Notes de cours CADL - session-2

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- The basic components of a neural network
- How to use gradient descent to optimize parameters of a neural network
- How to create a neural network for performing regression

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1 Introduction

1.1 Generalities

- Use data and gradient descent to teach the network what the values of the parameters of the network should be.
- Idea of machine learning: letting the machine learn from the data.
- We are interested in letting the computer figure out what representations it needs in order to better describe the data and some objective we've defined.

1.2 Gradient Descent

- Operations of the network are meant to transform the input data into something meaningful that we want the network to learn about.
- Parameters of the NW are random so output is random as well.
- If we need specific output, we can use "Gradient Descent": way to optimize set of parameters.

1.3 Defining Cost

- Mesure of the "error"
- Exemple : recognize apple or orange. Random network spit ou random 0s or 1s for apples and oranges. We can define :
 - if the network predicts a 0 for an orange, then the error is 0. If the network predicts a 1 for an orange, then the error is 1.
 - And vice-versa for apples. If it spits out a 1 for an apple, then the error is 0.
 If it spits out a 0 for an apple, then the error is 1.
- Defining error in terms of our parameters :

$$error = network(image) - true_label$$
 (1)

$$network(image) = predicted_label$$
 (2)

$$E = f(X) - y \tag{3}$$

1.4 Minimizing Error

- Feed the network many images (100 for e.g) to see what the network is doing on average.
- Changing network's parameters can have effect on the error.
- The error provides a "training signal" or a measure of the "loss" or our network.
- Assumptions in assuming our funtion is continuous and differentiable.
- Gradiant descent in a nutshell: "Error", "Cost", "Loss", or "Training Signal"

1.5 Backpropagation

- The gradient is just saying, how does the error changes at the current set of parameters.
- To figure out what is the gradian we use backpropagation. Whatever differences that output has with the output we wanted it to have, gets *backpropagated* to every single param in our network.
- Backprop is an effective way to find the gradient. Uses the *chain rule* to find the gradian of the error.
- y = mx + b linear function. The slope or gradian is m.
- The process described:

$$\theta = \theta - \eta * \nabla_{\theta} * J(\theta) \tag{4}$$

- $-\theta$: parameters
- $-\nabla$: gradient, with repect to parameters θ , ∇_{θ}
- J: error
- η : learning rate describes how far along this gradient we should travel, typically value between 0.01 to 0.00001

1.6 Local Minima/Optima and learning Rate

- Dilemma: find a local or global minima.
- The NW may have million of parameters, so the problem becomes more and more difficult.
- Wize choice of the learning rate:
 - To small we dont get any better cost where we started
 - To big the cost goes up and down

2 Creating a Neural Network

2.1 Exemple with sine wave

- Input X output y
- Here the input is values in an interval instead of images like before.
- The exemple is to create sine wave with uniform noise and create a neural network that is able to discover the sine wave.

```
# Create data : sine wave with random noise in the interval
n_obs = 1000
xs = np.linscape(-n, n, n_obs)
ys = np.sin(xs) + np.random.uniform(-0.5,0.5,n_obs)
plt.scatter(xs, ys)
```

• Train the NW to give any value on the x axis and have the value it should be on the y axis. (fundamental idea of regression: predicting some continuous output value given some continuous input value)

2.2 Defining cost

• Use of placeholder to define input and output values. Those variables will filled at the computation of the graph.

```
X = tf.placeholder(tf.float32, name='X')
Y = tf.placeholder(tf.float32, name='Y')
```

• Create session and define the parameters center and close to 0 with $tf.random_normal(nb_values, stddev=).eval()$

```
sess = tf.InteractiveSession()
n = tf.random_normal([1000], stddev=0.1).eval()
```

- Create **variables** using *tf. Variable*, it does need an initial value or we can call an initializer.
- Define two tf. Variable for weight and bias

- Use gradient descent to learn what the best value of W and b.
- Before that we have to know how to measure what the *best* mean for what we try to do.
- Let's define the absolute distance(val1, val2) from the predicted value to the assumed sine wave value.

```
cost = distance(Y_pred, tf.sin(X))
```

