# Precalculus
# Trigonometric functions computable with algebraic numbers using special angles

Todor Milev

2019

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$\cos(105^\circ)$

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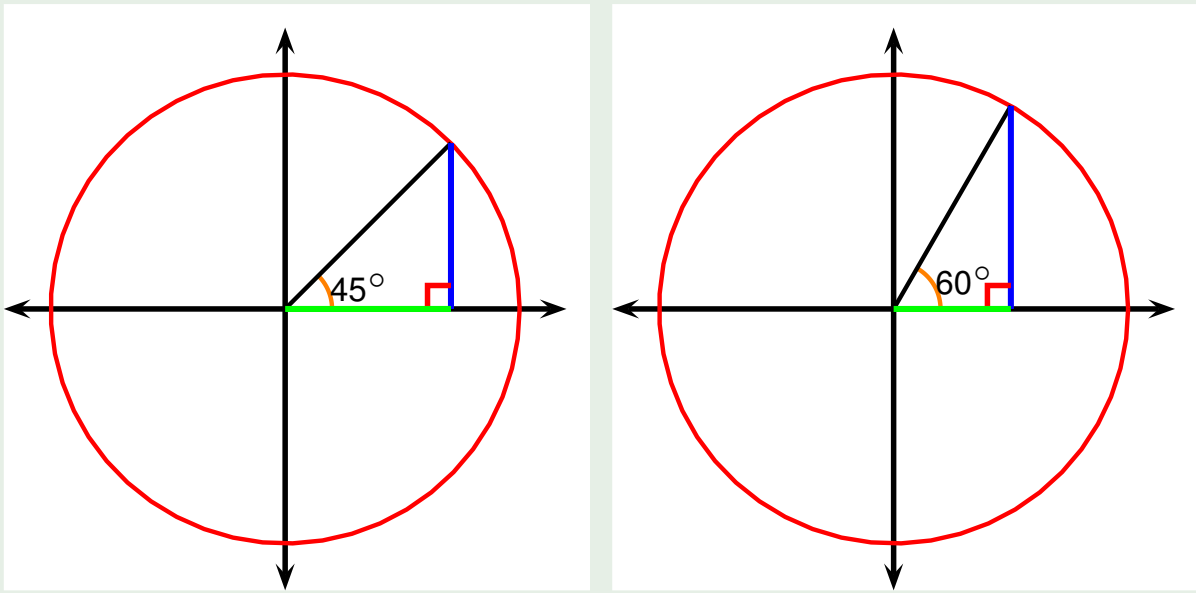

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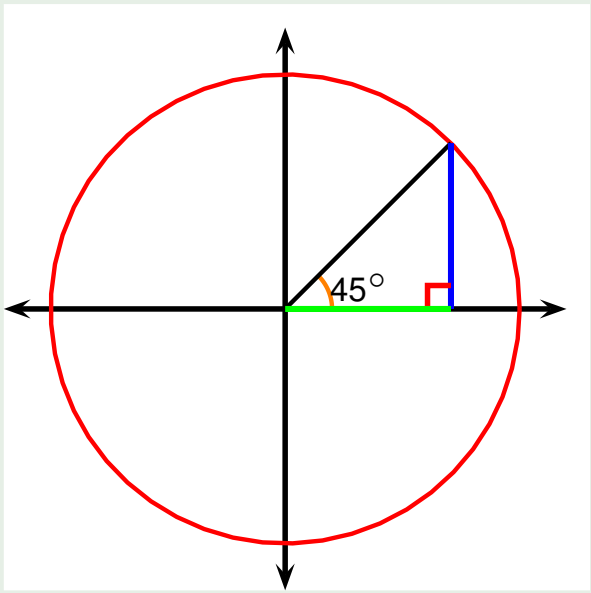
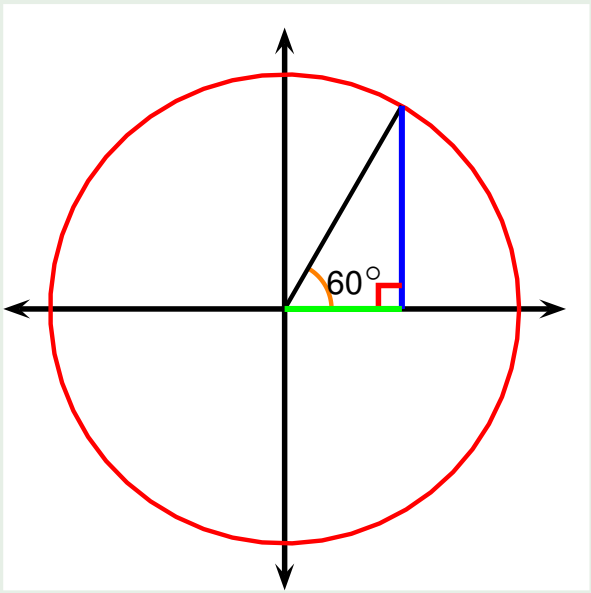
Angle sum f-la



