## Ryden - Chapter 2 Solutions

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## 1 Exercise 1

We want to calculate the mean free path l of an arrow fired in a forest, where the trees have radius R and the average number of trees per unit area is  $\Sigma$ . Thinking about scaling, if the trees were more tightly packed, then l should decrease, so then l should be inversely proportional to  $\Sigma$ . Similarly, if the trees are larger the arrow will not travel as far, so l should be inversely proportional to R. Thus, the solution is  $l = (R\Sigma)^{-1}$ . Given that R = 1 m and  $\Sigma = 0.005$  m<sup>-2</sup>, this means l = 200 m. Note this answer isn't perfect, because the trees protrude forward toward the path of the arrow, but computing this correction is tricky because it involves an integral over the impact parameter b of the arrow with respect to the tree it hits. To a first approximation, the true answer is somewhere between 199 m and 200 m.

## 2 Exercise 2

This problem is identical to Exercise 1 but in three dimensions. The number density of stars is given by  $n_*$ , and the average stellar radius is  $R_*$ , meaning the cross-sectional area is  $\sigma = 4\pi R_*^2$ . The mean free path is again inversely proportional to  $n_*$  and  $\sigma$ , so  $l = (\sigma n_*)^{-1}$ . Given that  $n_* = 10^9 \text{ Mpc}^{-3}$  and  $R_* = 7 \times 10^8 \text{ m}$ , this means  $l = 2.1 \times 10^{17} \text{ Mpc}$ .

Similarly, if galaxies are spaced according to  $n_g = 1 \text{ Mpc}^{-3}$  and  $R_g = 2000 \text{ pc}$ , then the mean free path to hit a galaxy is  $l_g = 20000 \text{ Mpc}$ . We see that a photon is fairly likely to pass through a galaxy, but not necessarily hit a star in that galaxy.

## 3 Exercise 3

Let us pretend our bodies are entirely made of water and we absorb all CMB photons that pass through us. Let us further assume that we are a nice, round 100 kg, and also a nice, spherical 1 m radius sphere, so that our volume is  $V = 4\pi/3$  m<sup>3</sup>. We know from the text that the number density of CMB photons is  $n_{\gamma} = 4.11 \times 10^8$  m<sup>-3</sup>.

TM: Finish this