## 3.2 Example: Linear regression

In this example, we will use the dataset "Advertising and Sales", which is available at www.kaggle.com. The datasets includes 4 features and 200 instances. The 3 features are "TV", "radio", "newspaper", which refer to the amount of resources that are allocated in each media. The 4<sup>th</sup> feature is the target feature "sales", which refers to the total sales number. For the purpose of this chapter, we will assume that the only feature that has strong impact on the target feature is "TV". Thus, we ignore the other two features. In addition, we will use 160 out of the 200 instances. For this example we will use the programming language "python".

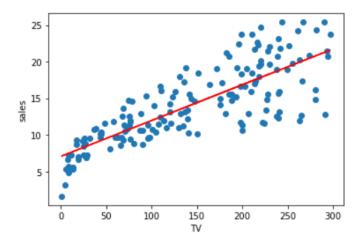
```
In [1]:
         import pandas as pd
         import matplotlib.pyplot as plt
         from sklearn.linear_model import LinearRegression
         import statsmodels.api as sm
In [2]: df=pd.read csv('Advertising.csv')
         df.drop('Unnamed: 0',inplace=True, axis=1)
Out[2]:
                 TV
                     radio newspaper sales
            0 230.1
                      37.8
                                 69.2
                                       22.1
                44.5
                      39.3
                                 45.1
            1
                                        10.4
            2
                17.2
                      45.9
                                 69.3
            3 151.5
                      41.3
                                 58.5
                                        18.5
            4
               180.8
                      10.8
                                 58.4
                                        12.9
            ...
                38.2
                       3.7
                                 13.8
                                        7.6
          195
          196
                94.2
                       4.9
                                  8.1
                                        9.7
              177.0
                                       12.8
          197
                       9.3
                                  6.4
                                       25.5
          198
              283.6
                      42.0
                                 66.2
              232.1
                       8.6
                                  8.7
                                        13.4
          199
         200 rows × 4 columns
```

First, we will handle our data because they should have a specific form, before they are used as an input to our model. Then we will fit the model to our data and we will plot the results.

```
In [3]: x = df[:160]['TV'].values
y = df[:160]['sales'].values
x=x.reshape(160,1)
y=y.reshape(160,1)
```

```
In [4]: lr = LinearRegression().fit(x,y)
    y_pred=lr.predict(x)
    plt.scatter(x,y)
    plt.xlabel('TV')
    plt.ylabel('sales')
    plt.plot(x,y_pred,color='red')
```

Out[4]: [<matplotlib.lines.Line2D at 0x2289b1c5df0>]



```
In [5]: x1 = sm.add_constant(x)
  est = sm.OLS(y, x1)
  est2 = est.fit()
  print(est2.summary())
```

OLS	Regression	Resu.	lts
-----	------------	-------	-----

Dep. Variable:	у	R-squared:	0.643			
Model:	OLS	Adj. R-squared:	0.641			
Method:	Least Squares	F-statistic:	284.6			
Date:	Mon, 29 Jan 2024	Prob (F-statistic):	3.58e-37			
Time:	10:31:23	Log-Likelihood:	-408.80			
No. Observations:	160	AIC:	821.6			
Df Residuals:	158	BIC:	827.7			
Df Model:	1					
Covariance Type:	nonrobust					

=========								
	coef	std err	t	P> t	[0.025	0.975]		
const	7.0688	0.483	14.634	0.000	6.115	8.023		
x1	0.0489	0.003	16.871	0.000	0.043	0.055		
Omnibus:		1.5	75 Durbi	n-Watson:		1.931		
Prob(Omnibus)	):	0.4	155 Jarqu	ie-Bera (JB):		1.414		
Skew:		-0.2	230 Prob(	JB):		0.493		
Kurtosis:		3.6	002 Cond.	No.		325.		

## Notes:

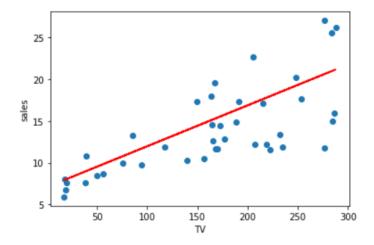
[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

## **Evaluation**

```
In [6]: x_test = df[160:]['TV'].values
    y_test = df[160:]['sales'].values
    x_test = x_test.reshape(40,1)
    y_test = y_test.reshape(40,1)
```

```
In [7]: y_pred=lr.predict(x_test)
    plt.scatter(x_test,y_test)
    plt.xlabel('TV')
    plt.ylabel('sales')
    plt.plot(x_test,y_pred,color='red')
```

## Out[7]: [<matplotlib.lines.Line2D at 0x228a210b0a0>]



```
In [8]: from sklearn import metrics
    MSE = metrics.mean_squared_error(y_test,y_pred)
    print('MSE =', round(MSE,2))
    MAE = metrics.mean_absolute_error(y_test,y_pred)
    print('MAE =', round(MAE,2))
    RMSE = MSE**(1/2)
    print('RMSE =', round(RMSE,2))
    R2 = metrics.r2_score(y_test,y_pred)
    print('R-squared =', round(R2,2))
```

MSE = 14.13 MAE = 3.08 RMSE = 3.76 R-squared = 0.47