# Calculus I
$$\int (ax + b)^p \mathbf{d}x, \text{ part 2}$$

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2019

## Example (Substitution Rule)

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$$\text{Then}\quad du = 2dx$$

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