# Data 621 Homework 3: Boston Crime Rates

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## **OVERVIEW**

In this homework assignment, we will explore, analyze and model a data set containing information on crime for various neighborhoods of a major city. Each record has a response variable indicating whether or not the crime rate is above the median crime rate (1) or not (0).

## Objective:

The objective is to build a binary logistic regression model on the training data set to predict whether the neighborhood will be at risk for high crime levels.

## DATA EXPLORATION

# **Data Summary**

The dataset consists of two data files: training and evaluation. The training dataset contains 13 columns, while the evaluation dataset contains 12. The evaluation dataset is missing column target which represend our responce variable and defines whether the crime rate is above the median crime rate (1) or not (0). We will start by exploring the training data set since it will be the one used to generate the regression model.

First we see that all data is numeric. The dataset does contain one dummy variable to identify if the property borders the Charles River (1) or not (0).

An important aspect of any dataset is to determine how much, if any, data is missing. We look at all the variables to see which if any have missing data. We look at the basic descriptive statistics as well as the missing data and their percentages:

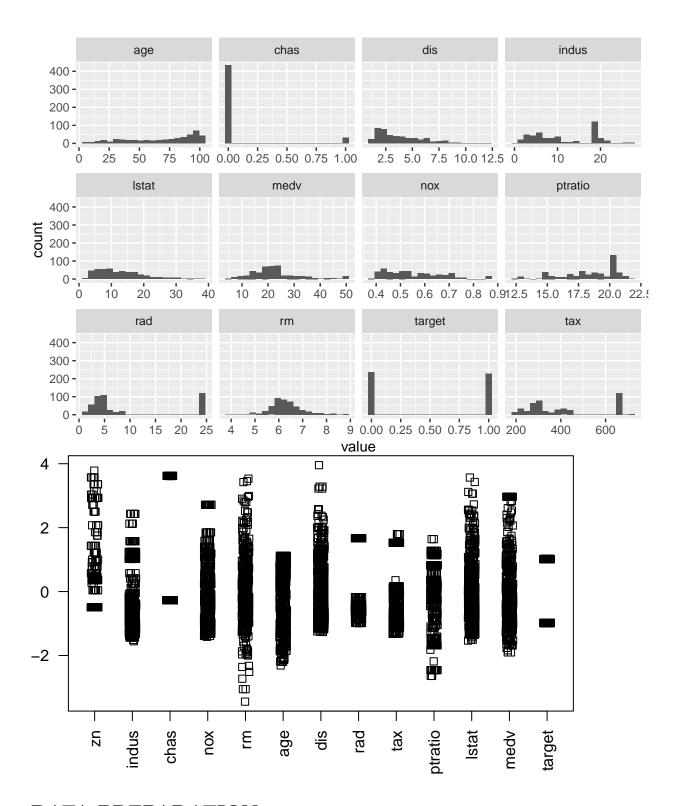
## chas 3 466 0.07 0.26 0.00 0.00 0.00 0.00 1.00 1.	7.28 1.00						
## chas 3 466 0.07 0.26 0.00 0.00 0.00 0.00 1.00 1.	1.00						
## nox 4 466 0.55 0.12 0.54 0.54 0.13 0.39 0.87 0.							
	).48						
## rm 5 466 6.29 0.70 6.21 6.26 0.52 3.86 8.78 4.	1.92						
## age 6 466 68.37 28.32 77.15 70.96 30.02 2.90 100.00 97.	7.10						
## dis 7 466 3.80 2.11 3.19 3.54 1.91 1.13 12.13 11.	1.00						
## rad 8 466 9.53 8.69 5.00 8.70 1.48 1.00 24.00 23.	3.00						
## tax 9 466 409.50 167.90 334.50 401.51 104.52 187.00 711.00 524.	1.00						
## ptratio 10 466 18.40 2.20 18.90 18.60 1.93 12.60 22.00 9.	9.40						
## lstat 11 466 12.63 7.10 11.35 11.88 7.07 1.73 37.97 36.	3.24						
## medv 12 466 22.59 9.24 21.20 21.63 6.00 5.00 50.00 45.	5.00						
## target 13 466 0.49 0.50 0.00 0.49 0.00 0.00 1.00 1.	1.00						
## skew kurtosis se na_count na_count_perc							
## zn 2.18 3.81 1.08 0 0							
## indus 0.29 -1.24 0.32 0 0							
## chas 3.34 9.15 0.01 0 0							
## nox 0.75 -0.04 0.01 0 0							
## rm 0.48 1.54 0.03 0 0							

```
## age
            -0.58
                      -1.01 1.31
                                          0
                                                         0
   dis
             1.00
                       0.47 0.10
                                          0
                                                         0
##
##
   rad
             1.01
                      -0.860.40
                                          0
                                                         0
                                          0
                                                         0
             0.66
                      -1.15 7.78
##
   tax
##
   ptratio -0.75
                      -0.40 0.10
                                          0
                                                         0
             0.91
                       0.50 0.33
                                          0
                                                         0
## 1stat
## medv
             1.08
                       1.37 0.43
                                          0
                                                         0
             0.03
                      -2.00 0.02
                                          0
                                                         0
## target
              indus
##
                                                             dis
                                                                     rad
         zn
                        chas
                                  nox
                                                                              tax
                                            rm
                                                    age
         0
##
                  0
                           0
                                    0
                                             0
                                                      0
                                                               0
                                                                        0
                                                                                0
## ptratio
              lstat
                        medv
                              target
          0
                   0
##
                           0
     0
   100
Observations
   200
   300
   400
                                                Present (100%)
##
     zn indus chas
                                            dis rad tax ptratio lstat medv target
                       nox
                               rm
                                    age
## 1
      0 19.58
                   0 0.605 7.929
                                                   5 403
                                   96.2 2.0459
                                                             14.7
                                                                  3.70 50.0
                                                                                    1
      0 19.58
                   1 0.871 5.403 100.0 1.3216
                                                  5 403
                                                             14.7 26.82 13.4
                                                                                    1
   3
      0 18.10
                   0 0.740 6.485 100.0 1.9784
                                                 24 666
                                                             20.2 18.85 15.4
                                                                                    1
   4 30
         4.93
                   0 0.428 6.393
                                    7.8 7.0355
                                                  6 300
                                                             16.6
                                                                   5.19 23.7
                                                                                    0
                   0 0.488 7.155
## 5
      0
         2.46
                                   92.2 2.7006
                                                   3 193
                                                             17.8
                                                                   4.82 37.9
                                                                                    0
      0
         8.56
                   0 0.520 6.781
                                  71.3 2.8561
                                                             20.9 7.67 26.5
                                                                                    0
                                                  5 384
```

# Missing and Invalid Data

No missing data was found in the dataset.

With missing data assessed, we can look into the data in more detail. To visualize this we plot histograms for each data. Several predictors like dist, chas, rad, zn and tax are not normally distributed and noticable outliers.



# DATA PREPARATION

# Fix missing values

No data was found missing.

#### Mathematical transformations.

Box Cox The Box Cox transformation tries to transform non-normal data into a normal distribution. This transformation attemps to estimate the  $\lambda$  for Y. With the exception of tax, all predictors have either no transformation extimate or were given a fudge value of 0.

```
## $zn
## Box-Cox Transformation
##
## 466 data points used to estimate Lambda
##
##
  Input data summary:
##
      Min. 1st Qu. Median
                              Mean 3rd Qu.
                                              Max.
##
             0.00
                      0.00
                             11.58
                                     16.25
                                            100.00
##
## Lambda could not be estimated; no transformation is applied
##
##
## $indus
## Box-Cox Transformation
## 466 data points used to estimate Lambda
##
## Input data summary:
##
      Min. 1st Qu. Median
                              Mean 3rd Qu.
                                              Max.
##
           5.145
                    9.690 11.105 18.100
                                           27.740
##
## Largest/Smallest: 60.3
## Sample Skewness: 0.289
##
## Estimated Lambda: 0.4
##
##
## $chas
## Box-Cox Transformation
## 466 data points used to estimate Lambda
##
## Input data summary:
      Min. 1st Qu. Median
                              Mean 3rd Qu.
## 0.00000 0.00000 0.00000 0.07082 0.00000 1.00000
## Lambda could not be estimated; no transformation is applied
##
##
## $nox
## Box-Cox Transformation
##
## 466 data points used to estimate Lambda
##
## Input data summary:
     Min. 1st Qu. Median
##
                              Mean 3rd Qu.
                                              Max.
   0.3890 0.4480 0.5380 0.5543 0.6240 0.8710
##
## Largest/Smallest: 2.24
```

```
## Sample Skewness: 0.746
##
## Estimated Lambda: -0.9
##
## $rm
## Box-Cox Transformation
## 466 data points used to estimate Lambda
##
## Input data summary:
##
     Min. 1st Qu. Median
                             Mean 3rd Qu.
                                              Max.
     3.863 5.887 6.210
                             6.291
                                    6.630
                                             8.780
##
##
## Largest/Smallest: 2.27
## Sample Skewness: 0.479
##
## Estimated Lambda: 0.2
##
##
## $age
## Box-Cox Transformation
##
## 466 data points used to estimate Lambda
##
## Input data summary:
##
     Min. 1st Qu. Median
                             Mean 3rd Qu.
                                              Max.
##
      2.90
           43.88 77.15
                             68.37
                                   94.10 100.00
##
## Largest/Smallest: 34.5
## Sample Skewness: -0.578
##
## Estimated Lambda: 1.3
##
##
## $dis
## Box-Cox Transformation
##
## 466 data points used to estimate Lambda
##
## Input data summary:
     Min. 1st Qu. Median
##
                             Mean 3rd Qu.
                                              Max.
##
     1.130 2.101 3.191
                             3.796 5.215 12.127
##
## Largest/Smallest: 10.7
## Sample Skewness: 0.999
## Estimated Lambda: -0.1
## With fudge factor, Lambda = 0 will be used for transformations
##
##
## $rad
## Box-Cox Transformation
##
```

