

# Towards real-world capable spatial memory in the LIDA cognitive architecture

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## Abstract

The ability to represent and utilize spatial information relevant to their goals is vital for intelligent agents. Doing so in the real world presents significant challenges, which have so far mostly been addressed by robotics approaches neglecting cognitive plausibility; whereas existing cognitive models mostly implement spatial abilities in simplistic environments, neglecting uncertainty and complexity.

Here, we take a step towards computational software agents capable to form spatial memories in realistic environments, based on the biologically inspired LIDA cognitive architecture. We identify and address challenges faced by agents operating with noisy sensors and actuators in a complex physical world, including near-optimal integration of spatial cues from different modalities for localization and mapping, correcting cognitive maps when revisiting locations, the structuring of complex maps for computational efficiency, and multi-goal route planning on hierarchical cognitive maps. We also describe computational mechanisms addressing these challenges based on LIDA, and demonstrate their functionality by replicating several psychological experiments.

*Keywords:*

spatial memory, LIDA, cognitive architecture, computational cognitive modeling

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## 1. Introduction

Spatial representations are important for biological as well as artificial agents, in order for these agents to be able to localize, and navigate to, important objects and places (such as food sources or shelters). Current computer models for learning spatial representations either neglect cognitive plausibility in favour of performance, such as Simultaneous Localization and Mapping (SLAM) in robotics, or are incapable of running in large-scale, complex, uncertain environments perceived through noisy sensors.

Since biological cognition has been shaped by the structure, constraints, and challenges of the physical world, we argue cognitive architectures should take these into account as well. This argument is in accordance with the roadmap for the BICA chal-

lenge, which also places importance on real-life capability (Samsonovich, 2012). This paper describes an effort to take the LIDA (Learning Intelligent Distribution Agent) cognitive architecture (Franklin et al., 2014) closer to this goal. We introduce a novel conceptual and partially implemented, hierarchical spatial memory model, inspired by the neural basis of spatial cognition in brains, and provide a preliminary interface to realistic environments via the Robot Operating System (ROS) (Quigley et al., 2009). We demonstrate these extensions in three-dimensional simulated environments which include simulated physics and high-quality graphics, based on the Player/Stage/Gazebo simulator<sup>1</sup>. This simulator presents the same interface to the agent as real devices, and an agent able to control a robot in Gazebo is also able to control the same robot in similar environments in the real world, without any

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<sup>1</sup><http://www.gazebo-sim.org/>

changes to the control code (Rusu et al., 2007).

This paper describes an effort to extend the LIDA cognitive architecture by cognitively and biologically plausible spatial mechanisms, which are capable of handling the challenges of the real world, associated with noisy sensors and large-scale environments. We hypothesize and implement approaches to tackle the sensory noise, uncertainty, and complexity of realistic environments.

We build on and integrate our previous work investigating biologically and cognitively plausible implementations of Bayesian localization (Madl et al., 2014), Bayesian nonparametric clustering for map structuring (Madl et al., submitted), and route planning based on activation gradients<sup>2</sup> (Madl et al., 2013). The method for cognitive map correction (loop closing) is presented for the first time below. Although based on established mathematical tools from robotics, it is - to our knowledge - the first mechanism for large-scale cognitive map correction implementable in brains, and consistent with the replay phenomena observed in the rodent hippocampus (Carr et al., 2011).

The present work is also (to our knowledge) the first to provide implementations of these mechanisms in a both cognitively and biologically plausible fashion (fitting behaviour data and implementable in brains), and integrated within the same cognitive architecture. Further contributions include concrete implementations of some features listed by the BICA Table (Samsonovich, 2010) which until now were only part of conceptual LIDA, including basic stereo colour vision, a cognitive map, spatial learning, and fusing information from multiple types of sensors and modalities via Bayesian update.

### 1.1. Related work

Apart from the complex perception problem, the most challenging problems for building spatial representations in realistic environments include localization and mapping under sensory noise, and correcting incorrect representations when revisiting known locations (loop closing). The robotics community has developed several solutions to these

problems - see (Thrun and Leonard, 2008; Durrant-Whyte and Bailey, 2006; Bailey and Durrant-Whyte, 2006; Williams et al., 2009). They have been designed to be accurate, not cognitively or biologically plausible, and rely on mechanisms which are difficult to implement in brains (e.g. many iterations performing operations on large matrices).

An exception is the partially connectionist RatSLAM system (Milford et al., 2004) which can learn robust maps in outdoor environments (Prasser et al., 2006), and close large loops successfully, if extended by a sophisticated data association method (Glover et al., 2010). Parts of it have been argued to be biologically plausible (Milford et al., 2010). However, RatSLAM has two disadvantages in the context of a cognitive model with long-term learning aiming for plausibility: 1) route planning only works along established routes (novel detours or shortcuts have not been demonstrated), 2) learned spatial information is mapped to a finite structure of fixed size (a continuous attractor network with wrapping connectivity) which cannot be expanded.

On the other hand, models which emphasize plausibility - cognitive architectures and plausible spatial memory models - mostly focus on simplistic simulated environments, usually with no sensory noise and limited size/complexity. There are a few neurally inspired spatial memory models which can deal with a limited amount of uncertainty and noise (Burgess et al., 2000; Strösslín et al., 2005; Barrera et al., 2011); but have only been tested in small indoor environments. See Madl et al. (2015) for a review.

## 2. Hypotheses

The LIDA cognitive architecture is based on Global Workspace Theory (GWT) (Baars, 2002; Baars and Franklin, 2009), an empirically supported theory of consciousness (Baars et al., 2013), and has been argued to be biologically plausible (Franklin et al., 2014, 2012). Just as the rest of LIDA can be mapped on to the underlying neuroscience (Franklin et al., 2012) (although not always in a one-to-one fashion), it is also the aim of the model proposed here to have parts which functionally correspond to the relevant areas in the brain representing space. This imposes some functional and connectivity constraints.

Apart from well-established implications of the neural representations in these brain areas, including the existence of a neural path integrator (Mc-

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<sup>2</sup>Route planning in navigation space based on activation gradients has been proposed before (Schölkopf and Mallot, 1995; Burgess et al., 2000), but not on a hierarchy - as it is in this work - which significantly improves its performance on multiglobal problems.

Naughton et al., 2006) and of cells representing current location (hippocampal ‘place cells’ (Moser et al., 2008)), the spatial memory model presented here also proposes and requires the following hypotheses. They are motivated by computational challenges facing agents operating in the real world - the ability to represent uncertainty, to estimate locations based on uncertain data, and to represent large amounts of spatial information efficiently are all essential for a real-life, embodied cognitive agent. Our choice of computational approaches (among all possible mechanisms) directly follow from these hypotheses.

1. Spatial uncertainty is encoded in brains, and spatial cues are integrated in an approximately Bayes-optimal fashion. The representation of uncertainty is a computational requirement for localization in the real world, given the unavoidable sensory inaccuracies and noise; and implies the existence of a mechanism for combining modalities with different accuracies. Apart from behavioural evidence substantiating such a mechanism (Cheng et al., 2007), we have found neural evidence based on single-cell recordings of rat hippocampal place cells in previous work, implying that these cells are able not only to represent, but also to combine, information from different modalities and the associated uncertainties (Madl et al., 2014).
2. Hippocampal replay (Carr et al., 2011) in awake mammals aids correcting cognitive maps based on revisited places (see Section 3). Despite local error correction by integrating spatial information, residual errors are still accumulating. This can lead to incorrect maps and to duplicate representations of the same places. Thus, a mechanism is required that can close loops, and correct maps, when revisiting places.
3. Instead of a single unitary and global map, cognitive maps are fragmented (Derdikman and Moser, 2010) and hierarchical (Hirtle and Jonides, 1985), and their structure arises from clustering, i.e. from a process grouping together objects which are ‘close’ in some psychological space. Hierarchical representations are ubiquitous in computer science and robotics, given their efficiency in terms of access and search time and memory use. These advantages are important for storing and accessing large-scale cognitive maps. We found evidence

for hierarchies and for a clustering mechanism accounting for them in (Madl et al., submitted).

4. Human multi-goal route planning is consistent with a simple navigation strategy based on spreading activation on a recurrently interconnected, hierarchical, grid-like network of nodes representing locations (see Section 3 and (Madl et al., 2013)).

