50 SHEETS 100 SHEETS 200 SHEETS

22-141 22-142 22-144

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- 1. Problem 6.2.1 text
- 2 Problem 6.2.7 text
- 3. Problem 6.4.1 text
- 4. Problem 7.2.5 text
- 5. Problem 7.2.6 text

(a) NO sample & hold: $6ce = \frac{0.5}{S+1} = \frac{0.5}{S(S+1)} = \frac{0.5}{S(S+1)} = \frac{0.5}{S(S+1)} = \frac{0.5}{S(S+1)}$

(b) with
$$5 \ R \ N$$
, $T = 0.4 \ S$

$$3 \left[\frac{1 - e^{-1}}{S} \frac{o.S}{(S + o.S)} \right] = \frac{(2 - 1)}{2} \frac{2}{(2 - 1)} \frac{1 - e^{-0.5 \cdot 0.4}}{(2 - e^{-0.2})} = \frac{o.1813}{z - o.8187}$$

$$6 (2) = \frac{o.1813}{Z - 0.6374} \Rightarrow (2) = 6 (2) \ R(2) = 6 (2) \frac{2}{Z - 1}$$

$$C(2) = \frac{o.1813}{(Z - 1)(2 - 0.6374)} = \frac{Z}{2} \left[\frac{1}{Z - 1} - \frac{1}{Z - 0.6374} \right]$$

$$C(k) = 0.5 \cdot \left[1 - \left[0.6374 \right]^{k} \right] = 0.5 \cdot \left[1 - e^{-0.45 k} \right]$$

$$C(kT) = 0.5 \cdot \left[1 - e^{-0.45 k} \right]$$

c) continuous time DC gain = $G_{Ce}(0) = 0.5$) same discrete time DC gain = $G_{Ce}(2)|_{Z=1} = 0.5$) same In steady state the sample 2 hold does not have any effect $= \frac{1}{100} = \frac$

Want
$$C_{SS}(z) = 20^2 \Rightarrow O_{SS} = 0.07 \cdot 20 = 1.4 \text{ Volts}$$

From problem 5.8 we have:
$$\frac{C(\frac{1}{2})}{O(2)} = \frac{\frac{z-1}{z} \times 0.6}{1+\frac{z-1}{z} \cdot (0.07) \times 0.6}$$
 with $\frac{C(z)}{(z-0.8181)} = \frac{z}{(z-0.8181)}$

equivalent s plane poles
$$z = e^{ST} = S = \frac{1}{T} \log z = S = -0.9256 \pm \frac{1}{3} \cdot \frac{3741}{10}$$

$$= 0 \quad \text{Time constant} \quad Z = \frac{1}{10} = 1.08 \text{ s} \quad \Rightarrow \quad \boxed{Ts \approx 4.3 \text{ sec}}$$

$$C(z) = G_{ce}(z) O(z) = \left(\frac{0.1873z + 0.1752}{z^{2} - 0.8056z + 0.831}\right) \cdot 1.4 \frac{z}{z - 1} \Rightarrow C_{ss} = \lim_{z \to 1} (z - 1) C(z) = 20 \#$$

(Note: can get the same result using the fact that count time DC gain = discrete time DC gain)

6.46.2) open loop:
$$G_0 = k \left[\frac{0.0187 z + 0.0175}{(z-1)(z-0.8187)} \right] \Rightarrow poles at: z=e^{ST} = 0$$

$$\Rightarrow (a) \zeta_1 = \frac{1}{0} = \infty; \quad \zeta_2 = \frac{1}{2} = 0.5$$

(b) closed loop: from 6.7 we have
$$z_{1,2} = 0.9116 \angle 0.1374$$

$$\Rightarrow \overline{\zeta}_{d} = \frac{-T}{\log |z|} = 1.08, \quad w_{nd} = \frac{1}{T} \sqrt{L_{n}^{2} + 0^{2}} = 1.657, \quad f_{d} = -\frac{L_{n}r}{(\ln^{2} + 0^{2})} = 0.558$$

(c) Analog system:
$$G_{cl} = \frac{40}{5^2 + 25 + 7.8}$$

= $w_n = \sqrt{7.8} = 1.68$, $w_n y = 1 // y = \frac{1}{w_n} = 0.598$, $Z = \frac{1}{y_{w_n}} = 1$

(d) Sampled Data Analog

Ts 4.3 sec 4 sec

Mp = 12%

$$M_p = \frac{9\pi}{1-3^2}$$

7.275)
$$R + \varepsilon$$
 $- \kappa - \frac{1-\varepsilon^{3}}{5} - \frac{1}{5+1}$

a)
$$G(z) = 3\left[\frac{1}{S(s+1)}\right] = \frac{2\left(1-e^{-T}\right)}{\left(z-1\right)\left(z-e^{-T}\right)} = G(z) = \left(\frac{z-1}{z}\right)G_1(z) = \frac{1-e^{-T}}{z-e^{-T}}$$

= Char. eq:
$$1 + \frac{k(1-e^{-T})}{2-e^{-T}} = 0 \iff 2 - e^{-T} + k(1-e^{-T}) = 0$$

For stability we need poles in
$$|z|<1 \Rightarrow |\bar{e}^T \cdot k(i-\bar{e}^T)|<1 \Leftrightarrow 0$$

$$-1 < \bar{e}^T \cdot k(i-\bar{e}^T)<1$$
left hand side ineq. yields: $k < \frac{1+\bar{e}^T}{1-\bar{e}^T}$
RMS yields: $-k(i-\bar{e}^T)<1-\bar{e}^T \Rightarrow -k<1 \Rightarrow k>-1$

$$-1 < K < \frac{1 + e^{-T}}{1 - e^{-T}}$$

c) If
$$k=-1$$
 -then we have a closed loop pole at $Z=1$, i.e.

$$G_{Ce}(z) = -\frac{(1-e^{-T})}{Z-1} \Rightarrow \text{Impulse response}: C(0) = 0$$

$$C(h) = -(1-e^{-T}), n>0$$
(note: since $C(n)$ constant $\Rightarrow Z(c(n)) \rightarrow \infty$ NOT BIBO STABLE)

d) if
$$K = \frac{1+e^{-T}}{1-e^{-T}}$$
 we have a closed loop pole at $Z = -1$, i.e.

$$G_{Ce} = \frac{1+e^{-T}}{Z+1} \Rightarrow \text{Impulse response:} \quad C(G) = 0 \quad (+e^{-T}) \cdot (-1) \quad n > 0$$

$$C(h) = (+e^{-T}) \cdot (-1) \quad n > 0$$
(again $|C(h)|$ constant $\Rightarrow Z |C(h)| \rightarrow \infty$, NOT BIBO STABLE)

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From problem 7.6 we have: $Z - e^{-T} + k(1 - e^{-T}) = 0$ stable $\longrightarrow -1 < k < \frac{1 + e^{-T}}{1 - e^{-T}}$ $\longrightarrow T = 0.01$ $\longrightarrow -1 < k < 20$ $\longrightarrow T = 0.1$ $\longrightarrow -1 < k < 20$ $\longrightarrow T = 0.1$ $\longrightarrow -1 < k < 20$

decreasing

e) with no sample & hold: +0 5+1

char eq: S+1+k=0, pole at $S=-(1+k) \Rightarrow Stable for <math>-1 < k < \infty$

d) As T of the upper range of stability for K to.

(if T > 0 > upper range of stability for k -> varinge of cont. time system)

Sampling reduces stability