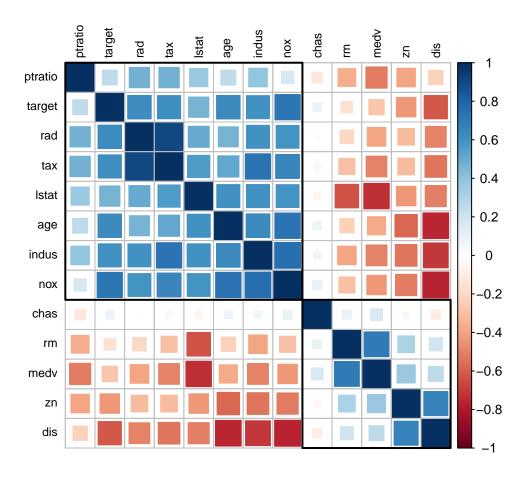
```
## 466 data points used to estimate Lambda
##
## Input data summary:
     Min. 1st Qu. Median
                             Mean 3rd Qu.
                                             Max.
      1.00
             4.00
                     5.00
                             9.53 24.00
##
## Largest/Smallest: 24
## Sample Skewness: 1.01
##
## Estimated Lambda: -0.2
## With fudge factor, Lambda = 0 will be used for transformations
##
##
## $tax
## Box-Cox Transformation
## 466 data points used to estimate Lambda
## Input data summary:
##
     Min. 1st Qu. Median
                             Mean 3rd Qu.
##
     187.0 281.0 334.5 409.5 666.0
                                            711.0
##
## Largest/Smallest: 3.8
## Sample Skewness: 0.659
##
## Estimated Lambda: -0.5
##
##
## $ptratio
## Box-Cox Transformation
## 466 data points used to estimate Lambda
##
## Input data summary:
##
     Min. 1st Qu. Median
                             Mean 3rd Qu.
      12.6 16.9
##
                   18.9
                             18.4
                                     20.2
                                             22.0
##
## Largest/Smallest: 1.75
## Sample Skewness: -0.754
##
## Estimated Lambda: 2
##
## $1stat
## Box-Cox Transformation
##
## 466 data points used to estimate Lambda
##
## Input data summary:
##
     Min. 1st Qu. Median
                             Mean 3rd Qu.
           7.043 11.350 12.631 16.930 37.970
##
##
## Largest/Smallest: 21.9
## Sample Skewness: 0.906
```

```
##
## Estimated Lambda: 0.2
##
##
## $medv
## Box-Cox Transformation
## 466 data points used to estimate Lambda
##
##
  Input data summary:
##
      Min. 1st Qu. Median
                              Mean 3rd Qu.
                                               Max.
            17.02
                                      25.00
##
      5.00
                     21.20
                             22.59
                                              50.00
##
## Largest/Smallest: 10
## Sample Skewness: 1.08
##
## Estimated Lambda: 0.2
##
##
## $target
## Box-Cox Transformation
## 466 data points used to estimate Lambda
##
## Input data summary:
##
     Min. 1st Qu. Median
                              Mean 3rd Qu.
                                               Max.
##
   0.0000 0.0000 0.0000 0.4914 1.0000
                                            1.0000
## Lambda could not be estimated; no transformation is applied
```

# Variable Creation / Removal

To determine how we can combine variables to create new one we start by looking at a correlation plot. The plot and cor funtion lists nox, age, rad,tax and indus as the strongest postively correlated predictors, while rad and distance are the strongest negatively correlated predictors.

```
## indus chas nox rm age dis
## [1,] 0.6048507 0.08004187 0.7261062 -0.1525533 0.6301062 -0.6186731
## rad tax ptratio lstat medv target
## [1,] 0.6281049 0.6111133 0.2508489 0.469127 -0.2705507 1
```



# **BUILD MODELS**

## General regression

We start by building a model with all the predictors in the dataset.

```
##
## Call:
## glm(formula = target ~ ., family = binomial(link = "logit"),
##
       data = crimeTrain)
##
## Deviance Residuals:
##
       Min
                 1Q
                      Median
                                    3Q
                                            Max
## -1.8464 -0.1445 -0.0017
                                0.0029
                                         3.4665
##
## Coefficients:
                 Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) -40.822934
                            6.632913
                                      -6.155 7.53e-10 ***
                -0.065946
                            0.034656
                                      -1.903 0.05706 .
## zn
## indus
                -0.064614
                            0.047622
                                      -1.357
                                               0.17485
## chas
                 0.910765
                            0.755546
                                        1.205
                                               0.22803
                49.122297
                            7.931706
                                        6.193 5.90e-10 ***
## nox
                -0.587488
                            0.722847
                                      -0.813 0.41637
## rm
## age
                 0.034189
                                               0.01333 *
                            0.013814
                                        2.475
## dis
                 0.738660
                            0.230275
                                        3.208 0.00134 **
## rad
                 0.666366
                            0.163152
                                        4.084 4.42e-05 ***
```

```
## 1stat
                 0.045869
                            0.054049
                                        0.849
                                               0.39608
                 0.180824
                            0.068294
                                        2.648
                                               0.00810 **
## medv
##
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
  (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 645.88
                              on 465
                                      degrees of freedom
## Residual deviance: 192.05
                              on 453
                                      degrees of freedom
## AIC: 218.05
##
## Number of Fisher Scoring iterations: 9
The Summary of this model shows several predictor are not relevant. We build a second model without these
predictors.
##
## Call:
  glm(formula = target ~ nox + age + dis + rad + tax + ptratio +
##
       medv, family = binomial(link = "logit"), data = crimeTrain)
##
## Deviance Residuals:
##
        Min
                   10
                         Median
                                        30
                                                 Max
## -2.01059 -0.19744
                      -0.01371
                                   0.00402
                                             3.06424
##
## Coefficients:
##
                 Estimate Std. Error z value Pr(>|z|)
                                      -6.286 3.26e-10 ***
## (Intercept) -36.824228
                            5.858405
                42.338378
                            6.639207
                                        6.377 1.81e-10 ***
## nox
## age
                 0.031882
                            0.010693
                                        2.982 0.002867 **
## dis
                 0.429555
                            0.171849
                                        2.500 0.012433 *
## rad
                 0.701767
                            0.139426
                                        5.033 4.82e-07 ***
                -0.008237
                            0.002534
                                       -3.250 0.001153 **
## tax
                 0.376575
                            0.108912
                                        3.458 0.000545 ***
## ptratio
                 0.093653
                            0.033556
                                        2.791 0.005255 **
## medv
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
  (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 645.88
                                      degrees of freedom
##
                              on 465
## Residual deviance: 203.45
                              on 458 degrees of freedom
## AIC: 219.45
## Number of Fisher Scoring iterations: 9
## [1] 1
## [1] 1
```

-0.006171

0.402566

## tax
## ptratio

0.002955

0.126627

-2.089 0.03674 \*

0.00148 \*\*

3.179

The new model has a slightly higher AIC which would tells us the first model is slightly less complex. For the 2 data sets p-value = 1 - pchisq(deviance, degrees of freedom) are 1. The Null hypothesis is still supported.

