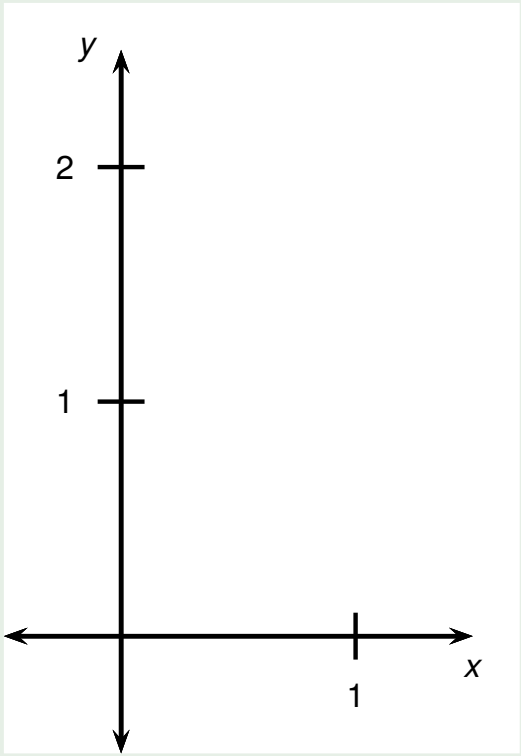
Calculus I
Area between two parabolas, part 2

Todor Milev

2019

Example



Find the area of the region enclosed by the parabolas $y = x^2$ and $y = 2x - x^2$.

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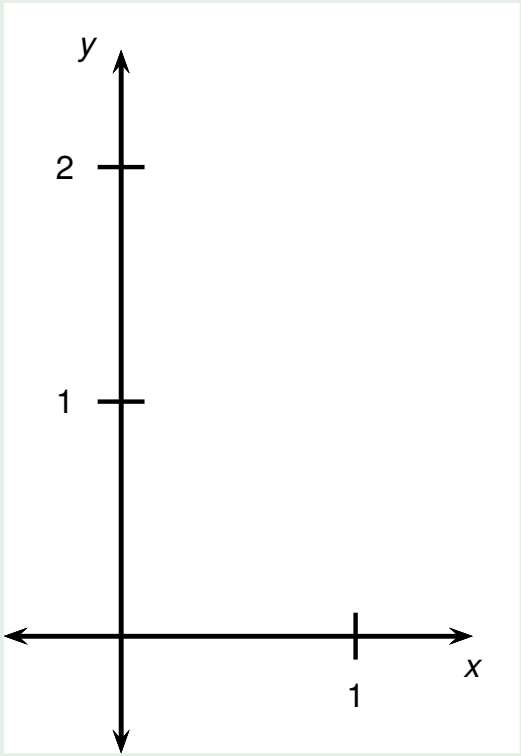

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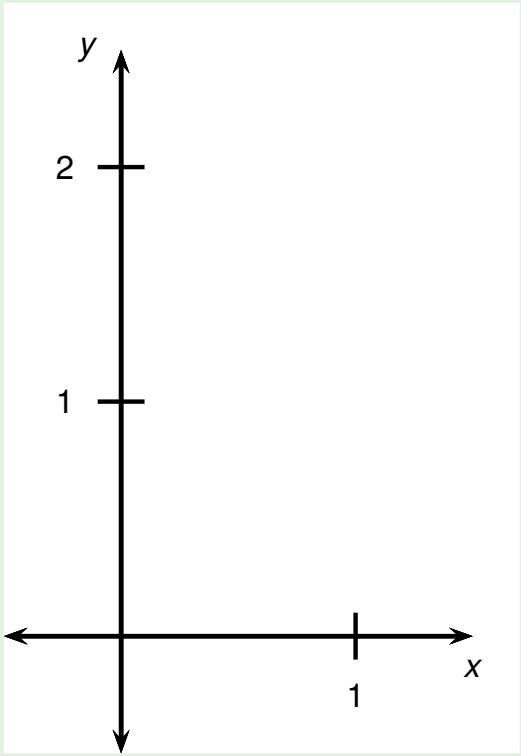