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$$\cos(105^\circ) = \cos(45^\circ + 60^\circ)$$

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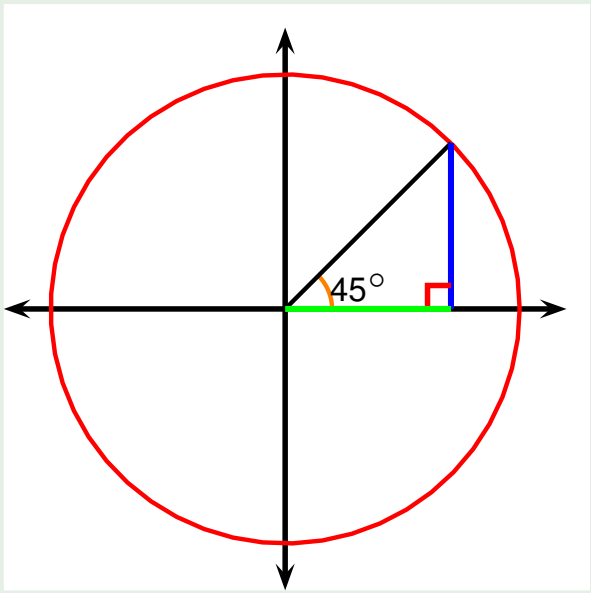
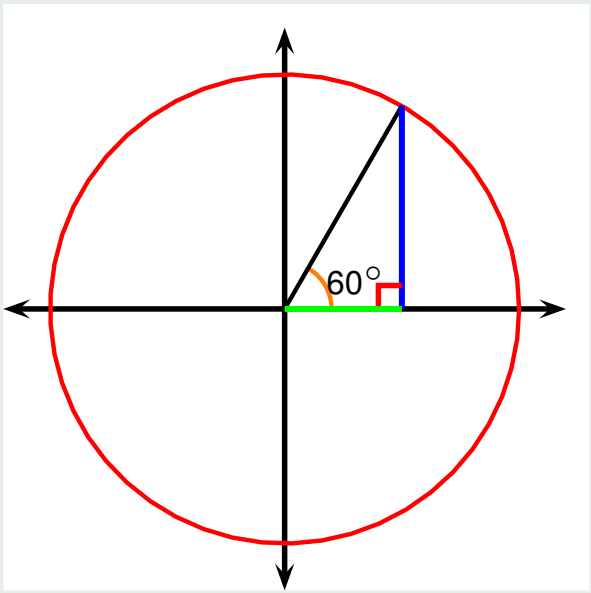
Angle sum f-la



