Calculus II

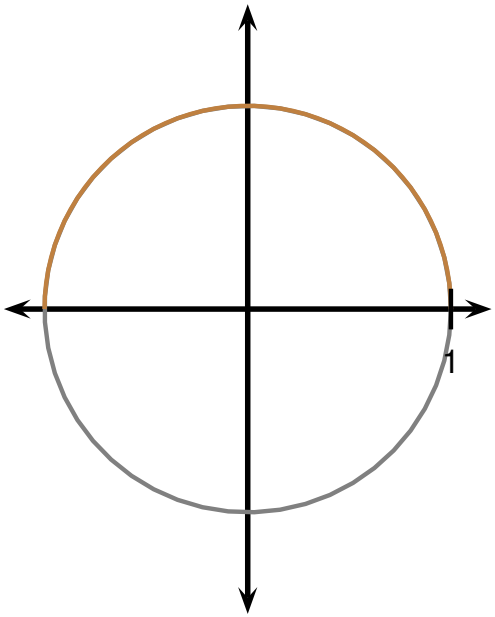
Simplify $\arccos(\cos(x))$

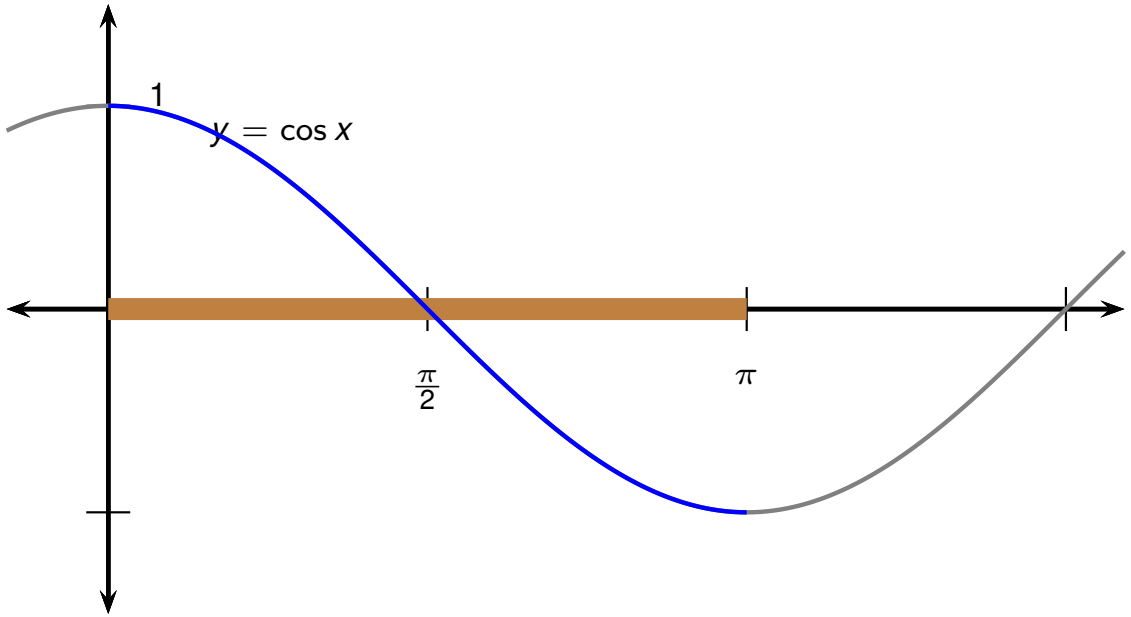
Todor Milev

2019

Example

Find $\arccos(\cos 4)$.





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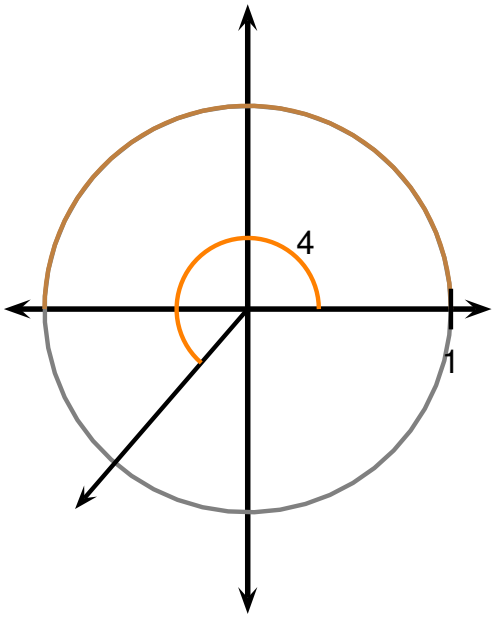
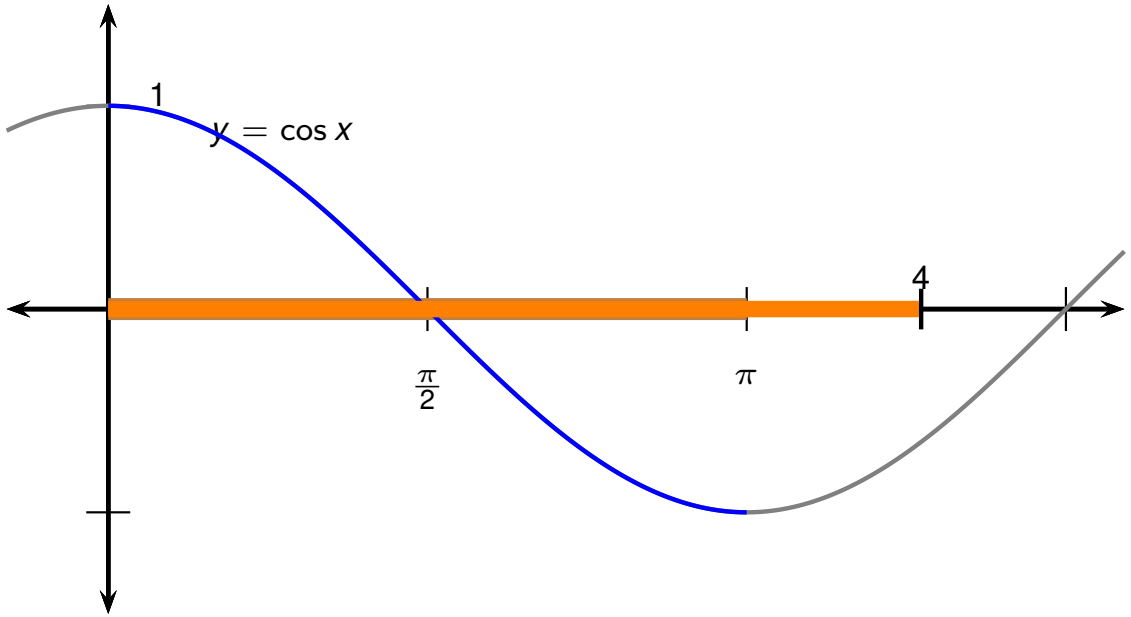
- 4 is not between 0 and π.





