Calculus I Lecture 0 Representing Functions

Todor Milev

https://github.com/tmilev/freecalc

2020

Outline

- Ways to Represent a Function
 - The Definition of a Function
 - The Vertical Line Test
 - Piecewise Defined Functions
 - Symmetry
 - Increasing and Decreasing Functions
 - A Note on Domains of Functions

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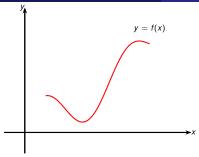
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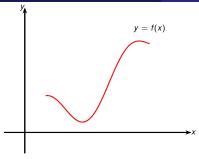
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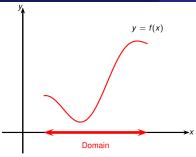


A function f is a rule that assigns to each element x in a set D exactly one element, called f(x), in a set E.



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• Functions are also synonymously called "maps".



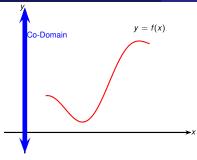
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Definition (Domain)

The set *D* in the definition of *f* is called the domain of *f*.

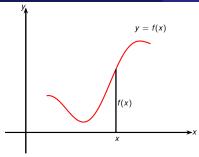
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Definition (Co-domain)

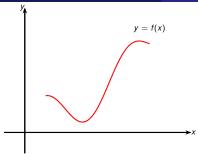
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A function f is a rule that assigns to each element x in a set D exactly one element, called f(x), in a set E.

Definition (Value of f at x)

The number f(x) is called the value of f at x and is read "f of x".



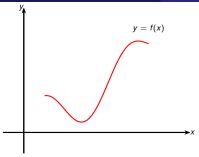
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• The value of *f* at *x* is also called the image of *x* under the map *f*.

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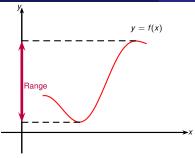
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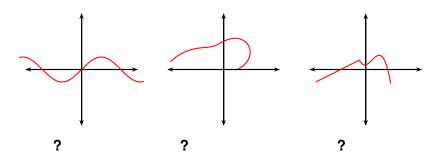
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Definition (Range)

The set of all possible values taken by f(x) as the element x runs over elements of D is called the range of f.

Question

Given a curve in the plane, is it the graph of a function or not?



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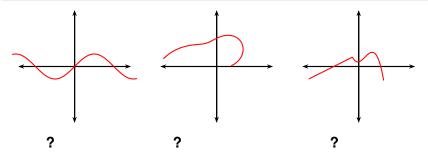
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The answer is as follows.

Proposition (The Vertical Line Test)

A curve in the plane is the graph of a function if and only if no vertical line intersects it more than once.



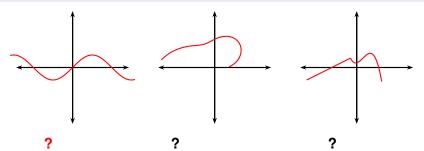
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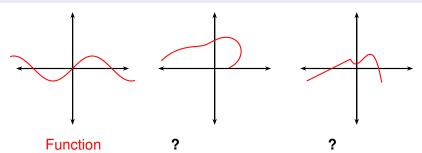
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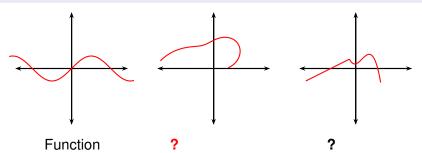
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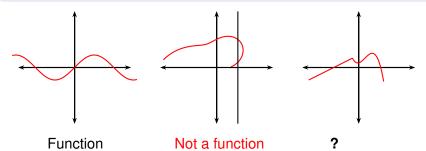
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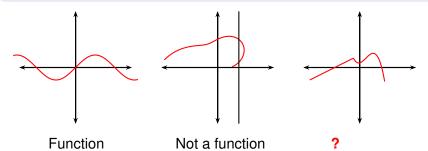
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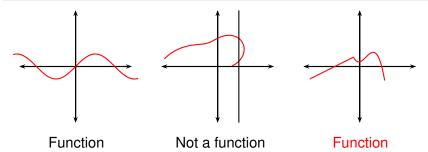
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Piecewise Defined Functions

Definition (Piecewise Defined Function)

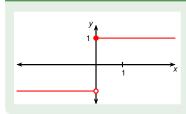
A piecewise defined function is a function that is defined by different algebraic formulas on different subsets of its domain.

Piecewise Defined Functions

Definition (Piecewise Defined Function)

A piecewise defined function is a function that is defined by different algebraic formulas on different subsets of its domain.

