#### **Precalculus**

# Division of a polynomial by a linear polynomial

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$$x - 1$$
  $x^3 + 2x^2 + 1$ 

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Divide with quotient and remainder  $x^3 + 2x^2 + 1$  by x - 1.

$$x - 1$$
  $x^3 + 2x^2 + 1$ 

Divide  $x^3$  by x.

Divide with quotient and remainder  $x^3 + 2x^2 + 1$  by x - 1.

$$\frac{x^2}{x-1} \quad \overline{x^3+2x^2 + 1}$$

Divide  $x^3$  by x.

Divide with quotient and remainder  $x^3 + 2x^2 + 1$  by x - 1.

$$x - 1$$
  $x^2$   $x^3 + 2x^2 + 1$  ?

Multiply  $x^2$  by divisor.

Divide with quotient and remainder  $x^3 + 2x^2 + 1$  by x - 1.

$$x - 1$$
  $x^{2}$   $x^{3} + 2x^{2} + 1$   $x^{3} - x^{2}$ 

Multiply  $x^2$  by divisor.

Divide with quotient and remainder  $x^3 + 2x^2 + 1$  by x - 1.

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Divide with quotient and remainder  $x^3 + 2x^2 + 1$  by x - 1.

$$\begin{array}{c|cccc}
x^2 & ? \\
\hline
x - 1 & x^3 + 2x^2 & +1 \\
& x^3 - x^2 & \\
\hline
3x^2 & +1
\end{array}$$

Divide  $3x^2$  by x.

Divide with quotient and remainder  $x^3 + 2x^2 + 1$  by x - 1.

$$\begin{array}{c}
x^2 + 3x \\
x - 1 & x^3 + 2x^2 + 1 \\
x^3 - x^2 & 3x^2 + 1
\end{array}$$

Divide  $3x^2$  by x.

Divide with quotient and remainder  $x^3 + 2x^2 + 1$  by x - 1.

$$\begin{array}{c}
x^{2} + 3x \\
x - 1 \\
- \\
x^{3} + 2x^{2} + 1 \\
\underline{x^{3} - x^{2}} \\
3x^{2} + 1 \\
\underline{?} \quad ?
\end{array}$$

Multiply 3x by divisor.

Divide with quotient and remainder  $x^3 + 2x^2 + 1$  by x - 1.

$$\begin{array}{c}
x^{2} + 3x \\
x - 1 \\
- \\
x^{3} + 2x^{2} + 1 \\
\underline{x^{3} - x^{2}} \\
3x^{2} + 1 \\
\underline{3x^{2} - 3x}
\end{array}$$

Multiply 3x by divisor.

Divide with quotient and remainder  $x^3 + 2x^2 + 1$  by x - 1.

$$\begin{array}{cccc}
x^2 + 3x \\
x - 1 & x^3 + 2x^2 & +1 \\
- & x^3 - x^2 \\
- & 3x^2 & +1 \\
3x^2 - 3x & ?
\end{array}$$

Divide with quotient and remainder  $x^3 + 2x^2 + 1$  by x - 1.

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Divide 3x by x.

Divide with quotient and remainder  $x^3 + 2x^2 + 1$  by x - 1.

$$\begin{array}{cccc}
x^2 + 3x + 3 \\
x - 1 & x^3 + 2x^2 & +1 \\
- & x^3 - x^2 \\
- & 3x^2 & +1 \\
3x^2 - 3x & \\
\hline
3x + 1
\end{array}$$

Divide 3x by x.

Divide with quotient and remainder  $x^3 + 2x^2 + 1$  by x - 1.

$$\begin{array}{c}
x^{2} + 3x + 3 \\
x - 1 \\
- \\
x^{3} + 2x^{2} \\
- \\
- \\
\underline{x^{3} - x^{2}} \\
3x^{2} + 1 \\
\underline{3x^{2} - 3x} \\
3x + 1 \\
\underline{? ?}
\end{array}$$

Multiply 3 by divisor.

Divide with quotient and remainder  $x^3 + 2x^2 + 1$  by x - 1.

$$\begin{array}{c}
x^2 + 3x + 3 \\
x - 1 \\
- \\
x^3 + 2x^2 \\
- \\
3x^2 + 1 \\
3x^2 - 3x \\
3x + 1 \\
3x - 3
\end{array}$$

Multiply 3 by divisor.

Divide with quotient and remainder  $x^3 + 2x^2 + 1$  by x - 1.

Divide with quotient and remainder  $x^3 + 2x^2 + 1$  by x - 1.

Quotient: 
$$x^2 + 3x + 3$$
  
 $x - 1$   $x^3 + 2x^2 + 1$   
 $x^3 - x^2$   
 $x^3 - x^2$ 

(Dividend) = (Quotient) · (Divisor) + (Remainder)  

$$(x^3 + 2x^2 + 1) = (x^2 + 3x + 3) · (x - 1) + 4$$

Quotient: 
$$x^{2} + 3x + 3$$
  
 $x - 1$   $x^{3} + 2x^{2} + 1$   
 $x^{3} - x^{2}$   
 $x^{3} - x^{3}$   
Remainder:  $x^{3} - x^{2}$ 

(Dividend) = (Quotient) · (Divisor) + (Remainder)  

$$(x^3 + 2x^2 + 1) = (x^2 + 3x + 3) \cdot (x - 1) + 4$$