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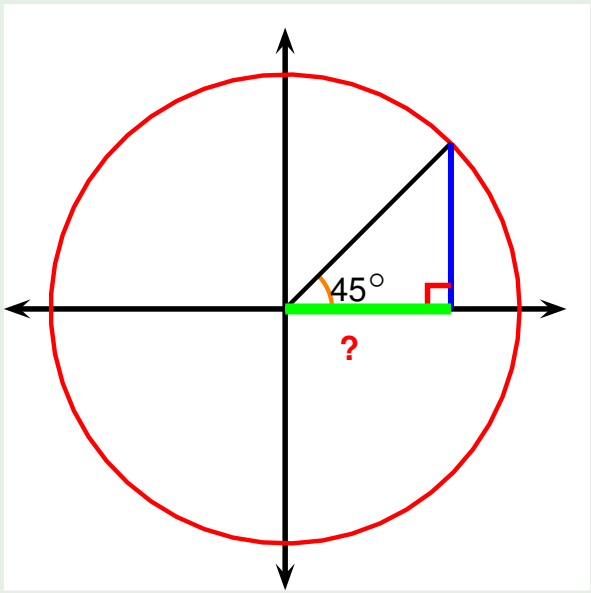
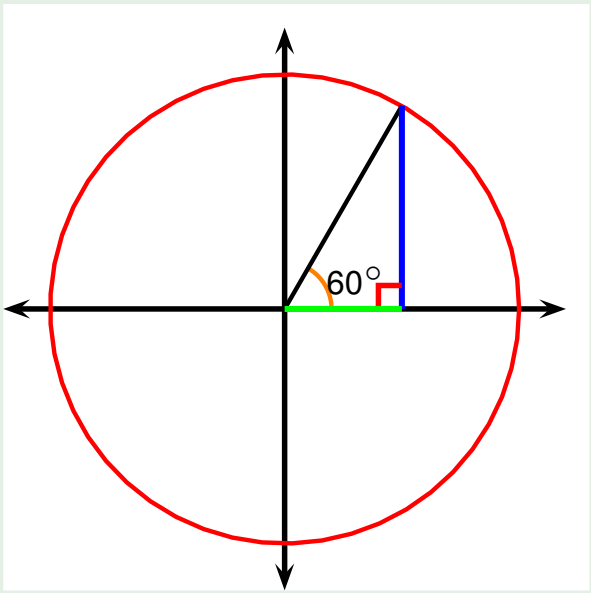
$$= ? \cdot ? - ? \cdot ?$$



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Angle sum f-la

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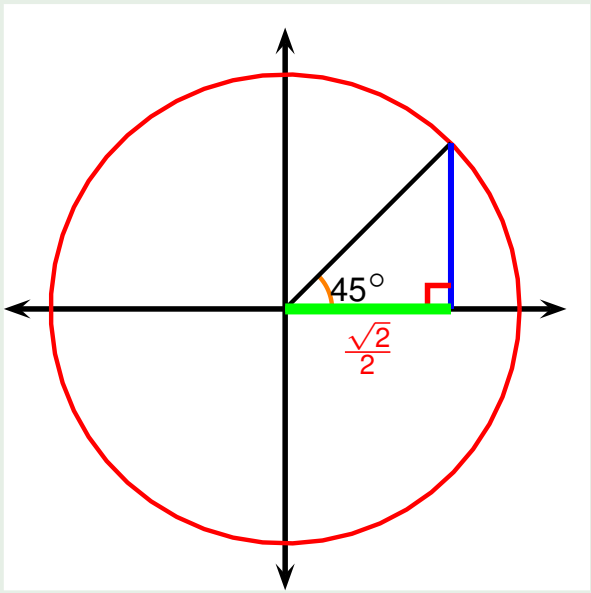


