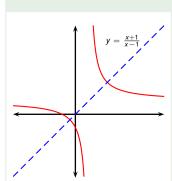
## Precalculus Inverse of fractional linear transformation

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## Example

Find 
$$f^{-1}(x)$$
 where  $f(x) = \frac{x+1}{x-1}$ .



Answer: 
$$f^{-1}(x) = \frac{x+1}{x-1}$$
,  $x \neq 1$ .

We deal with domains and ranges later:

$$y = \frac{x+1}{x-1}$$
 mult. by  $(x-1)$   
 $y(x-1) = x+1$   
 $x(y-1) = y+1$  div. by  $(y-1)$   
 $f^{-1}(y) = x = \frac{y+1}{y-1}$  relabel  $x, y$   
 $f^{-1}(x) = \frac{x+1}{x-1}$ 

We divided by  $y - \hat{1}$  so  $y \neq 1$ . Therefore the domain of  $f^{-1}$  is all real numbers except 1.

Can a non-identity function be its own inverse? Yes, *f* is.

What does it mean for f to be its own inverse? Graph of f is symmetric across y = x.