Calculus I Homework Trigonometry review

1. Convert from degrees to radians.

(n)
$$305^{\circ}$$
.

(p)
$$30_{\circ}$$
 .

(c)
$$36_{\circ}$$
.

$$\frac{\pi \mathcal{E}}{\hbar}$$

answer: $\frac{61\pi}{36} \approx 5.323254$

Suswer: $\frac{3}{20\pi}$

BEAMEL:
$$rac{\pi}{2}pprox 0.628318531$$

(j)
$$150^{\circ}$$
.

(p)
$$405^{\circ}$$
.

answet: $\frac{2\pi}{3}$

n . ioweiin

answet: $\frac{5\pi}{4}$

answer:
$$\frac{\pi}{4} pprox 0.785398163$$

answer:
$$\frac{5\pi}{6}$$

(d) 45° .

$$(r) -900^{\circ}.$$

answer: $\frac{\pi}{8} \approx 1.047197551$

(m)
$$270^{\circ}$$
.

(s)
$$-2014^{\circ}$$
.

(g) 90°.

(III) 210 s

answer: $\frac{3\pi}{2}$

2. Convert from radians to degrees. The answer key has not been proofread, use with caution.

answer: 2

(a) 4π .

(d) $\frac{4}{3}\pi$.

(g) 5.

(b) $-\frac{7}{6}\pi$.

3 suswer: 720°

answer: 240°

Survice: $\left(\frac{\pi}{600}\right)^{\circ} \approx 580^{\circ}$

189031.38- $\approx \pi \frac{7001}{09}$ - :150931

(b) $-\frac{1}{6}\pi$

(e) $-\frac{3}{8}\pi$.

(h) -2014.

(c) $\frac{7}{12}\pi$.

- (f) 2014π .
- answer: G. \ O Towers

answer: 362520°

answer: -3625200

answer: 105°

(a)
$$\sin \theta \cot \theta = \cos \theta$$
.

3. Prove the trigonometry identities.

(b)
$$(\sin \theta + \cos \theta)^2 = 1 + \sin(2\theta)$$
.

(c)
$$\sec \theta - \cos \theta = \tan \theta \sin \theta$$
.

(d)
$$\tan^2 \theta - \sin^2 \theta = \tan^2 \theta \sin^2 \theta$$
.

(e)
$$\cot^2 \theta + \sec^2 \theta = \tan^2 \theta + \csc^2 \theta$$
.

(f)
$$2\csc(2\theta) = \sec\theta\csc\theta$$
.

(g)
$$\tan(2\theta) = \frac{2\tan\theta}{1-\tan^2\theta}$$
.

(h)
$$\frac{1}{1-\sin\theta} + \frac{1}{1+\sin\theta} = 2\sec^2\theta.$$

(i)
$$\tan \alpha + \tan \beta = \frac{\sin(\alpha + \beta)}{\cos \alpha \cos \beta}$$
.

(j)
$$\tan(\alpha + \beta) = \frac{\tan \alpha + \tan \beta}{1 - \tan \alpha \tan \beta}$$

(k)
$$\sin(3\theta) + \sin \theta = 2\sin(2\theta)\cos \theta$$
.

(1)
$$\cos(3\theta) = 4\cos^3\theta - 3\cos\theta$$
.

(m)
$$1 + \tan^2 \theta = \sec^2 \theta$$
.

(n)
$$1 + \csc^2 \theta = \cot^2 \theta$$
.

(o)
$$2\cos^2(2x) = 2\sin^4\theta + 2\cos^4\theta - \sin^2(2\theta)$$
.

(p)
$$\frac{1 + \tan\left(\frac{\theta}{2}\right)}{1 - \tan\left(\frac{\theta}{2}\right)} = \tan\theta + \sec\theta.$$

4. Find all values of x in the interval $[0, 2\pi]$ that satisfy the equation.

(a)
$$2\cos x - 1 = 0$$
.
 $\frac{\varepsilon}{\mu G} = x$ so $\frac{\varepsilon}{\mu} = x$ signstif

(b)
$$\sin(2x) = \cos x$$
.
$$\frac{9}{2} = x \cdot 10^{\circ} \cdot \frac{9}{2} = x \cdot \frac{7}{2} = x \cdot \frac{7}{2} = x \cdot 10 \text{ assure}$$

(c)
$$\sqrt{3}\sin x = \sin(2x)$$
.