• We calculate the mean of the cost we have for every observation

```
cost = tf.reduce_mean(distance(Y_pred, tf.sin(X))
```

2.3 Training Parameters

• Use tensorflow optimizer

```
optimizer =
   tf.train.GradientDescentOptimizer(learning_rate=0.01).minimize(cost)
```

• Run the optimizer

```
with tf.Session() as sess:
    #initilization of all the tf.Variable
    sess.run(tf.global_varables_initializer())
    prev_training_cost = 0.0
    for it_i in range(n_iterations):
        sess.run(optimizer, feed_dict={X:xs, Y:ys})
        training_cost = sess.run(cost, feed_dict={X:xs}) #...,session=sess)

# each 10 iterations
    if it_i % 10 == 0:
        ys_pred = Y_pred.eval(feed_dict={X:xs})
        # print stuff like training_cost and plots

if np.abs(prev_training_cost - training_cost < 0.000001):
        break # if local minima found

prev_trianing_cost = training_cost</pre>
```

- The output doesn't look like a sine wave at all. Actually it's only a line.
- Training vs Testing: Have to learn more about the different between training and testing networks.

2.4 Stochastic and Mini Batch Gradient Descent

• Tricks to find the best local minima: using mini-batches of size batch_size.

```
idxs = np.arrange(100) # it will be changed to make it random
batch_size = 10
n_batches = idxs // batch_size
```

• Look some random subset of the datase because neural networks love order and would use it to its advantage. But order is irrelevant to our problem.

```
idxs = np.random.permutation(idxs)
```

• Generalise the entire dataset. We modify the code which runs the optomizer to include the mini-batches program.

```
idxs = np.random.permutation(range(len(xs)))
n_batches = len(idxs) // batch_size
for batch_i in range(n_batches):
   idxs_i = idxs[batch_i * batch_size: (batch_i+1) * batch_size]
   sess.run(optimizer, feed_dict={X:xs[idxs_i], Y:ys[idxs_i]})
training_cost = sess.run(cost, feed_dict={X:xs, Y:ys})
```

We get a better result: the line has a curve but it doesn't look like a sine wave.

- This method is:
 - Mini-batches: small pieces of data where we perform gradient descent
 - Stochastic: the order of the data is dandomized
- Use a function of training

```
def train(X, Y, Y_pred, n_iterations=100, batch_size=200,
    learning_rate=0.02):
```

- To get better result we can have a bigger set of parameters.
- We are going to multiply our input by 100 values, creating an "inner layer" of 100 neurons.
 - Define tf. Variables: Weights (multiplication) and biais (addition)

```
n_neurons = 100
W = tf.Variable(tf.random_normal([1,n_neurons], stddev=0.1))
b = tf.Variable(tf.constant(0), dtype=tf.float32, shape=[n_neurons])
```

- Operation with matrix and add every neuron's output

```
h = tf.matmul(tf.expand_dims(X, 1), W) + b)
Y_pred = tf.reduce_sum(h, 1)
```

- Retrain with new Y₋pred

```
train(X, Y, Y_pred)
```

- It takes longer to compute and the result is not better. Our function is still linear but the cost is going up and down: good sign = we can reduce the learning rate
- Input's Representation: important to consider the kind of input we are working on. We don't treat the types of data in the same way like:
 - sound using discrete fourier transform
 - text using word histograms

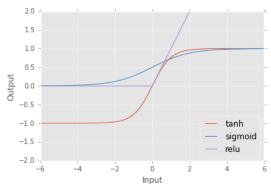
2.5 Over vs. Underfitting

• To approximate curve function we use polynomial function. We will try to learn the influence of each degree of this function

```
Y_pred = tf.Variable(tf.random_normal([1]), name='bias')
for pow_i in range(1,4):
    W = tf.Variable(
        tf.random_normal([1], stddev=0.1), name='weight_%d' % pow_i)
    Y_pred = tf.add(tf.multiply(tf.pow(X, pow_i), W), Y_pred)
```

2.6 Introducing Nonlinearities / Activation Function

- Use of non-linear functions also called activation functions. In every complex DL algorithm there are series of linear, followed by nonlinear operations.
- There are 3 functions used the most : tanh(), sigmoid(), relu()



• We modify the matrix multiplication by adding the non-linearity

```
h = tf.nn.tanh(tf.multiply(tf.expland_dims(X,1), W) + b, name='h')
```

• Fully-connected network: every neuron is multiplied by every single input value. We multiply our input by a matrix, add a bias, and then apply a non-linearity.

