

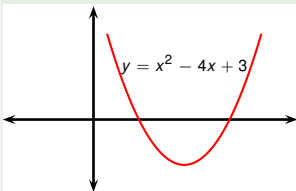
Precalculus

Find x -intercepts of a quadratic

Todor Milev

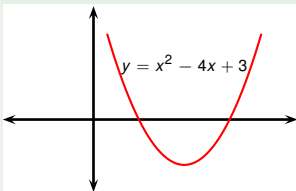
2019

Example



Find the x-intercepts of $x^2 - 4x + 3$.

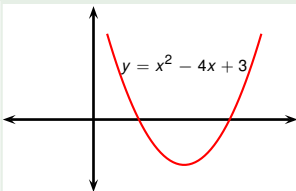
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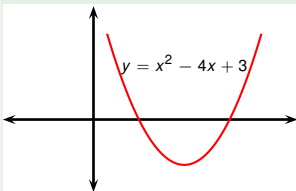
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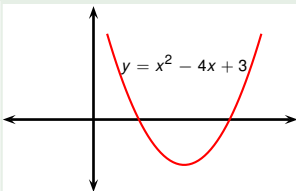
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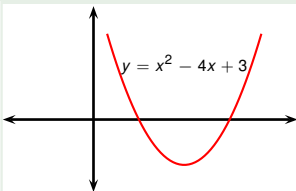
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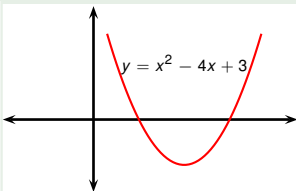
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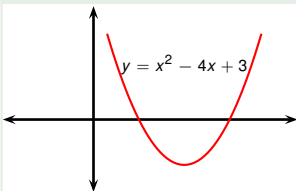
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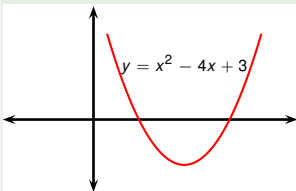
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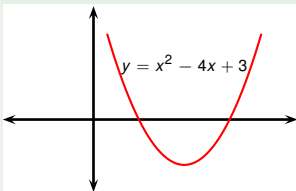
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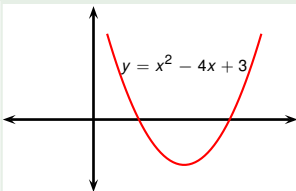
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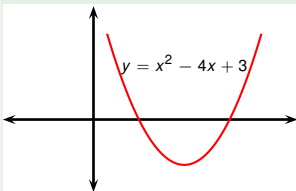
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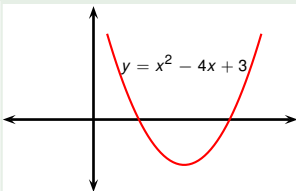
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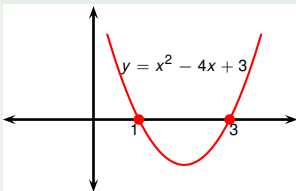
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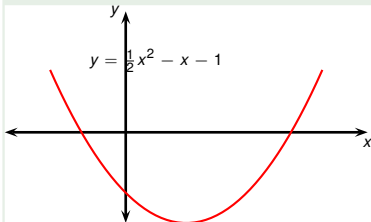
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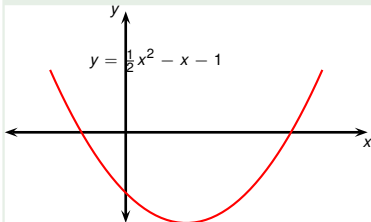
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Find the x -intercepts of $\frac{x^2}{2} - x - 1$.

