

3.-1 Setting x and y to 0 gives that

$$\vec{B}(\vec{r}) = \frac{\mu_0 IR}{4\pi} \int_0^{2\pi} \frac{z \cos \phi \hat{x} + z \sin \phi \hat{y} + R \hat{z}}{(R^2 \cos^2 \phi + R^2 \sin^2 \phi + z^2)^{3/2}} d\phi$$

However, because $\int_0^{2\pi} \cos \theta d\theta = 0$ (and similarly for sin),

$$\vec{B}(\vec{r}) = \frac{\mu_0 IR}{4\pi} \int_0^{2\pi} \frac{R \hat{z}}{(R^2 + z^2)^{3/2}} d\phi = \frac{\mu_0 IR}{4\pi} \frac{2\pi R}{(R^2 + z^2)^{3/2}} = \frac{\mu_0 IR^2}{2(R^2 + z^2)^{3/2}}$$

3.0 1.23 states

$$I \approx \sum_{j=0}^{n-1} \frac{1}{2} (F_j + F_{j+1}) \Delta x \equiv I_t$$

and 1.19 states that

$$I \approx \sum_{j=0}^{n-1} F_j \Delta x \equiv I_b$$

We can see that the first term of the trapezoidal approximation is

$$I_{t,1} = \frac{1}{2} (F_1 + F_2) \Delta x$$

and the second is

$$I_{t,2} = \frac{1}{2} (F_2 + F_3) \Delta x$$

with their sum being

$$I_{t,1+2} = \frac{1}{2} F_1 + F_2 + \frac{1}{2} F_3$$

It follows that

$$I_t = I_b - \frac{1}{2} F_1 + \frac{1}{2} F_n$$