ARE 231: Part 1: HW1 Due in class on the 14th

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Fall 2018

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After lecture I post a .dta file on the Canvas. Unzip it to get the Stata data set. Note that these are "real-ish" data, but they have been created to have approximately the covariance structure of some real data. Here is a description of the variables

| Item | EXPENDITURES: | PRICES: |
|-----------------------|--|------------------------|
| food at home | xfath | pfath |
| food in restaurants | xrest | prest |
| household operations | xhhop | phhop |
| car operations | xcaruse | pcaruse |
| public transportation | xtran | ptran |
| personal care | xcare | pcare |
| recreation | xrecr | prcer |
| tobbaco | xtob | ptob |
| alcohol | xalc | palc |
| women's clothing | xwclth | pwclth |
| men's clothing | $\mathbf{x}\mathbf{m}\mathbf{c}\mathbf{l}\mathbf{t}\mathbf{h}$ | pmcloth |
| children's clothing | $\mathbf{x}\mathbf{k}\mathbf{c}\mathbf{l}\mathbf{t}\mathbf{h}$ | pkclth |

| OTHER VARIABLES: | | |
|----------------------------|--------------|--|
| Household net income | nety | |
| Gender of head | hsex | |
| Age of head | hage | |
| Age of spouse (if present) | sage | |
| Number of kids | kids | |
| Number of Adults | ad | |
| Region | region | |
| Time | $_{ m time}$ | |

$\mathbf{2}$

Load the data into STATA. Examine the data for outliers, oddities, and possible mis-codes. Check means, maxima, and minimia of continuous variables and frequencies of categorical data against the summary statistics below. Check the demographic characteristics of your sample.

. sum

| Variable | 0bs | Mean | Std. Dev. | Min | Max |
|----------|-------|----------|-----------|----------|----------|
| region | 14994 | 3.02581 | 1.246699 | 1 | 5 |
| hnety | 14994 | 20652.37 | 11643.64 | -5532 | 71000 |
| hage | 14994 | 35.20108 | 8.266935 | 20 | 55 |
| hsex | 14994 | 1.328932 | .4698407 | 1 | 2 |
| snety | 9838 | 11913.58 | 11407.85 | -15000 | 70000 |
| sage | 9838 | 33.50508 | 7.63836 | 20 | 55 |
| nety | 14994 | 28502.31 | 15939.8 | 5050.627 | 71455.74 |
| xfath | 14994 | 3242.105 | 1905.458 | 0 | 17448.54 |
| xrest | 14994 | 1283.318 | 1319.746 | 0 | 16117.34 |
| xhhop | 14994 | 1662.291 | 1613.549 | 0 | 23814.82 |
| xwclth | 14994 | 846.2386 | 1035.544 | 9 | 24391.79 |
| xmclth | 14994 | 567.9294 | 717.4686 | 0 | 16857.31 |
| xkclth | 14994 | 53.68904 | 153.0824 | 0 | 2506.821 |
| xcaruse | 14994 | 2110.811 | 1805.092 | 0 | 17682.57 |
| xtran | 14994 | 386.751 | 659.7086 | 0 | 10232.39 |
| xcare | 14994 | 649.4383 | 494.8456 | 0 | 4532.063 |
| xrecr | 14994 | 1634.237 | 1710.11 | 0 | 23337.76 |
| xtob | 14994 | 501.8776 | 811.7445 | 0 | 8684.721 |
| xalc | 14994 | 580.4715 | 830.7408 | 0 | 15208.5 |
| pfath | 14994 | .8366482 | .2448178 | .3265014 | 1.14347 |
| prest | 14994 | .7594858 | .2576474 | .2619048 | 1.152542 |
| phhop | 14994 | .7911728 | .248994 | .2635426 | 1.081685 |
| pcaruse | 14994 | .7115704 | .2735375 | .1962521 | 1.31414 |
| ptran | 14994 | .7560718 | .3083149 | .1912682 | 1.244134 |
| pcare | 14994 | .825366 | .213055 | .3776119 | 1.039801 |
| precr | 14994 | .7760642 | .2356293 | .3125541 | 1.045887 |
| ptob | 14994 | .5463716 | .3018981 | .1021921 | 1.051254 |
| palc | 14994 | .7670915 | .2809425 | .2382838 | 1.178878 |
| pwclth | 14994 | .8597817 | .1974238 | .4707775 | 1.108847 |
| pmclth | 14994 | .8823521 | .2028664 | .5084102 | 1.164948 |
| pkclth | 14994 | .7977848 | .19513 | .406382 | 1.026748 |
| kids | 14994 | .918434 | 1.022303 | 0 | 3 |
| ad | 14994 | 1.656129 | .4750145 | 1 | 2 |
| time | 14994 | 3.561558 | 1.732526 | 1 | 6 |

3

Construct total (nondurable) expenditure x_h as the sum of expenditure on individual commodities. Plot the log of expenditure on 'food at home' against the log of total expenditure. Is 'food at home' a normal good? Is it a luxury or a necessity? Could you investigate the income elasticity of men's clothing this way?