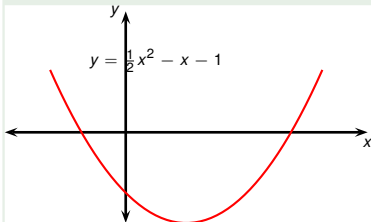
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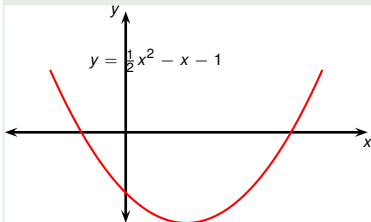
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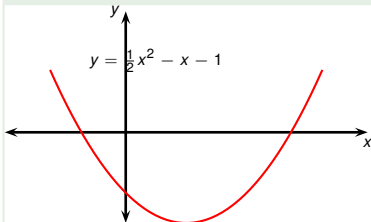
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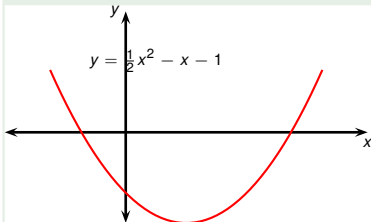
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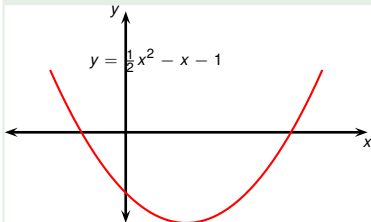
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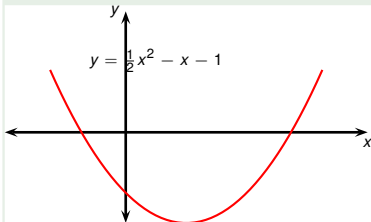
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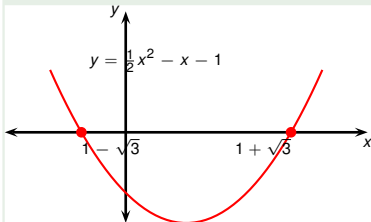
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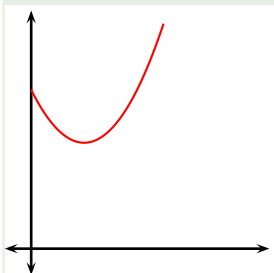
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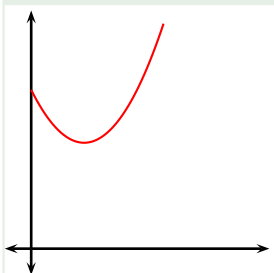
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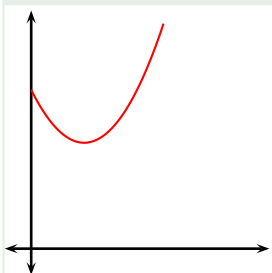
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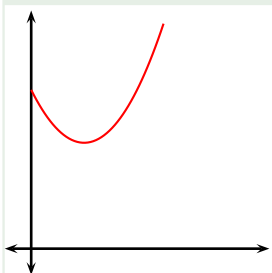
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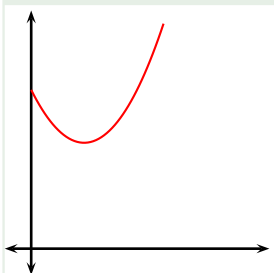
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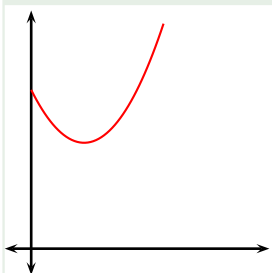
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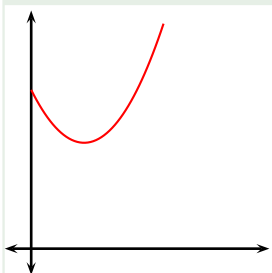
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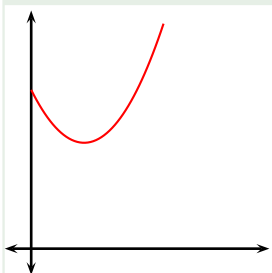
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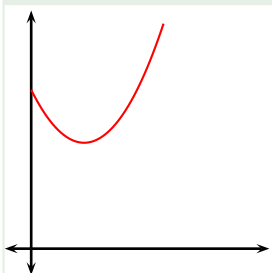
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