### 3. Spatial memory in brains

Spatial Memory encodes, stores and recalls spatial information about the environment and the self location of agents (biological or artificial), which they need to keep track of to successfully navigate. In most mammals, keeping track of position is achieved by path integration, which refers to updating the agent’s position based on a fixed point and the movement trajectory (based on information from proprioceptive and vestibular systems as well as sensory flow (Mittelstaedt and Mittelstaedt, 1980; Fortin, 2008)), and is a noisy process accumulating large errors if uncorrected (Etienne et al., 1996).

Spatial information can be encoded in an egocentric fashion - relative to the agents body and head direction - or as allocentric representations, relative to environmental landmarks/boundaries. Here, we will describe major brain areas associated with these representations, and their correspondences in LIDA. For reasons of space, these descriptions will be very brief. More detail can be found in Madl et al. (2015).

The ability to recognize objects (e.g. landmarks, shelters, food sources, ...) is a prerequisite for encoding useful spatial memories. The brain areas involved in this complex functionality include the sensory cortices and the areas marked (1a) and (1b) in Figure 1 (Kiani et al., 2007; Davachi et al., 2003; Winters and Bussey, 2005; Wilson et al., 2013). The recognition of places is associated with its own area in the parahippocampal cortex, often called the Parahippocampal Place Area (PPA) (Epstein, 2008).

Representations of allocentric (world centered) in mammalian brains include place cells in the hippocampus, which represent spatial locations, firing only in small spatially constrained areas in an environment (ranging from 20cm or less to several meters in diameter, O’Keefe and Burgess, 1996; Kjel-

strup et al., 2008). They also participate in associating objects with specific places (Kim et al., 2011; Manns and Eichenbaum, 2009). In these cells, ‘hippocampal replay’ has been observed - a sequence of place cells associated with visited locations is frequently re-activated either in the same order or in reverse, on rapid (sub-second) timescales; suggested to aid memory consolidation (Carr et al., 2011). Replay often occurs in reverse at the end of a run, and forward when anticipating a run, and contains distance information between the firing fields (Diba and Buzsáki, 2007). Head direction is encoded by cells in a network including the Anterior thalamic nuclei, mamillary body, subiculum and EC (Taube, 2007). Border cells (Lever et al., 2009; Solstad et al., 2008) and boundary vector cells (BVCs) (Burgess, 2008a; Barry et al., 2006) in the subiculum play a role in representing the distance (and, for BVCs, the direction) to boundaries in the environment. Path integration, i.e. maintaining a location estimate by integrating self-motion signals, is performed by grid cells in the medial EC (Hafting et al., 2005; McNaughton et al., 2006).

Together, these cell types form a core part of the ‘cognitive map’, i.e. a map-like allocentric representation of the environment (McNaughton et al., 2006; Burgess, 2008b); and allow animals to keep track of where they are (place cells and grid cells), which direction they are facing (head direction cells), and where boundaries (border cells / BVCs) and objects (place cells) might be in their vicinity (see markers 2a-2c in Figure 1).

In addition to allocentric representations, there are multiple egocentric brain areas encoding spatial information relative to the animal. This includes the visual and auditory systems, and the precuneus ((3) in Figure 1), which is the main brain area concerned with egocentric representations and their use in controlling body and limb-centered actions (Zahle et al., 2007; Kravitz et al., 2011; Vogetley et al., 2004) (for example, area 5d within the precuneus encodes ‘reach vectors’ between hand and target). The retrosplenial cortex (RSC) is involved with converting between egocentric and allocentric representations (Epstein, 2008). Finally, the basal ganglia encode guidance behaviours by means of associating spatial relations relative to the animal with actions (e.g. turn right at the rock). This is an effective strategy for well-known routes (Hartley et al., 2003); however, allocentric representations (‘cognitive maps’) are required in order to be able to plan novel routes or shortcuts.

## The LIDA cognitive architecture

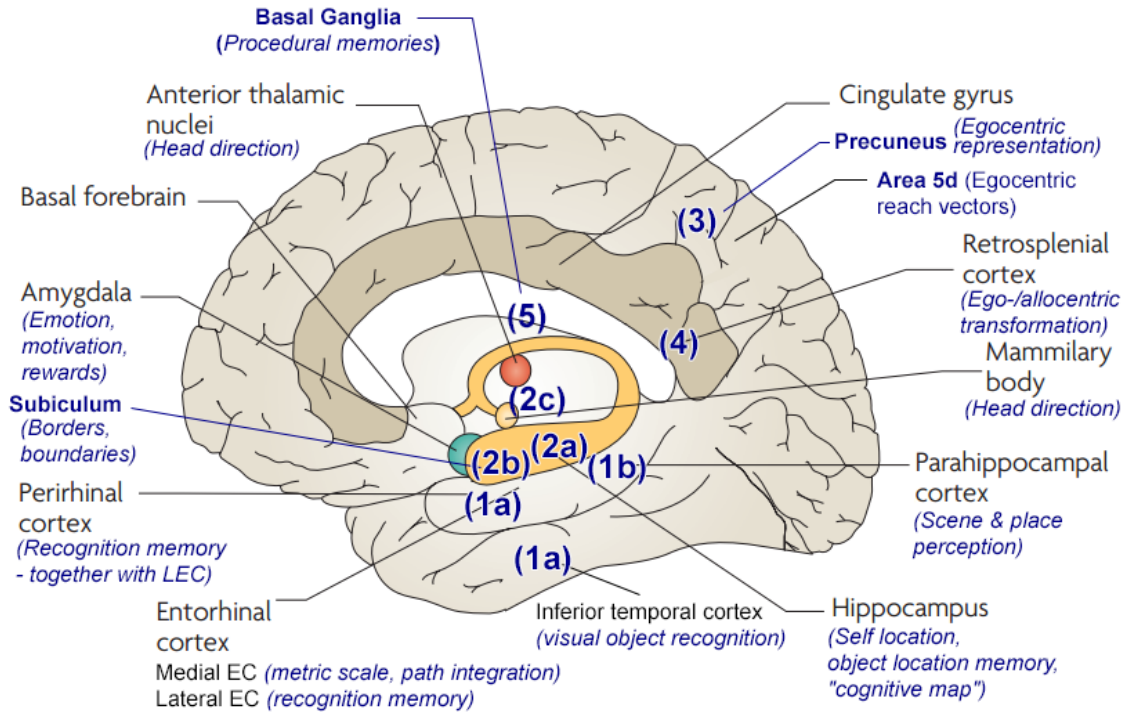
Here we will briefly introduce LIDA - see (Franklin et al., 2014, 2012) for a more detailed description of LIDA, and its relationship to the brain. The LIDA cognitive architecture is based on prevalent cognitive science and neuroscience theories (e.g. Global Workspace Theory, situated cognition, perceptual symbol systems, ... (Baars and Franklin, 2009)), and is one of the few cognitive models which are biologically plausible and to provide a plausible account for consciousness (Baars and Franklin, 2009; Baars et al., 2013), attention, feelings and emotions; and has been partially implemented (Franklin et al., 2014; Goertzel et al., 2010; Snider et al., 2011).

Similarly to the action-perception cycle in neuroscience (Freeman, 2002; Fuster, 2002), LIDA’s cognitive cycle has the purpose of selecting an action based on percepts (Figure 1 bottom). During each cycle the LIDA agent senses its environment, stores information in Sensory Memory and tries to recognize familiar objects, which are represented as nodes in Perceptual Associative Memory (PAM). It associates percepts with memories (declarative, episodic, spatial) recalled from a Sparse Distributed Memory (SDM) instance, creating models of the current situation (CSM) in the Workspace, which consist of the relevant PAM nodes copied to the Workspace. Several Structure Building Codelets<sup>3</sup> (SBC) - specialized ‘processors’ - operate on the pre-conscious representations in the Workspace. Subsequently, the agent decides what part is most in need of attention (Attention Codelets), which is moved to Global Workspace. Broadcasting the most salient<sup>4</sup> portion of CSM (bringing it to consciousness) enables the agent to choose actions applicable in the current situation from Procedural Memory and to select the action best serving its goals (Action Selection).