#### **AIC Step Method**

Another way of selecting which predictors to use in the model is by calculating the AIC of the model. This metric is similar to the adjusted R-square of a model in that it penalizes models with more predictors over simpler model with few predictors. We use Stepwise function in r to find the lowest AIC with different predictors.

```
## Start: AIC=218.05
## target ~ zn + indus + chas + nox + rm + age + dis + rad + tax +
##
       ptratio + lstat + medv
##
##
             Df Deviance
                            AIC
                  192.71 216.71
## - rm
              1
## - lstat
                  192.77 216.77
              1
                  193.53 217.53
## - chas
              1
## - indus
                  193.99 217.99
              1
## <none>
                  192.05 218.05
                  196.59 220.59
## - tax
              1
## - zn
                  196.89 220.89
              1
## - age
              1
                  198.73 222.73
## - medv
              1
                  199.95 223.95
## - ptratio 1
                  203.32 227.32
## - dis
                  203.84 227.84
              1
## - rad
                  233.74 257.74
              1
                  265.05 289.05
## - nox
              1
##
## Step: AIC=216.71
## target ~ zn + indus + chas + nox + age + dis + rad + tax + ptratio +
##
       lstat + medv
##
##
             Df Deviance
                            AIC
## - chas
              1
                  194.24 216.24
## - lstat
                  194.32 216.32
              1
## - indus
                  194.58 216.58
                  192.71 216.71
## <none>
## - tax
                  197.59 219.59
              1
## - zn
              1
                  198.07 220.07
## - age
              1
                  199.11 221.11
## - ptratio 1
                  203.53 225.53
                  203.85 225.85
## - dis
              1
## - medv
                  205.35 227.35
              1
## - rad
              1
                  233.81 255.81
                  265.14 287.14
## - nox
              1
##
## Step: AIC=216.24
## target ~ zn + indus + nox + age + dis + rad + tax + ptratio +
##
       1stat + medv
##
##
             Df Deviance
                            AIC
## - indus
                  195.51 215.51
## <none>
                  194.24 216.24
## - lstat
                  196.33 216.33
              1
## - zn
              1
                  200.59 220.59
## - tax
                  200.75 220.75
              1
## - age
              1
                 201.00 221.00
```

```
## - ptratio 1
                203.94 223.94
## - dis
                204.83 224.83
             1
## - medv
             1
                207.12 227.12
                241.41 261.41
## - rad
             1
## - nox
             1 265.19 285.19
##
## Step: AIC=215.51
## target ~ zn + nox + age + dis + rad + tax + ptratio + 1stat +
##
      medv
##
##
            Df Deviance
            1 197.32 215.32
## - lstat
                195.51 215.51
## <none>
## - zn
                202.05 220.05
## - age
                202.23 220.23
             1
## - ptratio 1
                205.01 223.01
## - dis
                205.96 223.96
             1
                206.60 224.60
## - tax
             1
## - medv
                208.13 226.13
             1
             1 249.55 267.55
## - rad
## - nox
             1 270.59 288.59
##
## Step: AIC=215.32
## target ~ zn + nox + age + dis + rad + tax + ptratio + medv
##
            Df Deviance AIC
                197.32 215.32
## <none>
                203.45 219.45
## - zn
             1
                206.27 222.27
## - ptratio 1
                207.13 223.13
## - age
             1
                207.62 223.62
## - tax
             1
## - dis
             1
                207.64 223.64
## - medv
                208.65 224.65
             1
## - rad
             1 250.98 266.98
             1 273.18 289.18
## - nox
##
## Call:
## glm(formula = target ~ zn + nox + age + dis + rad + tax + ptratio +
      medv, family = binomial(link = "logit"), data = crimeTrain)
##
## Deviance Residuals:
      Min 1Q Median
                                 3Q
                                        Max
## -1.8295 -0.1752 -0.0021
                             0.0032
                                     3.4191
##
## Coefficients:
               Estimate Std. Error z value Pr(>|z|)
## (Intercept) -37.415922 6.035013 -6.200 5.65e-10 ***
               -0.068648
                          0.032019 -2.144 0.03203 *
## nox
               42.807768
                          6.678692
                                    6.410 1.46e-10 ***
## age
               0.032950
                          0.010951
                                    3.009 0.00262 **
                          0.214050
                                    3.060 0.00222 **
## dis
               0.654896
## rad
               0.725109
                          0.149788 4.841 1.29e-06 ***
              ## tax
```

```
## ptratio
                 0.323628
                            0.111390
                                       2.905
                                              0.00367 **
## medv
                 0.110472
                            0.035445
                                       3.117
                                              0.00183 **
##
                     '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
  (Dispersion parameter for binomial family taken to be 1)
##
##
##
       Null deviance: 645.88
                             on 465
                                      degrees of freedom
## Residual deviance: 197.32 on 457
                                      degrees of freedom
## AIC: 215.32
##
## Number of Fisher Scoring iterations: 9
```

This reduces the predictors used in the model to these: zn nox age dis rad tax ptRation medv

It Removes these predictors: indus chas rm#

The AIC improves marginally from 218.05 (our original general model) to 215.32, but we also benefit by having a simpler model less prone to overfitting.

Also, the predictors in the model now are all signficant (under 0.05 pr level) and all but one under .01 or very significant. Which is much improved over the prior model

#### **BIC Method**

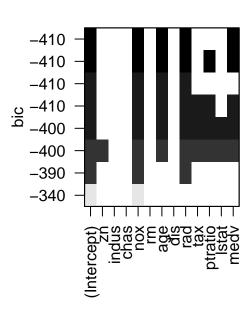
To determine the number of predictors and which predictors to be used we will use the Bayesian Information Criterion (BIC).

# **Subset Selection Using BIC**

# BIC - 380 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 - 340 -

Number of Predictors

# Predictors vs. BIC



The plot on the right shows that the number of predictors with the lowest BIC are nox, age, rad, and medv. We will use those predictors to build the next model

	Estimate	Std. Error	z value	$\Pr(> z )$
(Intercept)	-17.63	2.168	-8.131	4.246e-16
nox	23.62	3.936	6.003	1.942e-09
age	0.01824	0.009172	1.989	0.04673
$\operatorname{rad}$	0.4528	0.1093	4.144	3.413e-05
$\mathbf{medv}$	0.04481	0.02319	1.932	0.05338

(Dispersion parameter for binomial family taken to be 1)

## Step: AIC=243.97

Null deviance:	645.9 on 465 degrees of freedom
Residual deviance:	232.8 on $461$ degrees of freedom

