# Calculus I
# Derivative of $\frac{a}{x} = ax^{-1}$

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$= (2\pi)\left(\textbf{?}\right)$

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$$= -\frac{8\pi}{x^5}.$$