Precalculus
Exponent equation that reduces to quadratic, natural base

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Solve the equation

$$e^{2x} - 3e^{x} - 4 = 0$$

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Set $e^{x} = u$.

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Set $e^{x} = u$. Then $e^{2x} =$ **?** .

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$x \approx 1.3863$		