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- 4 is not between 0 and π.
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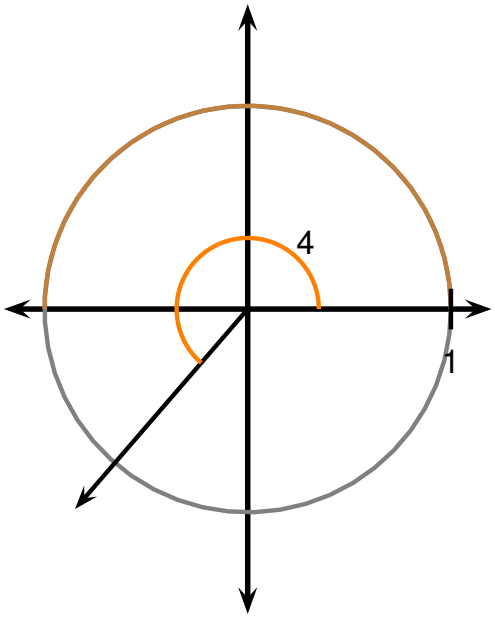

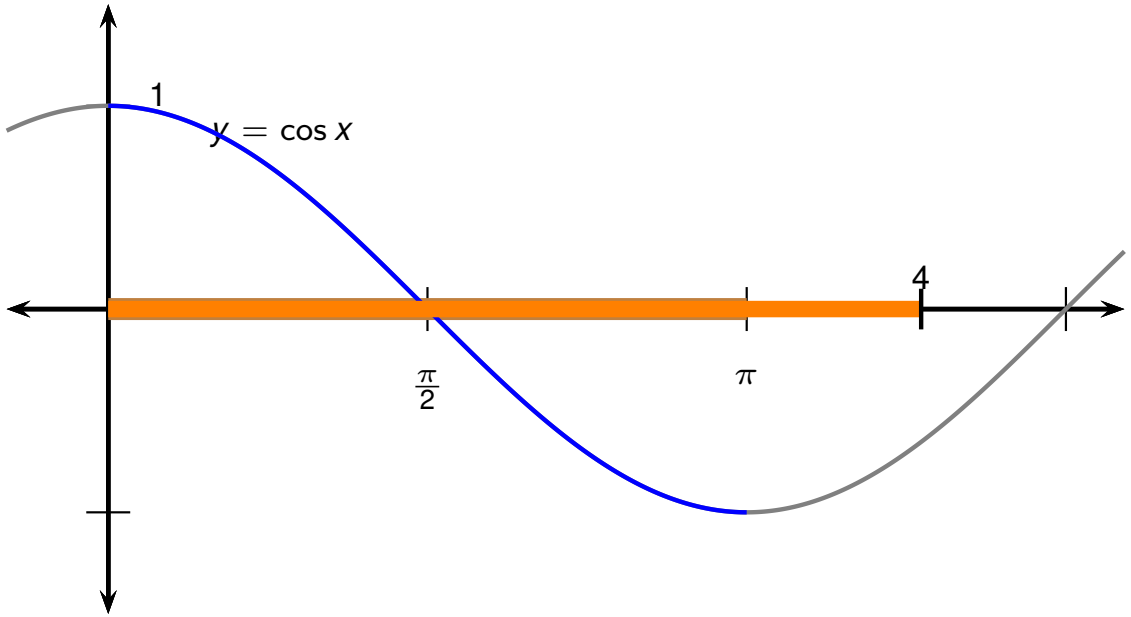

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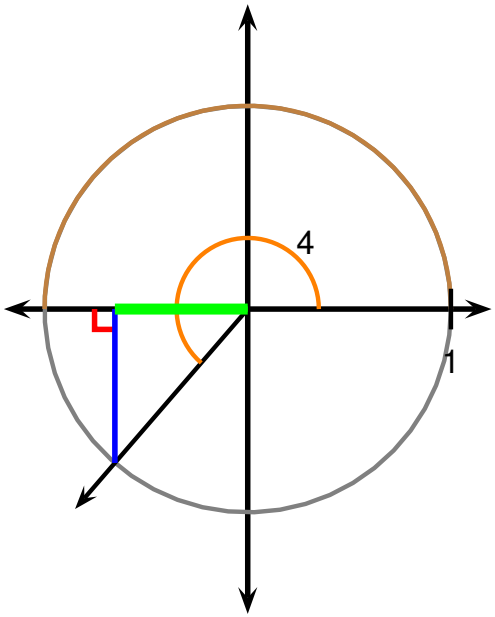

