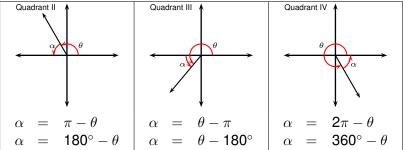
## **Precalculus**

# Compute the trigonometric functions of an angle not in the first quadrant

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The computation of the reference angle  $\alpha$  depends on the quadrant.

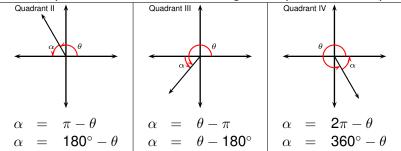


To compute trigonometric functions from obtuse ( $> 90^{\circ}$ ) or negative angles, we can use the following visual aid.

# Definition (Reference Angle)

Let  $\theta$  be an angle in standard position. Its reference angle is the acute positive angle formed by the terminal arm and the x axis.

The computation of the reference angle  $\alpha$  depends on the quadrant.

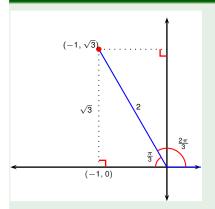


#### Observation

One can find the value of a trigonometric function of  $\theta$  as follows.

- Find the reference angle  $\alpha$  associated to  $\theta$ .
- Find the trig function of  $\alpha$ .
- Use the quadrant in which  $\theta$  lies to affix an appropriate sign to the function value.

## Example



Find the exact values of the trigonometric functions of  $\theta = \frac{2\pi}{3} = 120^{\circ}$ .

$$\sin\left(\frac{2\pi}{3}\right) = \frac{\sqrt{3}}{2} \quad \cos\left(\frac{2\pi}{3}\right) = -\frac{1}{2} \quad \tan\left(\frac{2\pi}{3}\right) = \frac{\sqrt{3}}{-1} = -\sqrt{3}$$

$$\csc\left(\frac{2\pi}{3}\right) = \frac{2}{\sqrt{3}} \quad \sec\left(\frac{2\pi}{3}\right) = -\frac{2}{1} = -2 \quad \cot\left(\frac{2\pi}{3}\right) = -\frac{1}{\sqrt{3}}$$