Calculus I

§ Definite integral of $\frac{1}{(ax+b)^n}$

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Example

Find
$$\int_{1}^{2} \frac{dx}{(2-3x)^2}$$
.

- Let u = 2 3x.
- Then du = -3 dx.
- Therefore $dx = -\frac{1}{3}du$.
- When x = 1, u = -1.
- When x = 2, u = -4.

$$\int_{x=1}^{x=2} \frac{dx}{(2-3x)^2} = -\frac{1}{3} \int_{u=-1}^{u=-4} \frac{du}{u^2} = -\frac{1}{3} \int_{-1}^{-4} u^{-2} du$$
$$= -\frac{1}{3} \cdot \left[-\frac{1}{u} \right]_{-1}^{-4} = \frac{1}{3} \left[\frac{1}{u} \right]_{-1}^{-4}$$
$$= \frac{1}{3} \left(\frac{1}{-4} - \frac{1}{-1} \right) = \frac{1}{3} \left(1 - \frac{1}{4} \right) = \frac{1}{4}.$$