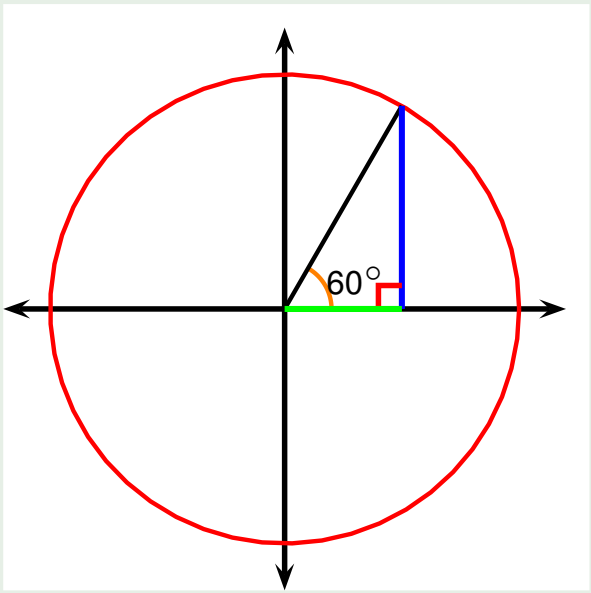

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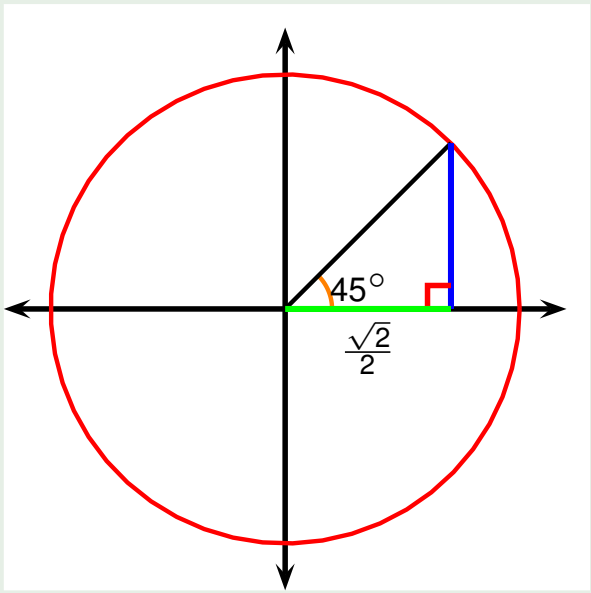


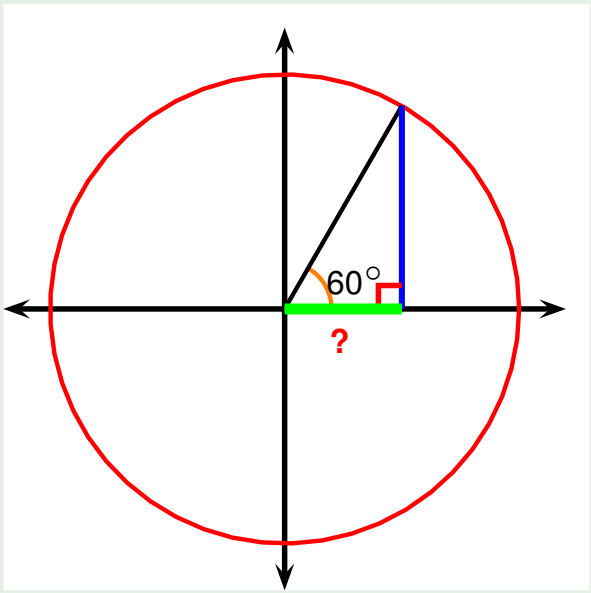

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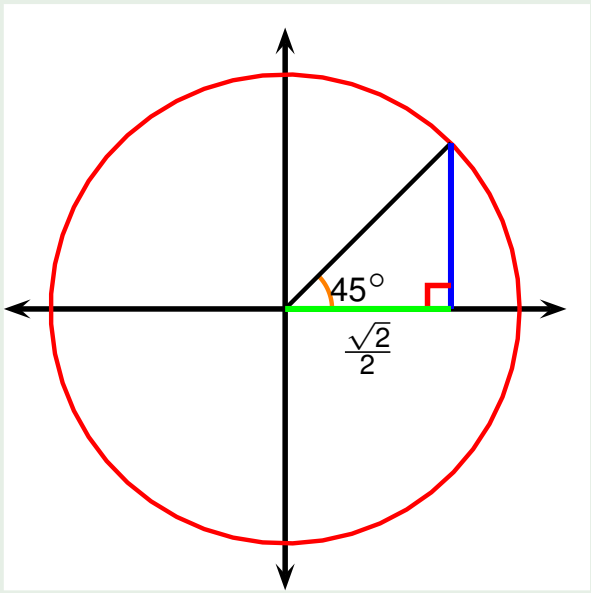


