{argmax}_x E(Y_{X=x_1} | X=x_0)$$

- Evaluating RDC-type expressions:

- Note that the agent is about to play machine x_0 , which means that (the unknown) $f_x(b, d)$ evaluated to x_0 .

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COUNTERFACTUAL DECISION-MAKING

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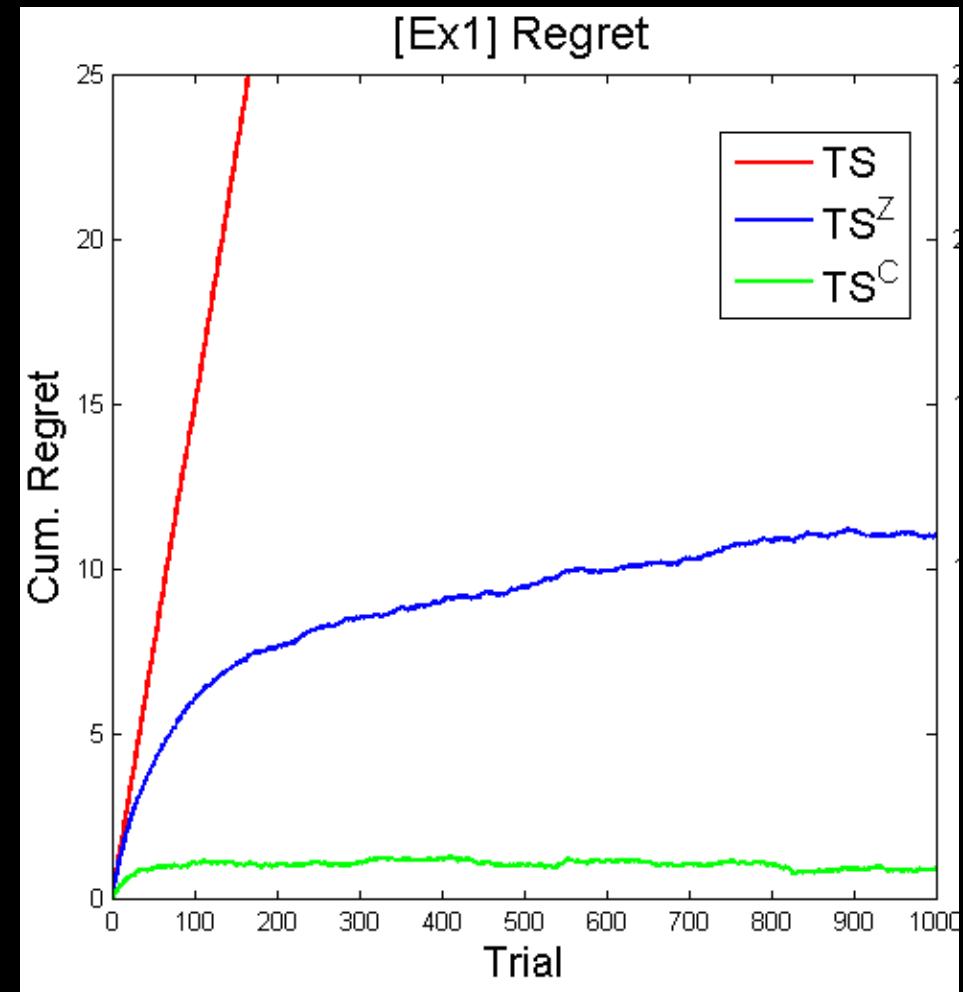
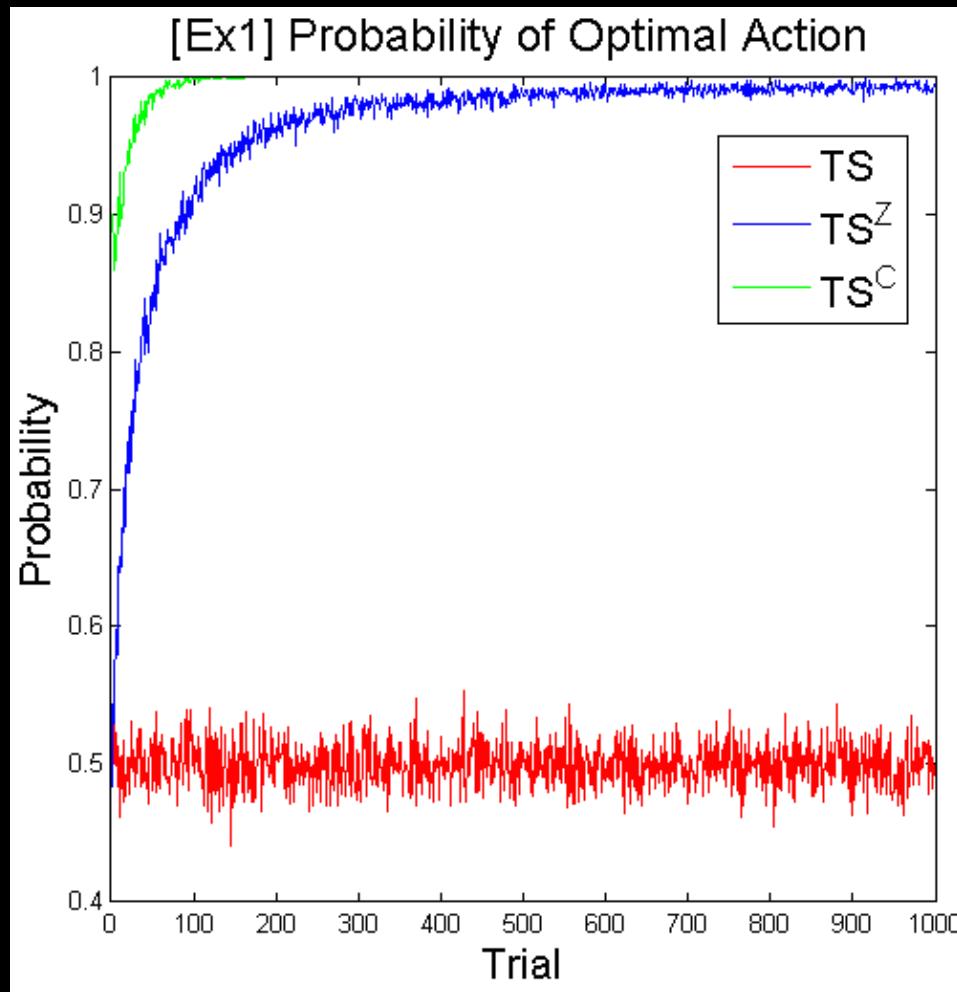
“I am about to play x_0 , would I be better off going with my intuition (x_0) or against it (x_1)?”

