Calculus I

§ Definite integral of $\frac{1}{(ax+b)^n}$

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2019

Find
$$\int_1^2 \frac{\mathrm{d}x}{(2-3x)^2}.$$

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- Then du = ?

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