Precalculus
Basic exponent equation of type $e^{px+q} = A$

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2019

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Solve the equation.

$$e^{5-3x} = 10$$

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\text{Calculator:}\quad x &\approx 0.8991.
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$$e^{3x-1} = 0$$

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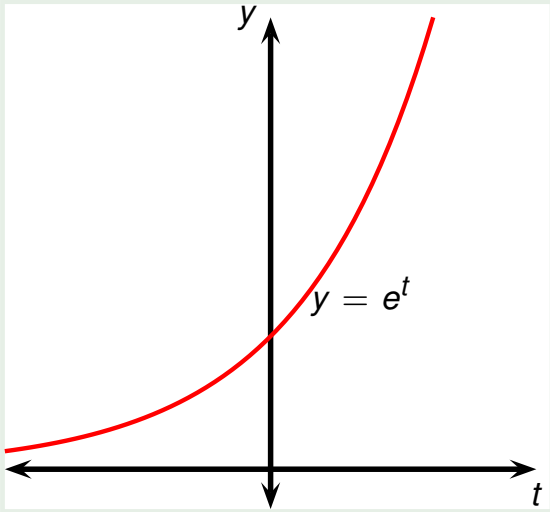

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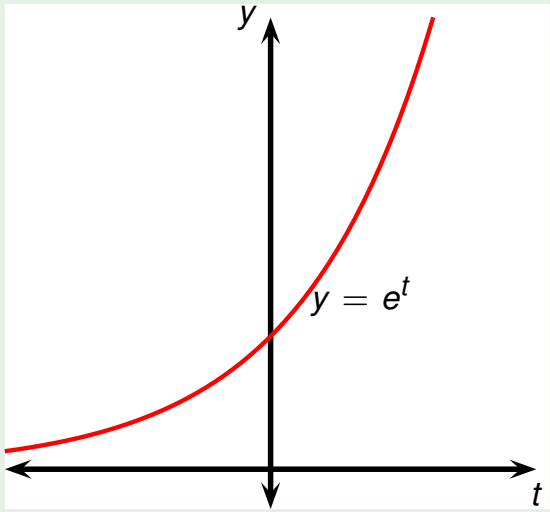

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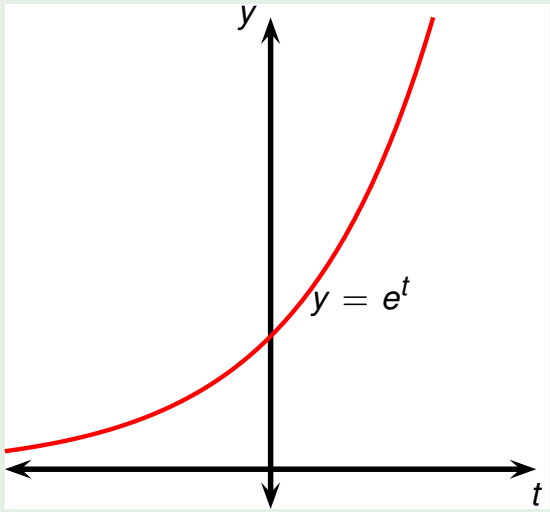

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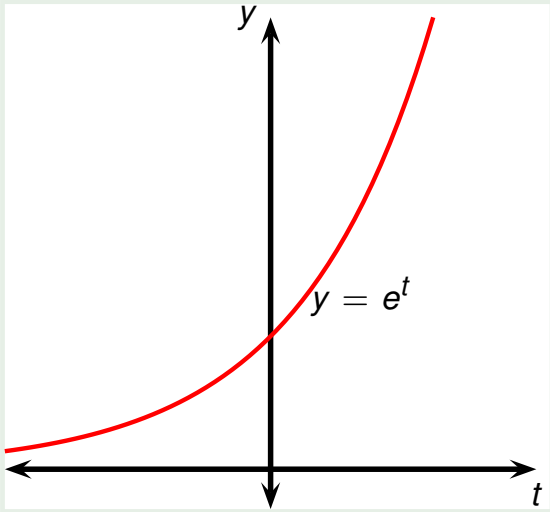

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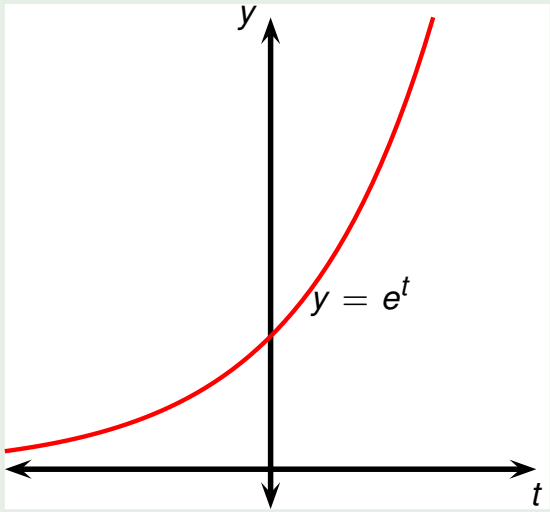

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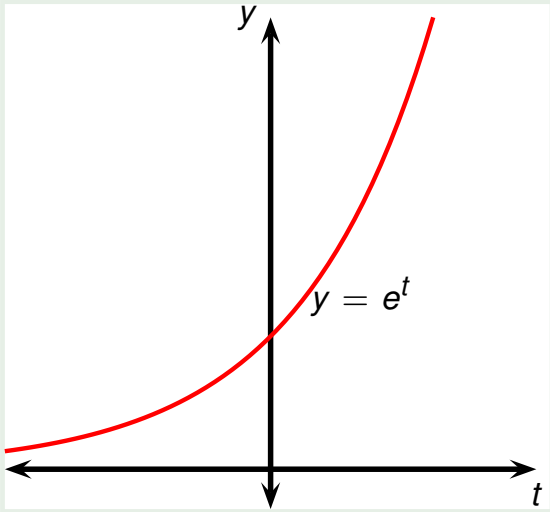

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