#### Forward Selection Method using some BoxCox transformed independent variables:

```
m4 <- step(glm(target~1, data=crimeTrain), direction = "forward", scope = ~zn + I(log(indus)) + I(sqrt(
## Start: AIC=680.3
## target ~ 1
##
##
                                   AIC
                   Df Deviance
## + I(nox^-1)
                    1
                        50.349 291.51
## + I(age^2)
                        66.713 422.64
                    1
## + I(dis^-0.5)
                    1
                        66.801 423.26
## + rad
                        70.518 448.50
## + I(log(indus))
                    1
                        74.068 471.38
## + I(tax^-1)
                    1
                        74.547 474.39
## + lstat
                        90.834 566.47
                    1
## + zn
                    1
                        94.762 586.20
## + I(ptratio^2)
                      107.479 644.88
                    1
## + medv
                    1
                       107.941 646.88
## + I(log(rm))
                    1
                      112.912 667.86
## + I(sqrt(chas))
                    1 115.720 679.31
                       116.466 680.30
## <none>
##
## Step: AIC=291.51
## target ~ I(nox^-1)
##
##
                   Df Deviance
                                  AIC
                        45.272 243.97
## + rad
                    1
## + I(tax^-1)
                    1
                        46.956 260.99
## + I(age^2)
                        49.650 286.99
                    1
## + I(ptratio^2)
                    1
                        49.778 288.19
## + I(log(rm))
                        49.876 289.10
## + medv
                        49.907 289.40
                    1
## + I(log(indus))
                        50.043 290.66
## <none>
                        50.349 291.51
## + zn
                        50.147 291.63
                    1
## + I(sqrt(chas))
                        50.305 293.10
                   1
## + lstat
                    1
                        50.336 293.38
## + I(dis^-0.5)
                        50.345 293.46
```

```
## target \sim I(nox^-1) + rad
##
                   Df Deviance
##
                                   AIC
                        44.061 233.33
## + medv
                    1
## + I(age^2)
                    1
                        44.442 237.35
                        44.674 239.77
## + I(log(rm))
                    1
## + I(tax^-1)
                        45.017 243.34
                    1
## <none>
                        45.272 243.97
## + I(sqrt(chas)) 1
                        45.113 244.33
## + lstat
                    1
                        45.149 244.71
## + I(dis^-0.5)
                    1
                        45.180 245.03
## + zn
                        45.223 245.47
                    1
## + I(ptratio^2)
                    1
                        45.240 245.64
## + I(log(indus)) 1
                        45.267 245.92
##
## Step: AIC=233.33
## target \sim I(nox^-1) + rad + medv
##
##
                   Df Deviance
                                   AIC
## + I(age^2)
                    1
                        43.027 224.27
## + I(tax^-1)
                    1
                        43.368 227.96
## + I(dis^{-0.5})
                        43.827 232.86
                    1
## + 1stat
                        43.834 232.93
                    1
## + I(log(indus)) 1
                        43.856 233.17
## <none>
                        44.061 233.33
## + I(ptratio^2)
                    1
                        43.956 234.23
## + I(sqrt(chas)) 1
                        44.030 235.01
## + I(log(rm))
                    1
                        44.052 235.24
## + zn
                    1
                        44.060 235.33
##
## Step: AIC=224.27
## target ~ I(nox^-1) + rad + medv + I(age^2)
##
##
                   Df Deviance
                                   AIC
## + I(dis^{-0.5})
                    1
                        42.184 217.05
## + I(tax^-1)
                        42.397 219.40
                    1
## <none>
                        43.027 224.27
## + I(log(indus)) 1
                        42.888 224.77
## + I(ptratio^2)
                        42.975 225.71
                    1
## + I(sqrt(chas))
                        43.004 226.02
                    1
## + lstat
                        43.006 226.05
                    1
## + zn
                        43.013 226.12
                    1
                        43.024 226.24
## + I(log(rm))
                    1
##
## Step: AIC=217.05
## target ~ I(nox^-1) + rad + medv + I(age^2) + I(dis^-0.5)
##
##
                   Df Deviance
                                   AIC
## + I(tax^-1)
                    1
                        41.399 210.29
## + I(log(indus))
                    1
                        41.866 215.53
                        42.184 217.05
## <none>
## + lstat
                    1
                        42.036 217.41
## + I(ptratio^2)
                        42.124 218.39
                    1
## + I(log(rm))
                    1
                        42.150 218.67
```

```
## + I(sqrt(chas)) 1
                       42.169 218.89
## + zn
                        42.173 218.93
                    1
##
## Step: AIC=210.29
## target \sim I(nox^-1) + rad + medv + I(age^2) + I(dis^-0.5) + I(tax^-1)
##
                   Df Deviance
                                  AIC
## + lstat
                        41.180 209.83
## <none>
                        41.399 210.29
## + I(log(indus)) 1
                        41.232 210.42
## + I(ptratio^2)
                        41.318 211.38
                    1
## + I(log(rm))
                    1
                        41.360 211.86
## + I(sqrt(chas))
                    1
                        41.374 212.02
                        41.396 212.27
## + zn
                    1
##
## Step: AIC=209.83
## target \sim I(nox^-1) + rad + medv + I(age^2) + I(dis^-0.5) + I(tax^-1) +
##
       lstat
##
##
                   Df Deviance
                                  AIC
## <none>
                        41.180 209.83
## + I(log(indus))
                        41.012 209.92
                   1
## + I(ptratio^2)
                        41.062 210.49
                    1
## + I(sqrt(chas))
                   1
                        41.159 211.59
## + zn
                    1
                        41.174 211.76
## + I(log(rm))
                    1
                        41.178 211.80
summary(m4)
##
## Call:
  glm(formula = target \sim I(nox^-1) + rad + medv + I(age^2) + I(dis^-0.5) +
       I(tax^-1) + lstat, data = crimeTrain)
## Deviance Residuals:
                         Median
       Min
                   1Q
                                       3Q
                                                Max
## -0.70627 -0.18647 -0.02143
                                  0.13160
                                            0.98687
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept) 2.099e+00 2.682e-01
                                       7.826 3.52e-14 ***
## I(nox^-1)
             -8.407e-01 8.932e-02 -9.413 < 2e-16 ***
                1.258e-02 2.698e-03
## rad
                                      4.661 4.13e-06 ***
## medv
                1.195e-02 2.464e-03
                                       4.850 1.69e-06 ***
## I(age^2)
               2.846e-05 7.544e-06
                                       3.772 0.000183 ***
## I(dis^-0.5) -7.689e-01 2.123e-01 -3.621 0.000326 ***
## I(tax^-1)
              -7.196e+01 2.332e+01 -3.086 0.002155 **
## lstat
               5.686e-03 3.647e-03
                                      1.559 0.119675
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for gaussian family taken to be 0.08991273)
##
##
       Null deviance: 116.47 on 465
                                      degrees of freedom
## Residual deviance: 41.18 on 458 degrees of freedom
```

```
## AIC: 209.83
##
## Number of Fisher Scoring iterations: 2
```

# SELECT MODELS

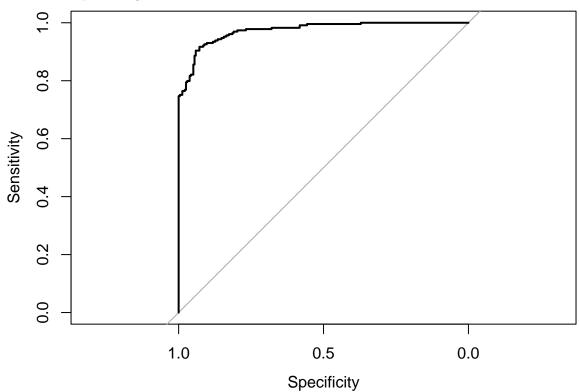
# Compare Model Statistics

#### Model 1 - General Model

## Complete general model

#### **ROC Curve**

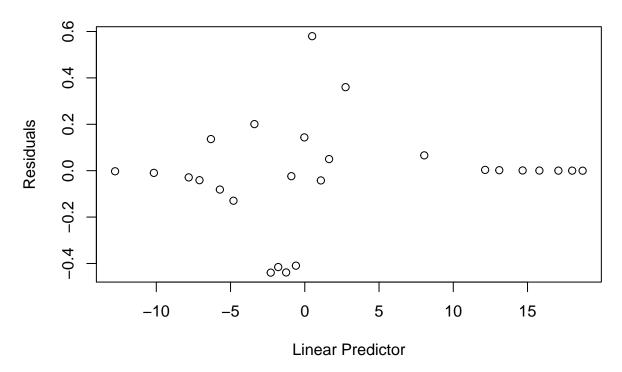
The ROC Curve helps measure true positives and true negative. A high AUC or area under the curve tells us the model is predicting well.



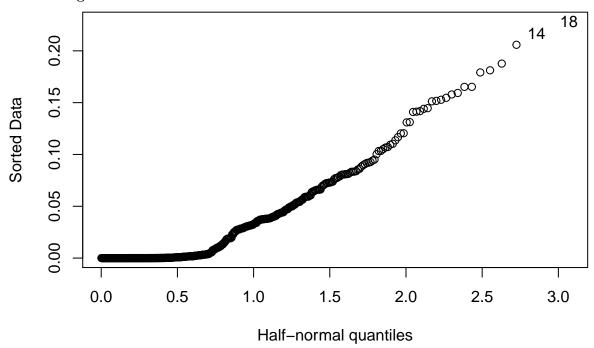
The AUC value of 0.97, tells us this model predicted values are acurate.

#### **Confusion Matrix**

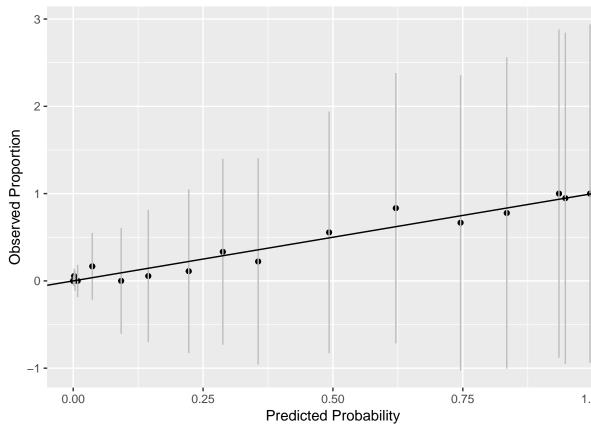
Create a binned diagnostic plot of residuals vs prediction There are definite patterns here, which bear investigating.



## Plot leverages.



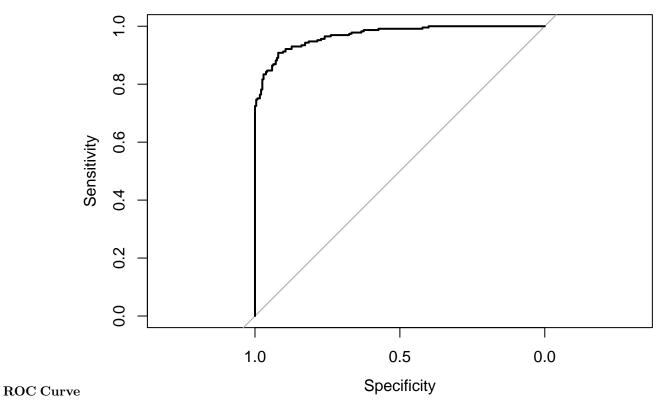
We don't see any strong outliers with the leverage plot. The points identified (14,18) are essentially in the plot of the line formed, so they are not likely pulling our model in any direction.