4

Suppose you wanted estimate parameters of a Cobb-Douglas utility function from this data. How would you do so? Based on your preliminary inspection of the data, are the data consistent with an assumption of Cobb-Douglas preferences? Why or why not?

5

Construct budget shares for each good i and household h: $w_{ih} = \frac{x_{ih}}{x_h}$.

Also construct a 'Stone' price index for each household:

$$P_h = \exp\left(\sum_{i=1}^{12} w_{ih} \ln p_{ih}\right)$$

Check that in 1992 the values of this index are about 1. Then construct real total expenditure for each household as,

$$rx_h = \frac{x_h}{P_h}$$

6

Estimate the parameters of a share equation for food at home (i = f) of the Working-Leser form:

$$w_{fh} = \alpha_f + \sum_{i=1}^{12} \gamma_i \ln p_i h + \beta_i \ln r x_h + e_{fh}$$

7

Try a RESET test of this parametric functional form. Hint: This can be done with a post-estimation command in Stata: estat ovtest.

8

Create the following aggregate commodities:

- xtran = xtran + xcaruse (transportation = public transportation + car use)
- xserv = xhhop + xcare (services = household operations + personal care)
- xvices = xalc + xtob (vices = alcohol + tobacco)
- xcloth = xmcltoh + xwcloth + xkcloth (clothing)

This gives seven composite commodities: xfath, xfrest, xtran, xserv, xrecr, xvices, xcloth.

Create prices for the four new commodities. To do this, first find the mean budget shares of the 12 original goods in each period (or period and region). Then construct new price for each household for the new commodities by taking weighted geometric means of the household prices. For example:

$$p_{vices,h} = \exp\left(\frac{\overline{w}_{alc,t}}{\overline{w}_{alc,t} + \overline{w}_{tobc,t}} \ln p_{alc,t} + \frac{\overline{w}_{tob,t}}{\overline{w}_{alc,t} + \overline{w}_{tobc,t}} \ln p_{tob,t}\right)$$

where the t subscript refers to the year in which household h is sampled. Check that you have done the construction correctly by confirming that the prices are about one in the base period/region.

9

Estimate by OLS the parameters of the seven equations:

$$w_{i,h} = \alpha_{i0} + \sum_{k=1}^{m} \alpha_{i,k} d_{k,h} + \sum_{j=1}^{7} \gamma_{i,j} \ln p_{j,h} + \beta_i \ln \frac{x_h}{P_h} + u_{i,h}$$

Where the price index P_h is the Stone price index created previously; The $d_{k,h}$ are m household demographic variables that affect demands. Examples are the number of adults or children in the household, the age of the person 1, and so on. You should choose your own set of demographics (keeping in mind the demographic heterogeneity in your sample.) Be careful to include the same demographics in each equation. (Why?) You may need to construct new variables.

10

Check that adding up automatically holds. That is, the columns of estimates sum to one or zero:

$$\sum_{i=1}^{7} \alpha_{i0} = 1; \quad \sum_{i=1}^{7} \alpha_{i,k} = 0 \forall k; \quad \sum_{i=1}^{7} \gamma_{i,j} = \forall j; \quad \sum_{i=1}^{7} \beta_i = 0$$

11

From your estimates, determine whether 'food at home' and 'clothing' are luxuries or necessities. Which good is the most price elastic?

12

Estimate six equations together by Seemingly Unrelated Regression (SURE). To do this, exclude the vices equation. (First try to run all seven equations together as a SURE system and see what happens.) Check that the parameter estimates are exactly the same as the OLS estimates. (Why is this the case?) Check that the dropping some other good gives exactly the same parameter estimates.

13

Look at the error covariance matrix for the SURE estimates. Can you make any sense of the covariances? Which errors are correlated and why?

14

Test for homogeneity in each of the seven demand equations estimated by OLS above. That is, use F-tests on the individual equations to test for:

$$\sum_{j=1}^{n} \gamma_{ij} = 0 \text{ for } i = 1, 2, \dots 7$$