

Calculus II

Convergence of sequences from limits of rational functions

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 &= \frac{1}{1 + 0}
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 &= \frac{1}{1 + 0} \\
 &= 1
 \end{aligned}$$