Plot Goodness of fit

We see that our predictors fall close to the line. (Note to group, need do adjust the min max line)

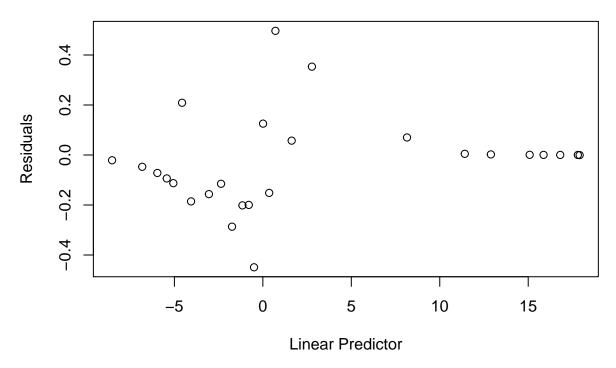
# Reduced general model

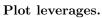


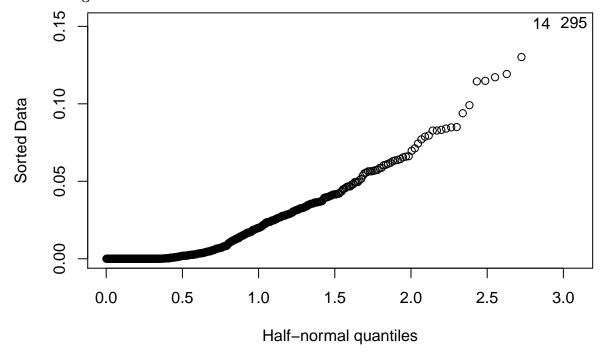
This model also show a high AUC value of 0.97. This tells us predicted values are acurate, although slightly lower.

#### **Confusion Matrix**

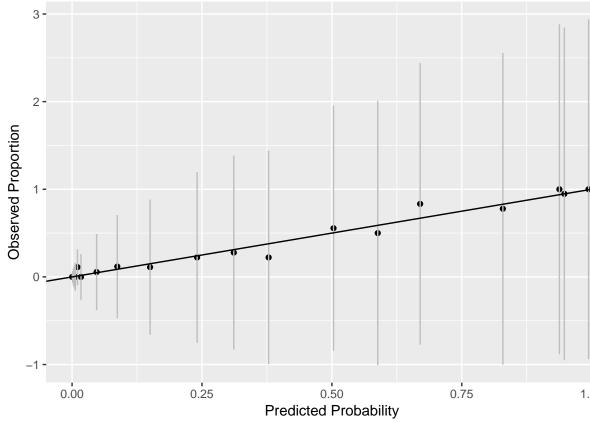
Create a binned diagnostic plot of residuals vs prediction There are definite patterns here, which bear investigating.







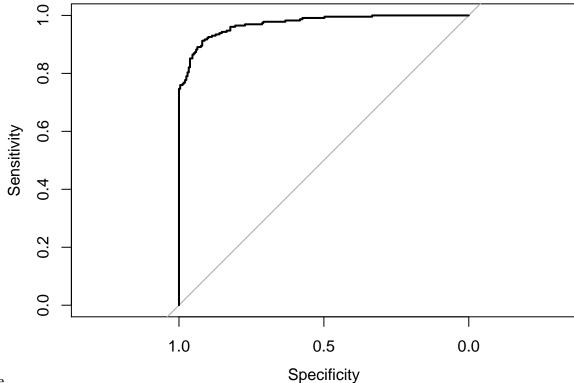
We don't see any strong outliers with the leverage plot. The points identified (14,18) are essentially in the plot of the line formed, so they are not likely pulling our model in any direction.



Plot Goodness of fit

We see that our predictors fall close to the line. (Note to group, need do adjust the min max line)

Model 2 - AIC Model

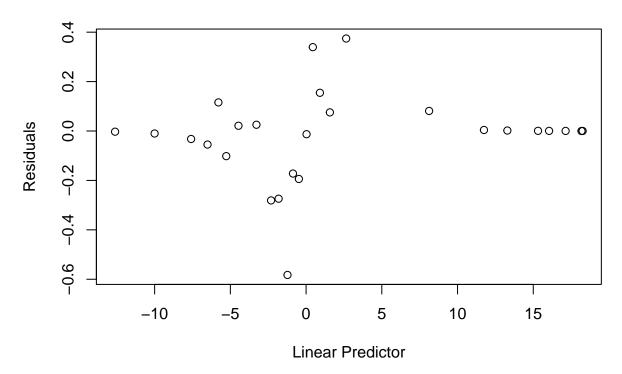


# **ROC Curve**

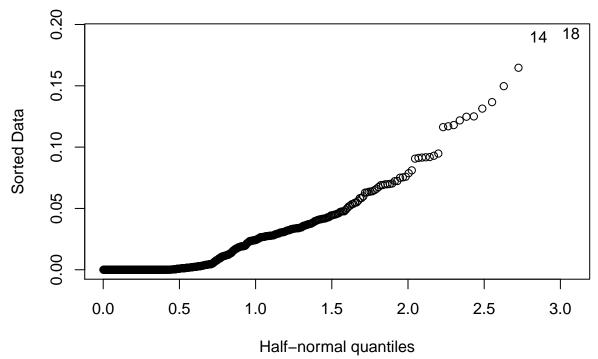
The AUC value of 0.97, tells us this model predicted values are acurate.

## **Confusion Matrix**

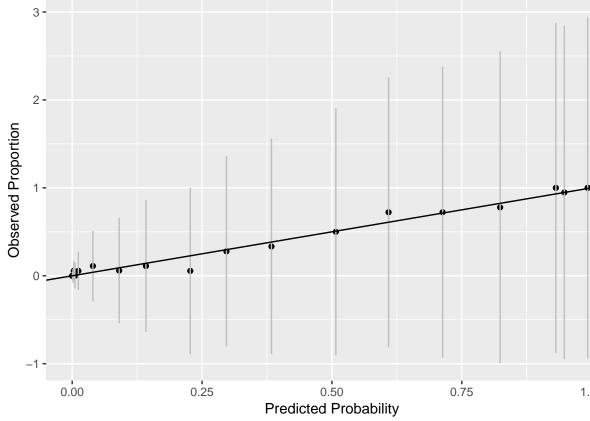
Create a binned diagnostic plot of residuals vs prediction



# Plot leverages.



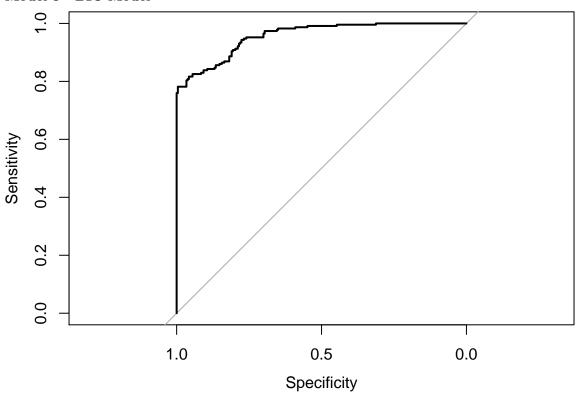
We don't see any strong outliers with the leverage plot. The points identified (14,18) are essentially in the plot of the line formed, so they are not likely pulling our model in any direction.



Plot Goodness of fit

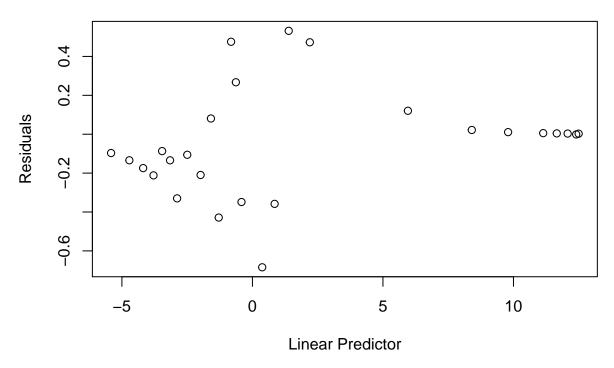
We see that our predictors fall close to the line. (Note to group, need do adjust the min max line)



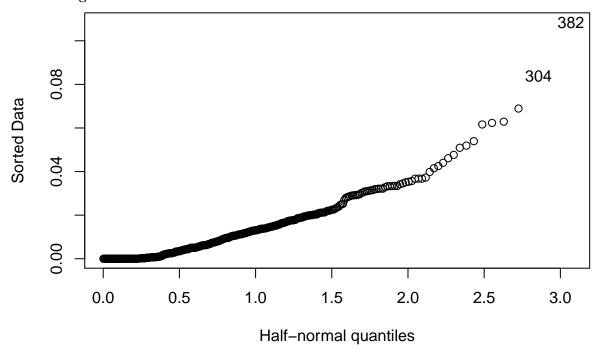


The AUC value of 0.96, although high for this model it has the lowest AUC score.

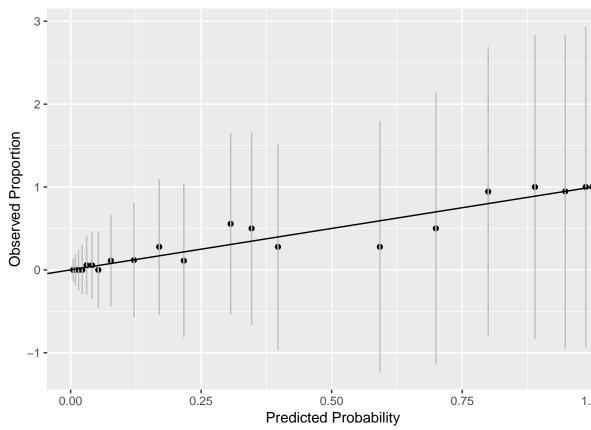
Create a binned diagnostic plot of residuals vs prediction



# Plot leverages.



We don't see any strong outliers with the leverage plot. The points identified (14,18) are essentially in the plot of the line formed, so they are not likely pulling our model in any direction.



