Precalculus
The inequality $b \geq \sin\theta \geq a$

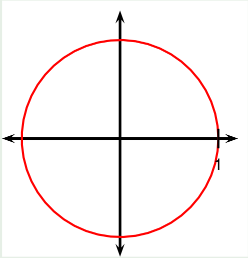
Todor Milev

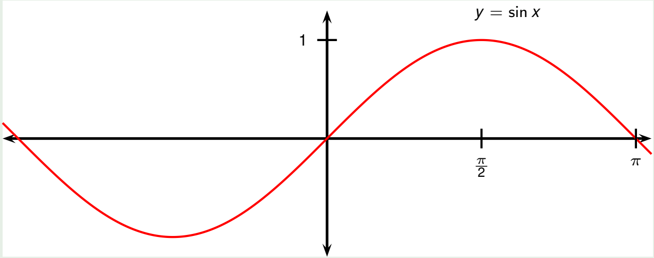
2019

Example

Solve. Among your solutions, find those between -360° and 450°.

$\frac{1}{2} \leq \sin\theta < \frac{\sqrt{3}}{2}$





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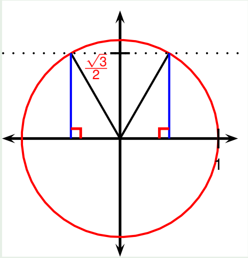

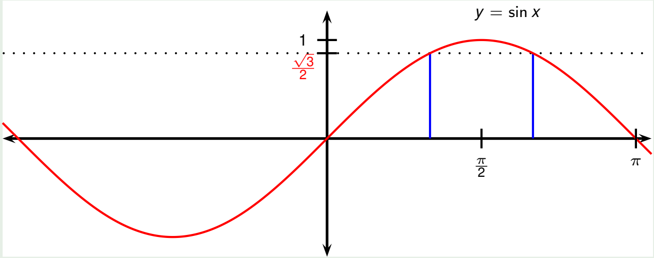

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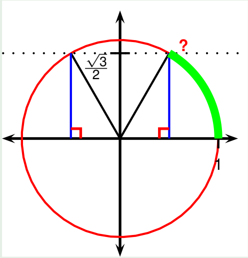

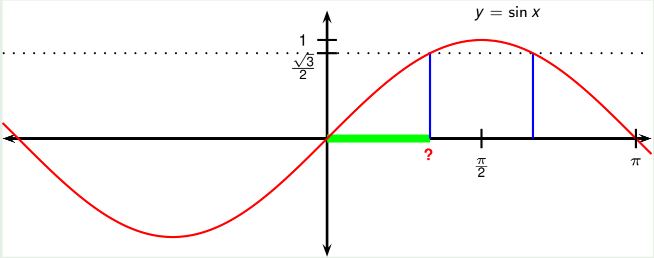

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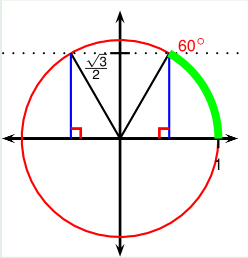

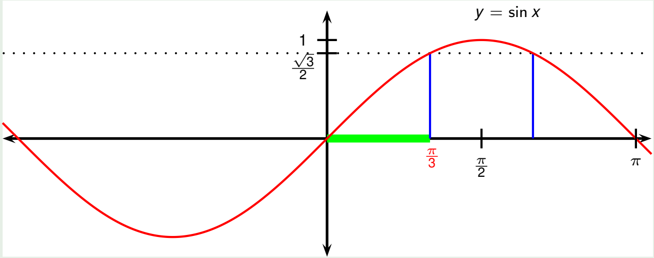

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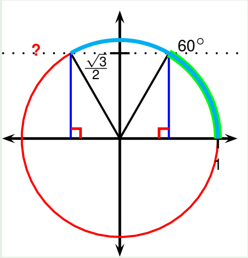

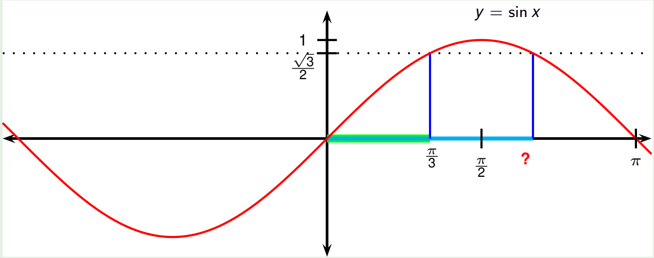

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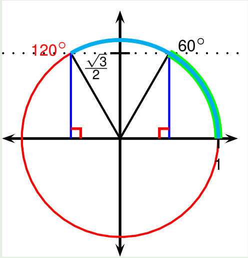