Example



$$f(x) = \begin{cases} 1 & \text{if} \quad x \ge 0 \\ -1 & \text{if} \quad x < 0 \end{cases}$$

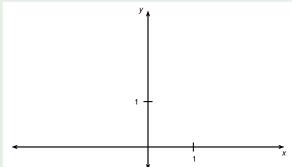
The filled red circle means (0, 1) is on the curve.

The open circle means (0,-1) is not on the curve.

The absolute value |x| of a number a is defined to be

$$|x| = \begin{cases} x & \text{if } x \geq 0 \\ -x & \text{if } x < 0. \end{cases}$$

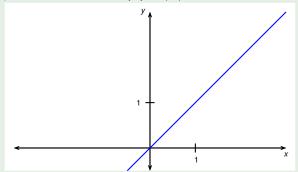
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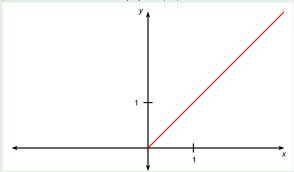
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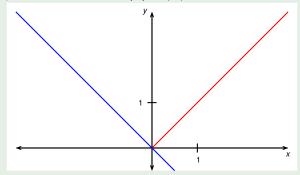
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Representing Functions

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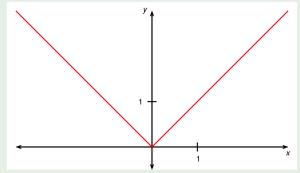
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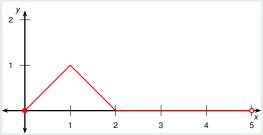
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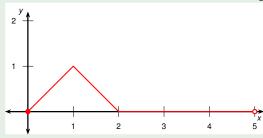
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Find a formula for the function *f* whose graph is given below.

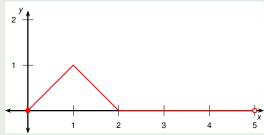


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Different formulas on [0, 1), [1, 2), and [2, 5).

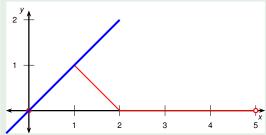
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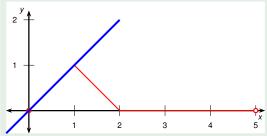
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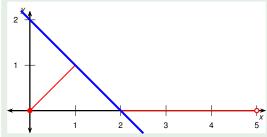
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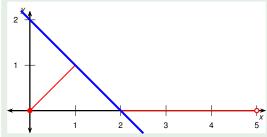
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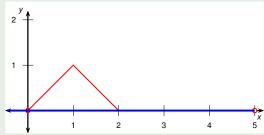
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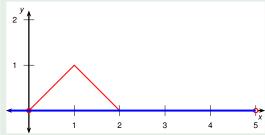
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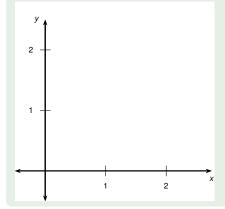
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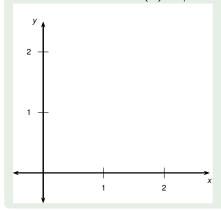
Sketch the function f(x) = |2x - 3|.



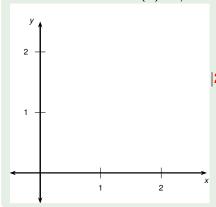
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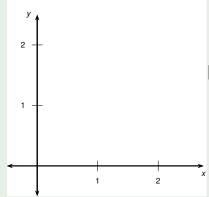


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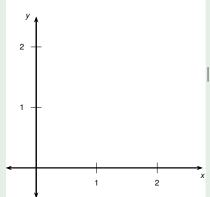
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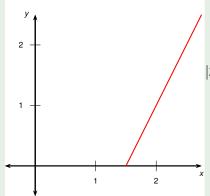


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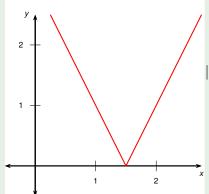


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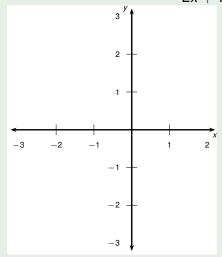
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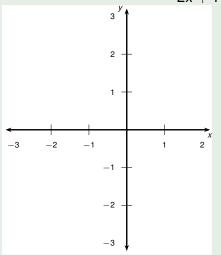
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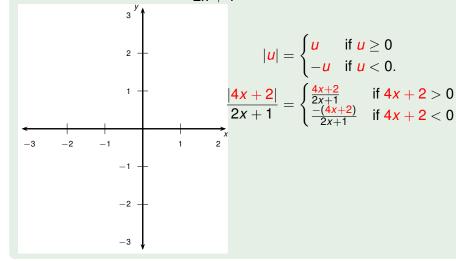