Figure 1 contains a tentative mapping to spatially relevant modules and mechanisms in LIDA to those in the brain, described below. It is intended to provide a starting point for the implementation of these mechanisms (taking inspiration from the

<sup>3</sup>In LIDA, the term codelet refers to small, special purpose processors or running pieces of software code; and corresponds to ‘processors’ in Global Workspace Theory (Baars and Franklin, 2009)

<sup>4</sup>We use ‘salient’ as an umbrella term for percepts which are important, urgent, insistent, novel, threatening, promising, arousing, unexpected etc.



## LIDA

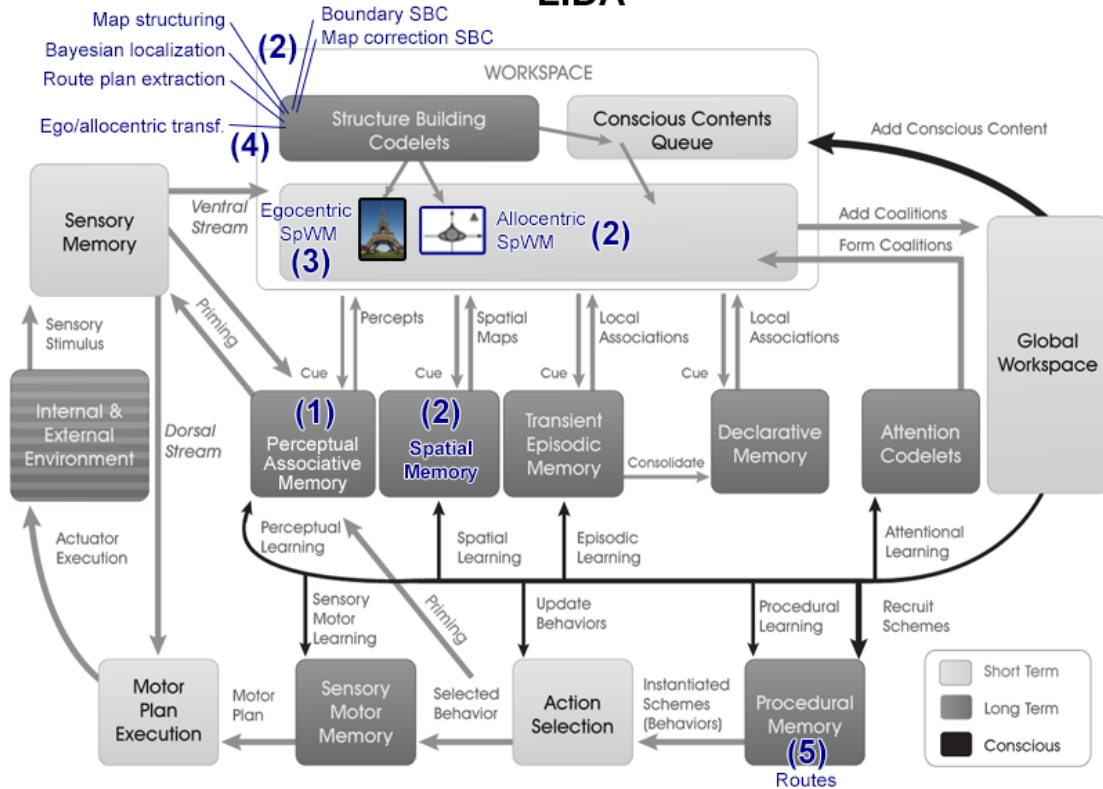


Figure 1: **Spatially relevant brain areas and LIDA modules.** Top: Neural correlates involved in spatial processing. Modified from (Bird and Burgess, 2008) with permission. Bottom: functionally corresponding modules and processes in LIDA. Only spatially relevant correspondences are marked here; see Franklin et al. (2014, 2012) for others.

underlying neural correlates), as well as to clarify LIDA’s functionality to readers with relevant neuroscience knowledge by pointing out functional correspondences. This tentative mapping is by no means intended to suggest that LIDA implements exact neural mechanisms. Although heavily inspired by and resting on results from cognitive neuroscience and psychology, LIDA is a model of minds, not of brains (Franklin et al., 2012).

### **Towards real-world capable spatial memory in LIDA**

The following subsections describe computational extensions made to LIDA in order to allow it to encode, store and recall spatial information obtained from real-world environments. Figure 2 provides an overview of these extensions. Note that some of these, such as the LIDA-ROS interface and the visual recognition mechanism in EPAM (Extended PAM), do not have correspondents in conceptual LIDA, and are not claimed to plausibly model minds. Rather, they make extensive use of already existing technologies for solving low-level problems (mainly vision and motor control), which are outside the scope of this work. Although efforts are under way to implement these mechanisms in a cognitively plausible fashion (see e.g. (McCall and Franklin, 2013; Agrawal and Franklin, 2014) for perceptual learning via cortical learning algorithms, and (Dong and Franklin, 2015) for action execution), they are not yet mature enough to facilitate the present application scenario.

#### *Perception, object and uncertainty representation*

LIDA’s PAM contains nodes and links which are the building blocks of ‘node structures’, which are similar to and inspired by Barsalou’s perceptual symbols (Franklin et al., 2014; Barsalou, 1999). PAM nodes represent higher-level features, such as objects, categories, relations, events, situations, feelings/emotions, etc; and are connected by PAM links, which are weighted and allow passing activation between the nodes. In the implementations in this paper, we have extended LIDA’s PAM by an object recognition system based on a convolutional neural network (CNN), yielding EPAM (Extended PAM).

CNNs are a kind of deep learning architecture designed to process 2D or 3D data such as images - on which they have led to several breakthroughs

(LeCun et al., 2015) -, and are usually trained by a gradient descent procedure called backpropagation. This algorithm has been criticized as not biologically realistic (Stork, 1989) (although there are versions of deep learning that can be implemented by biological neurons (Bengio et al., 2015)). However, despite these arguments concerning implementation, the representations found by state of the art CNNs trained on real-world images are highly similar to those recorded in the inferior temporal (IT) cortex of human and nonhuman primates (Khaligh-Razavi and Kriegeskorte, 2014; Yamins et al., 2013).

We have extended PAM by pre-trained CNNs<sup>5</sup> for object recognition (Szegedy et al., 2014) and road detection (Brust et al., 2015) - see Figure 3. The top layer (softmax layer) of the former was replaced by a classifier trained offline using a dataset of the buildings used in the Gazebo simulation, rendered from different perspectives and distances. (Learning should happen in a development fashion in LIDA, not offline; but this exceeds the scope of the current work). Since CNNs perform best on images containing a single object in the foreground, having difficulties with clutter, camera images were first segmented, and object recognition performed on the individual segments.

#### *Allocentric spatial memory and localization*

As described in Section 3, in brains, hippocampal place cells encode animals’ current location in the environment, as well as providing object-place associations. Their equivalent in LIDA is implemented via a special type of PAM nodes, ‘place nodes’, each of which represent a specific region in the environment, and which reside in the Workspace (as part of the Current Situational Model). Place nodes can be associated with objects perceived to be at that particular location via PAM links - for example, agents’ self-representation (‘self’ PAM node) can be associated with the place node representing their most likely location (which needs to be updated regularly). They are also initially connected recurrently to all their neighbours via PAM links. This has been argued to be a plausible connectivity pattern of the hippocampus (Moser et al., 2008; Csizmadia and Muller, 2008; Samsonovich and McNaughton, 1997).

