

Calculus I

Definite integrals of rational power monomials

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Example

Evaluate: $\int_1^9 \frac{2t^3 + t^2\sqrt{t} - 1}{t^2} dt$

$$\begin{aligned}
 &= \int_1^9 \left(2t + t^{\frac{1}{2}} - t^{-2} \right) dt = \left[\int (2t + t^{\frac{1}{2}} - t^{-2}) dt \right]_1^9 \\
 &= \left[\int 2t dt + \int t^{\frac{1}{2}} dt - \int t^{-2} dt \right]_1^9 \\
 &= \left[t^2 + \frac{t^{\frac{3}{2}}}{\frac{3}{2}} - \frac{t^{-1}}{-1} \right]_1^9 = \left[t^2 + \frac{2}{3} t^{\frac{3}{2}} + \frac{1}{t} \right]_1^9 \\
 &= \left(9^2 + \frac{2}{3} \cdot 9^{\frac{3}{2}} + \frac{1}{9} \right) - \left(1^2 + \frac{2}{3} \cdot 1^{\frac{3}{2}} + \frac{1}{1} \right) \\
 &= 81 + 18 + \frac{1}{9} - 1 - \frac{2}{3} - 1 = \frac{868}{9}.
 \end{aligned}$$