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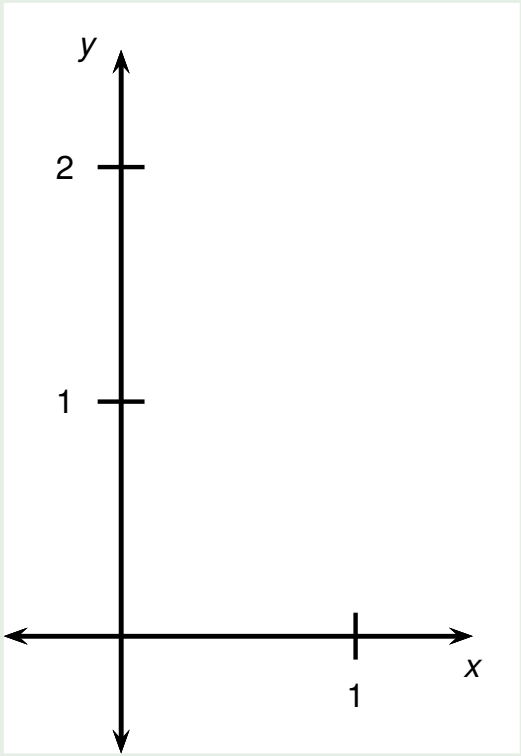

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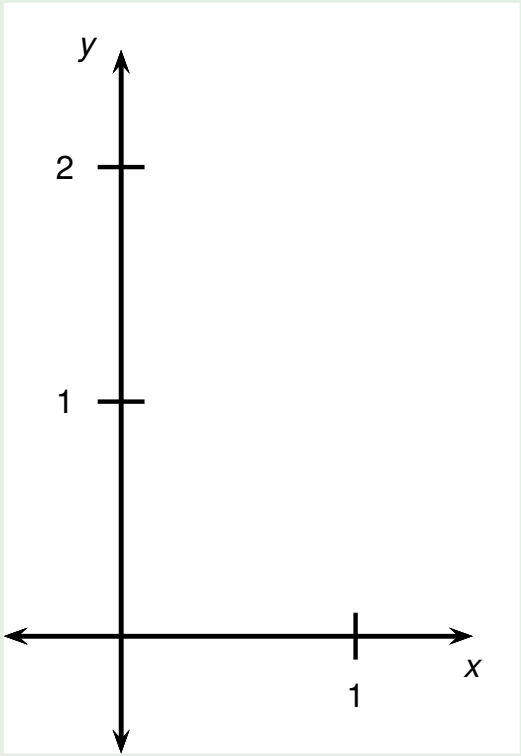

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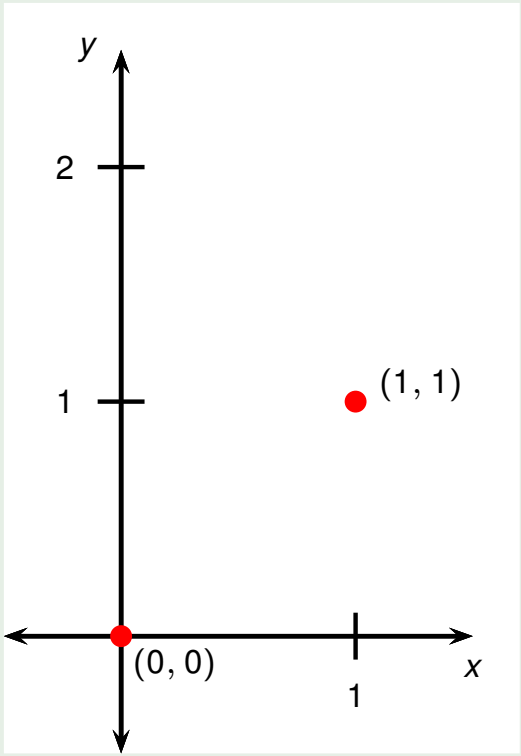

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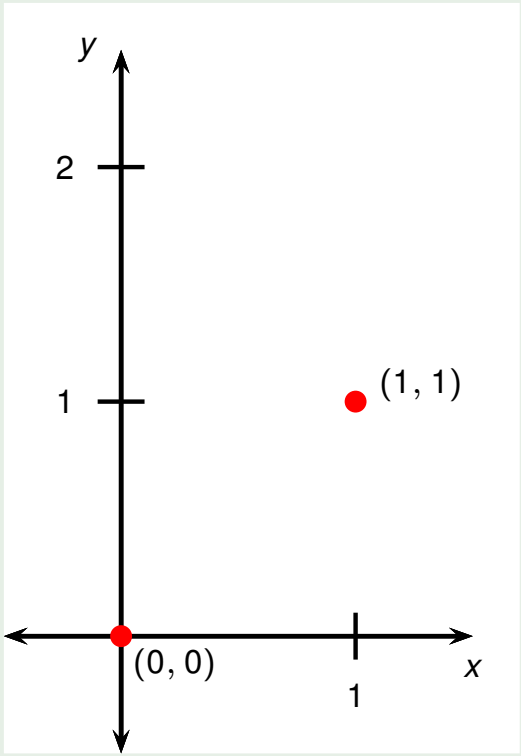