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<sup>5</sup>These CNNs were available from <https://github.com/BVLC/caffe/wiki/Model-Zoo> and <https://github.com/cvjenacv/cn24>

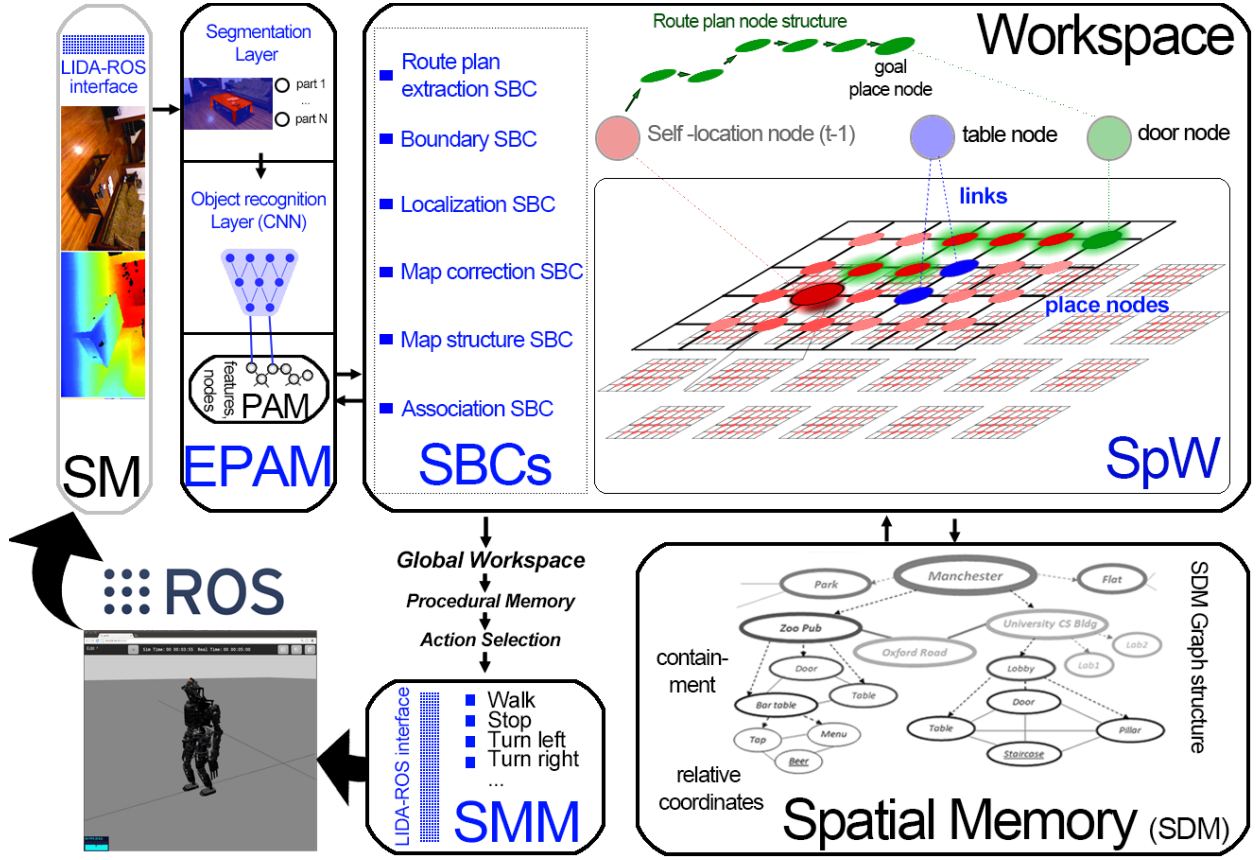


Figure 2: **Extensions to add spatial abilities to LIDA.** From the top left, clockwise: the LIDA-ROS interface transmits image and depth information (from stereo disparity) from the robot’s visual sensors to Sensory Memory (SM). Object recognition is performed by CNNs in EPAM (Extended PAM), which pass activation to recognized PAM nodes representing objects. These can be associated with the place nodes corresponding to their most likely location in SpW (Spatial Workspace) in the Workspace. These place nodes, links between them, and object associations constitute ‘cognitive maps’, and are constructed, updated, and organized by various Structure Building Codelets (SBCs). Those with enough activation to be broadcast consciously can be learned as long-term SDM representations; and can also recruit route-following behaviours in Procedural Memory and Action Selection, leading to the execution of a low-level action in Sensory-Motor Memory (SMM), which is transferred to the robot via the LIDA-ROS interface.

Any PAM node in the Workspace representing currently or recently perceived objects (obstacles, landmarks, goals, etc.) in LIDA’s Workspace can be associated via PAM links with spatial locations represented by place nodes. A node structure comprised of such object nodes, association links, and place nodes together constitute a ‘cognitive map’. Multiple ‘cognitive maps’ can be used within the same environment in a hierarchical fashion (there can be maps and sub-maps on different scales and resolutions, and relative position and containment relations between them). This is consistent with neural and behavioural evidence that the human cognitive map structured (Derdikman and Moser,

2010) and hierarchical (Hirtle and Jonides, 1985) (see (Madl et al., submitted) for more extensive literature and evidence). It should be mentioned that the regular grid-like pattern of these place nodes, imposed for computational simplicity, is not biologically realistic, as no regularities have been found in the distribution of firing fields of place cells (however, a regular grid has been observed in the EC).

Although these maps are temporary, created and updated in the Workspace, they can be stored in the Spatial Memory module (which can encode trees and sequences (Snaider and Franklin, 2014)) as long-term memories if they are salient enough to be broadcast consciously. This long-term memory



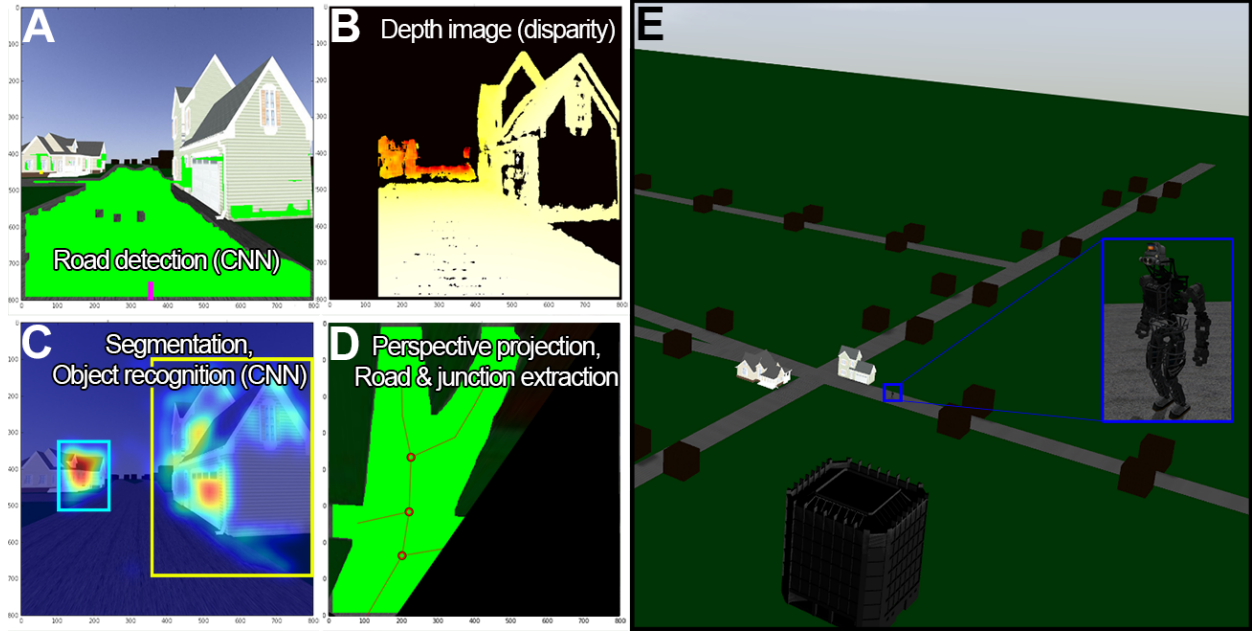


Figure 3: **Representations in Extended PAM (A-D) in one of the environments recreated in the Gazebo simulator (E).** A: Camera image with detected road. B: Depth image from binocular disparity. C: Likely objects from segmentation (hot colours), recognized by a CNN. D: Perceived road after denoising and projection based on the depth image.

storage mechanism has not been implemented yet.

Cognitive maps are assembled and updated by structure-building codelets (SBC) in the Workspace (LIDA’s pre-conscious working memory). Each of these SBCs addresses a computational challenge associated with endowing an autonomous agent with spatial capabilities (see Figure 2):

- the ‘Association SBC’ associates large objects recognized by EPAM with place nodes, making use of distance information from stereo disparity to infer their approximate position and size,
- the ‘Boundary SBC’ detects boundaries in the Workspace, removing links at the locations of these boundaries (currently performed at the boundaries of recognized roads), only leaving links between traversable places (facilitating planning),
- the ‘Localization SBC’ is responsible for updating the link between the Self PAM node and the place node representing the agents most likely current position in the environment, using Bayesian inference to combine spatial cues,
- the ‘Map correction SBC’ corrects the map (closes the loop) based on revisited locations

(see next section),

- the ‘Map structure SBC’ spawns new cognitive maps from parts of the current map, based on the proximity of objects represented on a map, in a process resembling clustering, and
- the ‘Route plan extraction SBC’ extracts shortest routes if a goal representation is present in the Workspace.