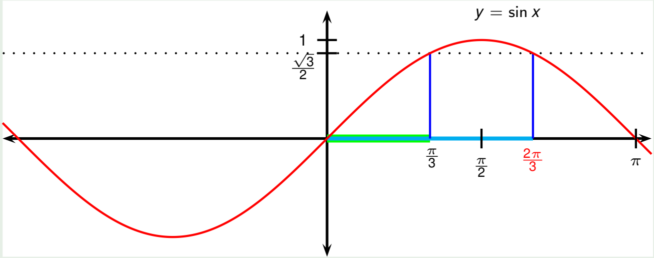

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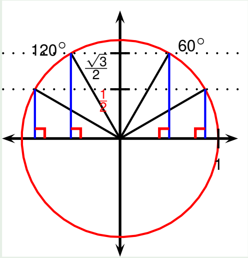

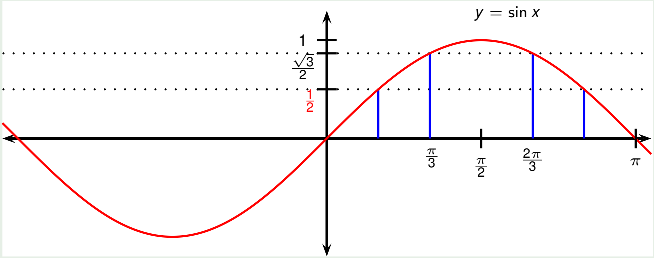

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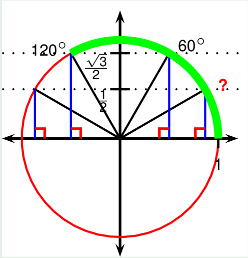

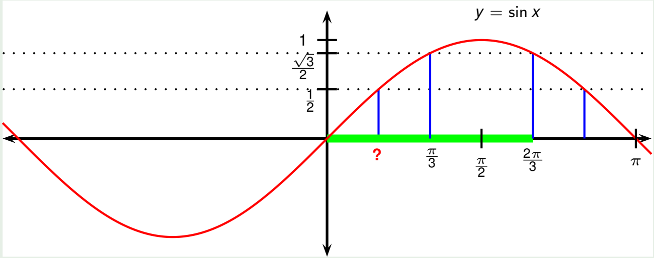

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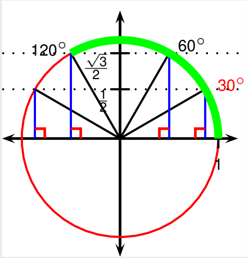

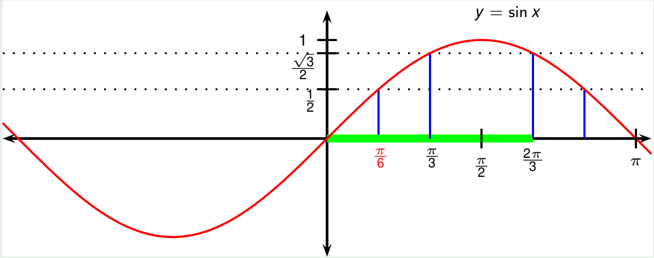

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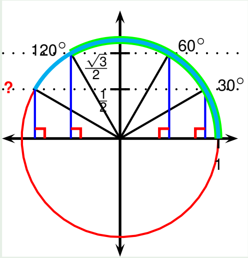

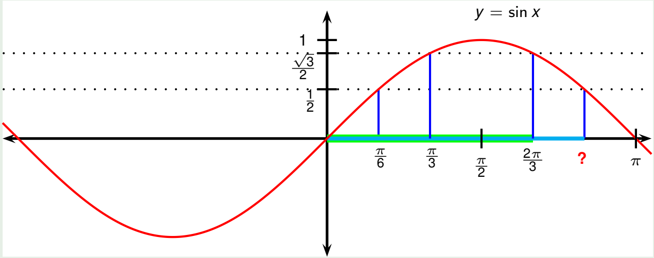

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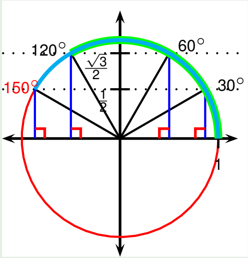