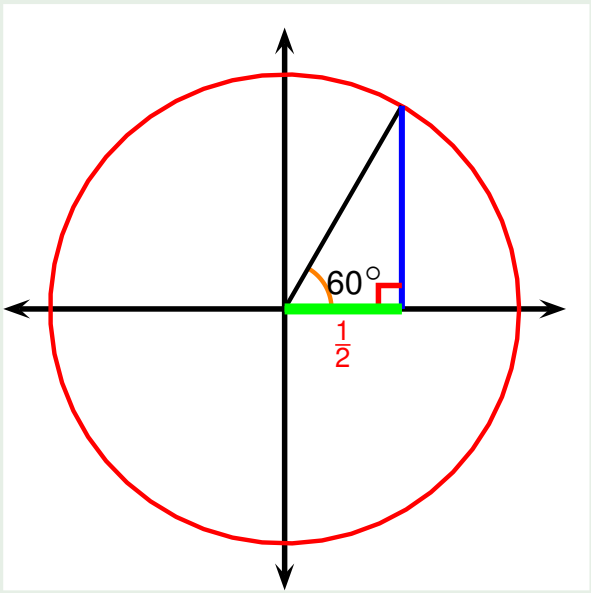

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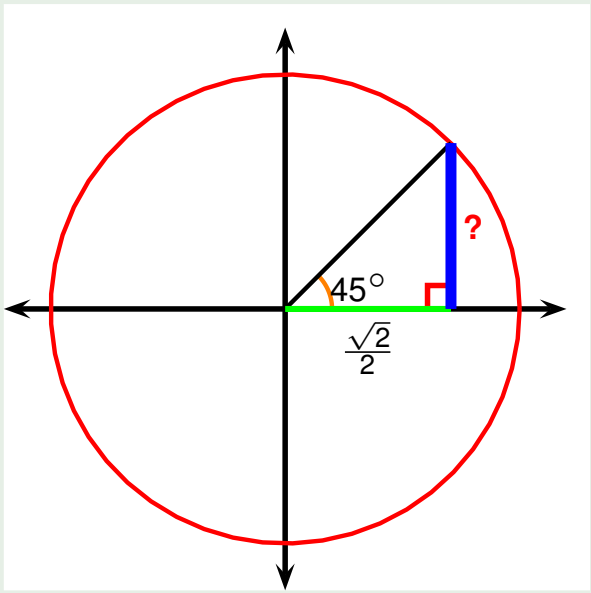


