## Calculus I Homework Mean Value and Extreme Value Theorems Lecture 15

1. Use the Intermediate Value theorem and the Mean Value Theorem/Rolle's Theorem to prove that the function has **exactly one** real root.

(a) 
$$f(x) = x^3 + 4x + 7$$
.

(b) 
$$f(x) = x^3 + x^2 + x + 1$$
.

(c) 
$$f(x) = \cos^3(\frac{x}{3}) + \sin x - 3x$$
.

2. Use the Intermediate Value theorem and the Mean Value Theorem/Rolle's Theorem to prove that the function has **exactly one** real root.

(a) 
$$x^5 + 7x = 2$$
.

(b) 
$$x^7 + x^5 + x^3 = 3$$
.

(c) 
$$2x - 1 = \sin x$$
.

(d) 
$$e^x + 2x = 3$$
.