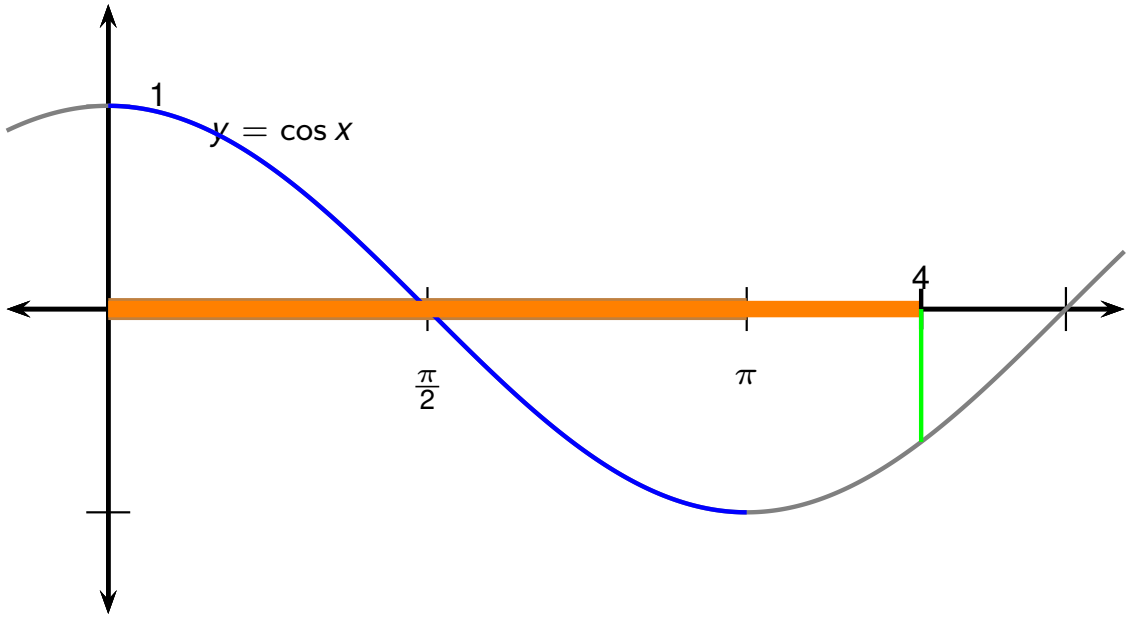

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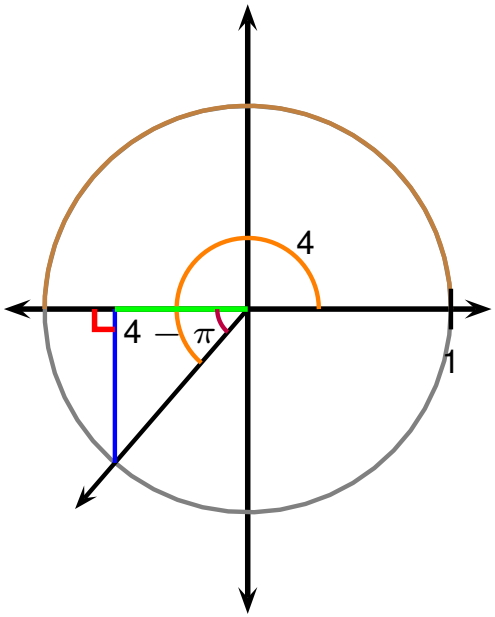

