2019

Calculus II ax Integrals of the form
$$\int \frac{ax}{(bx^2+c)^n} dx$$

Todor Milev

2019

Building blocks IIa and IIb

We solve building block IIb. For completeness, we solve block IIa again as well.

Example

$$\int \frac{x}{(x^2+1)^n} dx = \int \frac{1}{(x^2+1)^n} \frac{d(x^2+1)}{2}$$

$$= \frac{1}{2} \int u^{-n} du$$

$$= \begin{cases} \frac{1}{2} \ln(x^2+1) + C & \text{if } n=1\\ \frac{1}{2} \frac{(x^2+1)^{-n+1}}{(-n+1)} + C & \text{if } n \neq 1 \end{cases},$$

where we used the substitution $u = x^2 + 1$.