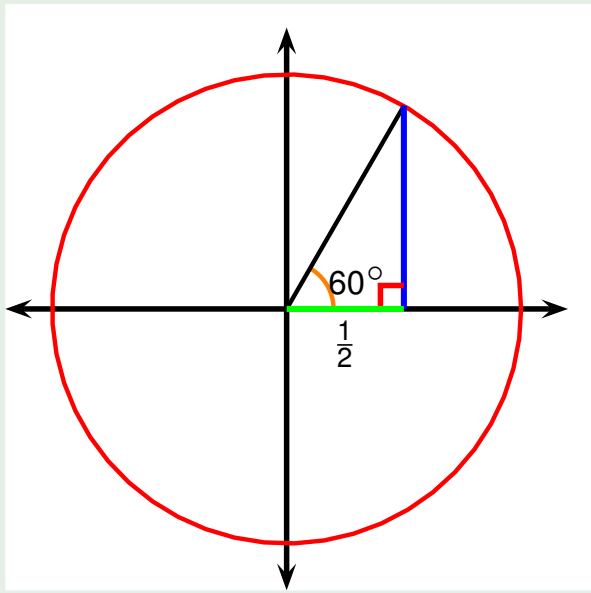

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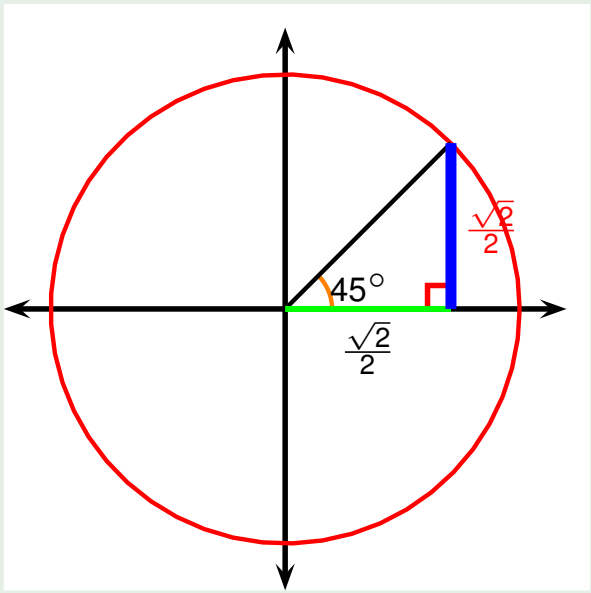


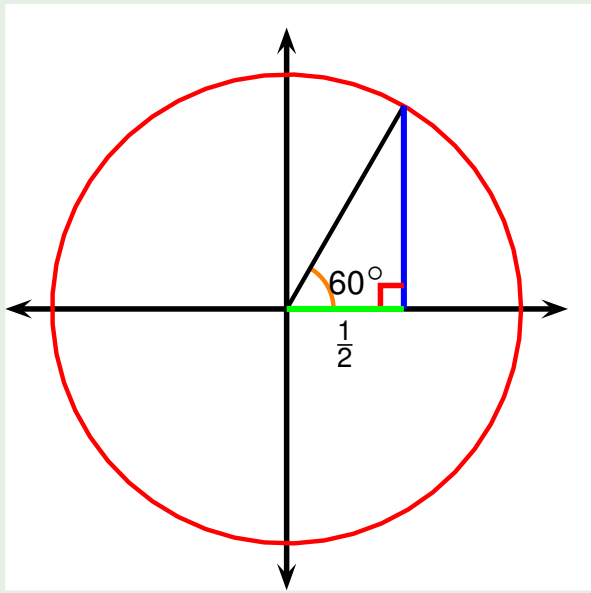

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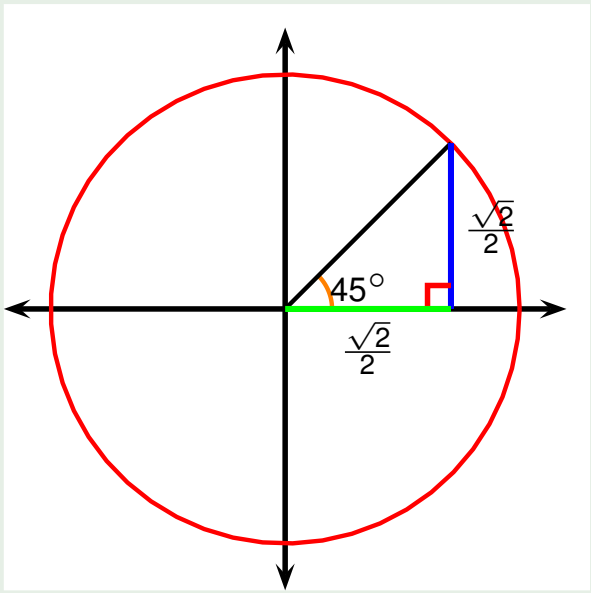