The Map structure SBC processes all place nodes which have associated objects, and clusters these objects based on 1) their spatial location, 2) their functional similarity, and 3) boundaries separating them; using Bayesian nonparametric clustering (as described and substantiated experimentally in (Madl et al., submitted)). Apart from accounting for the structure of cognitive maps, Bayesian nonparametric models has also been successful at accounting for category learning (Sanborn et al., 2006) and unifying rational models of categorization (Griffiths et al., 2007). This SBC groups together objects that are close to each other along the given features (in our case, spatial distance and functional similarity). The Map structure SBC spawns a new cognitive map (sub-map) for each



identified cluster, consisting of the objects in that cluster and their place nodes; and adjusts the density of place nodes depending on the area of this cognitive map (so that large-scale maps contain a low resolution and small-scale maps a high resolution place node grid). This process leads to a hierarchy of cognitive maps, a structure suggested to be employed by human spatial memory (Hirtle and Jonides, 1985; McNamara et al., 1989; Madl et al., submitted).

The Localization SBC is responsible for updating the agents estimated location after each movement, by linking its Self PAM node with the place node representing this location. Simply using path integration (odometry) to add up self-motion signals keeps accumulating errors (Etienne et al., 1996; Jeffery, 2007). This problem has been tackled in robotics in the framework of Bayesian inference, integrating information from odometry with sensory observations (the remembered vs. perceived locations of landmarks / boundaries in the environment) in a statistically optimal fashion (Thrun and Leonard, 2008). In its simplest form, this entails Bayesian integration of spatial cues. It has been argued that brains might employ a similar mechanism (Cheung et al., 2012; Madl et al., 2014).

Spatial uncertainty regarding the location of the agent, as well as the locations of recognized objects, is encoded as the parameters of multivariate Gaussians (i.e. means and covariances) attached to EPAM nodes in the Workspace and manipulated by the Localization SBC. After every movement, this SBC performs three steps. First, the location estimate of the agent is moved based on the self-motion signal. Second, the self-location estimate, and the landmark location estimates, are corrected in a Bayesian fashion (see equations (1) and (2) below). Finally, the links of the nodes representing them are updated to the place node corresponding to the best estimate. Correction takes into account the mean and uncertainty of the positions  $\mathbf{x}$  updated by path integration of all movement signals  $\mathbf{m}_1, \dots, \mathbf{m}_i \in M$ , as well as the current observations  $\mathbf{o}_1, \dots, \mathbf{o}_N \in O$  of landmark positions  $\mathbf{l}_{i,1}, \dots, \mathbf{l}_{i,N} \in L$ , expressed as probability distributions. It calculates the Bayesian posterior of the location given the measurements at each step  $i$ , and the previous movement signals:  $p(\mathbf{x}_i|L, M) = \eta p(\mathbf{x}_i|\mathbf{u}_{1:t})p(L|\mathbf{x}_i)$ . Since conditioning on the position renders landmark positions independent (Montemerlo et al., 2002), the distributions representing landmarks can simply be multi-

plied:

$$p(\mathbf{x}_i|O, L, M) = \gamma p(\mathbf{x}_i|M) \prod_{j=1}^N p(\mathbf{l}_{i,j}|\mathbf{o}_j, \mathbf{x}_i). \quad (1)$$

In the above,  $p(\mathbf{x}_i|M)$  represents the current location estimate from the path integration system (which adds up all movement signals  $\mathbf{m} \in M$ ),  $p(\mathbf{l}_j|\mathbf{o}_j, \mathbf{x}_i)$  represents estimated landmark positions, and  $\gamma$  is a constant normalization factors. After correcting the location estimate, the estimated landmark positions are also corrected:

$$p(\mathbf{l}_{i,j}|\mathbf{o}_j, \mathbf{x}_i) = \eta p(\mathbf{o}_j|\mathbf{l}_{i,j}, \mathbf{x}_i)p(\mathbf{l}_{i-1,j}) \quad (2)$$

In our case,  $p(\mathbf{o}_j|\mathbf{l}_{i,j}, \mathbf{x}_i)$  is a Gaussian centered at the location of the observed landmark (measured from stereo disparity).  $p(\mathbf{l}_{i-1,j})$  is simply the previous estimate of the same landmark, and  $\eta$  a normalization constant. The repeated steps of Bayesian localization which implement equations (1) and (2), expressed in this simple form<sup>6</sup>, are implementable in brains and in spiking neural networks (Figure 4).

Path integration has been shown to be performed by grid cells in the entorhinal cortex (McNaughton et al., 2006). We recently presented evidence that hippocampal place cells are able to perform the correction step, based on neuronal recordings of several hundred place cells and multiple different environments, in which the firing fields of these cells corresponded to the predictions of a Bayesian integration model (Madl et al., 2014). In the same paper, we have also suggested how coincidence detection, observed in place cells (Jarsky et al., 2005; Takahashi and Magee, 2009; Katz et al., 2007), can implement the multiplication in Equation (1). One can interpret each input spike as a sample from a probability distribution, in which case coincidence detection (which only leads to output spikes if the input spikes arrive in close temporal proximity) performs multiplication (Koch and Segev, 2000) of these distributions (see Figure 4). Finally, we have argued that phase resetting observed in grid cells can implement the update step, completing the localiza-

<sup>6</sup>Our formulation contains heavy simplifications compared to robotics solutions, which are far more accurate - for example, only taking into account local landmarks for the correction step, and omitting angles from the state representation. We sacrifice accuracy for plausibility, noting that humans are not very accurate at localization either (see Results).

tion cycle. Based on the observation that it partially accounts for single-cell recording data in multiple environments (Madl et al., 2014), and that it can be implemented as a biological neural network in a straightforward fashion, we think this kind of Bayesian correction constitutes a plausible model of local spatial error correction.

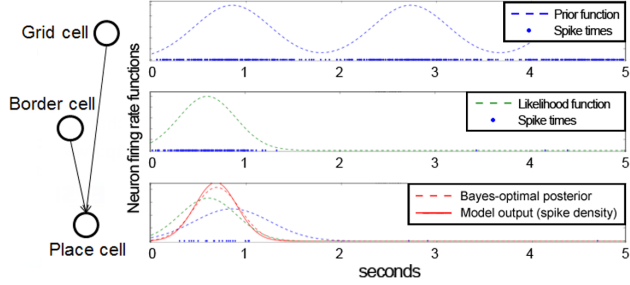


Figure 4: **Approximate Bayesian cue integration in spiking neurons.** Calculating the posterior probability distribution of the current location (equation (1)) requires multiplying a prior location distribution from path integration (represented by grid cells) with likelihood distributions from measurements of objects or boundaries (here represented by a border cell). If the place cell receiving input from the grid and border cells performs coincidence detection, it can multiply its inputs, yielding an approximate Bayesian posterior, and representing the associated uncertainty via the size of its firing field. A Bayesian model can account for hippocampal place field sizes in behaving rats. (Figure adapted from (Madl et al., 2014)).

The Route plan extraction SBC creates PAM node structures representing the shortest path to the agents current goal, if such a goal is currently present in the Workspace; leveraging the interconnected place node network constituting cognitive maps. The kind of recurrently interconnected network constituted by place nodes facilitates a very simple path planning mechanism (Figure 5). Assuming that every goal location  $G$  passes activation through the network, the distance to the goal can be decreased by moving to the adjacent neighbour node with the highest activation. If the nodes representing the locations of possible obstacles are connected with zero or near-zero weights, this mechanism can implement obstacle avoidance as well as path planning. Crucially, this activation-based planning mechanism operates on a hierarchy of ‘cognitive maps’, rather than on a single level. We argue that this allows better solutions of multi-goal navigation problems such as the travelling salesman problem. The evaluation of this planning mechanism against human data was briefly described in

(Madl et al., 2013) (for details see the Supplementary Information).