Note. If at step 2, we ...

- do not interrupt, allowing $X = x_0 \rightarrow P(x_0, y)$. EDT
- do interrupt and make $X = \text{rand}() = x_1 \rightarrow P(y | \text{do}(x_1))$. CDT
- do interrupt and make $X = \text{rand}() = x_1 | x_0 \rightarrow P(Y_{x_1} | x_0)$. RDT

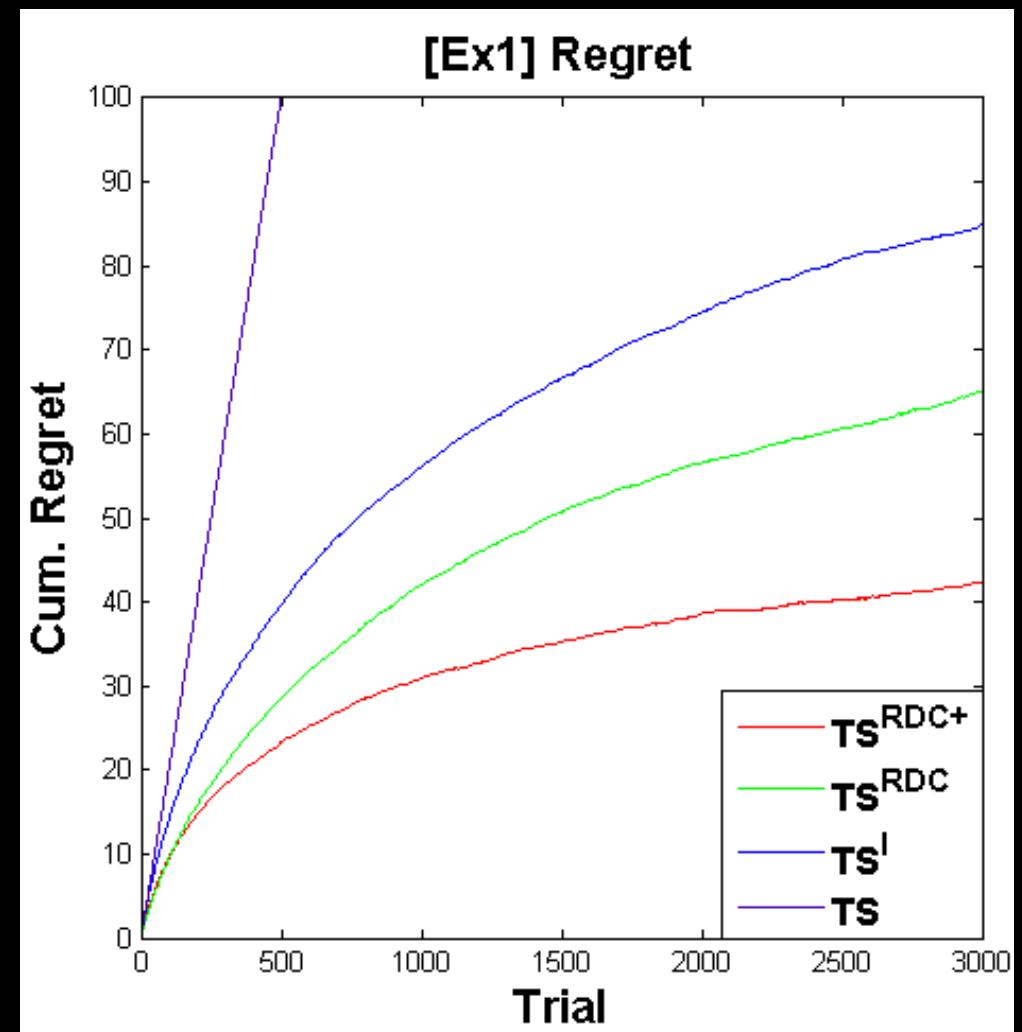
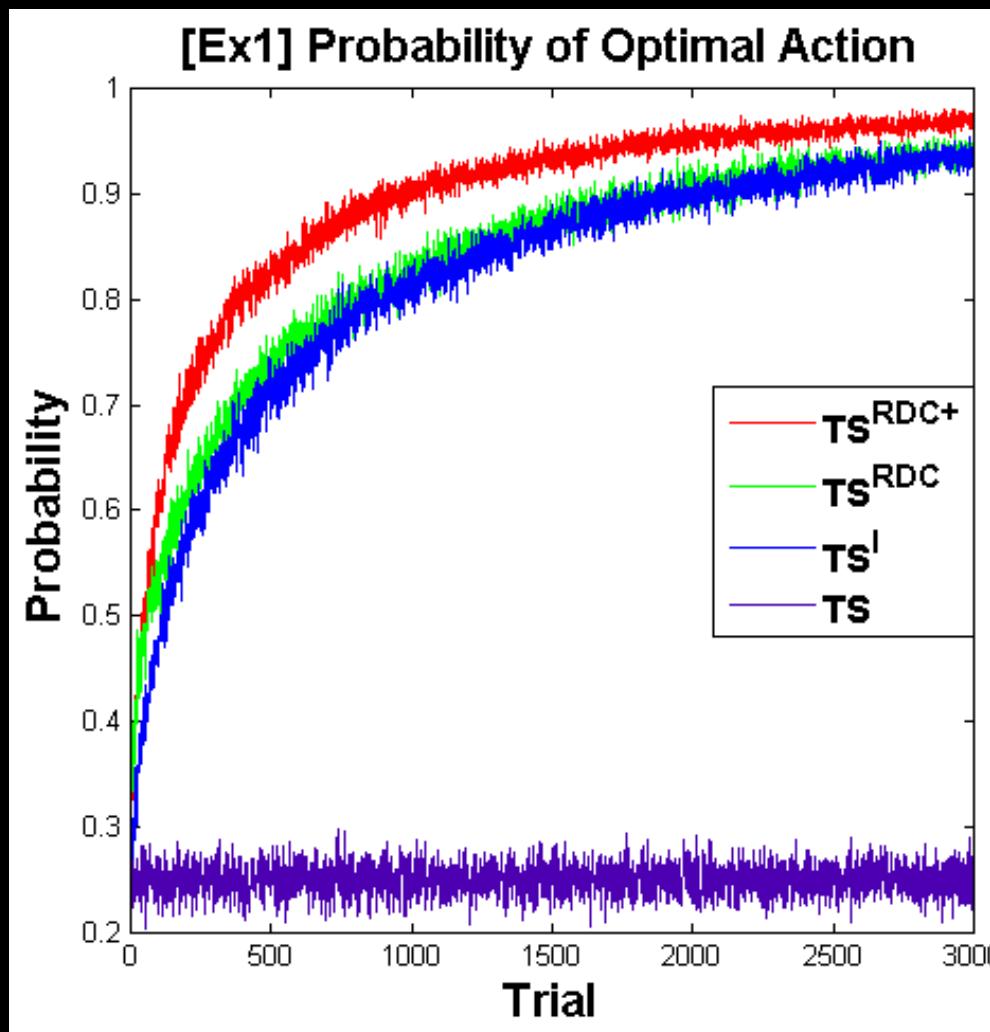
REGRET DECISION CRITERION: EXPERIMENTAL RESULTS

