# **Understanding Uncertainty Metrics**

This report explains the uncertainty metrics and visualizations for 5 images analyzed with VAE-UNet.

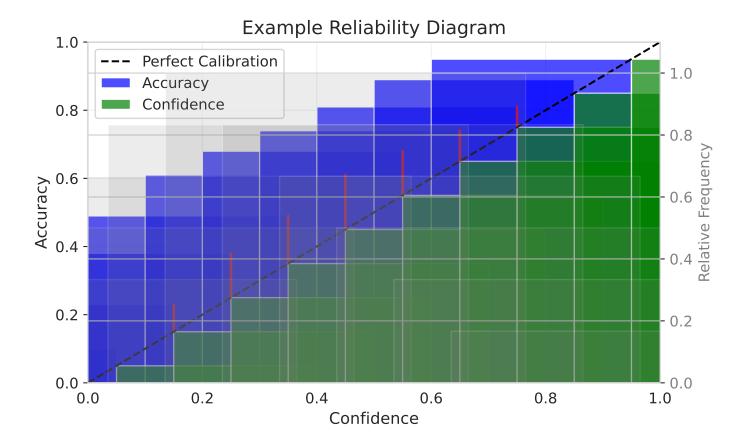
Mean Expected Calibration Error (ECE): 0.0048

Mean Dice Score: 0.6971

Mean Brier Score: 0.0055

Mean Sparsification Error: 0.9571

## Understanding Reliability Diagrams



#### RELIABILITY DIAGRAM EXPLANATION:

A reliability diagram shows how well a model's predicted probabilities match actual outcomes.

- Blue bars: The actual frequency of positive pixels in each confidence bin
- Green bars: The mean predicted probability (confidence) for each bin
- Gray histogram: Distribution of predictions across confidence levels
- Red lines: Highlight gaps between confidence and actual frequency
- Diagonal line: Perfect calibration (confidence = actual frequency)

#### INTERPRETATION:

- When blue bars are higher than green bars: Model is underconfident
- When green bars are higher than blue bars: Model is overconfident
- Expected Calibration Error (ECE): Weighted average of gaps between bars
  - Lower ECE values (closer to 0) indicate better calibration

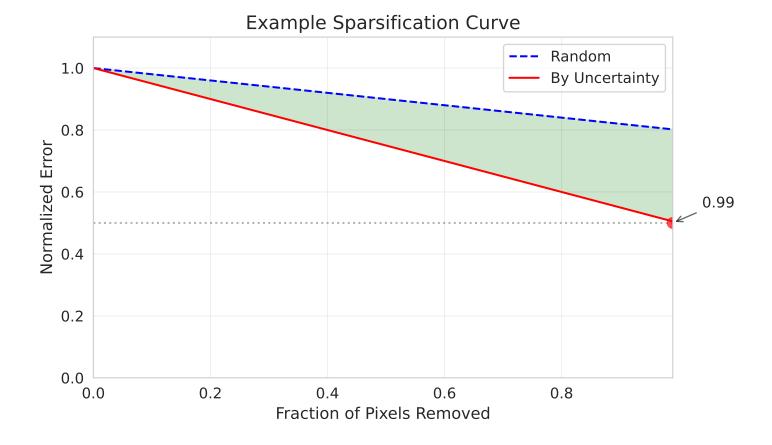
### **ECE Values Interpretation:**

- < 0.01: Excellent calibration
- 0.01-0.05: Good calibration
- 0.05-0.15: Fair calibration
  - > 0.15: Poor calibration

#### WHY IT MATTERS:

Good calibration means the confidence values from your model are reliable. For medical segmentation, this helps clinicians know when to trust the model's predictions.

## **Understanding Sparsification Curves**



#### SPARSIFICATION CURVE EXPLANATION:

A sparsification curve shows whether your model's uncertainty estimates correlate with actual errors.

- Blue dashed line: Error when removing pixels randomly
- Red solid line: Error when removing pixels with highest uncertainty first
  - Green/Red fill: Area between curves (Sparsification Error)
  - Red dot: Fraction of pixels that must be removed to halve the error

#### **INTERPRETATION:**

- If red line is below blue line (green area): Good uncertainty estimates! This means removing high-uncertainty pixels reduces error faster than random removal.
  - If red line is above blue line (red area): Poor uncertainty estimates. Your model's uncertainty doesn't correlate well with actual errors.
    - Sparsification Error (SE): Area between the curves
      - Positive SE: Good uncertainty estimates
      - Negative SE: Poor uncertainty estimates
    - Larger positive values indicate better uncertainty quality

#### WHY IT MATTERS:

Good uncertainty estimates help identify which predictions might be wrong and where the model needs human verification in clinical applications.

## Understanding the Visualization Plots

#### **CORRELATION MATRIX EXPLANATION:**

The correlation matrix shows how different metrics relate to each other:

- Values close to 1: Strong positive correlation (one increases, the other increases)
- Values close to -1: Strong negative correlation (one increases, the other decreases)
  - Values close to 0: Little or no correlation

### Key relationships to look for:

- Dice Score vs. Uncertainty Metrics: Does better performance correlate with better calibration?
  - ECE vs. Sparsification Error: Do different uncertainty metrics agree with each other?

#### CALIBRATION ANALYSIS PLOT EXPLANATION:

This plot helps understand the pattern of calibration errors:

- X-axis: Maximum Calibration Error (MCE) the largest calibration error in any bin
  - Y-axis: Mean Absolute Calibration Error (MACE) the average calibration error
- Color: Expected Calibration Error (ECE) weighted average of calibration errors
  - Size: Dice Score larger points indicate better segmentation performance

### Interpretation by location:

- Points near the diagonal: Errors are consistent across all confidence levels
  - Points below diagonal: Errors concentrated in specific confidence bins
    - Bottom-left corner: Best calibration overall (low errors)
- Larger points in bottom-left: Ideal models (good performance, good calibration)

#### PAIRPLOT EXPLANATION:

The pairplot shows the relationships between all pairs of metrics:

- Diagonal: Distribution of each individual metric
- Off-diagonal: Scatter plots showing relationship between pairs of metrics

#### TEMPERATURE SCALING:

If your model has an ECE of 0.005, that's excellent calibration! With temperature=2.0 giving better results, this suggests your model was slightly overconfident at the default temperature (T=1.0). Higher temperatures 'soften' predictions, making very confident predictions less extreme.