

## Precalculus

# Exponent equation that reduces to quadratic, natural base

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Solve the equation

$$e^{2x} - 3e^x - 4 = 0$$

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Set  $e^x = u$ . Then  $e^{2x} = ?$  .

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$$(\text{?} \quad ) (\text{?} \quad ) = 0$$

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$$x \approx 1.3863$$