1 Calculating Daily Percent Q_d , or perc Q_d

In hydrology, the quantity "Q" describes the amount of flow of a liquid with respect to time. The quantity "percent Q", or "perc Q", is then a proportion of the flow of a stream through a set of rotary screw-traps, at a specific river-mile, over the course of one day. When both trap-flow and stream-flow are measured over the same amount of time, perc Q can be interpreted as the proportion of total stream volume that flows through a set of traps.

Calculation of perc Q requires estimates of stream velocity and flow, or discharge, via either of the USGS and CDEC, whose automated gauges provide daily on-the-fly discharge estimates. Note that units commonly associated with flow include $\rm m^3/s$, $\rm ft^3/s$, and acre-feet/s, and emphasize a metric of volume per time. Biologists directly measure velocity at a particular rotary screw trap. Perc Q also requires an estimate of the cross-sectional area of water flowing through a screw-trap, which can vary based on stream turbulence. It additionally requires the proportion of time a trap successfully fished over the course of a day, as well as the status of a cone as either "full" or "half."

To derive perc Q, first write out its proportional definition.

$$\mathrm{perc}~Q = 100\% \times \frac{\mathrm{total~trap~flow}}{\mathrm{total~stream~flow}}$$

For brevity, designate as Q_d the total stream flow on the dth day, and q_{id} the flow through the ith trap on the dth day. Assume that on any one day, n traps operate at one particular river-mile. Then daily perc Q_d is

perc
$$Q_d = 100\% \times \frac{\text{total daily trap flow}}{\text{total daily stream flow}}$$
$$= 100\% \times \frac{\sum_{i=1}^{n} q_{id}}{Q_d}.$$

Denominator total daily stream flow Q_d

Gauges managed by the USGS or CDEC provide measurements of denominator total stream flows Q.

At the Red-Bluff Diversion Dam (RBDD) on the Sacramento River, local USGS gauge 11377100 at Bend Bridge records daily discharge, say D_d , in the units of cubic meters per second. These measurements are then converted to acre-feet per day. Acre-feet are used because the size of cone-widths, a key part in the calculation of the perc Q_d numerator, are measured in feet.

So then, the expression for total stream flow Q_d , in units of acre-feet / day, becomes

$$Q_d = D_d \frac{86400 \text{ s}}{1} \frac{1 \text{ acre}}{43560 \text{ ft}^2} / \text{day}$$

= $D_d \text{ acre-feet} / \text{day}$.

For example, suppose that a query on gauge 11377100 communicates that the discharge D_d on May 7, 2000 was 13900 ft³/s. Then the total stream volume over the course of one day, or Q_d in acre-feet / day, is

$$Q_d = D \frac{86400 \text{ s}}{1} \frac{1 \text{ acre}}{43560 \text{ ft}^2} / \text{ day}$$
$$= \frac{13900 \text{ ft}^3}{\text{s}} \frac{86400 \text{ s}}{1} \frac{1 \text{ acre}}{43560 \text{ ft}^2} / \text{ day}$$
$$\approx 27570.24 \text{ acre-feet} / \text{ day}.$$

Numerator total daily trap flow $\sum q_{id}$

Estimation of numerator daily trap-specific q_{id} are more subtle, and take into consideration the cross-section of flow through the screw-trap cone, as well as the proportion of time during the day during which a trap was fishing. Finally, half-cone status is considered as well.

To obtain an estimate of the total daily volume q_{id} that passes through the ith screw-trap, the daily velocity of stream flow v_{id} is measured, in ft/s. Velocity v_{id} is then multiplied by the cross-sectional area a_{id} of the screw-trap, in ft². Days on which the stream flow is more turbulent result in higher cross-sectional areas. The opposite is true on days with more placid stream conditions. Due to this, the daily cross-sectional square-footage may change slightly day-to-day. Table 1 lists cross-sectional square footages a_{id} , as a function of the height h of water in the ith cone, in inches, as measured from the bottom. For example, very placid days may record a water height of 45 inches, leading to a cross-sectional area a_{id} of 22.7 ft², while turbulent days may whip water within the cone to a height of 51 inches, resulting in a cross-sectional area a_{id} of 26.6 ft².

Table 1: Cross-sectional square-footage a as a function of the height h of water within the cone, as measured from the bottom, rounded to the nearest inch. Water heights measured outside the range listed, or not measured at all, assume a height of 48 inches.

