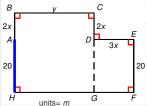
Precalculus

§ Geometric-text problems leading to polynomial systems, part 1

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Example



A field is enclosed by a wall AH and fencing at

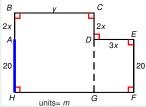
the rest of the boundary, as depicted. Given:
$$|EF| = |AH| = 20 \text{ m}, |BC| = y \text{ m},$$

$$|20|AB| = |DC| = 2x \text{ m}, |DE| = 3x \text{ m}; \text{ fencing}$$
length, excluding wall, is 130 m; area of *HBCG* is 3 times that of *DEFG*. Find the length $|HF|$.

Fence length =
$$130m$$

 $2y + 2 \cdot 2x + 2 \cdot 3x + 20 = 130$
 $10x + 2y = 110$ | Div. by 2
 $5x + y = 55$
 $y = 55 - 5x$
 $Area(HBCG) = 3 \cdot Area(DEFH)$
 $y \cdot (2x + 20) = 3 \cdot 3x \cdot 20$
 $(55 - 5x)(2x + 20) - 180x = 0$
 $110x + 1100 - 10x^2 - 100x - 180x = 0$
 $-10x^2 - 170x + 1100 = 0$ | Div. by -10

Example



A field is enclosed by a wall AH and fencing at

the rest of the boundary, as depicted. Given:
$$|EF| = |AH| = 20 \text{ m}, |BC| = y \text{ m},$$
 $|AB| = |DC| = 2x \text{ m}, |DE| = 3x \text{ m}; fencing length, excluding wall, is 130 m; area of $|AB| = 3$ times that of $|AB| = 3$ find the length $|AB$$

$$y = 55 - 5x$$

$$-10x^{2} - 170x + 1100 = 0$$

$$x^{2} + 17x - 110 = 0$$

$$(x -5)(x + 22) = 0$$

$$x = 5 \text{ or } x = 22$$

$$y = 55 - 5x$$

$$= 55 - 5 \cdot 5 = 30$$

$$|HF| = (y + 3x)m$$

$$= (30 + 3 \cdot 5)m$$

$$= 45m$$