Assignment 1 writeup

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1 Problem 1

(a)

We have

$$\operatorname{softmax}(\mathbf{x} + c)_{i} = \frac{e^{x_{i} + c}}{\sum_{j} e^{x_{j} + c}}$$

$$= \frac{e^{c}(e^{x_{i}})}{e^{c} \sum_{j} e^{x_{j}}}$$

$$= \frac{e^{c}}{e^{c}} \frac{e^{x_{i}}}{\sum_{j} e^{x_{j}}}$$

$$= \frac{e^{x_{i}}}{\sum_{j} e^{x_{j}}}$$

$$= \operatorname{softmax}(\mathbf{x})_{i},$$

so $softmax(\mathbf{x} + c) = softmax(\mathbf{x})$, as desired.