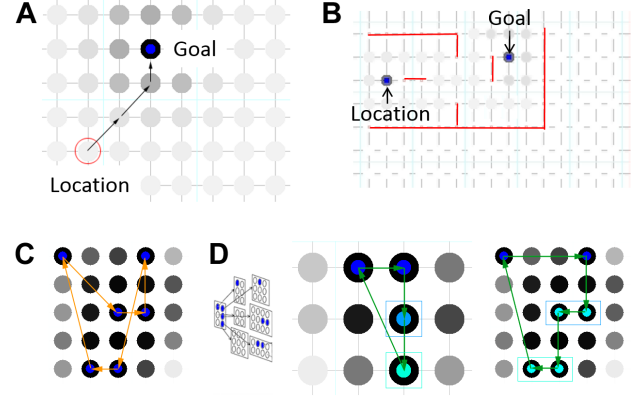


Figure 5: **Route planning on recurrently interconnected place nodes.** A: Single goal routes can be obtained by following an activation gradient to a goal. B: Obstacle avoidance can be implemented by setting connection weights to zero near boundaries (red lines). C: On a flat grid, following activation gradients can lead to sub-optimal paths for multi-goal navigation. D: However, when operating on a hierarchy - planning rough, low-resolution routes first, and then refining them on higher resolution maps -, this mechanism can yield near-optimal solutions.

The Map correction SBC serves the role of making large-scale corrections (as opposed to the local corrections made by the Localization SBC) when revisiting a known location. It is described in detail in the next subsection.

#### Loop closing - fixing previously learned maps

If uncorrected, accumulating path integration errors eventually render learned spatial representations useless; a problem necessitating the use of other modalities for map learning. Integrating spatial information in an approximately statistically optimal (Bayesian) fashion, as described above, helps correct local maps. However, only the agent’s current location and the locations of currently perceived objects are updated with our procedure. When traversing large cycles (loops) in an environment and returning to a previously visited location, the remaining errors still accumulate and prevent this loop to be represented correctly, causing multiple representations of the same places (of subsequently revisited places) - see Figure 6.

Therefore, a mechanism is needed to correct the representation of locations encountered during

loops (such a correction is called ‘loop closure’ or ‘closing the loop’ in robotics literature (Williams et al., 2009)). This section outlines a biologically plausible solution to this problem, and its relation to phenomena observed in hippocampal neurons. This solution is also used by the Map correction SBC to correct errors in learned cognitive maps.

Although the problem of accumulating errors and the resulting need to correct maps with sensory information has been identified early in spatial modelling literature (McNaughton et al., 1996), the question how brains might ‘close the loop’ has received very little attention, and no plausible mechanisms have been proposed to the authors’ knowledge. The large majority of robotics solutions to this problem require many iterations over huge matrices containing information regarding every position ever visited (Thrun and Leonard, 2008; Durrant-Whyte and Bailey, 2006; Bailey and Durrant-Whyte, 2006; Williams et al., 2009), and are thus neurally implausible. However, a probabilistic perspective on this problem can still help find a plausible candidate algorithm, consistent with hippocampal replay as the correction mechanism, which we summarize below.

First, let us assume that it is sufficient to correct the route taken during the loop. Local, currently perceived landmark positions are corrected separately as described above. When performing large-scale loop closing, our scheme applies the same correction to a position and the local landmarks around it<sup>7</sup>. We also make the assumption that correction only concerns position representations and not angular representations, since there is neuronal evidence for the former but not the latter (replay of encountered information happens in place cells, but has not been observed for direction-sensitive neurons such as head-direction cells in the post-subiculum (Brandon et al., 2012)).

The available information includes the path  $X$  consisting of estimated, recently visited locations  $\mathbf{x}_0, \dots, \mathbf{x}_m \in X$ , and a set of constraints  $\mathbf{c}_1, \dots, \mathbf{c}_m \in C$  specifying how far two locations should be from each other - this includes distances from the path integration system for subsequent locations, and equivalence constraints (with zero distance) when

revisited places are recognized. We will temporarily assume simultaneous access to all path integration constraints, and will drop this implausible requirement later. Each constraint between two locations is represented as a Gaussian with the measured distance  $\mathbf{c}_i$  as the mean, and the associated uncertainty represented by the covariance  $S_i$  (e.g. path integration is inexact - high uncertainty; but a recognized revisited place is at the same location - low uncertainty). The correct path is the one that is most consistent with all known constraints (known distances between the locations); or, from a probabilistic perspective, the one that maximizes the conditional probability of the locations constituting the path, given the constraints<sup>8</sup>:

$$P(X|C) \propto \prod_{i=1}^m P(\mathbf{c}_i|X). \quad (3)$$

Since each constraint is represented as a Gaussian over the distance between a pair of locations  $a_i$  and  $b_i$ ,  $P(\mathbf{c}_i|X) \propto \mathcal{N}(\mathbf{x}_a - \mathbf{x}_b; \mathbf{c}_i, S_i)$ , and the conditional probability is

$$P(X|C) \propto \prod_{i=1}^m \exp\left(-\frac{1}{2}\|\mathbf{x}_a - \mathbf{x}_b - \mathbf{c}_i\|_{S_i}^2\right). \quad (4)$$

We will denote the discrepancy between the constraint  $i$  and the difference between corrected locations  $a_i$  and  $b_i$  as  $\mathbf{d}_i = \mathbf{x}_a - \mathbf{x}_b - \mathbf{c}_i$ . Under ideal conditions without noise and errors, all  $\mathbf{d}_i$  would be zero; but in realistic environment there will be discrepancies between estimated and measured differences. The ‘best’ path estimate maximizes  $P(X|C)$ , or equivalently minimizes its negative logarithm  $-\log P(X|C)$  (minimizes the discrepancies):

$$X_{ML} = \arg \max_X P(X|C) = \arg \min_X \sum_{i=1}^m \|\mathbf{d}_i\|_{S_i^{-1}}^2 \quad (5)$$

The constraints can be represented as the edges of a graph which has the locations along the path

<sup>7</sup>Unlike the strong evidence for hippocampal replay concerning place cells representing recently visited locations, it is unclear whether cells associated with landmarks are also ‘replayed’. Therefore, we forgo separate landmark correction in loops for now.

<sup>8</sup>In robotic SLAM solutions, the path likelihood would also depend on all landmark observations. We omit them here because our loop closing procedure updates each position along with the path together with its local landmarks, applying the same translation to both, which renders the observation conditionals constant; once again sacrificing accuracy for plausibility.

as vertices. Let us denote the incidence matrix  $H$  of this graph, such that  $H_{i,j}$  is 1 if there is a link between  $i$  and  $j$ ,  $-1$  for links between  $j$  and  $i$ , and 0 if there is no link. We can express the distances between the pairs of locations for which there is a constraint, given any hypothetical locations  $X$ , as  $C' = HX$ . The discrepancy between actual and hypothetical distances becomes  $C - C'$ , and the associated uncertainty a matrix  $S$  containing the  $S_i$  as sub-matrices, which yields the ML equation in matrix form - expressing that the best hypothetical locations are the ones minimizing the discrepancy.

$$X_{ML} = \arg \min_X (C - HX)^T S^{-1} (C - HX) \quad (6)$$

This formulation is called linear least squares SLAM (Frese, 2006) in robotics literature (where the solution is made more complicated - but more accurate - by also representing and correcting angles along the path, making the equations non-linear). The minimum in equation (6) is given by  $X = (H^T S^{-1} H)^{-1} H^T S^{-1} C$ , and can be re-written to a form  $Ax = b$  and approximated using the Gauss-Seidel method - which has been shown to be implementable as a neural network (Delgado and Fausett, 1995). Unfortunately, this requires accessing every visited location in  $X$  and all uncertainties  $S_i$ , which cannot be implemented in a biological neural network within the sub-second durations of hippocampal replay (Carr et al., 2011). Obtaining uncertainty estimates from the encoding suggested in Figure 4 would take seconds for every place cell.

