

Calculus I

Homework

Review of basic functions

1. Evaluate the difference quotient and simplify your answer.

(a) $\frac{f(2+h) - f(2)}{h}$, where $f(x) = x^2 - x - 1$.

(b) $\frac{f(a+h) - f(a)}{h}$, where $f(x) = x^2$.

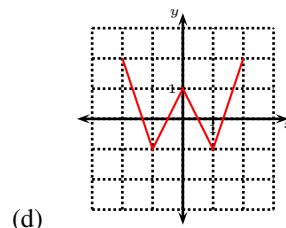
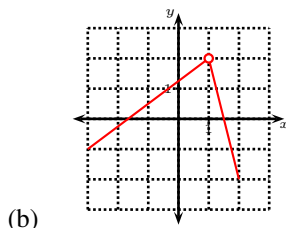
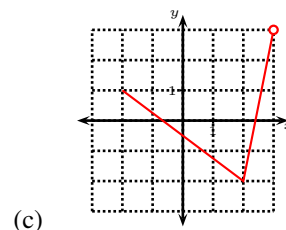
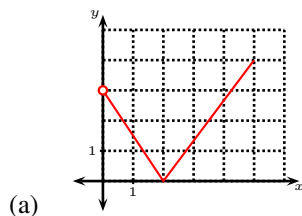
(c) $\frac{f(a+h) - f(a)}{h}$, where $f(x) = x^3$.

(d) $\frac{f(a+h) - f(a)}{h}$, where $f(x) = x^4$.

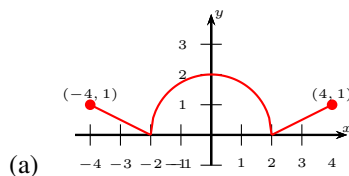
(e) $\frac{f(x) - f(a)}{x - a}$, where $f(x) = \frac{1}{x}$.

(f) $\frac{f(x) - f(1)}{x - 1}$, where $f(x) = \frac{x-1}{x+1}$.

2. Write down a formula for a function whose graphs is given below. The graphs are up to scale. Please note that there is more than one way to write down a correct answer.



3. Write down formulas for function whose graphs are as follows. The graphs are up to scale. All arcs are parts of circles.



4. Evaluate the difference quotient and simplify your answer.

(a) $\frac{f(2+h) - f(2)}{h}$, where $f(x) = x^2 - x - 1$.

(b) $\frac{f(a+h) - f(a)}{h}$, where $f(x) = x^2$.

(c) $\frac{f(a+h) - f(a)}{h}$, where $f(x) = x^3$.

(d) $\frac{f(a+h) - f(a)}{h}$, where $f(x) = x^4$.

(e) $\frac{f(x) - f(a)}{x - a}$, where $f(x) = \frac{1}{x}$.

(f) $\frac{f(x) - f(1)}{x - 1}$, where $f(x) = \frac{x-1}{x+1}$.

5. Find the implied domain of the function.

(a) $f(x) = \frac{x+4}{x^2-4}$.

(b) $f(x) = \frac{2x^3-5}{x^2+5x+6}$.

(c) $f(t) = \sqrt[3]{3t-1}$.

(d) $g(t) = \sqrt{5-t} - \sqrt{1+t}$.

(e) $h(x) = \frac{1}{\sqrt[6]{x^2-7x}}$.

(f) $f(u) = \frac{u+1}{1+\frac{1}{u+1}}$.

(g) $F(x) = \sqrt{10-\sqrt{x}}$.

6. Find the implied domain of the function.

(a) $f(x) = \frac{x+4}{x^2-4}$.

(b) $f(x) = \frac{2x^3-5}{x^2+5x+6}$.

(c) $f(t) = \sqrt[3]{3t-1}$.

(d) $g(t) = \sqrt{5-t} - \sqrt{1+t}$.

(e) $h(x) = \frac{1}{\sqrt[6]{x^2-7x}}$.

(f) $f(u) = \frac{u+1}{1+\frac{1}{u+1}}$.

(g) $F(x) = \sqrt{10-\sqrt{x}}$.

7. Compute the composite functions $(f \circ g)(x)$, $(g \circ f)(x)$. Simplify your answer to a single fraction. Find the domain of the composite function.

(a) $f(x) = \frac{x+2}{x-2}, g(x) = \frac{x-1}{x+2}$.

(b) $f(x) = \frac{x+1}{3x-2}, g(x) = \frac{x-2}{x-1}$.

(c) $f(x) = \frac{2x+1}{3x-1}, g(x) = \frac{x-2}{2x-1}$.

(d) $f(x) = \frac{x+1}{x-2}, g(x) = \frac{x+2}{2x-1}$.

(e) $f(x) = \frac{5x+1}{4x-1}, g(x) = \frac{4x-1}{3x+1}$.

(f) $f(x) = \frac{3x-5}{x-2}, g(x) = \frac{x-2}{x-4}$.

(g) $f(x) = \frac{x-3}{x+2}, g(y) = \frac{y+3}{y-4}$.

8. Find the functions $f \circ g$, $g \circ f$, $f \circ f$ and $g \circ g$ and their implied domains. The answer key has not been proofread, use with caution.

(a) $f(x) = x^2 + 1, g(x) = x + 1$.

(b) $f(x) = \sqrt{x+1}, g(x) = x + 1$.

(c) $f(x) = 2x, g(x) = \tan x$.

In this subproblem, you are not required to find the domain.

(d) $f(x) = \frac{x+1}{x-1}, g(x) = \frac{x-1}{x+1}$.