- Greedy Casino Parametrization

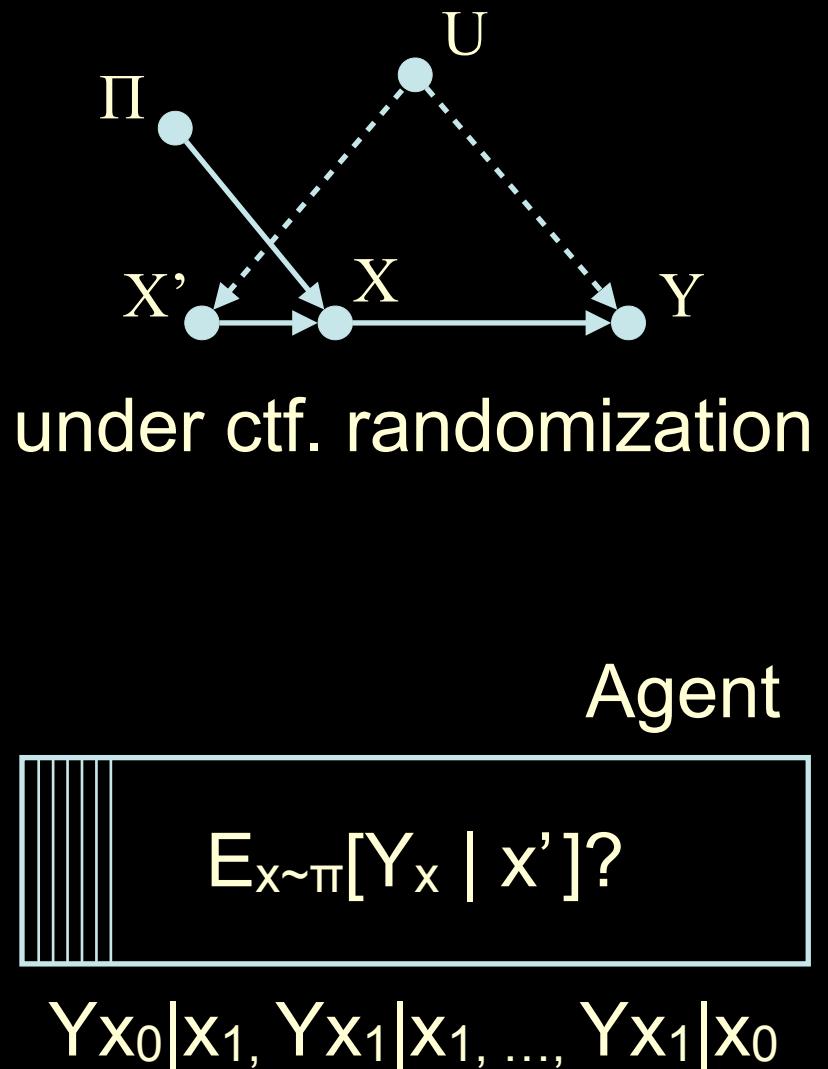
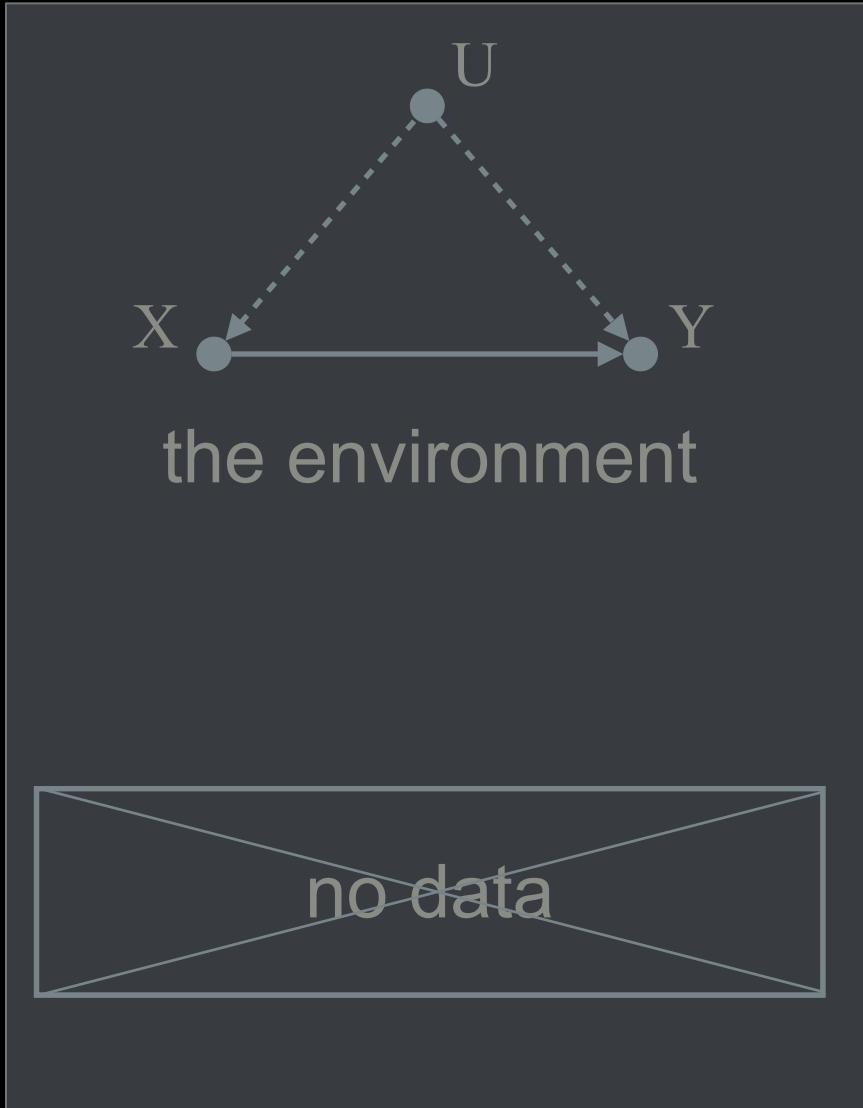


REGRET DECISION CRITERION: EXPERIMENTAL RESULTS

- What if the experimental distribution is available (4-arm case)?



