

A real-time particle filter for bus arrival prediction with discrete CDFs for journey planning

Tom Elliott

University of Auckland, Auckland, New Zealand

E-mail: tom.elliott@auckland.ac.nz

Thomas Lumley

University of Auckland, Auckland, New Zealand

E-mail: t.lumley@auckland.ac.nz

Summary. The prediction of transit vehicle arrival time is a complex problem with the added difficulty of its real-time nature. Reliable predictions require the combination of both vehicle and network states, implying that real-time traffic congestion information is incorporated into the predictions. Inevitably, however, there is a lot of uncertainty around arrival times: road speeds fluctuate, particularly around peak time, and multi-modality is added with every stop passed (which may or may not cause the bus to stop depending on passenger demand). Therefore, not only do we need to predict arrival time, but also assess and report the uncertainties involved. We present a method of using a particle filter to combine the states of both vehicle and network to obtain arrival time distributions. These are then discretised in such a way that allows real-time calculation of event probabilities for use in journey planning applications.

Keywords: particle filter, transport, real-time, GTFS, transit networks, journey planning

1. Introduction

- the problem of predicting bus arrival - it needs to use real-time traffic information Citation Needed (2020)
- however, many deployed methods are either specific to a provider/city, or don't make use of real-time data (only vehicle position and/or arrival delays, e.g., in Auckland)
- since the only logical source of "traffic data" in this setting is the transit vehicles themselves, makes sense to develop framework that uses them to estimate real-time network state Elliott and Lumley (2020)

- in this example, particle filter is used to obtain a sample of points from the arrival time distribution - many many points, which cannot possibly be distributed or stored efficiently
- we propose a method of reducing this to a simple discrete CDF of arrival time (in minutes)
- we show that these results can be used to answer some common journey planning questions, in real-time, which outperform current “method”

Some of the references include:

- Cathey and Dailey (2003)
- Yu et al. (2006, 2010, 2011)
- Hans et al. (2015)

2. Background

Before describing the process of obtaining arrival time distributions, we must first define the framework with which we obtain vehicle and network state estimates. Elliott and Lumley (2020) present a process for constructing a transit road network from raw GTFS data.

most of this section will be removed/cut-down to just the basic concepts

2.1. GTFS static and real-time

The structure of public transport systems is very similar across the globe, so much so that Google developed GTFS (Google Developers, 2006) to standardise the way transport agencies organise and distribute transit data. GTFS consists of two core components: *static*, which contains pre-defined information, such as routes and stops, and *real-time*, which contains vehicle location and other data collected in real-time.

Static GTFS contains *structural* data, describing information one might observe on a printed timetable. This includes route information about trips (instances of a route at a specific time), the geographical path the vehicle takes, and the stops it services. This provides the basis of transit data, and plays a key role in developing the aforementioned *transit network*.

Real-time GTFS describes how live data, such as the location of a bus, or its time of arrival at or departure from a bus stop, is formatted. Vehicle

locations allow users to track the progress of the vehicle along its route, and are often updated every 10–30 seconds. In some implementations, such as in Auckland, they are also triggered by events such as arrival at a bus stop or (major) intersection. Arrival and departure events, on the other hand, are triggered whenever the bus arrives at or departs from a bus stop (or at least thinks it does), and include the time of the event and, if scheduled arrival times are available, the *delay* between scheduled and actual arrival (or departure).

A huge benefit of GTFS being adopted widely around the world is that developers can easily access transit feeds for different providers in different cities and countries using the same structure. Any application developed using (only) GTFS information can, technically, be redeployed to any other system also using GTFS. For this reason, we opted to develop our application framework based solely on GTFS data, as described next.

2.2. A transit road network

One important predictor of bus arrival is travel time (Shalaby and Farhan, 2004). However, previous research has focused on situations where either only a single route is considered, or else different routes and combined by manually locating common road segments. This is, of course, not easy or even possible to automate. Elliott and Lumley (2020) proposed a method of developing a transit road network from only GTFS data by identifying *nodes* (bus stops and intersections) and the *edges* (roads) between them.

Here, we use the simplest version of this method, which places nodes at bus stops. Thus, any two routes that share the same sub-sequence of bus stops are assumed to follow the same path between them (this is almost always the case). By expressing the route as a series of nodes and road segments, we can begin to share information across routes.

The goal is to model vehicles as they travel along their respective routes, estimating their average speed along each road segment. Having traversed a road segment, the data is passed to the network to update the real-time traffic state. This can in turn be used, optionally with a forecasting function, to predict a future travel time of a bus along the road, which is used in arrival time prediction.

2.3. Particle filters estimating vehicle state

Estimation of vehicle state in real-time commonly uses *recursive Bayesian estimation*, in which the posterior becomes the prior for the next iteration.

Particle filters are a powerful method of estimating successive states, as they make few assumptions and, most importantly, cover a large range of possible trajectories, even when there is a high degree of multimodality as is the case with transit data (e.g., around bus stops). Here, I give a brief overview of the particle filter which was used by Elliott and Lumley (2020) to estimate vehicle state.

