

Minimize  $f_0(x)$

$x$  is optimization variable

$f_0$  is an objective function

Optimization seeks to find the global minimum for an objective function, subject to constraints

Convex optimization

If the objective function is convex, the optimization problem is called convex optimization

Example problem:  $y = x^2 + 3$

Note that: derivative is 0 at

- local minimums
- local maximums
- global minimums
- global maximums

Take first derivative:  $y' = 2x$

2nd derivative test:  $y'' = 2$

If the 2nd derivative is positive, it is a minimum. Otherwise, it is a maximum

In the context of machine learning:

- Optimization is an iterative process
- The gradient tells us which way to change our parameters

### **Problems with optimization**

- Local minimums of the objective function
- All kinds of different constraints