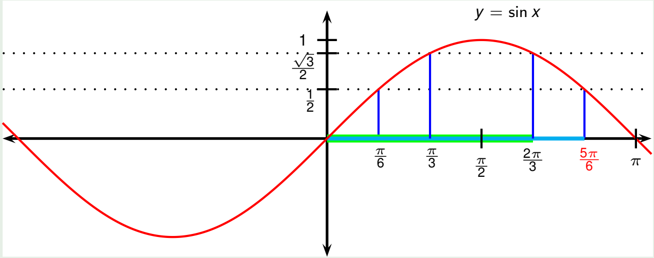

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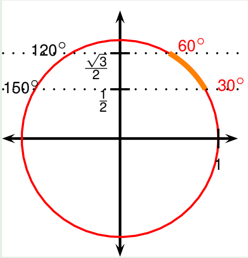

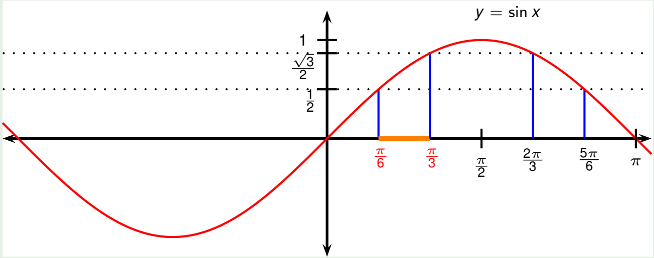

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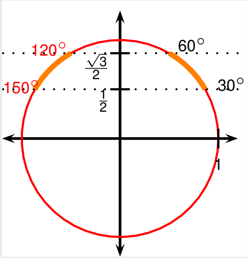

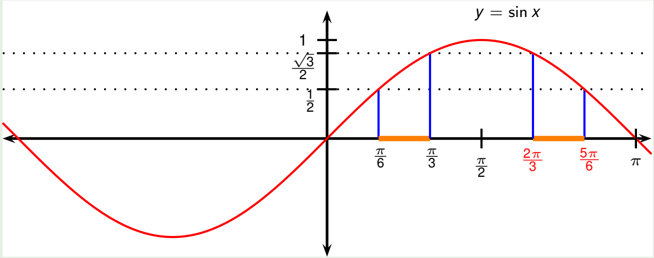

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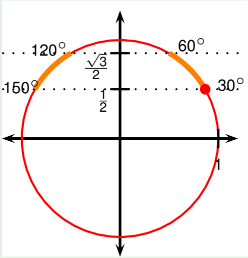

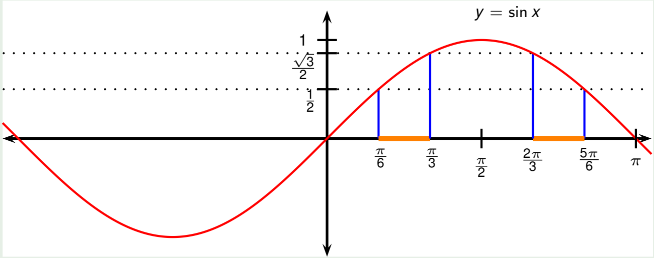

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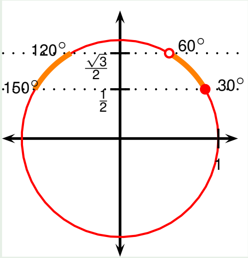

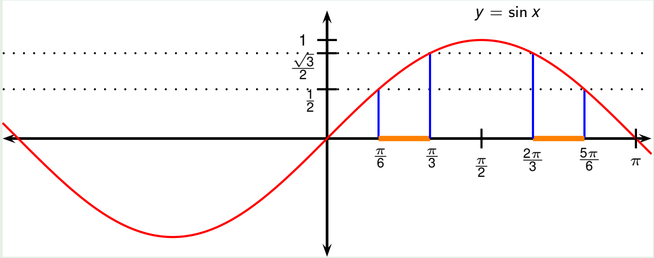

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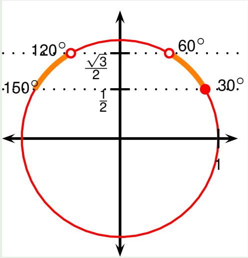