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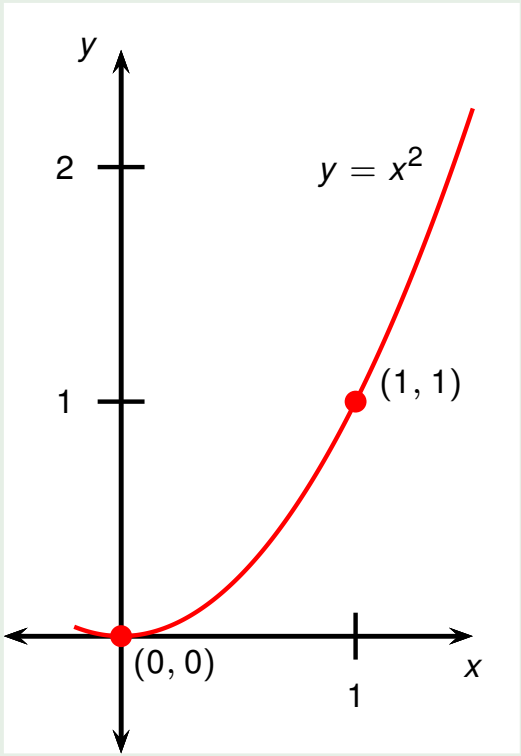

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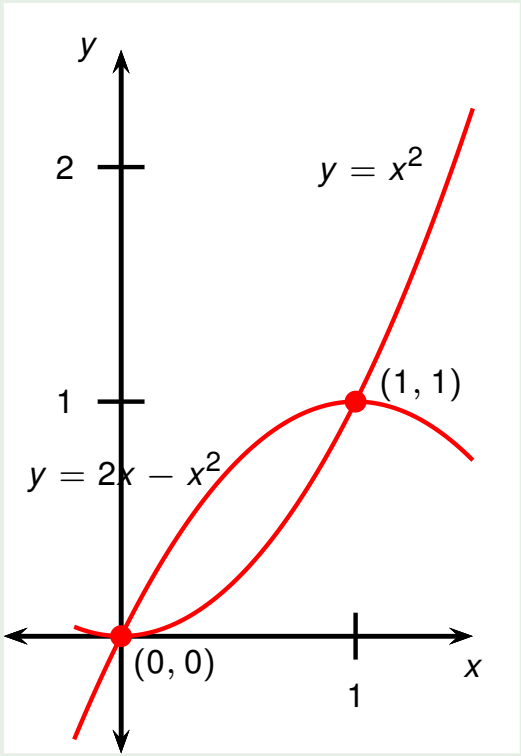

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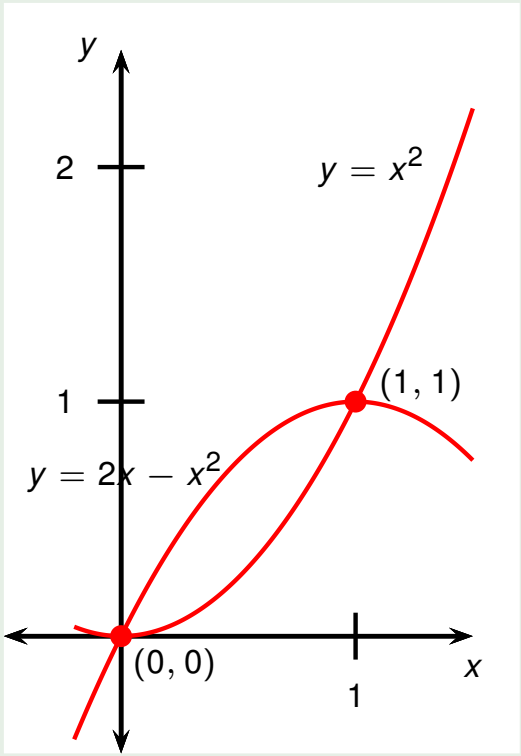