#### Plot Goodness of fit

We see that our predictors fall close to the line.

# Pick the best regression model

```
##
## Call:
   glm(formula = target ~ ., family = binomial(link = "logit"),
##
       data = crimeTrain)
##
##
   Deviance Residuals:
##
       Min
                  1Q
                       Median
                                     3Q
                                             Max
##
   -1.8464
            -0.1445 -0.0017
                                0.0029
                                          3.4665
##
## Coefficients:
##
                  Estimate Std. Error z value Pr(>|z|)
## (Intercept) -40.822934
                             6.632913
                                        -6.155 7.53e-10 ***
## zn
                -0.065946
                             0.034656
                                        -1.903
                                                0.05706 .
## indus
                 -0.064614
                             0.047622
                                        -1.357
                                                0.17485
                             0.755546
                                                0.22803
## chas
                  0.910765
                                         1.205
                 49.122297
                             7.931706
                                         6.193 5.90e-10 ***
## nox
                 -0.587488
                             0.722847
                                        -0.813
                                                0.41637
## rm
## age
                  0.034189
                             0.013814
                                         2.475
                                                0.01333 *
## dis
                  0.738660
                             0.230275
                                         3.208
                                                0.00134 **
## rad
                  0.666366
                             0.163152
                                         4.084 4.42e-05 ***
## tax
                 -0.006171
                             0.002955
                                        -2.089
                                                0.03674 *
## ptratio
                  0.402566
                             0.126627
                                         3.179
                                                0.00148 **
                  0.045869
                             0.054049
                                         0.849 0.39608
## lstat
```

```
0.180824
                             0.068294
                                        2.648 0.00810 **
##
  Signif. codes:
##
                     '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
##
   (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 645.88
                              on 465
                                       degrees of freedom
## Residual deviance: 192.05
                              on 453
                                       degrees of freedom
##
  AIC: 218.05
##
## Number of Fisher Scoring iterations: 9
```

Metric	Model 1	Model 2	Model 3	Model 4
AIC	218.0469179	215.3228528	242.7968243	209.8265226
BIC	271.9213312	252.6205235	263.5177525	247.1241933

From the above we see that Model 4, found by using the step forward selection method to do stepwise reduction of models achieves both the lowest AIC and the lowest BIC. Considering that it returns the best by both of those measures, this is the model we will use against future data (e.g., an evaulation dataset.)

#### Conclusion

The final model selected with best AIC and BIC was model 4, which includes a Box Cox transformation. The best logistic regression model without transformation was model 2, with the lowest combination of AIC and BIC. Both model 4 and model 2 were used to predict outcomes using the evaluation data set.

#### Model 4 Evaluation

```
##
                            2
                                         3
                                                                    5
                                                                                  6
##
    0.23290969
                  0.46707798
                               0.53401943
                                             0.47377039
                                                          0.18116389
                                                                        0.22707653
##
                            8
                                         9
                                                                                 12
                                                      10
                                                                   11
    0.31726795
                  0.05238456
                               -0.01928392
                                             0.02079947
                                                          0.36175503
                                                                        0.31684788
##
##
             13
                           14
                                        15
                                                      16
                                                                   17
                                                                                 18
##
    0.62107178
                  0.68536094
                               0.66209469
                                             0.37850731
                                                          0.28928192
                                                                        0.64521511
             19
                           20
                                                                   23
##
                                        21
                                                      22
                                                                                 24
##
    0.13567823
                -0.08554369
                              -0.28393681
                                             0.14893165
                                                          0.27122208
                                                                        0.23111746
             25
                           26
                                        27
                                                                   29
                                                                                 30
##
                                                      28
##
    0.20886975
                  0.26572067
                               0.04522059
                                             1.10529854
                                                          1.14395035
                                                                        0.80086859
##
             31
                           32
                                        33
                                                      34
                                                                   35
                                                                                 36
                                                                        1.10530173
##
    1.10030433
                  1.12005903
                               1.08777600
                                             1.21222859
                                                          1.12788637
##
             37
                           38
                                        39
                                                      40
    1.15076375
                 1.01502028
                               0.54173080
                                            0.41166762
```

#### Model 2 Evaluation

```
2
##
                                          3
   5.187335e-02 6.563639e-01 7.292303e-01 4.263767e-01 1.075746e-01
##
              6
                                          8
                                                        9
                                                                    10
##
  3.126897e-01 3.879178e-01 1.399105e-02 5.651298e-03 1.860232e-03
##
             11
                           12
                                         13
                                                       14
                                                                    15
## 5.023729e-01 4.167837e-01 8.408851e-01 7.429792e-01 6.503036e-01
                                         18
                                                       19
##
                           17
                                                                    20
  1.492647e-01 4.026110e-01 9.672516e-01 7.932839e-02 8.509218e-07
                                         23
                                                      24
## 3.840253e-06 5.173182e-02 1.517637e-01 1.987527e-01 1.781289e-01
```

```
## 26 27 28 29 30

## 6.770735e-01 1.355059e-04 1.000000e+00 1.000000e+00 9.999947e-01

## 31 32 33 34 35

## 1.000000e+00 1.000000e+00 1.000000e+00 1.000000e+00

## 36 37 38 39 40

## 1.000000e+00 1.000000e+00 9.999999e-01 8.022854e-01 3.953354e-01
```

For model 2 we can also use a threshold of 0.5, or 50%, and compute the binary prediction.

All models were computed using the entire training dataset. Because models were selected using AIC and BIC metrics rather than evaluating them using cross validation, the dataset was not initially split in training and validate. Similar results are obtained performing this split, as can be seen by reproducing model 2 with only 80% of the training set.

```
## Start: AIC=218.05
## target ~ zn + indus + chas + nox + rm + age + dis + rad + tax +
       ptratio + lstat + medv
##
##
             Df Deviance
                  192.71 216.71
## - rm
              1
                   192.77 216.77
## - 1stat
              1
## - chas
              1
                   193.53 217.53
## - indus
              1
                  193.99 217.99
                   192.05 218.05
## <none>
## - tax
                  196.59 220.59
              1
                  196.89 220.89
## - zn
              1
## - age
                  198.73 222.73
              1
## - medv
              1
                   199.95 223.95
## - ptratio
              1
                  203.32 227.32
## - dis
                  203.84 227.84
                  233.74 257.74
## - rad
              1
## - nox
                  265.05 289.05
##
## Step: AIC=216.71
## target ~ zn + indus + chas + nox + age + dis + rad + tax + ptratio +
##
       1stat + medv
##
##
             Df Deviance
## - chas
                  194.24 216.24
                  194.32 216.32
## - 1stat
              1
## - indus
                  194.58 216.58
## <none>
                   192.71 216.71
## - tax
                   197.59 219.59
              1
## - zn
              1
                   198.07 220.07
## - age
              1
                   199.11 221.11
## - ptratio
              1
                  203.53 225.53
## - dis
              1
                  203.85 225.85
## - medv
                  205.35 227.35
              1
## - rad
              1
                  233.81 255.81
## - nox
              1
                  265.14 287.14
##
```

```
## Step: AIC=216.24
## target ~ zn + indus + nox + age + dis + rad + tax + ptratio +
      lstat + medv
##
##
           Df Deviance
                       AIC
## - indus 1 195.51 215.51
## <none>
                194.24 216.24
          1 196.33 216.33
## - lstat
## - zn
            1
                200.59 220.59
## - tax
                200.75 220.75
            1
## - age
             1
                201.00 221.00
                203.94 223.94
## - ptratio 1
                204.83 224.83
## - dis
             1
## - medv
               207.12 227.12
            1
## - rad
           1 241.41 261.41
            1 265.19 285.19
## - nox
##
## Step: AIC=215.51
## target ~ zn + nox + age + dis + rad + tax + ptratio + lstat +
      medv
##
##
           Df Deviance AIC
          1 197.32 215.32
## - lstat
## <none>
                195.51 215.51
## - zn
            1 202.05 220.05
## - age
            1
               202.23 220.23
## - ptratio 1
                205.01 223.01
## - dis
            1
                205.96 223.96
## - tax
            1 206.60 224.60
## - medv
           1 208.13 226.13
            1 249.55 267.55
## - rad
## - nox
            1 270.59 288.59
##
## Step: AIC=215.32
## target ~ zn + nox + age + dis + rad + tax + ptratio + medv
           Df Deviance
##
                        AIC
## <none>
                197.32 215.32
## - zn
               203.45 219.45
            1
## - ptratio 1 206.27 222.27
## - age
            1
                207.13 223.13
## - tax
             1
                207.62 223.62
## - dis
               207.64 223.64
            1
## - medv
            1 208.65 224.65
## - rad
           1 250.98 266.98
           1 273.18 289.18
## - nox
##
## glm(formula = target ~ zn + nox + age + dis + rad + tax + ptratio +
##
      medv, family = binomial(link = "logit"), data = crimeTrain)
##
## Deviance Residuals:
##
      Min
           1Q Median
                                3Q
                                        Max
```

```
## -1.8295 -0.1752 -0.0021
                                0.0032
                                         3.4191
##
## Coefficients:
##
                 Estimate Std. Error z value Pr(>|z|)
## (Intercept) -37.415922
                            6.035013
                                      -6.200 5.65e-10 ***
                -0.068648
                                       -2.144 0.03203 *
## zn
                            0.032019
## nox
                42.807768
                            6.678692
                                        6.410 1.46e-10 ***
## age
                 0.032950
                            0.010951
                                        3.009
                                               0.00262 **
## dis
                 0.654896
                            0.214050
                                        3.060
                                               0.00222 **
## rad
                 0.725109
                            0.149788
                                        4.841 1.29e-06 ***
## tax
                -0.007756
                            0.002653
                                       -2.924
                                               0.00346 **
## ptratio
                 0.323628
                            0.111390
                                        2.905
                                               0.00367 **
## medv
                 0.110472
                            0.035445
                                        3.117
                                               0.00183 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
  (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 645.88
                              on 465
                                      degrees of freedom
## Residual deviance: 197.32
                              on 457
                                       degrees of freedom
## AIC: 215.32
##
## Number of Fisher Scoring iterations: 9
```

