

Calculus I

Homework Limits involving ∞

Lecture 5

1. Show the following limits do not exist and compute whether they evaluate to ∞ , $-\infty$, or neither.

(a) $\lim_{x \rightarrow 3^+} \frac{x^2 + x - 1}{x^2 - 2x - 3}.$

(c) $\lim_{x \rightarrow 1^+} \frac{x^2 + 1}{\sqrt{x^2 + 3} - 2}.$

(e) $\lim_{x \rightarrow 2^+} \frac{\sqrt{x^3 - 8}}{-x^2 + x + 2}.$

(b) $\lim_{x \rightarrow 3^-} \frac{x^2 + x - 1}{x^2 - 2x - 3}.$

(d) $\lim_{x \rightarrow 1^-} \frac{x^2 + 1}{\sqrt{x^2 + 3} - 2}.$

(f) $\lim_{x \rightarrow -1^+} \frac{\sqrt[3]{x^2 + 2x + 1}}{x^2 - 2x - 3}.$

2. Find the limit or show that it does not exist. If the limit does not exist, indicate whether it is $\pm\infty$, or neither. The answer key has not been proofread, use with caution.

(a) $\lim_{x \rightarrow \infty} \frac{x - 2}{2x + 1}.$

(i) $\lim_{x \rightarrow -\infty} \frac{\sqrt{x^2 + 1}}{x + 1}.$

(r) $\lim_{x \rightarrow \infty} \cos x.$

(b) $\lim_{x \rightarrow \infty} \frac{1 - x^2}{x^3 - x - 1}.$

(j) $\lim_{x \rightarrow \infty} \frac{\sqrt{16x^6 - 3x}}{x^3 + 2}.$

(s) $\lim_{x \rightarrow \infty} \frac{x^4 + x}{x^3 - x + 2}.$

(c) $\lim_{x \rightarrow -\infty} \frac{x - 2}{x^2 + 5}.$

(k) $\lim_{x \rightarrow -\infty} \frac{\sqrt{16x^6 - 3x}}{x^3 + 2}.$

(t) $\lim_{x \rightarrow \infty} \sqrt{x^2 + 1}.$

(d) $\lim_{x \rightarrow -\infty} \frac{3x^3 + 2}{2x^3 - 4x + 5}.$

(l) $\lim_{x \rightarrow \infty} \frac{\sqrt{3x^2 + 2x + 1}}{x + 1}.$

(u) $\lim_{x \rightarrow -\infty} (x^4 + x^5).$

(e) $\lim_{x \rightarrow \infty} \frac{\sqrt{x} + x^2}{\sqrt{x} - x^2}.$

(m) $\lim_{x \rightarrow \infty} \sqrt{4x^2 + x} - 2x.$

(v) $\lim_{x \rightarrow -\infty} \frac{\sqrt{1 + x^6}}{1 + x^2}.$

(f) $\lim_{x \rightarrow \infty} \frac{3 - x\sqrt{x}}{2x^{\frac{3}{2}} - 2}.$

(n) $\lim_{x \rightarrow -\infty} x + \sqrt{x^2 + 3x}.$

(w) $\lim_{x \rightarrow \infty} (x - \sqrt{x}).$

(g) $\lim_{x \rightarrow \infty} \frac{(2x^2 + 3)^2}{(x - 1)^2(x^2 + 1)}.$

(o) $\lim_{x \rightarrow \infty} \sqrt{x^2 + 2x} - \sqrt{x^2 - 2x}.$

(x) $\lim_{x \rightarrow \infty} (x^2 - x^3).$

(h) $\lim_{x \rightarrow \infty} \frac{x^2 - 3}{\sqrt{x^4 + 3}}.$

(p) $\lim_{x \rightarrow -\infty} \sqrt{x^2 + x} - \sqrt{x^2 - x}.$

(y) $\lim_{x \rightarrow \infty} x \sin x.$

(q) $\lim_{x \rightarrow \infty} \sqrt{x^2 + ax} - \sqrt{x^2 + bx}.$

(z) $\lim_{x \rightarrow \infty} \sqrt{x} \sin x.$

3. Find the horizontal and vertical asymptotes of the graph of the function. If a graphing device is available, check your work by plotting the function.

(a) $y = \frac{2x}{\sqrt{x^2 + x + 3} - 3}.$

(g) $y = \frac{1 + x^4}{x^2 - x^4}.$

(b) $y = \frac{3x^2}{\sqrt{x^2 + 2x + 10} - 5}.$

(h) $y = \frac{x^3 - x}{x^2 - 7x + 6}.$

(c) $y = \frac{3x + 1}{x - 2}.$

(i) $y = \frac{x - 9}{\sqrt{4x^2 + 3x + 3}}.$

(d) $y = \frac{x^2 - 1}{2x^2 - 3x - 2}.$

(j) $y = \frac{\sqrt{x^2 + 1} - x}{x}.$

(e) $y = \frac{2x^2 - 2x - 1}{x^2 + x - 2}.$

(k) $f(x) = \frac{x}{\sqrt{x^2 + 3} - 2x}$

(f) $f(x) = \frac{-5x^2 - 3x + 5}{x^2 - 2x - 3}$