2.7 Going Deeper

• Give useful name within *scopes*. Otherwise the names of the operations are not helpful.

```
W = tf.get_variable( name='W', shape=[n_input, n_output],
    initializer=tf.random_normal_initializer(mean=0.0, stddev=0.1))
```

- This new initializer will create new random value when $sess.run(tf.global_variables_initializer())$ is called
- Possible to visualize the network using **Tensorboard**.

3 Image Inpainting

3.1 Description

• This NW will try to demonstrate how the NW we've created bedfore can realize more complicated tasks on the following image:



- We will teach the NW to go from the location on an image frame to a particular color.
- Given any position in an image, the NW will need to learn what color to paint.
- Start
 - Declare input and output

```
# positions in the image
xs = []
# coresponding colors
ys = []
```

- Storage

```
# for loop on the image
xs.append([row_i, col_i])
ys.append(img[row_i,col_i])
xs = np.array(xs)
ys = np.array(ys)
```

- Normalization

```
xs = (xs - np.mean(xs)) / np.std(xs)
```

- Goint to use regression to predict the value of a pixel biven its (row, col) position.
- Place input and output in placeholder in which we specify the partially their shape

```
X = tf.placeholder(tf.float32, shape=[None,2], name='X')
Y = tf.placeholder(tf.float32, shape=[None,3], name='Y')
```

3.2 Building the Network

- We are going to create a multi-layers NW.
- We take the *linear()* function created previously.

```
h = activation(h)
return h
```

• We use for loop to create the NW

```
n_neurons = [2, 64, 64, 64, 64, 64, 64, 64, 3]
current_input =X
for layer_i in range(1, len(n_neurons)):
    current_input = linear(
        X = current_input, # returned value of the function
        n_input = n_neurons[layer_i - 1],
        n_output = n_neurons[layer_i],
        activation = tf.nn.relu if (layer_i+1) < len(n_neurons) else None,
        scope = 'layer_'+str(layer_i))
Y_pred = current_input</pre>
```

3.3 Training

• Define the cost

```
cost = tf.reduce_mean(tf.reduce_sum(distance(Y_pred, Y), 1))
```

• Use another opitmizer AdamOptimizer (in general better than GradientDescentOptimizer).

```
optimizer = tf.train.AdamOpitmizer(0.001).minimize(cost)
```

- Ready to launch the process
 - Start the session

```
with tf.Session() as sess:
```

- Initialize variables (W and b) in the graph so we can use them

```
sess.run(tf.global_variables_initializer())
prev_training_cost = 0.0
```

- Loop for over number of iterations:

```
for it_i in range(n_iterations):
```

* Permutation of the input (randomness used for the optimizer)

```
idxs = np.random.permutation(range(len(xs)))
```

* Computation of the number of mini-batches

```
n_batches = len(idxs) // batch_size
```

* Loop for over the number of mini-batches

```
for batch_i in range(n_batches):
```

· Take the subinterval of input of the current mini-batch

```
idxs_i = idxs[batch_i*batch_size: (batch_i+1)*batch_size]
```

· Run the optimizer by feeding input X and output Y to calculate the parameters W and b

```
sess.run(optimizer, feed_dict={X:xs, Y:ys})
```

* Compute the cost to visualize the progression

```
training_cost = sess.run(cost, feed_dict={X:xs, Y:ys})
print(it_i, training_cost)
```

- Visualize the result by plotting

```
ys_pred = Y_pred.eval(feed_dict={X:xs}, session=sess)
img = np.clip(ys_pred.reshape(img.shape), 0, 255).astype(np.uint8)
```

