Fa23: 1)if given a logistic curve, and probabilities, get the y value made at each x value, and multiply the y values to get your answer (1\*.9\*.4) = 0.36 /2) gradient descent, do derivative of function, then plug into function |start - alpha(d/d(start))| ex: alpha = 0.5, starting at (0,0) and the derivative is 2x+1 == (0-0.5(2(0)+1) = 0 - 0.5 = 0.5), so now it's (0.5, 0).

NOTE when doing derivatives, chain rule, bring the exponent down, and do derivatives inside the parenthesis. / 3a) for soft margin svm and given W, b and X and y, do | w\*x (w1\*x1) + (w2\*x2) - b | if > 0, it is +1, if less than 0, it is -1. / 3b) large C value separates data with minimal slack, rbf kernel can capture scattered patterns, use a smaller C value if there are outliers of colors in areas they don't belong, RBF kernel with high gamma handles scattered data across the map/ 4)design matrix is: replace values with said values (X), XtX would have to be the row(1st matrix)\*colum(2nd matrix),

be a transpose, so it must

Done by y(wx+b)//

y = y1, y2, y3/ w must be a 2x1 matrix/ that is a 3x1 matrix, can do process of elimination/ fw,b is (w1\*w2 + w1)/ intercept is the first element of w/\fw,b must be a number 5a) calculate Minkowski distance using given points sqrt(|zi - xi|<sup>2</sup>) zi being z1, z2, etc/5b 3NN classify get y values of closest distances, and choose most frequent /5c 3-NN regression predict = y value of smallest distances, and do average of y values /5d weighted 3-NN classify z Sum inverse (1/x) of distances for each class, then assign z to the class with the highest number with its y'. Since the closest neighbor belongs to class 1 and has the highest weight z is classified as class 1.// 6a) look at threshold, remove values below number//6b) **r\_regression** features most linearly correlated with y, k = 2 means only two options //6c) f regression is variance and correlation/ 7 t/f) if two functions are same w/ a different constant, it is an alternative//gradient desc doesn't call to f// hinge loss = max(0,1- y(wx+b)) // cannot build a 3nn model without errors// cannot train an SVM, then remove support vectors//**SVM**(supportVectorMachine) margin = 2/||w|| (w =  $sqrt(x^2+y^2+z^2)$ )/ every decision tree and kNN regression function is a step function// gradient desc can fail if stuck in a local min/max// 8a) min/max rescaling = (x - min(x))/(max(x)- min(x)) // 8b) OneHOtEncoder: binary encoder: set 1 where values are true, columns are 'if' // 9a1) entropy of node in bits by finding total(zeros)/sum(y) and total(ones)/ sum(y) and then doing H(S)=-(p0\*log2(p0)+p1\*log2(p1))// SP24: logistic model & estimate probability: 1/1+e^-(wx+b) // t/f: product of probabilities can underflow in fixed-precision computer arithmetic. CANNOT OVERFLOW/ differentiating a sum is easier than differentiating a product/ cannot use In() to find a closed-form expression// In() is strictly increasing, maximizing same as minimizing negative log // SVM classify x by wx+b. If >0, +1. If <0, -1// svm constraint holds if >1.

(output)

0

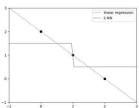
feature, threshold, find midpoints of all features for a threshold, then use y column to see class 0, and class 1. Then ones that fit threshold, do how many count(zeros) / total(zeros), then add count(ones)/total(zeros). We want the most ones displayed on one side of a threshold.

for a decision tree, use x1 values to calculate a midpoint, use a threshold for x1, do average of the fitted threshold, and MSE  $(x1 - avg)^2/n$  (n being number of how many fit the threshold), then do for x2. Once done, do (examples/total examples)\*MSE + 2nd MSE threshold to get the answer/ 5) standardRescaling = (x<sub>orignal</sub> - mean)/stddev 6) cosine similarity distance =  $(z^*x)/(||z||^*||x||) \setminus ||z|| = \operatorname{sqrt}(z^{1^2}+z^{2^2})$ , once cosine sim distance is found, subtract/add to y value to solve. 7a) MSE =  $1/n * (y_1 - y_1^{hat})^2$ , do  $wx_1 + b$  and  $wx_2 + b$ , then do  $((wx_1 + b)^2 + (wx_2 + b)^2) / n$  to