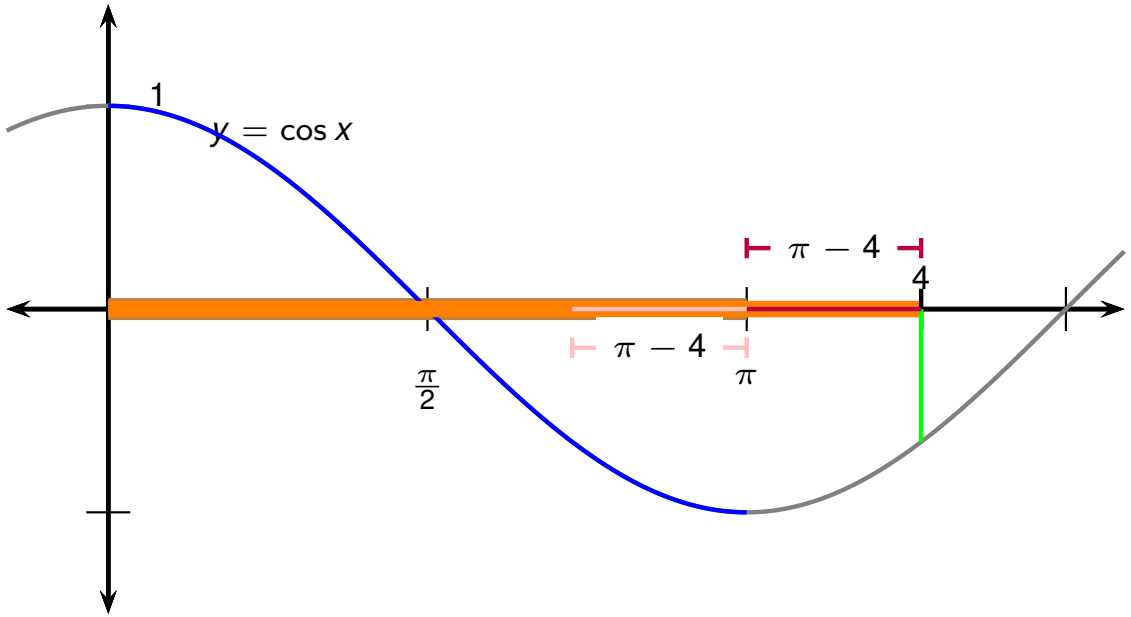

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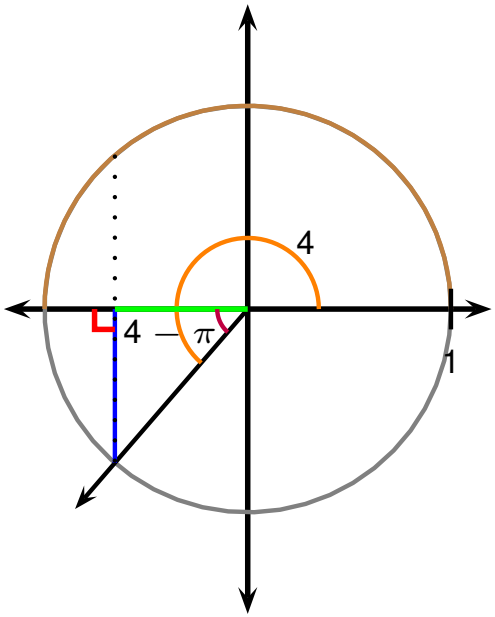

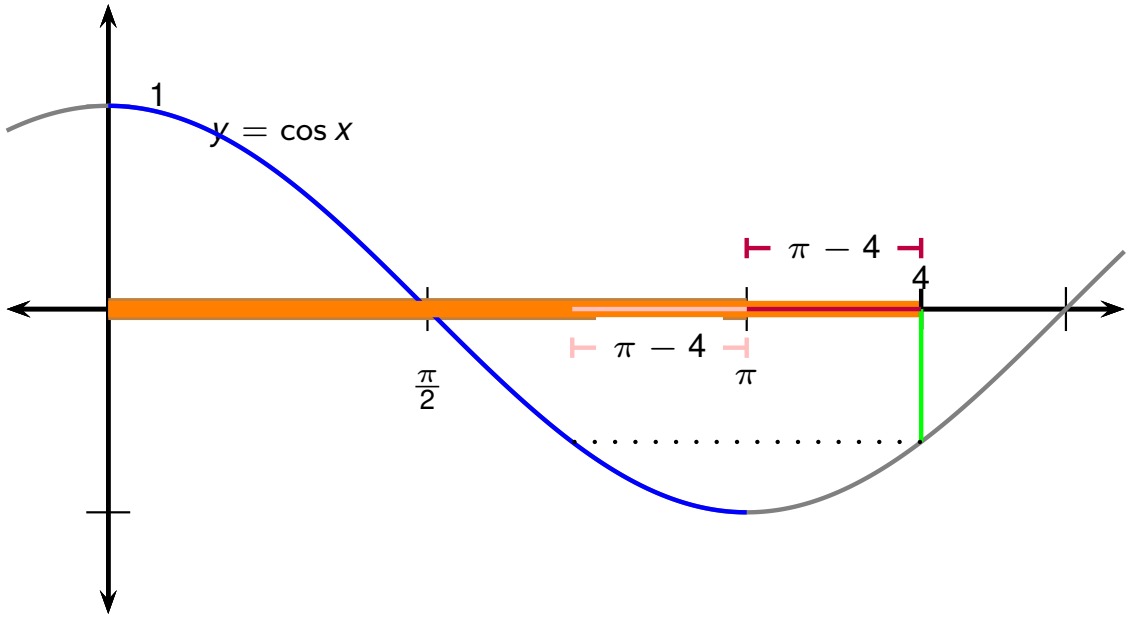

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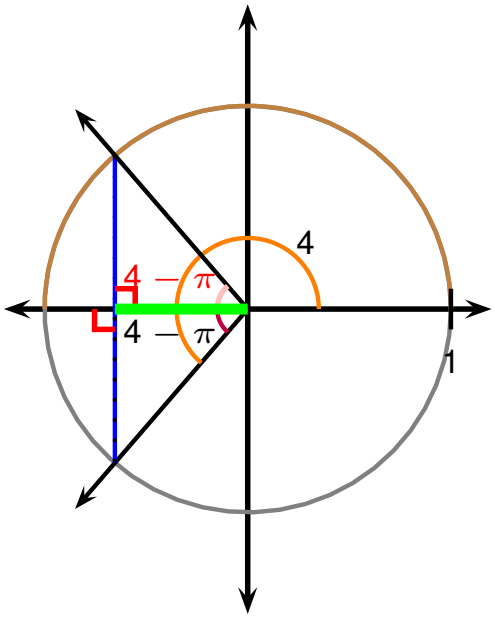