In a recursive Bayesian model, the underlying state we are interested in is denoted $\mathbf{x} = \mathbf{x}_{0:k} = [\mathbf{x}_0, \mathbf{x}_1, \dots, \mathbf{x}_k]$. It can rarely be observed directly, and instead we obtain measurements $\mathbf{y} = \mathbf{y}_{1:k} = [\mathbf{y}_1, \dots, \mathbf{y}_k]$. In a particle filter (Gordon et al., 1993), this state is represented by a weighted sample of *points*, and makes use of the delta measure δ ,

$$p(\mathbf{x}_{k-1} | \mathbf{y}_{0:k-1}) \approx \sum_{i=1}^N w_{k-1}^{(i)} \delta_{\mathbf{x}_{k-1}^{(i)}} (\mathbf{x}_{k-1}).$$

Elliott and Lumley (2020) describe the particle filter in detail, with discussion of its use for modelling transit vehicles in real-time. However, here we only discuss the merits of the particle filter, and need no more details than given already.

The main advantage of the particle filter is, as mentioned, its ability to cope with a wide range of plausible, discontinuous trajectories. This often happens in transit data as the bus passes bus stops at which it may or may not stop. It's main downside is the computational demand, since we need 1000s of particles in memory for each vehicle, and perform transitions and updates to each of them. However, Elliott and Lumley (2020) have shown that, so long as it is programmed efficiently, the particle filter can run fast enough to be feasible in a real-time setting, at least for updating vehicle states.

In the next section, we make use of the flexible nature of the particle filter in that each particle is transitioned independently, making it possible to account for a wide variety of complex behaviours. These most notably include bus stops, which introduce a lot of uncertainty, but also layovers, which can result in a wide temporal gap between possible arrival times.

The particle filter allows us to estimate the state of a vehicle and, most importantly, it's average speed along road segments:

$$p(b_\ell | \mathbf{y}_{1:k}) \approx \sum_{i=1}^N w_k^{(i)} \delta_{b_\ell^{(i)}} (b_\ell).$$

2.4. Estimating network state

Having obtained an estimate of the speed of each vehicle along a road, we can proceed to updating the state of the road network itself. This uses a Kalman filter to update the state, β_c , using the estimated vehicle speeds.

This all provides a flexible method for modelling real-time traffic conditions in any network using only GTFS, and not rely on other data sources (for example taxis or video cameras).

We use a hierarchical model on vehicle travel times, as individual vehicles have different average speeds, even if they travel at the same time, due to different driver behavior and other factors. The between-vehicle noise parameter ψ_ℓ describes this, and is estimated from historical data.

The observations are also uncertain, as they are estimated from the particle filter. We can assume between-vehicle and measurement uncertainties are independent, so the total variance of observations is

$$\text{Var}[b_\ell | \mathbf{y}_{1:k}] = e_\ell^2 + \psi_\ell^2.$$

The system noise q is also estimated from historical data. Together we can quickly update the network state using the information variance of the Kalman filter (since this allows data from multiple sources simultaneously, which can happen when two or more buses are travelling one behind the other).

The result is an estimate of the state of the network at time t_c ,

$$p(\beta_c | \cup_m \cup_\ell b_{\ell,c,m}) \sim \mathcal{N}(\beta_\ell, \mathbf{P}^2).$$

This can be used to predict the travel time of buses.

If a forecast function is available, we could also forecast future travel time based on current state and historical trends, and this would be incorporated.

3. Predicting arrival time

Accurate, reliable prediction of bus arrival time requires knowledge of both vehicle and network states, represented by \mathbf{x}_k and β_c , respectively. Since there is a high degree in the uncertainty of these, particularly when forecasting future network states around peak times, it is crucial to incorporate this uncertainty into the arrival time distribution and, ultimately, decision making processes.

The particle filter presents a robust method of sampling all of the possible trajectories the vehicle might take (Hans et al., 2015).

- initial state incorporates uncertainty (shape, multimodality) of vehicle state
- trajectory of each particle = one possible path the bus might take
- accounts for uncertainty in (forecasted) road speed, correlations, etc
- result makes no assumptions about shape of distribution

The main downside of the particle filter is the computational demand of it, often requiring 5000-10000 particles per bus.

- Elliott and Lumley (2020) showed the pf is feasible in real-time for modelling
- need to also show predictions can be done quickly and usefully
- reduce number of particles where possible

Our implementation is described in section 3.1. To examine the effectiveness of our approach, we run our method on a full day and compared the predictions with the actual arrivals, as well as the currently used “GTFS” predictions. These are discussed in section 3.2.

3.1. Particle filter ETAs

In our application, the vehicle state is already represented by a set of N particles,

$$p(\mathbf{x}_{k|k} | \mathbf{y}_k) \approx \sum_{i=1}^N w_k^{(i)} \delta_{\mathbf{x}_k^{(i)}}(\mathbf{x}_k)$$

which we use directly. However, were vehicle states available in some other form, one would simply take a sample from the posterior state estimate $p(\mathbf{x}_{k|k} | \mathbf{y}_k)$. This gives us a sample of plausible bus states for which we can predict individual arrival times at upcoming stops.