• The entire code

```
n_{iterations} = 500
batch_size = 50
with tf.Session() as sess:
   # Here we tell tensorflow that we want to initialize all
   # the variables in the graph so we can use them
   # This will set W and b to their initial random normal value.
   sess.run(tf.global_variables_initializer())
   # We now run a loop over epochs
   prev_training_cost = 0.0
   for it_i in range(n_iterations):
       idxs = np.random.permutation(range(len(xs)))
       n_batches = len(idxs) // batch_size
       for batch_i in range(n_batches):
          idxs_i = idxs[batch_i * batch_size: (batch_i + 1) *
              batch_size]
          sess.run(optimizer, feed_dict={X: xs, Y: ys})
       training_cost = sess.run(cost, feed_dict={X: xs, Y: ys})
       print(it_i, training_cost)
       if (it_i + 1) % 20 == 0:
          ys_pred = Y_pred.eval(feed_dict={X: xs}, session=sess)
          fig, ax = plt.subplots(1, 1)
          img = np.clip(ys_pred.reshape(img.shape), 0,
              255).astype(np.uint8)
          plt.imshow(img)
```

4 Homework

4.1 Goals

- Learn how to create Neural Network
- Learn to use a NN to paint a image
- Apply creative thinking to the inputs, outputs and definition of a NW

4.2 Part One: Fully Connected Network

• Create the operations for connecting an input to a NW, defined by a *tf.placeholder*, to a series of fully connected, or linear, layers using the formula:

$$\mathbf{H} = \phi(\mathbf{XW} + \mathbf{b}) \tag{5}$$

- H: output layer representing the "hidden" activations of a network
- $-\phi$: linearity
- **X** : input to that layer
- **W**: layer's weight matirx
- **b** : layer's bias
- The part XW is the most compicated part of the equation scaling and rotating our input.
- By stacking a lot of "linear" + "nonlinear" operations in a series, we can create a **deep neural network**.
- Choising nonlinearities: trial and error. Depends on the normalization scheme: the expected output.
- Keep in mind the functions *relu*, *sigmoid* and *tanh* for their properties expecially for the final output layer of the NW

4.2.1 Code

- Create a placeholder for the input X

```
X = tf.placeholder(dtype=tf.float32, shape=[None, 2], name='X')
```

- Create the paramaters \mathbf{W} and \mathbf{b}

```
W = tf.get_variable(dtype=tf.float32, shape=[2,20],
   intializer=tf.random_normal_initializer, name='W')
b = tf.get_variable(dtype=tf.float32, shape=[20],
   intializer=tf.constant_initializer, name='b')
```

- Matrix multiplication XW and addition with b: XW + b

```
h = tf.matmul(X, W)
h = tf.nn.bias_add(h,b)
```

- Nonlinearity relu

```
h = tf.nn.relu(h, name='relu')
```

- New "linear" function using tf.get_scope. If there is already a variable created with the same name, TF will raise an exception. Consider 3 solutions:
 - * In an interactive console

```
tf.reset_default_graphe()
```

- * Typo error creating another layer with the same name
- * Should use context manager when creating graphs and running sessions

```
g = tf.Graph()
with tf.Session(graph=g) as sess:
   Y_pred, W = linerar(X, 2, 3, activation=tf.nn.relu)
```

4.3 Part Two: Image Painting Network

Load an image

```
img = plt.imshow(dirname)
```

- Collect location of pixel and the related (R,G,B) colors using for loops. Convert the lists of input and output to arrays np.array()
- Normalize the input xs

```
xs = (xs - np.mean(xs)) / np.std(xs)
```

• Create placeholder for the input and the true output

```
# first reset the graph
tf.reset_default_graph()
X = tf.placeholder(dtype=tf.float32, shape=[None,2], name='X')
Y = tf.placeholder(dtype=tf.float32, shape=[None,3], name='Y')
```

- Create 8 layers of neurons: {2, 20, 20, 20, 20, 20, 20, 3}
 - -2 is the input layer

$$H_1 = \phi(XW_1 + b_1) \tag{6}$$

- All the 20 are the hidden layers

$$H_i = \phi(H_{i-1}W_i + b_i) \tag{7}$$

- 3 is the output layer

$$Y_{pred} = \phi(H_6W_7 + b_7) \tag{8}$$

4.3.1 Cost function

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