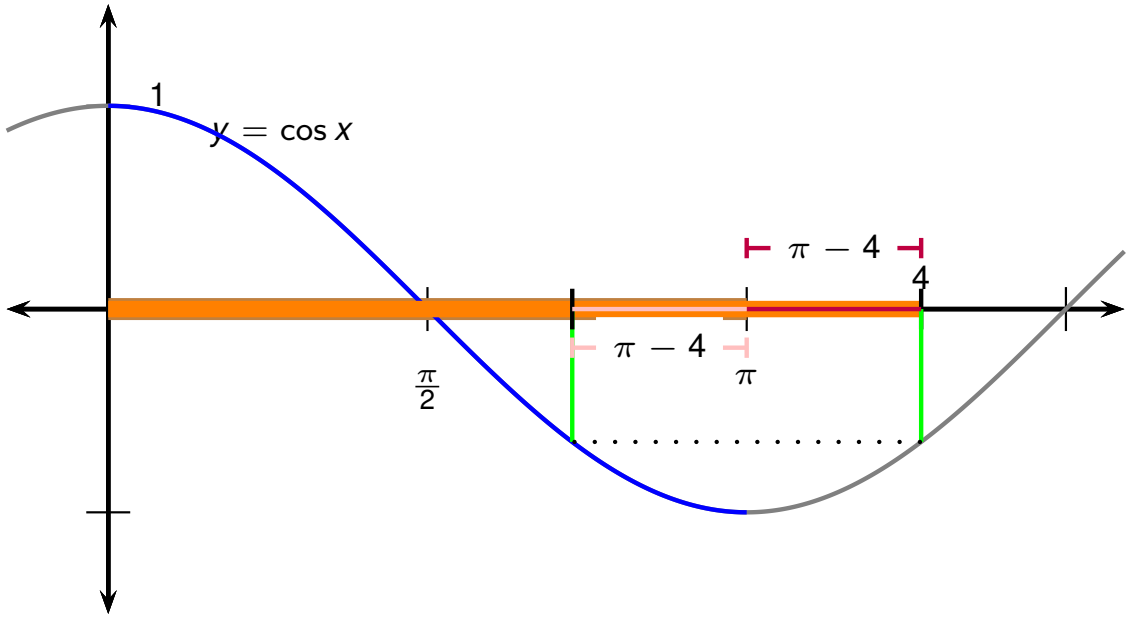

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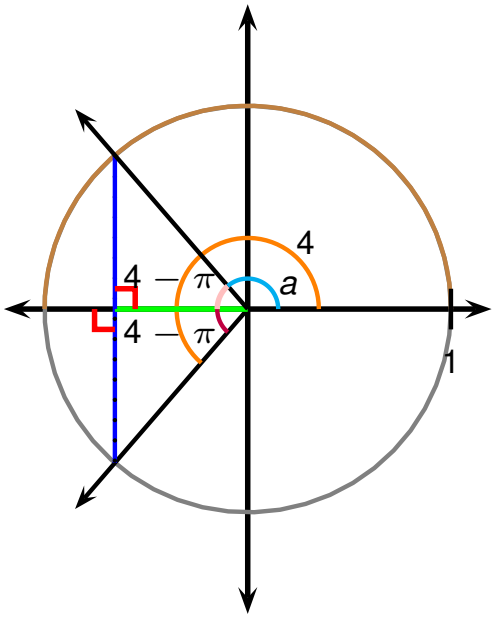