The final model preservers the predictors in the model with 100% of the training set. With the remaining 20% we can also build a confusion matrix, with similar results as seen in the analysis.

```
## ## targethat 0 1 ## 0 43 4 ## 1 2 45
```

## APPENDIX

#### Code used in analysis

library(ggplot2) library(tidyr) library(MASS) library(psych) library(kableExtra) library(dplyr) library(faraway) library(gridExtra) library(reshape2) library(leaps) library(pROC) library(caret) library(naniar) library(pROC) crimeTrain <- read.csv("crime-training-data\_modified.csv") crimeEval <- read.csv("crime-evaluation-data\_modified.csv")

#### **OVERVIEW**

In this homework assignment, we will explore, analyze and model a data set containing information on crime for various neighborhoods of a major city. Each record has a response variable indicating whether or not the crime rate is above the median crime rate (1) or not (0).

#### Objective:

The objective is to build a binary logistic regression model on the training data set to predict whether the neighborhood will be at risk for high crime levels.

#### DATA EXPLORATION

#### Data Summary

 $\begin{array}{l} {\rm crimed 1 < - describe(crimeTrain, na.rm = F) \ crimed1} \\ {\rm na.cm = F) \ crimed1} \\ {\rm na.$ 

 $colsTrain < -ncol(crimeTrain) colsEval < -ncol(crimeEval) \ missingCol < -colnames(crimeTrain) [!(colnames(crimeTrain) \ missingCol < -colnames(crimeTrain) \$ 

The dataset consists of two data files: training and evaluation. The training dataset contains 13 columns, while the evaluation dataset contains 12. The evaluation dataset is missing column target which represend our responce variable and defines whether the crime rate is above the median crime rate (1) or not (0). We will start by exploring the training data set since it will be the one used to generate the regression model.

 $\label{eq:text-sum} $$\operatorname{text}^{-\alpha}$ is $\operatorname{data}$ is numeric" ) = TRUE $$\{$ \operatorname{text}^{-\alpha}$ in $\operatorname{data}$ is numeric" }$$ else $$\{$ \operatorname{text}^{-\alpha}$ or all data is numeric" }$$ maxMeanMedianDiff<-round(max(abs(sapply(crimeTrain, median, na.rm = T) - sapply(crimeTrain, mean, na.rm = T))*100/(sapply(crimeTrain, max, na.rm = T)-sapply(crimeTrain, min, na.rm = T))),2)$$$ 

First we see that all data is numeric. The dataset does contain one dummy variable to identify if the property borders the Charles River (1) or not (0).

 $nas < -as. data. frame(sapply(crimeTrain, function(x) sum(is.na(x)))) nasp < -as. data. frame(sapply(crimeTrain, function(x) round(sum(is.na(x))/nrow(crimeTrain) 100,1))) \\ colnames(nas) < -c("name") maxna < -max(nas) \\ maxnaname < -rownames(nas)/nas \\ name = = maxna \\ percent < -round(maxna/nrow(crimeTrain) 100,1))$ 

An important aspect of any dataset is to determine how much, if any, data is missing. We look at all the variables to see which if any have missing data. We look at the basic descriptive statistics as well as the missing data and their percentages:

 $kable(crimed1, "html", escape = F) \%>\% \ kable\_styling(bootstrap\_options = c("striped", "hover", "condensed"), full\_width = T) \%>\% \ column\_spec(1, bold = T) \%>\% \ scroll\_box(width = "100\%", height = "500px") \ sapply(crimeTrain, function(x) \ round(sum(is.na(x))/nrow(crimeTrain)*100,1)) \ vis\_miss(crimeTrain) \ head(crimeTrain)$ 

Missing and Invalid Data

No missing data was found in the dataset.

With missing data assessed, we can look into the data in more detail. To visualize this we plot histograms for each data. Several predictors like dist, chas, rad, zn and tax are not normally distributed and noticable outliers.

attach(crimeTrain[,-1]) ggplot(gather(crimeTrain[,-1]), aes(value)) + geom\_histogram(bins = 20) + facet\_wrap(~key, scales = "free\_x") stripchart(data.frame(scale(crimeTrain)), method = "jitter", las=2, vertical=TRUE)

Mathematical transformations.

Box Cox The Box Cox transformation tries to transform non-normal data into a normal distribution. This transformation attemps to estimate the  $\lambda$  for Y. With the exception of tax, all predictors have either no transformation extimate or were given a fudge value of 0.

crimeTrain bct <- apply(crimeTrain, 2, BoxCoxTrans) crimeTrain bct

Variable Creation / Removal

To determine how we can combine variables to create new one we start by looking at a correlation plot. The plot and cor funtion lists nox, age, rad,tax and indus as the strongest postively correlated predictors, while rad and distance are the strongest negatively correlated predictors. cor(crimeTrain\$target, crimeTrain[-c(1)], use="na.or.complete")

corrplot::corrplot(cor(crimeTrain[,1:13]), order = "hclust", method='square', addrect = 2, tl.col = "black", tl.cex = .75, na.label = " ")

BUILD MODELS

General regression

We start by building a model with all the predictors in the dataset.

```
m1<-glm(target~.,data=crimeTrain,family="binomial"(link="logit")) summary(m1)
```

The Summary of this model shows several predictor are not relevant. We build a second model without these predictors.

```
m1.1 < -glm(target \sim nox + age + dis + rad + tax + ptratio + medv, data = crimeTrain, family = "binomial" (link = "logit")) \\ summary(m1.1)
```

1-pchisq(m1.1deviance, m1.1df.residual) 1-pchisq(m1deviance, m1df.residual)

The new model has a slightly higher AIC which would tells us the first model is slightly less complex. For the 2 data sets p-value = 1 - pchisq(deviance, degrees of freedom) are 1. The Null hypothesis is still supported.

AIC Step Method Another way of selecting which predictors to use in the model is by calculating the AIC of the model. This metric is similar to the adjusted R-square of a model in that it penalizes models with more predictors over simpler model with few predictors. We use Stepwise function in r to find the lowest AIC with different predictors.

```
m2 < -step(m1) summary(m2)
```

This reduces the predictors used in the model to these: zn nox age dis rad tax ptRation medv

It Removes these predictors: indus chas rm#

The AIC improves marginally from 218.05 (our original general model) to 215.32, but we also benefit by having a simpler model less prone to overfitting.

Also, the predictors in the model now are all significant (under 0.05 pr level) and all but one under .01 or very significant. Which is much improved over the prior model

BIC Method

To determine the number of predictors and which predictors to be used we will use the Bayesian Information Criterion (BIC).

```
regfit.full <- regsubsets(factor(target) ~ ., data=crimeTrain) par(mfrow = c(1,2)) reg.summary <- summary(regfit.full) plot(reg.summarybic, xlab = "NumberofPredictors", ylab = "BIC", type = "l", main = "SubsetSelectionUsingBIC")BIC_num < -which.min(reg.summarybic) points(BIC_num, reg.summary$bic[BIC_num], col="red", cex=2, pch=20) plot(regfit.full, scale="bic", main="Predictors vs. BIC") par(mfrow = c(1,1))
```

The plot on the right shows that the number of predictors with the lowest BIC are nox , age, rad, and medv. We will use those predictors to build the next model

```
m3 < glm(target \sim nox + age + rad + medv, family=binomial, data = crimeTrain) crimeTrainpredicted_m3 < -predict(m3, crimeTrain, type = 'response')crimeTraintarget_m3target < -ifelse(crimeTrainpredicted_m3>0.5, 1, 0) pander::pander(summary(m3))
```

Forward Selection Method using some BoxCox transformed independent variables:

```
{r} m4 <- step(glm(target~1, data=crimeTrain), direction = "forward", scope = ~zn + I(log(indus)) + I(sqrt(chas)) + I(nox^-1) + I(log(rm)) + I(age^2) + I(dis^-.5) + rad + I(tax^-1) + I(ptratio^2) + lstat + medv) summary(m4)
```

SELECT MODELS Compare Model Statistics

Model 1 - General Model

Complete general model

#### **ROC Curve**

The ROC Curve helps measure true positives and true negative. A high AUC or area under the curve tells us the model is predicting well.

targethat<-predict(m1,type="response") g<-roc(target~targethat,data=crimeTrain) plot(g)

The AUC value of 0.96, tells us this model predicted values are acurate.