Water height	Cross-Sectional
h	Area a
(in)	ft^2
45	22.7
46	23.3
47	24.0
48	24.6
49	25.3
50	26.0
51	26.6
52	27.2
Other	24.6

In addition to daily measurements concerning cross-sectional areas, the amount of time t_{id} , in seconds, the *i*th trap fished during that day is recorded.

Together, these measurements provide an estimate of the unadjusted daily volume of water V_{id} that passes through the trap, which is then converted to acre-feet, similar to the daily denominator Q_d of total stream flow. So,

$$V_{id} = v_{id}a_{id}t_{id} \frac{1 \text{ acre}}{43560 \text{ ft}^2}.$$

However, on many days, the *i*th trap fails to fish an entire 24 hours, or 86400 s. In this case, the estimation of volume is expanded, so as to estimate the total daily volume for that day. For example, a trap that fished for only 12 hours would have its estimated volume multiplied by two, so as to estimate a daily volume V_{id} . To account for this, V_{id} is multiplied by 86000 s/ t_{id} . Thus, if a trap fishes an entire day of 86400 s, the original estimate of volume V_{id} is multiplied by one. Call this final expanded volume V'_{id} . Then it follows that

$$V'_{id} = v_{id}a_{id}t_{id} \frac{1 \text{ acre}}{43560 \text{ ft}^2} \frac{86400 \text{ s}}{t_{id}}$$
$$= v_{id}a_{id} \frac{1 \text{ acre}}{43560 \text{ ft}^2} \frac{86400 \text{ s}}{1}.$$

The cancellation of the amount of seconds spent fishing t_{id} when calculating V'_{id} makes sense here because $v_{id}a_{id}$ provides a 1 s estimate of flow. Multiplication of this resulting number by 86400 s thus provides a daily volume estimate.

Finally, days on which a cone was set at half-cone have volume estimates halved. This is easily incorporated into the final expression for q_i via a multiplier, c_{id} , say. So, c_{id} takes on values of one during days with full-cone operation, but values of 1/2 on half-cone days. Thus, the estimate of volume flowing through the ith trap over one day is

$$V'_{id} = v_{id}a_{id}c_{id} \frac{1 \text{ acre}}{43560 \text{ ft}^2} \frac{86400 \text{ s}}{1}.$$

Thus, the volume that flowed over the course of one day is the flow q_{id} ; i.e., $q_{id} = V'_{id} / \text{day}$.

For example, on May 7, 2000, the velocity v_{id} within table EnvDataRaw in the CAMP.mdb for the RBDD at subSiteID 42020 was 3.2 ft/s. Additionally, in table trapVisit, find that on this same day and subSiteID that the trap was in the full-cone configuration via variable halfConeID, as well as evidence that it was fishing for approximately 24 hours via variable visitTime. Finally, take note that the cone depth at the start of trapping via coneDepthAtStart was 48 inches, implying that the cross-sectional area a_{id} was 24.6 ft². Then the volume of water V_i' that flowed through the trap is

$$\begin{split} V'_{id} &= v_{id} a_{id} c_{id} \, \frac{1 \text{ acre}}{43560 \text{ ft}^2} \, \frac{86400 \text{ s}}{1} \\ &= \frac{3.2 \text{ft}}{\text{s}} \, \frac{24.6 \text{ft}^2}{1} \, 1 \, \frac{1 \text{ acre}}{43560 \text{ ft}^2} \, \frac{86400 \text{ s}}{1} \\ &= 156.14 \text{ acre-feet.} \end{split}$$

meaning that over the course of one day, the flow $q_i=156.14$ acre-feet / day. In the case that only this one trap 42020 were functioning on May 7, 2000, then the estimated percent Q_d for this day would then be

perc
$$Q_d = 100\% \times \frac{\text{total daily trap flow}}{\text{total daily stream flow}}$$

$$= 100\% \times \frac{\sum_{i=1}^{1} q_{id}}{Q_d}$$

$$= 100\% \times \frac{\frac{156.14 \text{ acre-feet}}{1 \text{ day}}}{\frac{27570.24 \text{ acre-feet}}{1 \text{ day}}}$$

$$= 100\% \times 0.005665$$

$$= 0.5665\%.$$

Thus, on May 7, 2000, approximately one-half of one percent of the total stream flow of the Sacramento River flowed through rotary-screw trap 42020.