Integrals of the form $\int tan^m x sec^n x dx$, n-positive and even

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Example

$$\int \tan^8 x \sec^4 x dx = \int \tan^8 x \sec^2 x \sec^2 x dx$$

$$= \int \tan^8 x \sec^2 x d (\tan x) \qquad \text{Can we rewrite } \sec^2 x \text{ via } \tan x?$$

$$= \int \tan^8 x \left(1 + \tan^2 x \right) d(\tan x) \qquad \text{Set } u = \tan x$$

$$= \int u^8 \left(1 + u^2 \right) du$$

$$= \int \left(u^8 + u^{10} \right) du$$

$$= \frac{u^9}{9} + \frac{u^{11}}{11} + C$$

$$= \frac{\tan^9 x}{9} + \frac{\tan^{11} x}{11} + C \qquad .$$