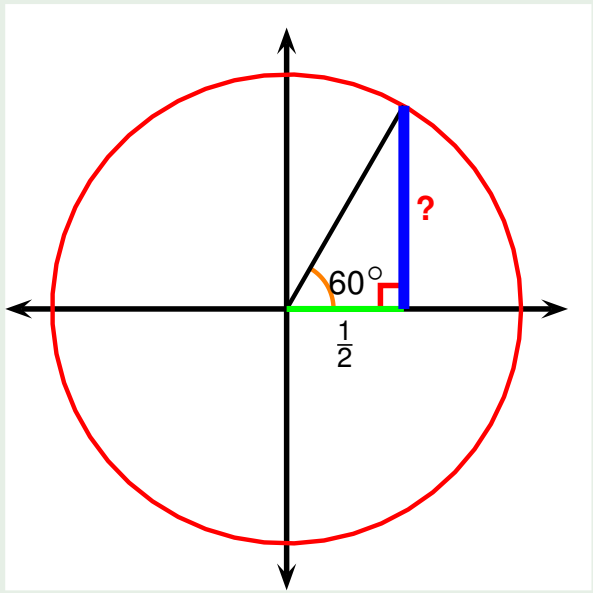

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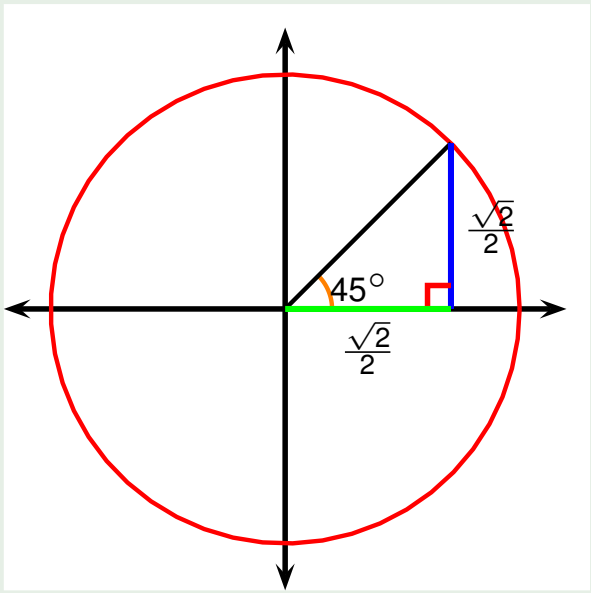