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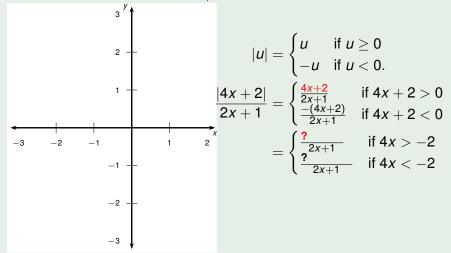
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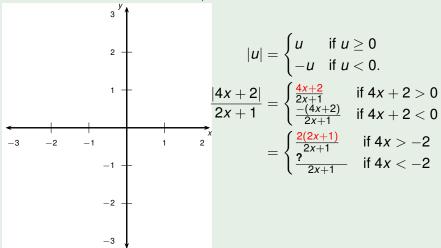
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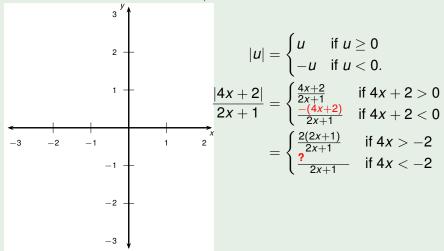
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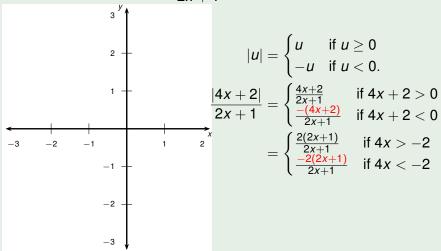
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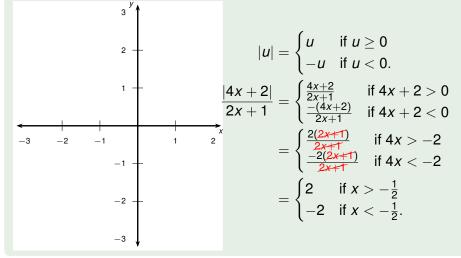
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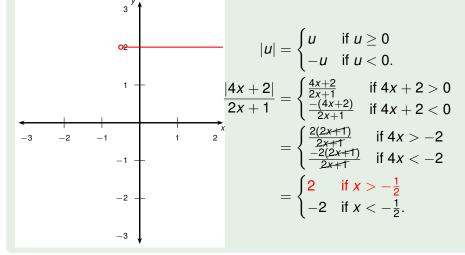
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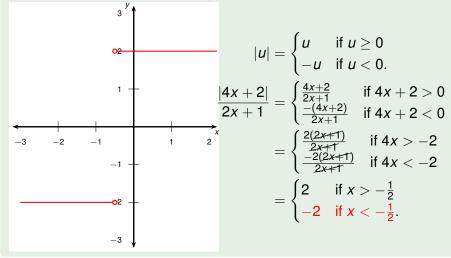
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Definition (Even and Odd Functions)

A function f is called even if f(-x) = f(x) for all x in its domain. A function f is called odd if f(-x) = -f(x) for all x in its domain.

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The function $f(x) = x^2$ is even:

The function $g(x) = x^3$ is odd:

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$$f(-x) = (-x)^2 = x^2 = f(x).$$

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Symmetry

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$$g(-x) = (-x)^3 = -x^3 = -g(x).$$

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Example

$$f(x) = x^5 + x$$

$$q(x) = 1 - x^4$$

$$h(x)=2x-1$$

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Definition (Increasing and Decreasing Functions)

A function f is called increasing on an interval I if $f(x_1) < f(x_2)$ whenever $x_1 < x_2$ in I.

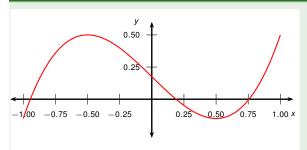
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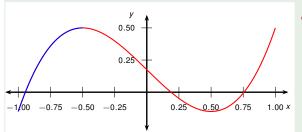


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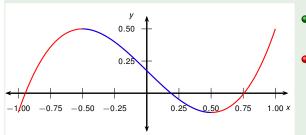
Lecture 0

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Todor Miley

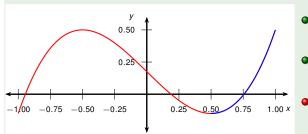
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- f is increasing on $[\frac{1}{2}, 1]$.

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- Taking $\log x$ if $x \le 0$ is not allowed in this course; taking $\log 0$ is not allowed in any course.