Fortunately, there is a more plausible solution which can be implemented neurally. It has been argued that Spike-Time Dependent Plasticity (STDP) can implement gradient descent in biological neurons (Bengio et al., 2015). Our starting point is the stochastic gradient descent-based maximization of  $P(X|C)$  described in (Olson et al., 2006), which suggests the following gradient with respect to constraint  $i$ :

$$\Delta X \approx \alpha (JS^{-1}J)^{-1} J_i^T S_i^{-1} d_i, \quad (7)$$

where  $\alpha$  is a learning rate,  $J$  is the full Jacobian of all constraints with respect to the locations, and  $J_i$  the Jacobian of constraint  $i$ . Because constraints apply to locations incrementally (with zero sensory errors, the correct current location would be  $x_c = \sum_i c_i$ ), the Jacobian is also incremental, spreading out the discrepancy  $d_i = (x_a - x_b - c_i)$

over an entire loop (by means of having a structure similar to the incidence matrix). This means the Jacobian need not be explicitly computed or represented. For a given loop closed by  $c_i$  with uncertainty  $S_i$ , let us assume unchanging path integration uncertainties  $S_P$  for each movement within the loop, and introduce a loop precision parameter  $A_i$  specifying the uncertainty of the current loop closure in relation to that of path integration,  $A_i = S_i/S_P$ . The correction applied to any single location  $x_j$  visited after the recognized previous location  $a_i$  (i.e. if  $j > a_i$ ) thus becomes:

$$\Delta x_j \approx \alpha d_i \frac{\sum_{k=a+1}^j S_i^{-1}}{\sum_{k=a+1}^{\min(j,b)} S_P^{-1}} = \alpha A_i d_i p_j, \quad (8)$$

where  $p_j = (\min(j, b_i) - a_i - 1) / (b_i - a_i - 1)$  denotes how far  $x_j$  lies along the loop, with  $0 \leq p_j \leq 1$ .

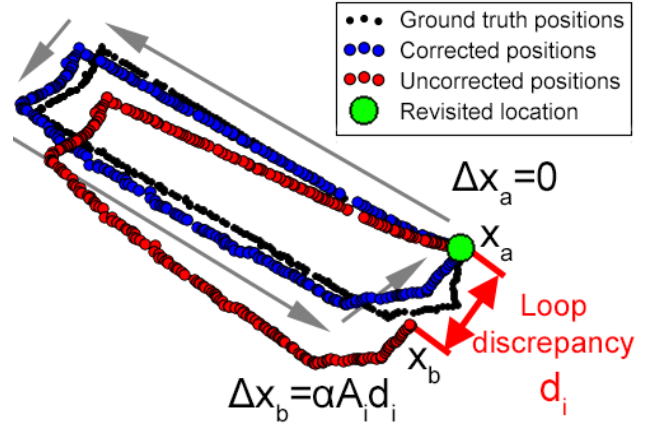


Figure 6: **Loop closing performed by the Map correction SBC.** Correcting estimated positions along a path when re-visiting a known place (large green dot), after traversing a large loop. Recognizing this place yields the knowledge that current estimated location  $x_b$  should equal  $x_a$ ; and the correction  $d_i$  based on the discrepancy is applied proportionally to all visited places along the loop. This backward correction is consistent with hippocampal replay.

Conveniently, we can neglect path integration constraints - they are already included in the path  $X$ , and, since they concern subsequent locations with  $b = a + 1$ , they lead to  $\Delta x = 0$  according to equation (8). The updates only concern loop closing constraints. Given that the distance to the same place when re-visiting it is zero,  $d_i = x_a - x_b$ . Furthermore, we don't have to re-activate all locations ever visited; only those in the loop. The ensuing

correction mechanism is simple (and easily implementable with neurons): when a loop closure is detected, the locations along the loop are iteratively corrected with the discrepancy between estimated and observed location according to equation (8). All locations subsequent to a re-visit are corrected by as much as the last point in the loop. The iteration proceeds backwards, starting at the estimated location at the re-visited place, and has to run several times to approximate a near-optimal solution. This is consistent with backward replay of visited locations in hippocampal place cells (Carr et al., 2011), with the presence of distances between locations encoded in such replays (Diba and Buzsáki, 2007), and with the observation that replay happens significantly more often than the number of times the animal re-visits places.

The described procedure carried out regularly by the Map correction SBC after a loop closure has been detected. It simply spreads out the discrepancy  $\mathbf{d}_i$  proportionally along the place nodes representing the traversed loop, according to Equation (8) (see Figure 6). The Map correction SBC also corrects the positions of encountered buildings, and of the traversed road, stored on the cognitive map (i.e. the same correction is applied to building nodes and road nodes as to the  $\mathbf{x}_j$  closest to them).

Apart from behavioural predictions regarding cognitive map accuracy, validated in the next subsection, and the prediction that hippocampal replay (Carr et al., 2011) might (also) serve the purpose of correcting cognitive maps, this suggested mechanism also yields a quantitative prediction on a cellular level, assuming that the synaptic strength place cells depends on the distance  $d_{pf}$  between their place fields. For example, (Csizmadia and Muller, 2008) suggest that the synaptic weight converges to  $S = \exp(-kd_{pf})$ . which for small  $kd_{PF}$  can be approximated by  $S = 1 - kd_{pf}$ . Furthermore, STDP implies a weight change proportional to the change in post-synaptic voltage potential (Bengio et al., 2015). Under these assumptions, our suggested cognitive map correction mechanism implies that after re-visiting a location, during subsequent hippocampal replay, for a pair of place cells which are sufficiently close together for the approximation to hold, changes in post-synaptic voltage potential will be approximately proportional to the correction magnitude  $\Delta\mathbf{x}$ , i.e. to the amount the place field has shifted during replay. It is clear from empirical data that place fields shift after re-visiting locations in an environment (Mehta et al., 2000), and

that backward replay contains distance information between place fields (Diba and Buzsáki, 2007). We leave the verification of the mentioned prediction for future work.

## Results

This section reports results obtained by LIDA agents with the extensions described above, reproducing data from psychological experiments. These experiments were chosen to compare the agent’s spatial estimation accuracies, and cognitive map structures, with human subjects.

Instead of free exploration, the routes in the experiments below were pre-programmed into the agents’ long term memory, by storing the turns to be taken in the form of schemes (percept-action mappings) in Procedural Memory, for the following reasons. In Experiment 1, closely reproducing the participant trajectories (as opposed to exploration behaviour) was crucial to modelling accumulating uncertainty. In Experiments 2 and 3, subjects’ exploration trajectories in their home towns were not known (having happened years or decades before the experiment). Furthermore, exploring environments on the scale of the participant cities modelled in Experiment 2 in tractable timeframes would have required an intelligent exploration strategy, which we have not implemented yet in LIDA. Therefore, the agent was given the turns it should take.

All other information came from noisy sensors, and no ground truth information was provided to the agents, which makes the experiments suitable for evaluating spatial representation accuracy.

### *Experiment 1 - Localization and cue integration*

In order to substantiate the Bayesian localization and cue integration mechanism, we have replicated a behavioural experiment Nardini et al. (2008) investigating the integration of self-motion and sensory information in location estimation. In this experiment, subjects were asked to pick up a series of glowing objects in a dark room and to subsequently return the first object to its original location. In the self-motion+landmarks condition, there were three landmarks available for orientation, and subjects were not disoriented - both sources of information were available. In the landmarks condition, subjects were disoriented by turning to deprive them of orientation information. In the self-motion condition, subjects were not disoriented but the landmarks were turned off.

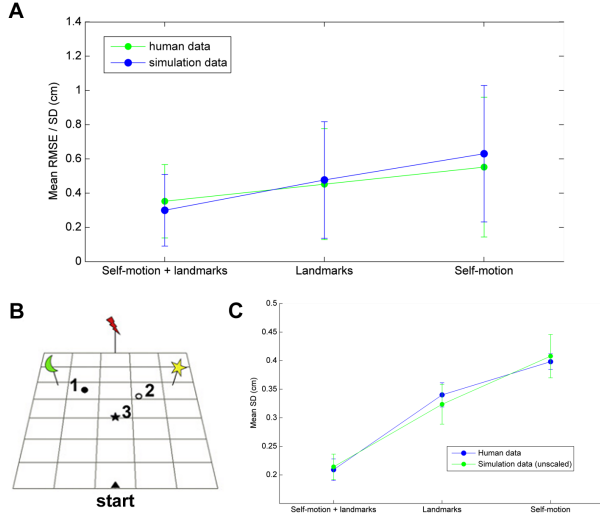


Figure 7: **Position errors and standard deviations in the cue integration experiment by Nardini et al. (2008).** A. Mean RMSE (root mean squared errors) of participants, and mean SD (standard deviation), for the responses of human subjects (green) and the agent (blue), respectively. B. The experiment environment. Participants had to pick up objects 1-3 in order, and then replace object 1. The colored objects (moon, star, lightning) are the landmarks. (From Nardini et al. (2008)). C. Mean SD of participants (green) and the agents (blue)

To simulate this experiment, the same environmental layout (with accurate object distances) was reproduced in a simulation. The agent performed Bayesian localization as described above. Distance estimation inaccuracies were set to 3%, which is a frequently observed distance estimation error in virtual (Waller, 1999; Murgia et al., 2009) and real environments (Plumert et al., 2005; Grechkin et al., 2010). The two remaining noise parameters (linear and angular self-motion estimation inaccuracies) were adjusted to fit the data using coordinate descent. Path integration errors were modelled by multiplicative 1-mean Gaussian noise, since variability in human odometry is proportional to magnitude (Durgin et al., 2009). Figure 7 shows the simulation results, which are consistent with the empirical data for adult subjects.