get MSE // **7b)** to find **best fit line**, do  $mu_1 = mean(x_1+x_2)$  and  $mu_2 = mean(y_1+y_2)$ , then do  $((x_1-mu_1)(y_1-mu_2)+(x_2-mu_1)(y_2-mu_2)) / ((x_1-mu_1)(y_1-mu_1))^2$  to get w, to get b, do  $(y_2-mu_2) - w(x_1-mu_1)$  // logistic regression is exponential, no need for additional function/ linear regression model IS sensitive to the signs of label// weighted kNN are inversely proportional to distance// SGD can use more iterations with a smaller learning rate  $\alpha$  than GD//Lasso regression tends to set most coefficients to zero.)

**FA24**: gradient desc can fail if alpha is too big; will have + and - values in each iteration/ gradient desc can fail by descending without bound//clf.SVM) if nonlinear and not complex. Choose **kernel = rbf** and **low gamma**, **less complex** // Two clouds, linearly separable, few outliers, choose **linear kernel**; with low **C** value, low c = more outliers // Random mixed points inside disk (nonlinear), choose **rbf kernel**, and **high gamma**, makes shape tight

SP23:  $P(y=1|x) = 1/(1+e^{-(wx+b)})$  // Gradient desc can fail to converge on **convex** function if stuck in local min// decisiontreeclassifiers are blocky, KNN is **blocky** and has turns, RBF is **curvy** //  $I(0) = -\log 2(\text{zerocount/total})$  //



## **FINAL**

<u>K-means on data</u> -  $\{x\}$  =  $\{1,2,3\}$  c1 = 2, c2 = 3, do |x-c1| and |x-c2|, whichever is lower, assign to c value. Once done, do the average of each c (c1 = 1.5, c2 = 3). If k = 3. Choose three numbers in  $\{x\}$  unless given. If 2nd iteration, use first iterations found.

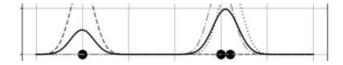
<u>Grid vs random search</u> - grid needs to be fine and goes through individual values in a range, Takes a lot of time also needs specific options to run well. - random search samples values at the mean, and samples from range rather than individual, more random.

<u>T/F</u> - If 0 < d < p < D, PCA on **p** to **d** is same as **D** to **d** | if x,y = -1, (wx+b) >0 is FALSE | threshold is required to predict yhat for Ir | same outcome when MSE and logarithm of MSE is minimized | y wx + b = -1, 0, 1, w is normal to all 3 functions | Ridge regression fixes overfiting of training data | **bagging** and **random forest** methods use resampling with replacement from training examples | **Boosting** builds models sequentially and fixes issues as it builds | **k-NN** may benefit from standardizing features | **Decision trees** don't benefit from standardizing features. | standardizing x in **linear regression** does not benefit | PCA uses greatest variability in the data.

Yes / No - methods used for feature selection/extraction: Lasso regression, Correlation, Kernel-trick, Principal component analysis, Permutation feature importance | methods not used: Kernel Trick, Kernel Density Estimation, Gradient Descent, Ridge Regression Gaussian Curves - Look at the graph, and at each point. Get the y values at each point for each color. Get the average of each value on each point, then get the average of the values.

• (1.6+0+0)/3 at 1 - At 4, (1.6+1.4+0)/3 - At 4.2. (1.4+1.6+0)/3 - (1+1+1.6)/3 = 1.2 if asked for another point, find the values for each color at that point, then do the average to get the answer.

• For density function: the height of the bell curve is at stddev, or where the graph changes shape. Group the bell curves together



<u>Gradient Boosting -</u> Do the average of y values. Dont worry about what X is, because its not considered. Otherwise, it is where the predicted y value is.

To train a 2nd model, do y values - average of y values/predicted values.