TASK 3. COUNTERFACTUAL LEARNING



APPLICATION: HUMAN-AI COLLABORATION (CAN HUMANS BE OUT OF THE LOOP?*)

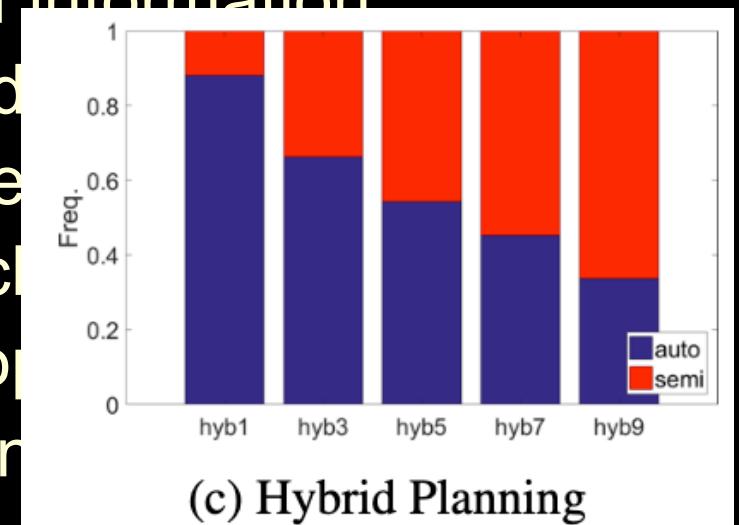
- Observation from the RDC, if $E[Y_x|x'] = E[Y|do(x)] \rightarrow$ the human's intuition has no value of information.
- In words, the human expert could be replaced without sacrificing the performance of the system, at least in principle full autonomy can be achieved.
- Contribution: New Markovian properties (L_2, L_3) that establishes whether an agent can be autonomous.

Env. Model	Optimality		Autonomy
	A_{exp}	A_{ctf}	
MDPUC ⁻	✓	✓	✓
MDPUC	✗	✓	✗
MDPUC ⁺	✗	✓	✗
DSCM ⁻	✓	✓	✓
DSCM	✗	✓	✗

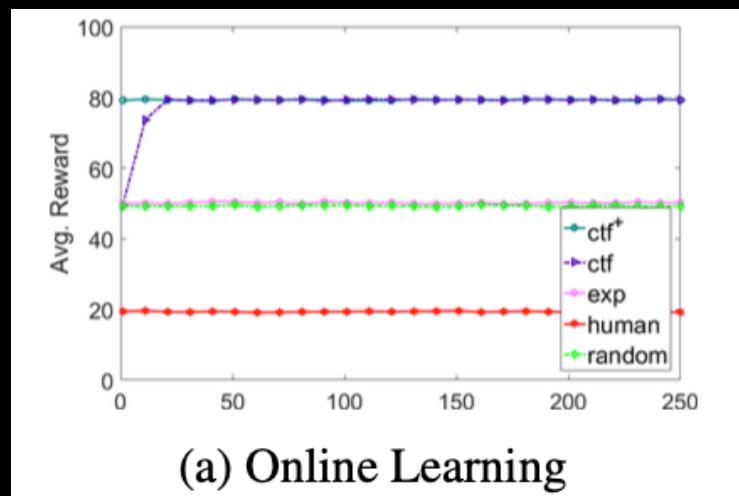
* For details, see [R-64 @CausalAI].

APPLICATION: HUMAN-AI COLLABORATION (CAN HUMANS BE OUT OF THE LOOP?*)

- Observation from the RDC, if $E[Y_x|x'] = E[Y|do(x)] \rightarrow$ the human's intuition has no value of information
- In words, the human expert could be sacrificing the performance of the system principle full autonomy can be achieved
- Contribution: New Markovian property establishes whether an agent can be out of the loop



Env. Model	Optimality		Autonomy
	A_{exp}	A_{ctf}	
MDPUC ⁻	✓	✓	✓
MDPUC	✗	✓	✗
MDPUC ⁺	✗	✓	✗
DSCM ⁻	✓	✓	✓
DSCM	✗	✓	✗

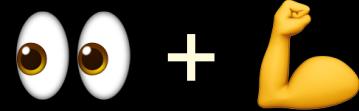


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SUMMARY CRL TASKS

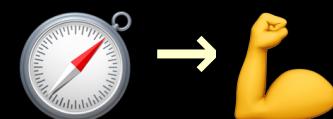
CRL CAPABILITIES (I)

1. Generalized Policy Learning (on+offline)



- Online learning is too costly and learning from scratch is usually impractical. Still, the assumptions of offline learning are rarely satisfied in practice.
- Goal: Move towards more realistic learning scenarios where the two modalities come together, extracting as much causal information as possible from confounded data, and using it in the most efficient way.