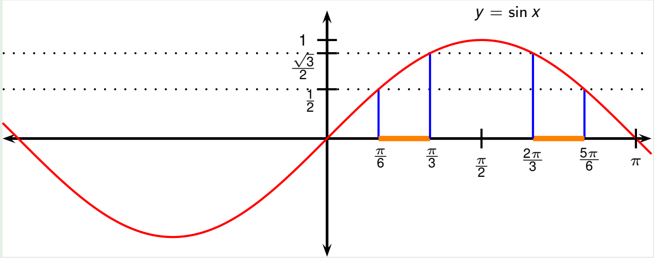

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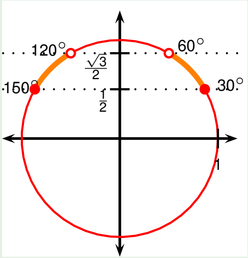

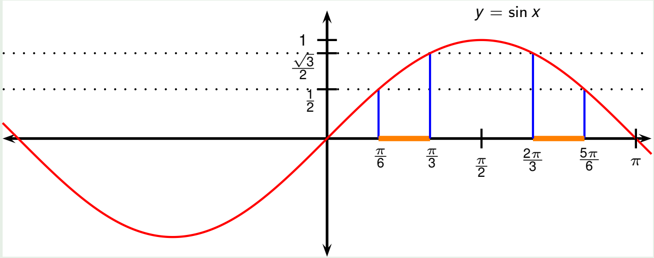

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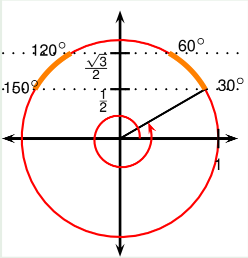

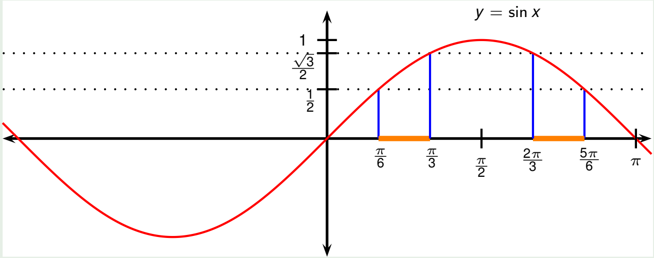

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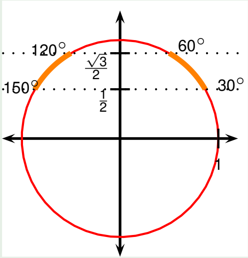

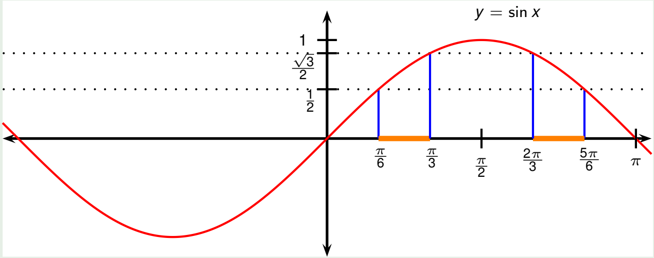

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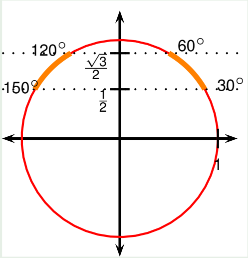

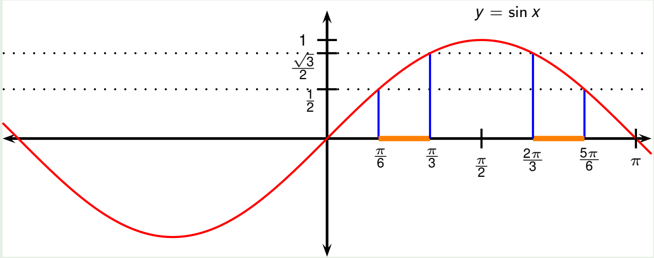

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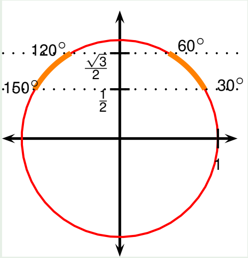