Binary Classifier V >>>>>>>>>

Question 8

- Kernel regression get the y values of each bell curve and add it to a group (x, y, z). Add them together, and divide the group by the sum of them (xyz)/(x+y+z). Then get the y value of dataset, and multiply it by the divided group and add (x/xyz \* a) + (y/xyz \* b) + (z/xyz \* c)
- Y = f(x) for x = 1 get the y value of each color, and multiply them by the y dataset, and add them together to get the answer / 8b is easy, just look at y value of x = 1
- Estimated regression function Blue is more important than orange, Hitting the edge is not realistic, make sure the dots are being touched

  Predicted ŷ

Actual y = 0

Actual y = 1

TN

FN

FP

## Question9 - model assessment

- Y is real answer, yhat is predicted, if yhat = y, is correct (if
  It is a TN or TP. but if y is 0 and yhat is 1, is FP, viceversa
  Is a FN. (1 = postive). Remember recall and precision formula
- Calculating AUC 1st(FP = 0, TP = 0.5) or 2nd(FP = 0.5, TP = 1). For 1st(0, 0.5) 0.5 0 = 0.5. Next do 0.5 \* (2nd(FP) + 2nd(TP)) do it again, but do 0.5 \* 2nd(TP + 2nd(TP)).
   Add 0.5 \* (2nd(FP) + 2nd(TP)) + 0.5 \* 2nd(TP + 2nd(TP)) to get answer.
- If TPR = 0, AUC is 0 because it is predicting wrong all the time
- low FN and high TP, **Recall** / high TP and low FP, **precision**. THINK LOGICALLY FOR THESE QUESTIONS

### **RANDOM STUFF**

Precision - proportion of relevant documents (TP/ (TP + TN))

<u>Recall</u> - proportion of relevant documents returned to relevant documents available (TP/(TP+FN))

<u>False negative def</u> - predicts a negative outcome that is positive, cons - missed opportunity for correction, and bad for healthcare, leads to not detecting disease

<u>False positive def - incorrectly predicts</u> a positive that is negative, cons - unnecessary testing, leads to making right things wrong, false alarms and wrongful accusations

Random forest - chooses random subsets for trees based on depth, trees and features

<u>Gradient boosting</u> - builds trees sequentially vs independently (random forest)

<u>Imbalance datasets solutions -</u> oversample, undersample, make synthetic examples, train test split

Combine models

 Average predictions, stacking (uses more info and uses different models for information)

<u>Unsupervised learning</u> - works with no y value,

- Clustering
  - Chooses examples and has a centroid, labels each example closest to centroid, until a convergence is found
- DBSCAN
  - Puts x in cluster if too close to other points with threshold epsilon and n, the number of values that can be in a cluster. Neighbors of clusters are clusters
  - o Good for noisy data, weird shaped data, outliers of DB scan have no neighbors
- Dimension reality
  - Maps x into vector with less features to reduce noise and to be able to visualize it
  - PCA benefits
    - Saves memory, space and computation time due to compressing information, can visualize data up to [0, 10]^D

### **Homeworks**

<u>HW4 -</u> Training Data: Linear regression, because it has the lowest MSE, meaning it fits the data better

Test Data: Ridge, because it reduces over/under fitting on unknown data and reduces noise Feature Selection: Lasso, because many of the w coefficients are close to 0, so lasso would already make those 0s irrelevant

### **Review bs**

#### Question 5

- Std is where the curve changes
- KERNEL DENSITY ESTIMATION
- Zeros at the curve, via the color
  - Look at the color
  - (1.6+0+0)/3 at 1
  - o At 4, (1.6+1.4+0)/3
  - o At 4.2. (1.4+1.6+0)/3
  - (1+1+1.6)/3 = 1.2

### Question 9

• ???

#### Question 7 (weird graph one)

- Hard margin means linearly separable
- Blue is +1, red and green is -1
- For each of the 1 vs rest classifier, find the rest of the signed distance of boundaries
- Questions
  - For blue, make diagonal SVM???

# Question 8c

- Three weights have to sum to one
  - 1/2 1/2 0
  - Got by adding (0 + 1.5+1.5 )/sum of 3 values
- 8b is easy, just look at y value of x = 1
- 8c
- Blue is more important than orange
- o Hitting the edge is not realistic, make sure the dots are being touched

#### Question 6

- What does x = 2 do????
  - o Starts with a constant model, which is the average of y
  - Does nothing??? Just a constant model. IT DOES NOTHING.