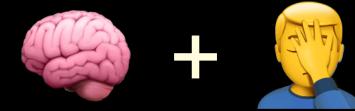
2. When and where to intervene?



- Agents usually have a fixed policy space (actions), and intervening is usually assumed as beneficial.
- Goal: Understand when interventions are needed and whenever this is the case, what should be changed in the system to bring about the desired outcome.

CRL CAPABILITIES (II)

3. Counterfactual Decision-Making (intentionality, regret & free will)



- Agents act in a reflexive manner, without considering the reasons (causes) for behaving in a certain way.
- Goal: Endow agents with the capability of taking their own intent into account, which will lead to a new notion of regret based on counterfactual randomization.

4. Generalizable and Robust Decision-Making (transportability & structural invariances)



- The knowledge acquired by an agent is usually circumscribed to the domain where it was deployed.
- Goal: Allow agents to extrapolate knowledge, making more robust and generalizable claims by leveraging the causal invariances shared across environments.

CRL CAPABILITIES (III)

5. Learning Causal Models by Combining Observations & Experimentation



- Agents have a fixed causal model, constructed from templates or from background knowledge.
- Goal: Allow agents to systematically combine the observations and interventions it's already collecting to construct an equivalence class of causal models.

6. Causal Imitation Learning



- Mimicking is one of the common ways of learning. Whenever the demonstrator has a different causal model, imitating may lead to disastrous side effects.
- Goal: Understand the conditions so that imitation by behavioral cloning is valid and leads to faster learning. Otherwise, introduce more refined imitation modalities.

CRL (CHEAT SHEET)

5. L

1. Generalized Policy Learning (on+offline)

Combining $L_1 + L_2$ interactions to learn policy Π .

2. When and where to intervene?

Identifying subset of L_2 and optimize the policy space.

3. Counterfactual Decision-Making

Optimization function based on L_3 counterfactual & random.

4. Generalizability and Robustness

Generalizing from training environment (SCM M) to SCM M^* .

5. Learning Causal Model G

Combining $L_1 + L_2$ interactions to learn G (of M).

6. Causal Imitation Learning

Learning L_2 -policy based on partially observable L_1 -data (expert).

• Go

behavioral cloning is valid and leads to faster learning.
Otherwise, introduce more refined imitation modalities.

CONCLUSIONS

- CI & RL are fundamentally intertwined and novel learning opportunities emerge when this connection is fully realized.
 - The structural invariances encoded in the causal graph (w.r.t. SCM M) can be leveraged and combined with RL allocation procedures leading to robust learning.
 - Still, failure to acknowledge distinct invariances of the environment (M) almost always leads to poor decision-making.
- CRL opens up a new family of learning problems that were neither acknowledged nor understood before, including the combination of online & offline learning (GPL), when/where to intervene, counterfactual decision-making, generalizability across environments, to cite a few.
- Program: Develop a principled framework for designing causal AI systems integrating [observational, experimental, counterfactual] data, modes of reasoning, knowledge.
 - Leads to a natural treatment to human-like explainability and rational decision-making.

CONCLUSIONS

- CI & RL are fundamentally intertwined and novel learning opportunities emerge when this connection is fully realized.
 - The structural invariances encoded in the causal graph (w.r.t. SCM M) can be leveraged and combined with RL allocation procedures leading to robust learning.
 - Still, failure to acknowledge distinct invariances of the environment (M) almost always leads to poor decision-making.

- Causal Reinforcement Learning is a field where neither causality nor reinforcement learning have been applied to intervene, counterfactual decision-making, generalizability across environments, to cite a few.

- Program: Develop a principled framework for designing causal AI systems integrating [observational, experimental, counterfactual] data, modes of reasoning, knowledge.
 - Leads to a natural treatment to human-like explainability and rational decision-making.



THANK
YOU!

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