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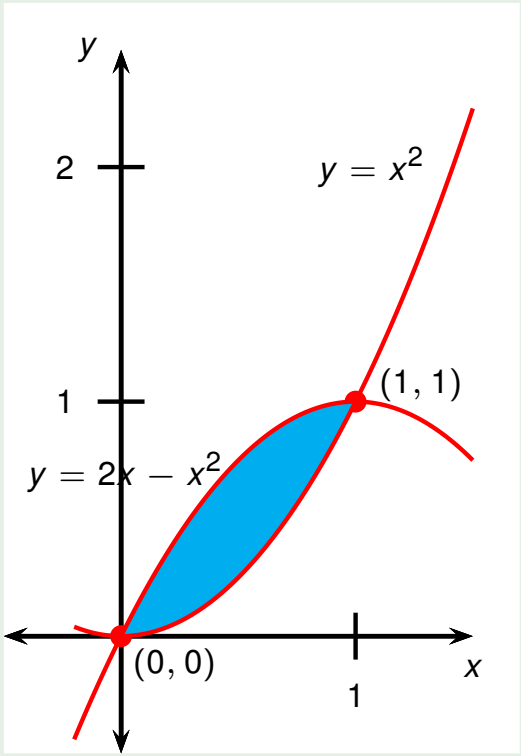

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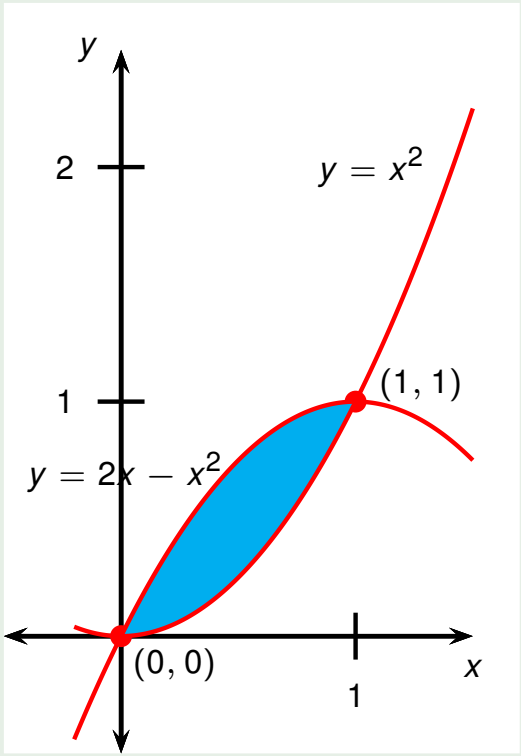

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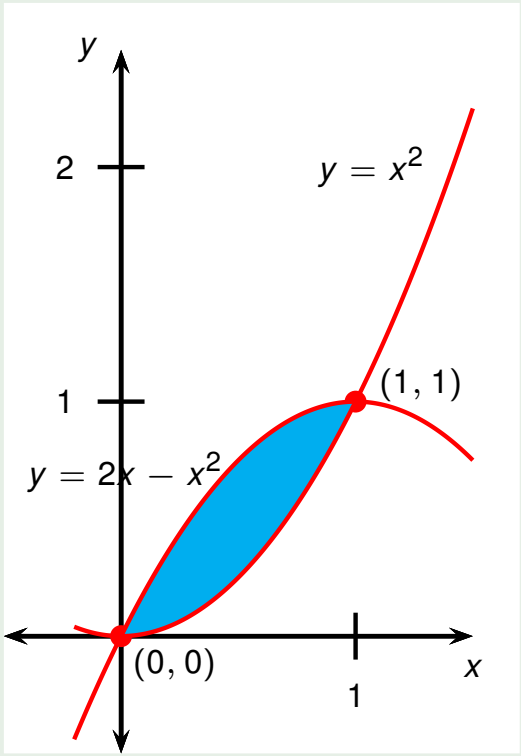

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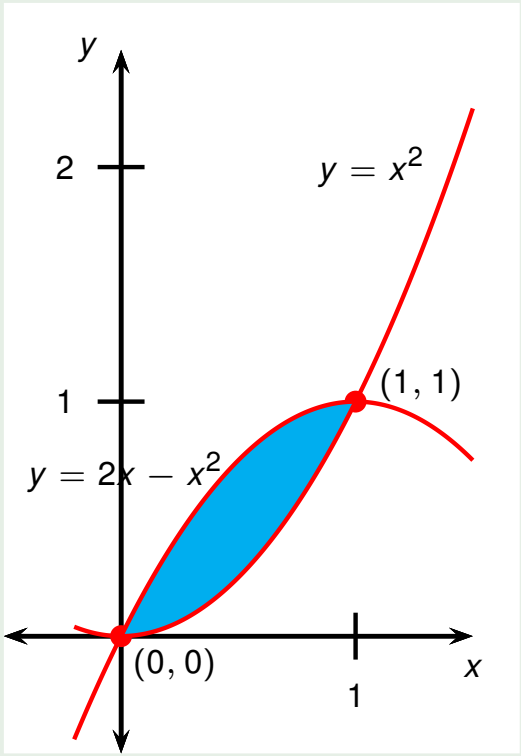