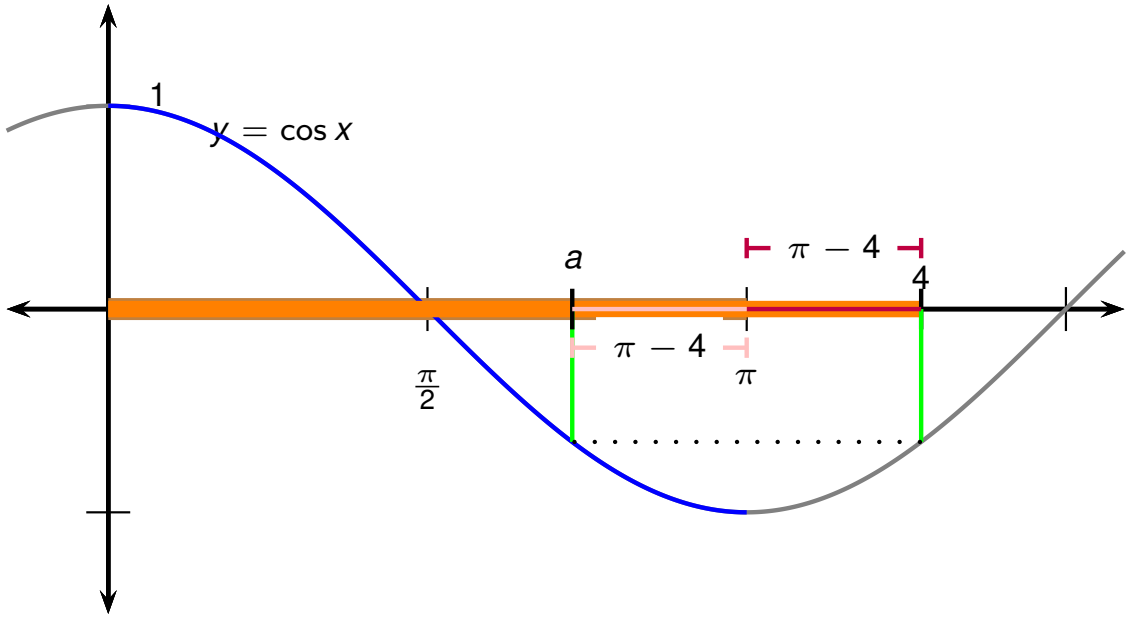

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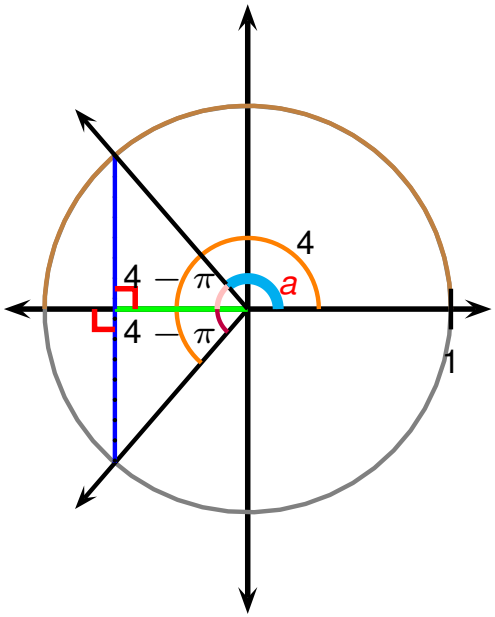
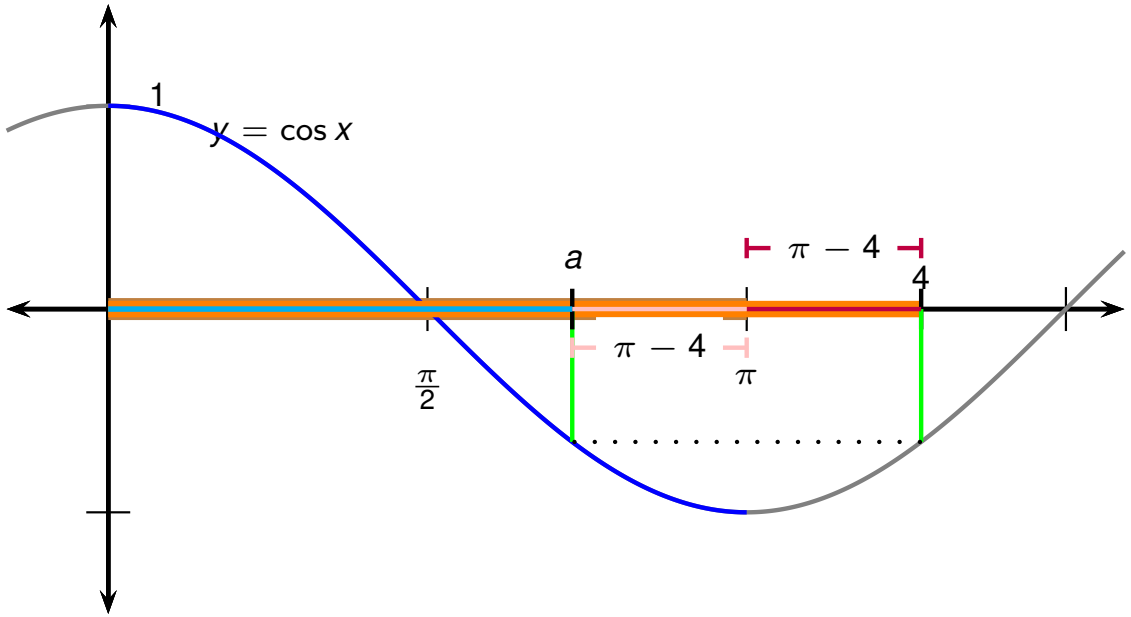
$$a = \ ?$$





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Find $\arccos(\cos 4)$.

- 4 is not between 0 and π.
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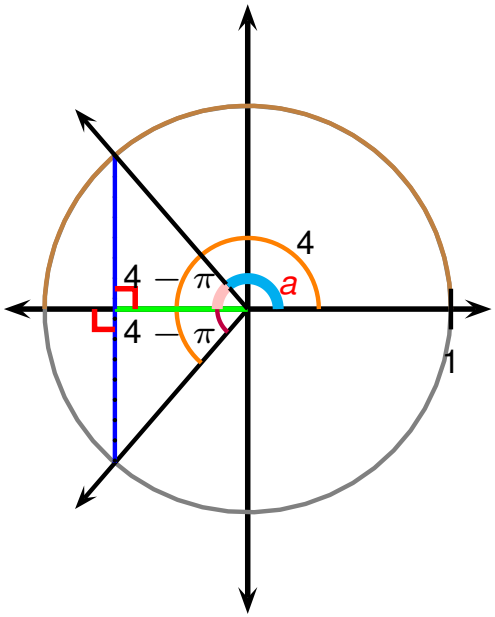
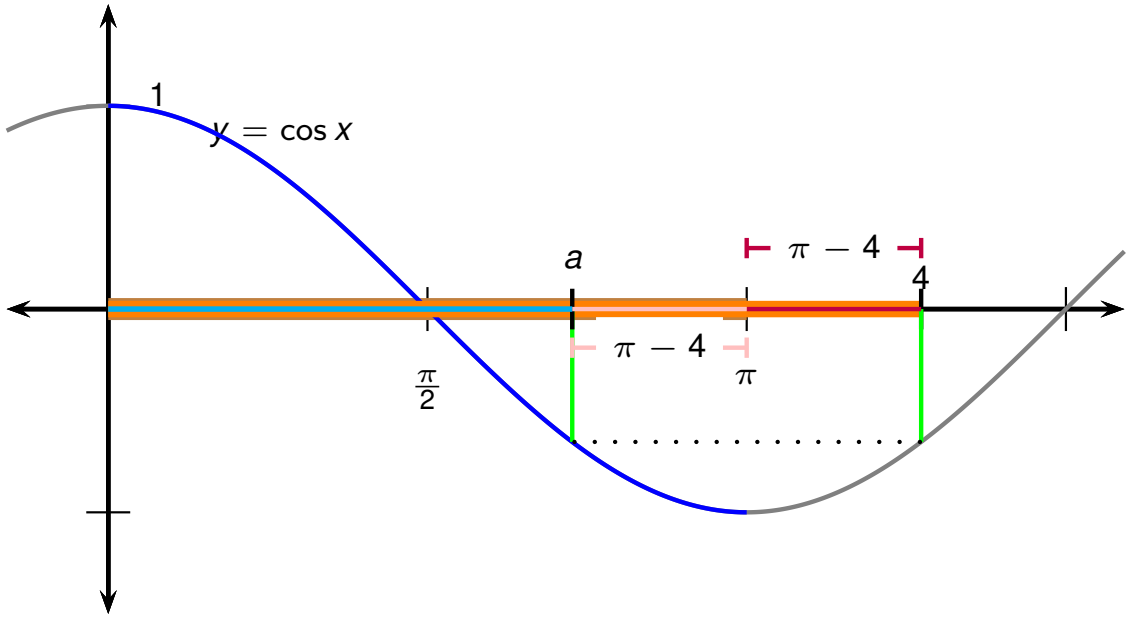
$$a = \pi - (4 - \pi)$$





