Analytic function Dif A function of defined in a region D is mid to be analytic at a point a siff is differentiable at every point of some neighbourhood of a. Statement Suppose fer=ucrotivers is analytic in an openset O Write ?=x+e/y. There un, uy vo and vy exists of every point of O Moreover, They satisfy the pair of equations 4 = vy and uy = -vx. These equations are called pain of Cauchy Riemann egnations. Proof: We shall prieter to write. ひま)こひ(カナ) Take a point to EO. Sonce f is analytic at every point of 0. So by definition of analyticity, the function is differentiable at Therefore $\lim_{\xi \to z} \frac{f(\xi) - f(z)}{z - z} = f'(\xi)$ exists Suppose Z - To along the (20-l-, 2) line y = x (No. 3, - Ry) 以(れる)+いとのるる) - いいのな) -いといる) $(2, \%) \rightarrow (x_0, \%) \qquad (2-x_0) + i(\%-\%)$ $\lim_{N\to\infty}\frac{k(x,\xi_0)-k(x_0,y_0)}{x-x_0}+i\lim_{N\to\infty}\frac{y(x,y_0)-y(x_0,y_0)}{x-x_0}\geq f'(\xi_0)$ Similarly, along the line x=xo (no, y) ->(no, y) + i v (no, y)

