

Calculus I

Definite integral of linear function, part 2

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2019

Example

$$\int_0^3 (x^3 - 6x) dx$$

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$$\int_0^3 (x^3 - 6x) dx = \left[\int (x^3 - 6x) dx \right]_0^3$$

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