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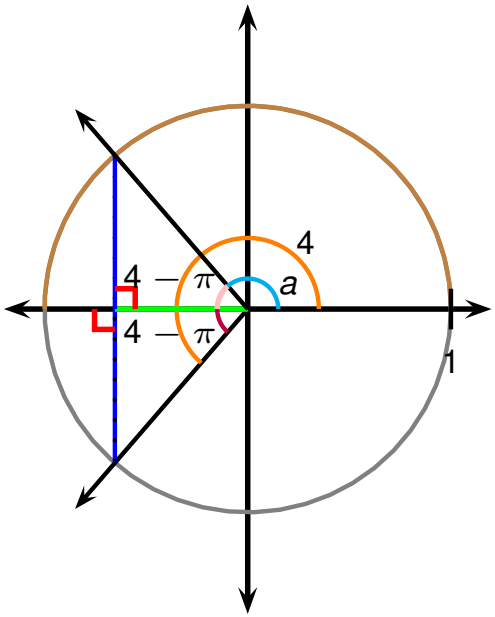
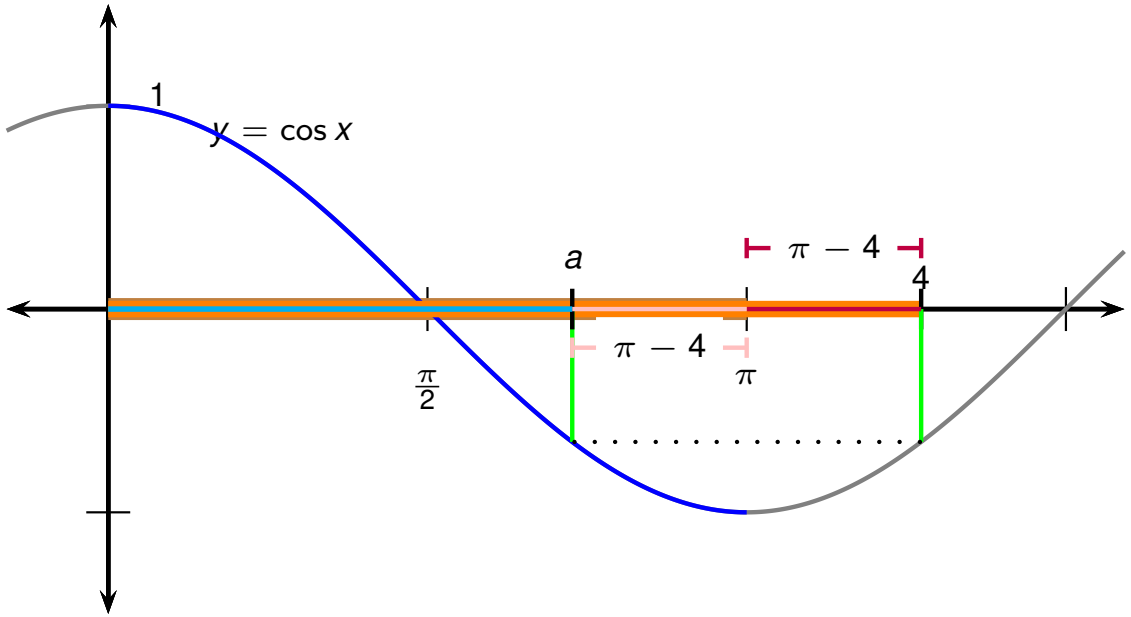
$$a = \pi - (4 - \pi) = 2\pi - 4$$





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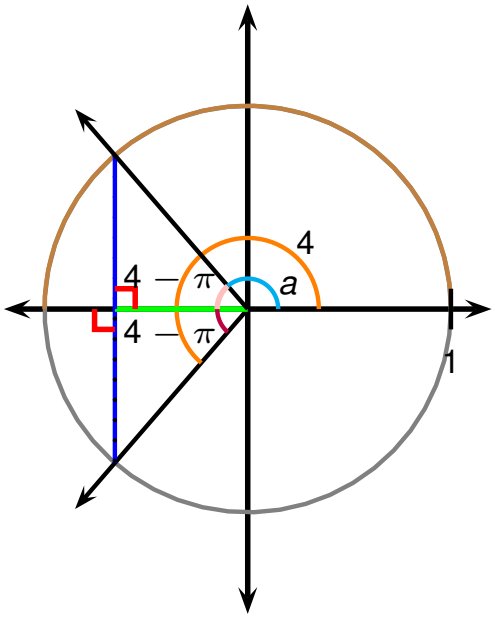

