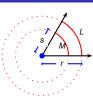
## **Precalculus**

# Find circle arclength from radius and angle

**Todor Miley** 

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# Arc-length of a circle arc



#### **Proposition**

Let two circles have common center and radii s and r. Suppose an arbitrary geometric angle with vertex at the common center of the circles cuts off short arcs of length

M and L. Then 
$$\frac{s}{r} = \frac{M}{L}$$
. 
$$\frac{s}{r} = \frac{M}{L}$$
 Choose  $s = 1$ , relabel  $M = \alpha$ 

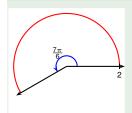
The angle-measure of a geometric angle is the arc-length cut off from a radius 1 circle, therefore we get the following.



## Corollary

The arc-length cut off by an angle with measure  $\alpha$  from a circle of radius r equals  $\alpha r$ .

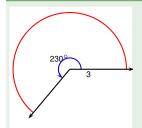
#### Example



Find the length of an arc of a circle of radius 2 cut off by an angle of measure  $\frac{7\pi}{6}$  (= 210°).

arc-length = 
$$\alpha r = \frac{7\pi}{6} \cdot 2 = \frac{7\pi}{3} \approx 7.33038$$
 (units)

#### Example



Find the length of an arc of a circle of radius 3 cut off by an angle of measure 230°.

$$lpha = 230^\circ$$

$$= 230^\circ \frac{\pi \text{ rad}}{180^\circ} = \frac{23}{18} \pi \text{ rad}$$

$$\text{arc-length} = \alpha r = \frac{23\pi}{18} \cdot 3 = \frac{23\pi}{6} \approx 12.043$$

Convert to radians