#### Experiment 2 - Cognitive map accuracy (real environments)

Here we replicate map accuracies of Experiment 3B in (Madl et al., submitted), in which participants were asked to pick 8 very familiar buildings (such that they knew how to walk from any one

to the other), and to create a sketch map by indicating their positions on a featureless canvas on a computer. Sketch maps were linearly translated, rotated and scaled to fit the correct map best using Procrustes analysis (Gower, 1975). Each subject produced three sketch maps, of which those not significantly better than random guessing were excluded. Sketch maps spanning an area larger than  $4km^2$  were also excluded to reduce computational load. This left 19 participants, and a total of 28 different maps (environments) in 21 different cities. To reduce computational load, only the roads (and adjacent buildings) were modelled which allowed getting from one of these buildings to the other, i.e. which lay along one of the  $\binom{8}{2} = 28$  shortest routes between two respective buildings for each map. These roads and buildings were recreated with the correct real-world distances in the simulation (geospatial information was obtained via Google Maps API<sup>9</sup>), yielding multiple routes several kilometers long.

Figure 8 compares the errors of the maps learned by the agent with human sketch maps, after adjustment of the linear and angular path integration noise parameters by coordinate descent. Map errors are measured as the sum of squared errors (SSE) between the correct geographical building locations, and the locations estimated by the participants / by the model. Unlike the model predictions, which are already in the correct reference frame, human data is linearly translated, rotated and scaled first to fit the correct map. Errors averaged over all maps are  $1.07km^2$  ( $\sigma = 0.85$ ) for humans, and  $1.08km^2$  ( $\sigma = 1.39$ ) for the model, and the model errors correlate with human errors with  $r_{m,h} = 0.80$  ( $p = 2.42 \cdot 10^{-7}$ ), with a coefficient of determination (proportion of explained variance) of  $R^2 = 0.60$  which suggests that the model explains the majority of the variance in human map error data.

Note that this model only uses the eight buildings the participant indicated as being very familiar to recognize having revisited a place and to correct maps. Along routes of this size, humans can presumably re-identify more than these eight places. Even in areas without salient landmarks, a matching visual sequence while walking can trigger a feeling of familiarity. We will implement this kind of episodic sequence-based place recognition in future work.

<sup>9</sup><https://developers.google.com/maps/>

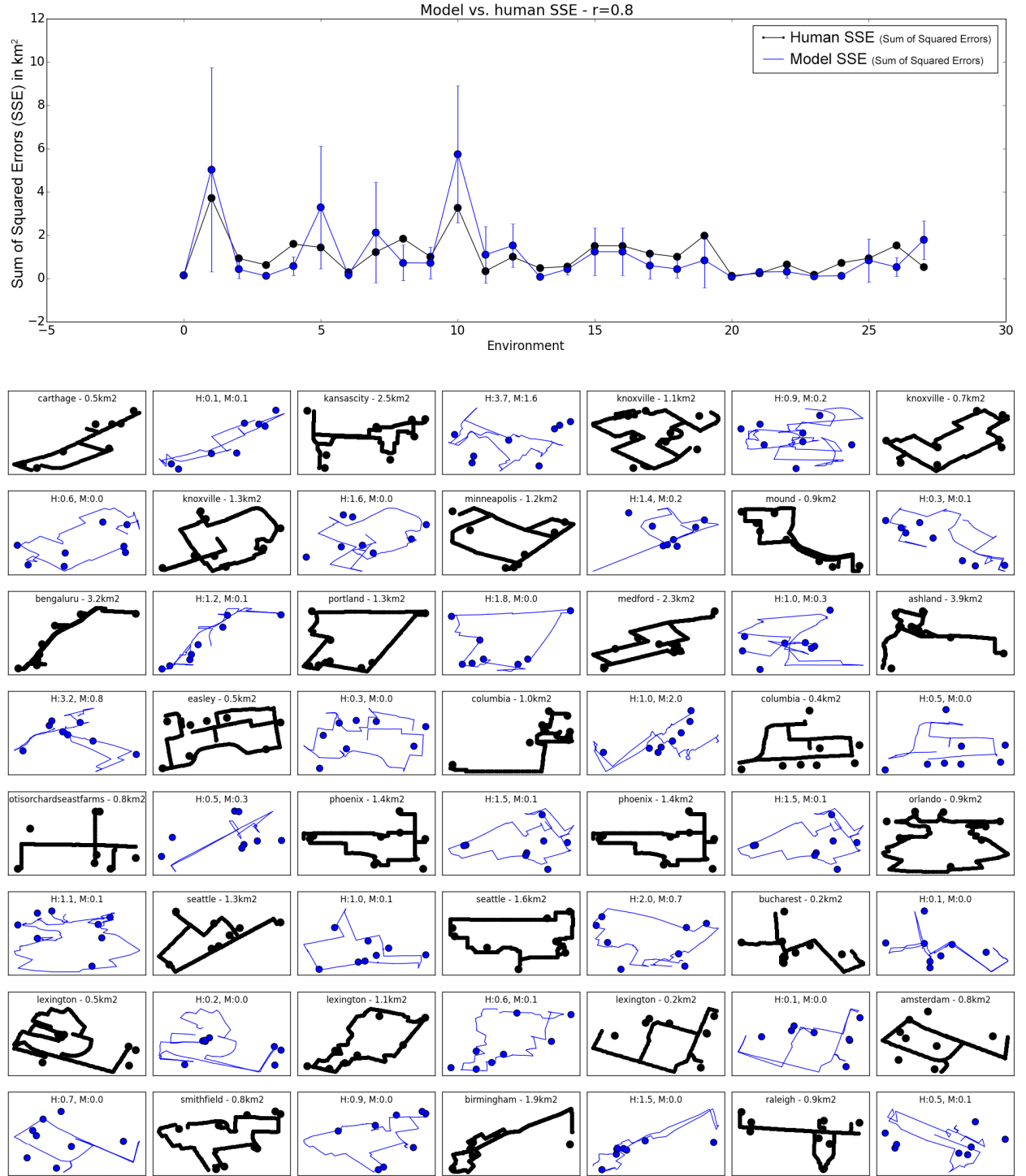


Figure 8: Comparison with human and model errors over all environments (top), and plots containing the ground truth (black) and learned (blue) street and salient building locations. Titles indicate the city name and region area for the ground truth, and (H)uman and (M)odel errors for the model subplots.



## Conclusion

In order to tackle challenges posed by noisy sensors and complex, uncertain environments, we have extended LIDA by CNN-based perception, and by mechanisms for learning and correcting cognitive maps facilitating navigation. These include novel reinterpretations of coincidence detection in place cells as approximate Bayesian cue integration, and hippocampal replay as cognitive map correction; and suggested computational and algorithmic models of these phenomena, consistent with the ‘Bayesian brain’ paradigm (Knill and Pouget, 2004). We have also compared spatial representation accuracies to human subjects. Although a large number of issues remain to be solved for real-world-capable autonomous agents (including developmental learning of perceptual representations and affordances, visual place recognition in the absence of salient landmarks, long-term spatial and episodic memories, transferring learned spatial knowledge and expectations between environments, and spatial reasoning, to name just a few), we believe these extensions provide a first step towards a cognitive architecture combining biological plausibility and real-world functionality.

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