	u_0	u_1	u_2	u_3	u_4	u_5	u_6
i_0	5	5	2	0	1	?	?
i_1	4	?	?	0	?	2	?
i_2	?	4	1	?	?	1	1
i_3	2	2	3	4	4	?	4
i_4	2	0	4	?	?	?	5
	↓	↓	↓	↓	↓	↓	↓
$\bar{u}_j$	3.25	2.75	2.5	1.33	2.5	1.5	3.33

a) Original utility matrix $\mathbf{Y}$ and mean user ratings.

	u_0	u_1	u_2	u_3	u_4	u_5	u_6
i_0	1.75	2.25	-0.5	-1.33	-1.5	0	0
i_1	0.75	0	0	-1.33	0	0.5	0
i_2	0	1.25	-1.5	0	0	-0.5	-2.33
i_3	-1.25	-0.75	0.5	2.67	1.5	0	0.67
i_4	-1.25	-2.75	1.5	0	0	0	1.67

b) Normalized utility matrix $\bar{\mathbf{Y}}$.

	u_0	u_1	u_2	u_3	u_4	u_5	u_6
u_0	1	0.83	-0.58	-0.79	-0.82	0.2	-0.38
u_1	0.83	1	-0.87	-0.40	-0.55	-0.23	-0.71
u_2	-0.58	-0.87	1	0.27	0.32	0.47	0.96
u_3	-0.79	-0.40	0.27	1	0.87	-0.29	0.18
u_4	-0.82	-0.55	0.32	0.87	1	0	0.16
u_5	0.2	-0.23	0.47	-0.29	0	1	0.56
u_6	-0.38	-0.71	0.96	0.18	0.16	0.56	1

c) User similarity matrix $\mathbf{S}$.

	u_0	u_1	u_2	u_3	u_4	u_5	u_6
i_0	1.75	2.25	-0.5	-1.33	-1.5	0.18	-0.63
i_1	0.75	0.48	-0.17	-1.33	-1.33	0.5	0.05
i_2	0.91	1.25	-1.5	-1.84	-1.78	-0.5	-2.33
i_3	-1.25	-0.75	0.5	2.67	1.5	0.59	0.67
i_4	-1.25	-2.75	1.5	1.57	1.56	1.59	1.67

d) $\hat{\mathbf{Y}}$

Predict normalized rating of u_1 on i_1 with $k = 2$

Users who rated i_1 : $\{u_0, u_3, u_5\}$

Corresponding similarities: {0.83, -0.40, -0.23}

$\Rightarrow$ most similar users: $\mathcal{N}(u_1, i_1) = \{u_0, u_5\}$

with **normalized ratings {0.75, 0.5}**

$$\Rightarrow \hat{y}_{i_1,u_1} = \frac{0.83 * 0.75 + (-0.23) * 0.5}{0.83 + |-0.23|} \approx 0.48$$

e) Example

	u_0	u_1	u_2	u_3	u_4	u_5	u_6
i_0	5	5	2	0	1	1.68	2.70
i_1	4	3.23	2.33	0	1.67	2	3.38
i_2	4.15	4	1	-0.5	0.71	1	1
i_3	2	2	3	4	4	2.10	4
i_4	2	0	4	2.9	4.06	3.10	5

f) Full $\mathbf{Y}$