

We will try to find the relative difference between two powers,  $P_C$  - the highest input power at which the earth will freeze over, and  $P_H$  - the lowest input power at which the earth will be completely covered in water.

To do this, we must first make a few assumptions:

- The earth consists only of ice or water.
- At temperature  $T = 0^\circ C$  (or below), the earth is completely covered in ice.
- At temperature  $T = 20^\circ C$  (or above), the earth is completely filled in water.
- Ice reflects 70% of all radiation it is exposed to.
- Water reflects 10% of all radiation it is exposed to.
- Due to a greenhouse effect, 50% of all radiation reflected is re-absorbed.
- Let  $P$  denote the total power coming into the earth.
- The earth's radius is 40,000km

Now, let's define  $P_a(T)$  - the Power Absorbed by the earth (as a function of temperature, since temperature affects the composition of earth). We know  $P$  is the total power coming, and that- depending on the composition of the earth- a certain part is reflected outward, let's call this  $P_r(T)$ . Furthermore, 50% of the amount reflected is re-absorbed.

$$\text{So } P_a(T) = P - P_r(T) + .5 * P_r(T) = P - .5 * P_r(T)$$

We know  $P_r(T) = .7 * P$  for  $T \leq 0$ , as the earth will be entirely composed of ice at these temperatures. And for  $T \geq 20$ ,  $P_r(T) = .1 * P$ , as the earth will be entirely composed of water at these temperatures.

Let's assume that  $P_r(T)$  in between these regions is linear. This makes physical sense as the earth will be a mix of ice and water. Furthermore,  $P_r(T)$  should be decreasing in this region.