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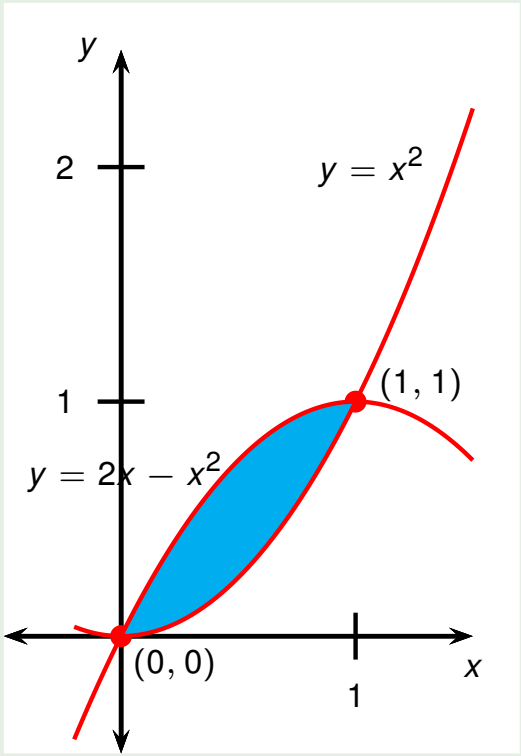

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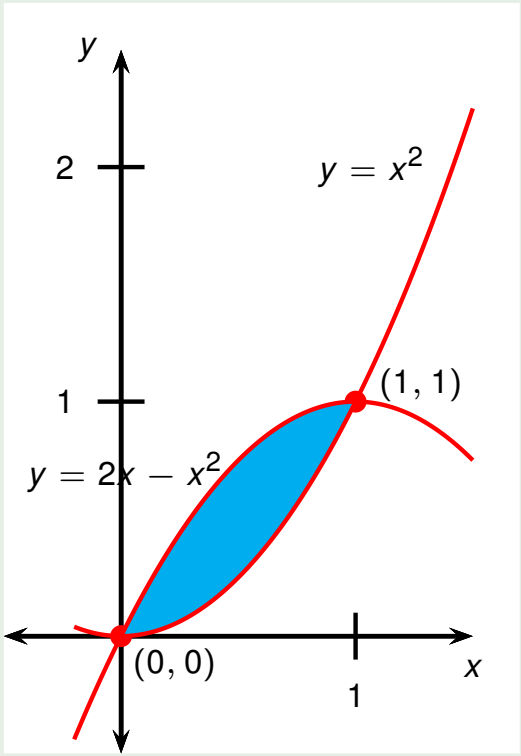

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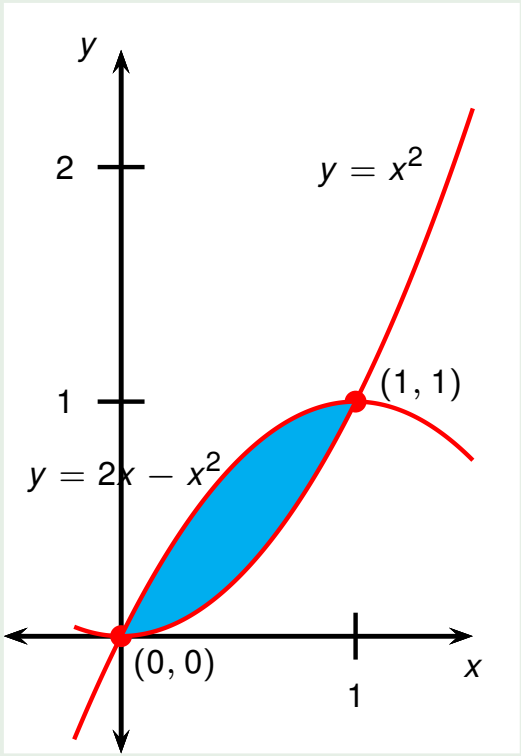

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