#### **Confusion Matrix**

targethat[targethat<0.5]<-0 targethat[targethat>=0.5]<-1 table(targethat,crimeTrain\$target)

Create a binned diagnostic plot of residuals vs prediction There are definite patterns here, which bear investigating.

crimeMut <- mutate(crimeTrain, Residuals = residuals(m1), linPred = predict(m1)) grpCrime <- group\_by(crimeMut, cut(linPred, breaks=unique(quantile(linPred, (0:25/26))))) diagCrime <- summarise(grpCrime, Residuals = mean(Residuals), linPred = mean(linPred)) plot(Residuals ~ linPred, data = diagCrime, xlab="Linear Predictor")

#### Plot leverages.

halfnorm(hatvalues(m1))

We don't see any strong outliers with the leverage plot. The points identified (14,18) are essentially in the plot of the line formed, so they are not likely pulling our model in any direction.

#### Plot Goodness of fit

linPred <- predict(m1) crimeMut <- mutate(crimeTrain, predProb = predict(m1, type = "response")) grpCrime <- group\_by(crimeMut, cut(linPred, breaks = unique(quantile(linPred, (0:25)/26))))

 $\label{eq:hldf} $$ hlDf <- summarise(grpCrime, y= sum(target), pPred=mean(predProb), count = n()) \ hlDf <- mutate(hlDf, se.fit=sqrt(pPred * (1-(pPred)/count))) \ ggplot(hlDf,aes(x=pPred,y=y/count,ymin=y/count-2se.fit,ymax=y/count+2se.fit)) + geom_point()+geom_linerange(color=grey(0.75))+geom_abline(intercept=0,slope=1) + xlab("Predicted Probability") + ylab("Observed Proportion")$ 

We see that our predictors fall close to the line. (Note to group, need do adjust the min max line)

Reduced general model

#### **ROC Curve**

targethat<-predict(m1.1,type="response") g<-roc(target~targethat,data=crimeTrain) plot(g)

This model also show a high AUC value of 0.96. This tells us predicted values are acurate, although slightly lower.

#### **Confusion Matrix**

targethat[targethat<0.5]<-0 targethat[targethat>=0.5]<-1 table(targethat,crimeTrain\$target)

Create a binned diagnostic plot of residuals vs prediction There are definite patterns here, which bear investigating.

crimeMut <- mutate(crimeTrain, Residuals = residuals(m1.1), linPred = predict(m1.1)) grpCrime <- group\_by(crimeMut, cut(linPred, breaks=unique(quantile(linPred, (0:25/26))))) diagCrime <- summarise(grpCrime, Residuals = mean(Residuals), linPred = mean(linPred)) plot(Residuals ~ linPred, data = diagCrime, xlab="Linear Predictor")

#### Plot leverages.

halfnorm(hatvalues(m1.1))

We don't see any strong outliers with the leverage plot. The points identified (14,18) are essentially in the plot of the line formed, so they are not likely pulling our model in any direction.

#### Plot Goodness of fit

```
 linPred <- predict(m1.1) \ crimeMut <- \ mutate(crimeTrain, \ predProb = predict(m1.1, \ type = "response")) \ grpCrime <- \ group\_by(crimeMut, \ cut(linPred, \ breaks = unique(quantile(linPred, \ (0:25)/26))))
```

 $\label{eq:hldf} $$hlDf <- summarise(grpCrime, y= sum(target), pPred=mean(predProb), count = n()) \ hlDf <- mutate(hlDf, se.fit=sqrt(pPred * (1-(pPred)/count))) \ ggplot(hlDf,aes(x=pPred,y=y/count,ymin=y/count-2se.fit,ymax=y/count+2se.fit)) + geom_point()+geom_linerange(color=grey(0.75))+geom_abline(intercept=0,slope=1) + xlab("Predicted Probability") + ylab("Observed Proportion")$ 

We see that our predictors fall close to the line. (Note to group, need do adjust the min max line)

Model 2 - AIC Model

#### **ROC Curve**

targethat<-predict(m2,type="response") g<-roc(target~targethat,data=crimeTrain) plot(g)

The AUC value of 0.96, tells us this model predicted values are acurate.

#### **Confusion Matrix**

targethat[targethat<0.5]<-0 targethat[targethat>=0.5]<-1 table(targethat,crimeTrain\$target)

#### Create a binned diagnostic plot of residuals vs prediction

crimeMut <- mutate(crimeTrain, Residuals = residuals(m2), linPred = predict(m2)) grpCrime <- group\_by(crimeMut, cut(linPred, breaks=unique(quantile(linPred, (0:25/26))))) diagCrime <- summarise(grpCrime, Residuals = mean(Residuals), linPred = mean(linPred)) plot(Residuals ~ linPred, data = diagCrime, xlab="Linear Predictor")

#### Plot leverages.

halfnorm(hatvalues(m2))

We don't see any strong outliers with the leverage plot. The points identified (14,18) are essentially in the plot of the line formed, so they are not likely pulling our model in any direction.

#### Plot Goodness of fit

```
linPred <- predict(m2) crimeMut <- mutate(crimeTrain, predProb = predict(m2, type = "response")) grpCrime <- group_by(crimeMut, cut(linPred, breaks = unique(quantile(linPred, (0:25)/26))))
```

 $\label{eq:hldf} $$hlDf <- summarise(grpCrime, y= sum(target), pPred=mean(predProb), count = n()) \ hlDf <- mutate(hlDf, se.fit=sqrt(pPred * (1-(pPred)/count))) \ ggplot(hlDf,aes(x=pPred,y=y/count,ymin=y/count-2se.fit,ymax=y/count+2se.fit)) + geom_point()+geom_linerange(color=grey(0.75))+geom_abline(intercept=0,slope=1) + xlab("Predicted Probability") + ylab("Observed Proportion")$ 

We see that our predictors fall close to the line. (Note to group, need do adjust the min max line)

Model 3 - BIC Model

 $targethat < -predict(m3, type="response") \ g < -roc(target \sim targethat, data = crimeTrain) \ plot(g) \ targethat[targethat < 0.5] < -0 \ targethat[targethat > = 0.5] < -1 \ table(targethat, crimeTrain\$target)$ 

The AUC value of 0.96, although high for this model it has the lowest AUC score.

#### Create a binned diagnostic plot of residuals vs prediction

crimeMut <- mutate(crimeTrain, Residuals = residuals(m3), linPred = predict(m3)) grpCrime <- group\_by(crimeMut, cut(linPred, breaks=unique(quantile(linPred, (0:25/26))))) diagCrime <- summarise(grpCrime, Residuals = mean(Residuals), linPred = mean(linPred)) plot(Residuals ~ linPred, data = diagCrime, xlab="Linear Predictor")

#### Plot leverages.

halfnorm(hatvalues(m3))

We don't see any strong outliers with the leverage plot. The points identified (14,18) are essentially in the plot of the line formed, so they are not likely pulling our model in any direction.

#### Plot Goodness of fit

```
 lin Pred <- \ predict(m3) \ crime Mut <- \ mutate(crime Train, \ pred Prob = predict(m3, \ type = "response")) \\ grp Crime <- \ group\_by(crime Mut, \ cut(lin Pred, \ breaks = unique(quantile(lin Pred, \ (0:25)/26)))) \\
```

 $\label{eq:hldf} $$hlDf <- summarise(grpCrime, y= sum(target), pPred=mean(predProb), count = n()) \ hlDf <- mutate(hlDf, se.fit=sqrt(pPred * (1-(pPred)/count))) \ ggplot(hlDf,aes(x=pPred,y=y/count,ymin=y/count-2se.fit,ymax=y/count+2se.fit)) + geom_point()+geom_linerange(color=grey(0.75))+geom_abline(intercept=0,slope=1) + xlab("Predicted Probability") + ylab("Observed Proportion")$ 

We see that our predictors fall close to the line.

Pick the best regression model

```
m1AIC <- AIC(m1) \ m1BIC <- BIC(m1) \ m2AIC <- AIC(m2) \ m2BIC <- BIC(m2) \ m3AIC <- AIC(m3) \ m3BIC <- BIC(m3) \ m4AIC <- AIC(m4) \ m4BIC <- BIC(m4) \ summary(m1)
```