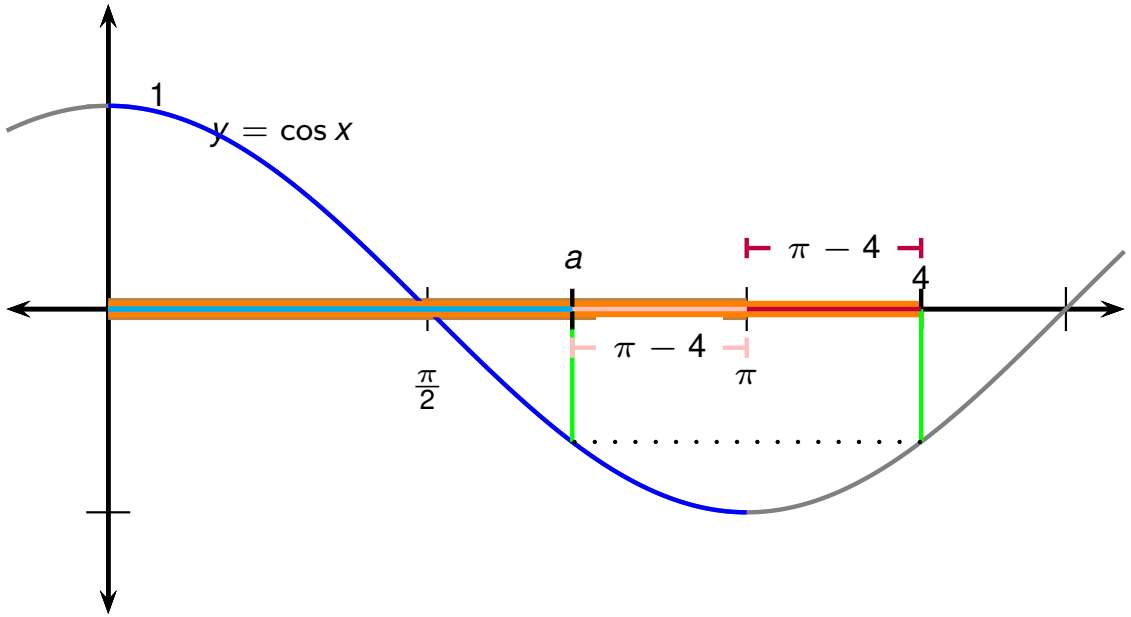

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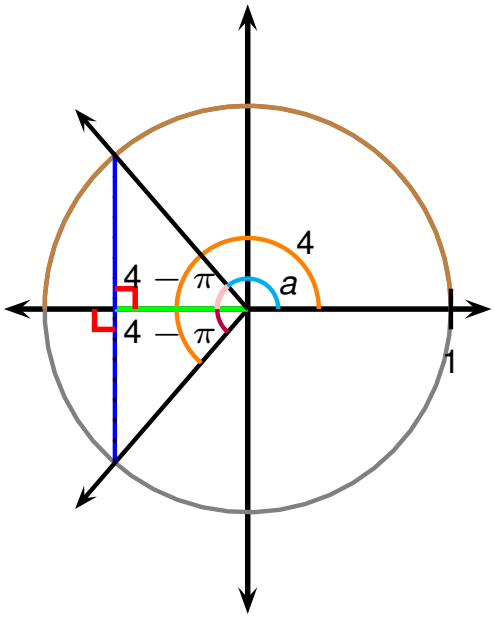

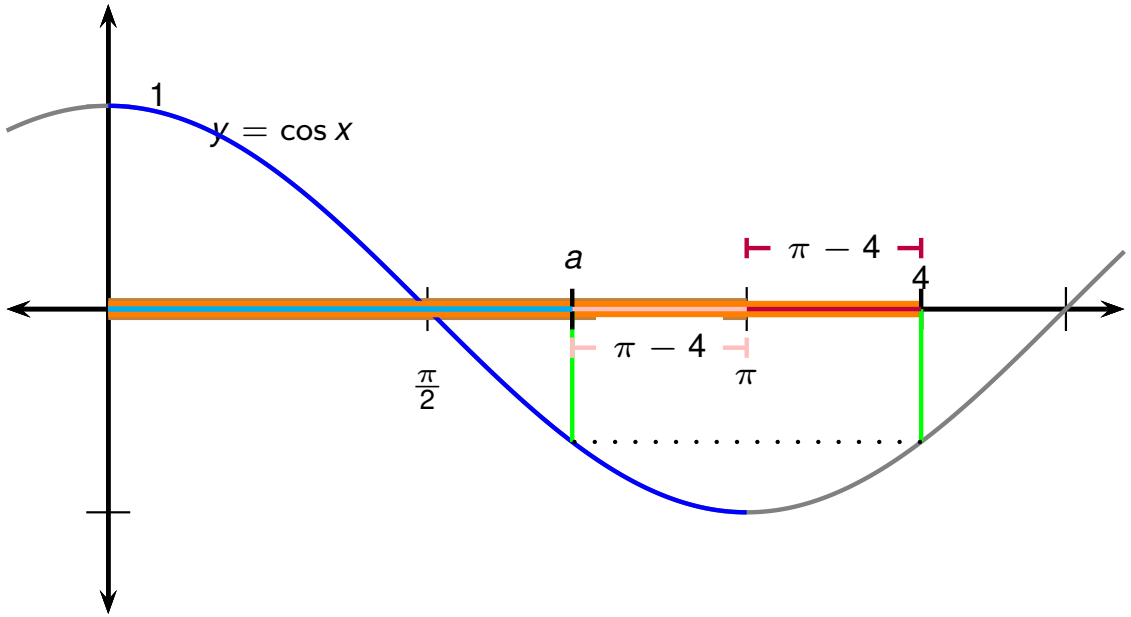

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