Precalculus
Basic exponent equation of type $c^{px+q} = Ad^{rx+s}$

Todor Milev

2019

Example

Solve.
$$3^{2x+5} = 5 \cdot 2^{-x+1}$$

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$$\left(2^{\log_2 3}\right)^{2x+5} = 5 \cdot 2^{-x+1}$$

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$$x \approx -1.1038 \qquad \text{Calculator}$$