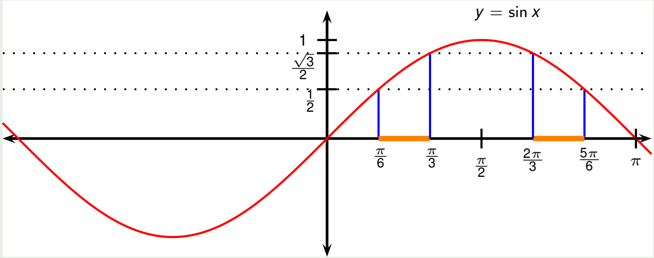

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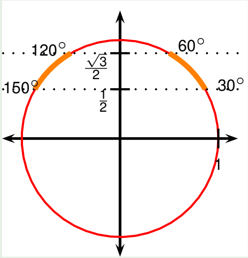

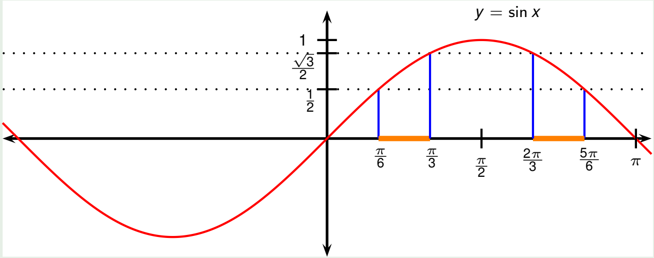

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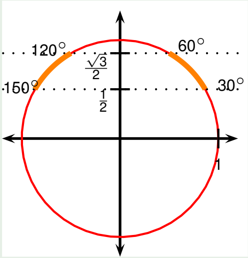

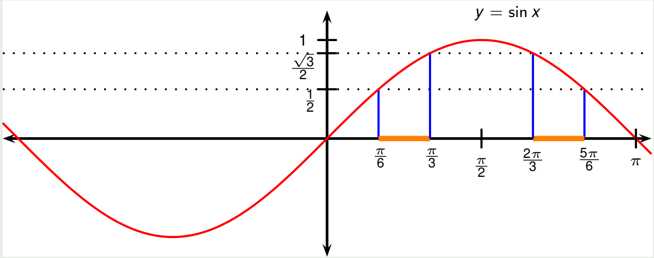

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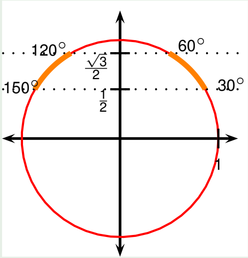

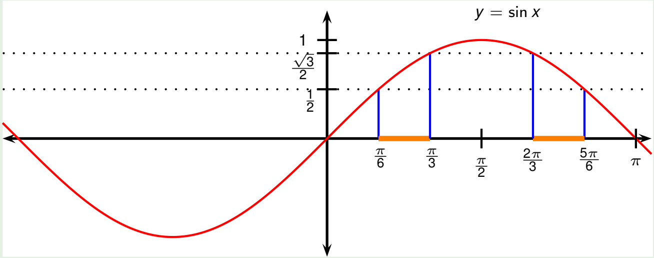

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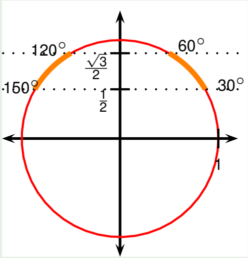

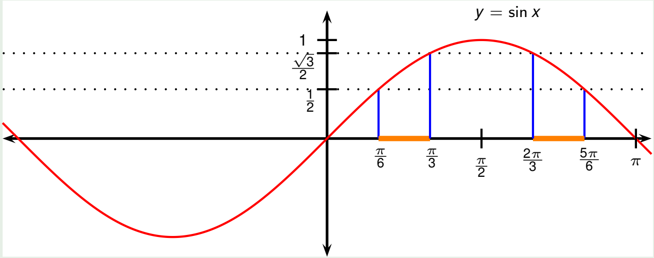

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In radians:

$x \in \left[-\frac{11\pi}{6}, -\frac{5\pi}{3}\right) \cup \left[-\frac{4\pi}{3}, -\frac{7\pi}{6}\right) \cup \left[\frac{\pi}{6}, \frac{\pi}{3}\right) \cup \left[\frac{2\pi}{3}, \frac{5\pi}{6}\right) \cup \left[\frac{13\pi}{6}, \frac{7\pi}{3}\right)$