As with the vehicle model described by Elliott and Lumley (2020), we can iteratively forecast each particle’s arrival at all upcoming stops. This involves incorporating network state (vehicle speeds along roads) as well as bus stopping behaviour. These two aspects are described individually below, and each particle simply iterates between them until it reaches the end of the route.

[introduce trip state]

3.1.1. Road segment travel times

[mostly copy 5-step process from thesis section 5.2.1]

Each particle begins having travelled $x_k^{(i)}$ meters along the route, with a current speed of $\dot{x}_k^{(i)}$. The first travel time required is, therefore, the time to reach the end of the current road segment, $\ell^{(i)}$, assuming the bus maintains its current speed. From the transit network construction, we know that segment $\ell^{(i)}$ starts $\mathcal{D}_{\ell^{(i)}}$ meters along the route and has a length of $\mathcal{L}_{\ell^{(i)}}$ meters, so the distance remaining is

$$\bar{z}^{(i)} = \mathcal{D}_{\ell^{(i)}} + \mathcal{L}_{\ell^{(i)}} - x_k^{(i)}$$

which will take the particle

$$z^{(i)} = \frac{\bar{z}^{(i)}}{\dot{x}_k^{(i)}} \text{ seconds}$$

to complete.

[once trip state introduced, the above becomes:]

... particle has completed $100p_\ell^{(i)}\%$ of the segment. If the vehicle is nearing the end of the segment (less than 200 meters remaining), we keep the particle's initial speed $\dot{x}_k^{(i)}$. Otherwise, we simulate a speed from the network state with mean β_ℓ , uncertainty \mathbf{P}_ℓ , and between-vehicle variability ψ_ℓ , as follows:

$$\dot{x}_\ell^{(i)*} = \begin{cases} \dot{x}_k^{(i)} & (1 - \hat{p}_k)\mathcal{L}_\ell < 200, \\ v_\ell^{(i)} \sim \mathcal{N}_T(\beta_\ell, \mathbf{P}_\ell^2 + \psi_\ell^2, 0, \mathbb{V}_\ell), & \text{otherwise.} \end{cases}$$

Now the travel time to the end of the current segment can simply be obtained as

$$\tilde{z}^{(i)} = \frac{(1 - \hat{p}_k^{(i)})\mathcal{L}_\ell}{\dot{x}_\ell^{(i)*}}.$$

We now store an iterative variable *travel-time-so-far* with the time taken to reach the end of the current segment, $\eta^{(i)} = \tilde{z}^{(i)}$.

3.1.2. Bus stops

3.1.3. Arrival time distribution

3.2. Results

4. A discretized CDF approximation for journey planning

- CDF makes it possible to answer many (often complex) journey planning questions

- $P(\text{catch})$
- $P(\text{arrive on time})$
- $P(\text{transfer})$
- this is a simple computation - can be done client side (i.e., on a user's phone) by passing CDF (small size, as e.g., JSON)

4.1. Simplified ETA CDF

- round to minutes
- compute the CDF by definition “number of particles arriving within x minutes”

5. Discussion

- what this means
- how this makes JP more accessible

5.1. Future Work

- automated route selection
- improved particle filter
- improved network construction
- improved network state forecasts

5.2. Conclusion

- simple conclusion of the paper

References

Cathey, F. W. and Dailey, D. J. (2003) A prescription for transit arrival/departure prediction using automatic vehicle location data. *Transportation Research Part C: Emerging Technologies*, **11**, 241–264.

Citation Needed (2020) *Missing citations*.

Elliott, T. and Lumley, T. (2020) Modelling the travel time of transit vehicles in real-time through a GTFS-based road network using GPS vehicle locations. *Australian & New Zealand Journal of Statistics*, **62**.

- Google Developers (2006) What is GTFS? <https://developers.google.com/transit/gtfs/>.
- Gordon, N. J., Salmond, D. J. and Smith, A. F. M. (1993) Novel approach to nonlinear/non-gaussian bayesian state estimation. *IEE Proceedings F Radar and Signal Processing*, **140**, 107–113.
- Hans, E., Chiabaut, N., Leclercq, L. and Bertini, R. L. (2015) Real-time bus route state forecasting using particle filter and mesoscopic modeling. *Transportation Research Part C: Emerging Technologies*, **61**, 121–140.
- Shalaby, A. and Farhan, A. (2004) Prediction model of bus arrival and departure times using AVL and APC data. *Journal of Public Transportation*, **7**, 41–61.
- Yu, B., Lam, W. H. K. and Tam, M. L. (2011) Bus arrival time prediction at bus stop with multiple routes. *Transportation Research Part C: Emerging Technologies*, **19**, 1157–1170.
- Yu, B., Yang, Z.-Z., Chen, K. and Yu, B. (2010) Hybrid model for prediction of bus arrival times at next station. *Journal of Advanced Transportation*, **44**, 193–204.
- Yu, B., Yang, Z.-Z. and Yao, B. (2006) Bus arrival time prediction using support vector machines. *Journal of Intelligent Transportation Systems*, **10**, 151–158.