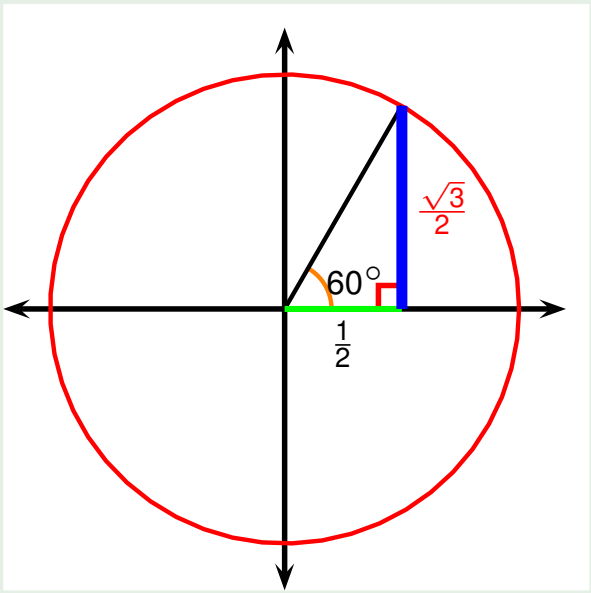

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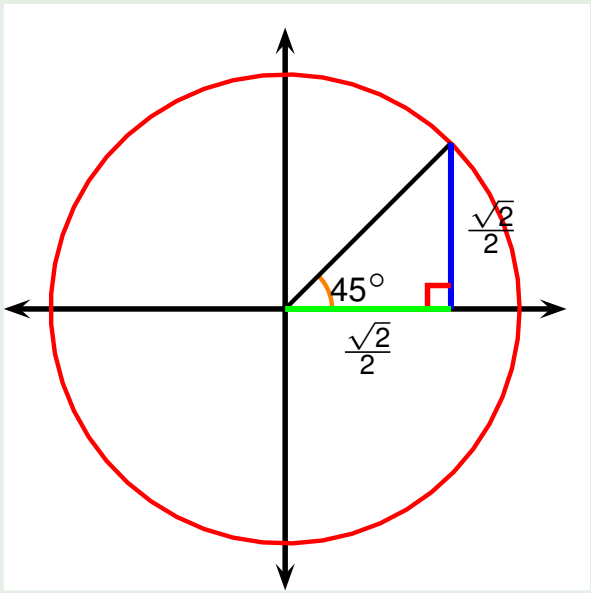
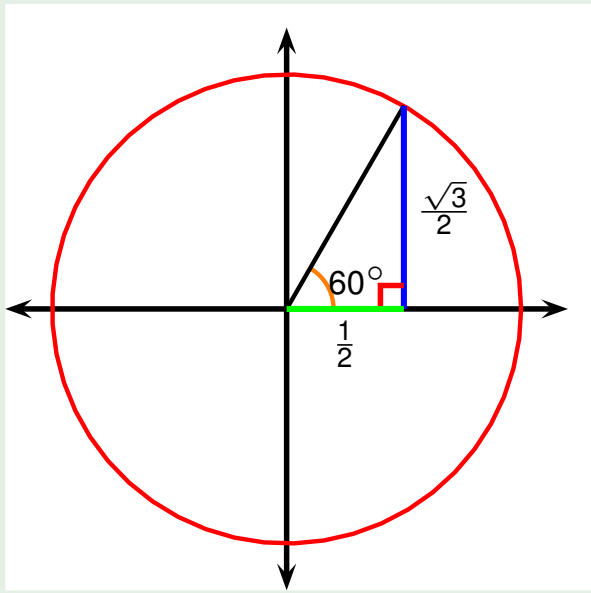
$$= \frac{\sqrt{2} - \sqrt{6}}{4}.$$



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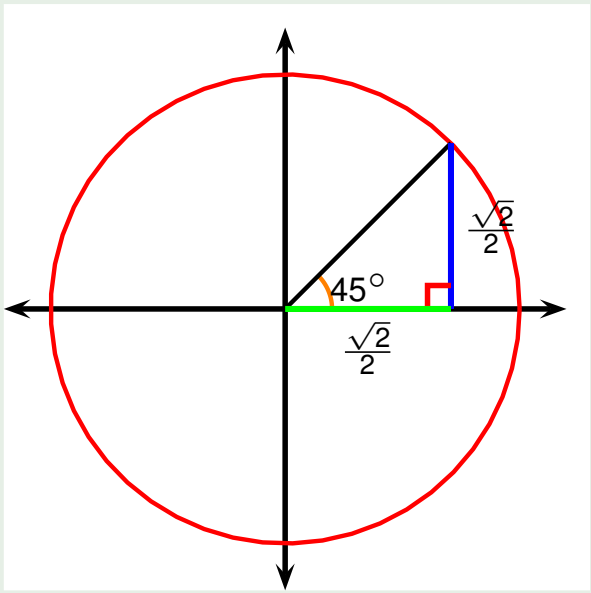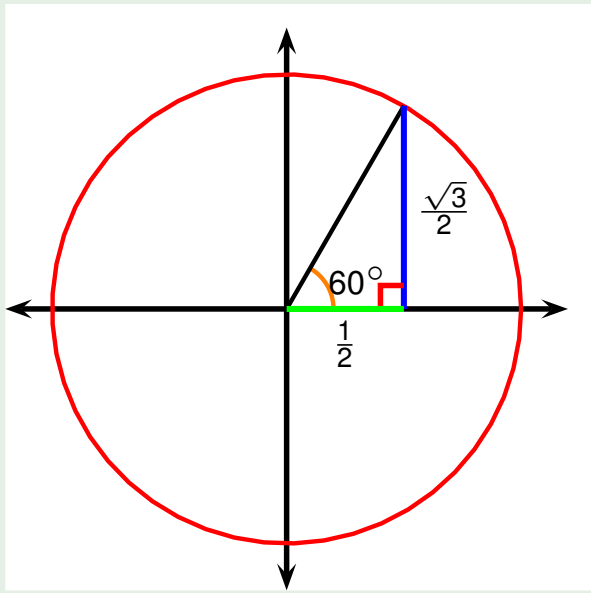
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