(d)
$$2\sin^2x=1$$
.
$$\frac{v}{wL}=x \text{ 10}, \frac{v}{wG}=x \cdot \frac{v}{w}=x \cdot \frac{v}{w}=x \text{ 120MSUR}$$

(e)
$$2+\cos(2x)=3\cos x$$
.
$$\frac{\varepsilon}{\frac{\pi}{2}}=x \text{ 10} \cdot \frac{\varepsilon}{\underline{\pi}}=x \cdot \underline{\pi}z=x \cdot 0=x \text{ Jansure}$$

(f)
$$2\cos x + \sin(2x) = 0$$
.

answer:
$$x = \frac{\pi}{2}$$
, $x = \frac{3\pi}{2}$

$$(\mathbf{g}) \ \ 2\cos^2 x - \left(1+\sqrt{2}\right)\cos x + \frac{\sqrt{2}}{2} = 0.$$

$$\frac{\frac{\mathfrak{p}}{ML} \cdot \frac{\mathfrak{E}}{MQ} \cdot \frac{\mathfrak{E}}{M} \cdot \frac{\mathfrak{E}}{M}}{2} \cdot \frac{\mathfrak{E}}{M} \cdot \frac{\mathfrak{p}}{M} = x \text{ idensite}}{2}.$$

$$\max_{x \in \mathcal{X}, \pi, 0, \frac{\pi}{\delta}} \frac{1}{\delta} \cdot \frac{\pi}{\delta} = x \text{ (b) } \left| \tan x \right| = 1.$$

$$\frac{\pi}{\delta} \cdot \pi \cdot 0, \frac{\pi}{\delta} = x \cdot \frac{\pi}{$$

(i)
$$3\cot^2 x = 1$$
.
$$\frac{\mathcal{E}}{\mathcal{E}\mathcal{E}} = x \cdot \frac{\mathcal{E}}{\mathcal{E}\mathcal{E}} = x \cdot \frac{\mathcal{E}}{\mathcal{E}} = x$$

(j)
$$\sin x = \tan x$$
.
 $\mu_{\zeta} = x \text{ 10} \cdot \mu = x \cdot_{0} = x \text{ :lowsup}$

Solution. 4.g Set $\cos x = u$. Then

$$2\cos^2 x - (1+\sqrt{2})\cos x + \frac{\sqrt{2}}{2} = 0$$

becomes

$$2u^2 - (1 + \sqrt{2})u + \frac{\sqrt{2}}{2} = 0.$$

This is a quadratic equation in u and therefore has solutions

$$u_{1}, u_{2} = \frac{1 + \sqrt{2} \pm \sqrt{(1 + \sqrt{2})^{2} - 4\sqrt{2}}}{4}$$

$$= \frac{1 + \sqrt{2} \pm \sqrt{1 - 2\sqrt{2} + 2}}{4}$$

$$= \frac{1 + \sqrt{2} \pm \sqrt{(1 - \sqrt{2})^{2}}}{4}$$

$$= \frac{1 + \sqrt{2} \pm (1 - \sqrt{2})}{4} = \begin{cases} \frac{1}{2} & \text{or} \\ \frac{\sqrt{2}}{2} \end{cases}$$

Therefore $u = \cos x = \frac{1}{2}$ or $u = \cos x = \frac{\sqrt{2}}{2}$, and, as x is in the interval $[0, 2\pi]$, we get $x = \frac{\pi}{3}, \frac{5\pi}{3}$ (for $\cos x = \frac{1}{2}$) or $x = \frac{\pi}{4}, \frac{7\pi}{4}$ (for $\cos x = \frac{\sqrt{2}}{2}$).