

## Practice Exercise 7: O-notation

**Exercises a-b.** Suppose that each of the following expressions represents the number of logical operations in an algorithm as a function of  $n$ , the size of the list being manipulated. For each expression, determine the **dominant term** and then classify the algorithm in **simplified O-notation**.

(a).  $1000n^3 + n^2 \log_{10} n + 2n^3 \log_2 n + 20200^7$

- 1a. What is the dominant term?
- 1b. What is the O-notation?

(b).  $8n^2 + 7^{89} \log_8 n + 2^n + 56n^4$

- 2a. What is the dominant term?
- 2b. What is the O-notation?

**Exercises c-k.** Find the running time (O-notation) in terms of  $n$  for each section. Do *not* try to understand what the functions do, but simply look at their execution times.

### Exercise (c)

```
int function computation(int result, int n)
{
    for (int i = 3; i <= n; ++i)
        result += i * n;
    return result;
}
```

### Exercise (d)

```
void function tables(int k)
{
    for (int i = 0; i < k; ++i)
        for (int j = 0; j <= k; ++j)
            a[i] += a[j] + i + j;
}
```

### Exercise (e)

```
long factorial (int n)
{
    if (n <= 1)
        return 1;
    else
        return n * factorial (n - 1);
}
```

**Exercise (f)**

```
bool DoublyList::search(const int& searchData) const
{
    bool found = false;
    Node *current = first;

    while (current != NULL && !found)
    {
        if (current->getData() == searchData)
            found = true;
        else
            current = current->getNextLink();
    }
    return found;
}
```

**Exercise (g)**

```
void modifyArray(int a[], int size, int item)
{
    int max = a[0];

    for (int i = 1; i < size / 2; ++i)
    {
        if (max < a[i])
            max = a[i];
    }
    for (int j = 1; j <= size; ++j)
    {
        ++max;
        cout << max;
    }
}
```

**Exercise (h)**

```
void doSomething(int n)
{
    for (int k = 1; k <= n / 2; ++k)
    {
        cout << (k * k) << endl;
        for (int j = 1; j <= n; ++j)
            cout << (n * n * n * n) << " ";
    }
}
```

**Exercise (i)**

```
bool myFunction (int k)
{
    int x = k + 2;
    while (x > 1) x /= 2;
    return (k > x);
}
```

**Exercise (j)**

```
bool anotherFunction(const vector<int>& v1)
{
    if (v1.size() == 0) return false;
    else
    {
        int size = static_cast<int>(v1.size());
        for (unsigned int i = 0; i < size - 1; ++ i)
            for (unsigned int j = size/2; j < size - 1; ++j)
                if (v1[i] != v1[j+1]) return true;
    }
    return false;
}
```

**Exercise (k)**

```
void thisFunction(int n)
{
    for (int k = 0; k < n; ++k)
    {
        j = n;
        while (j > 0)
        {
            cout << j << " ";
            j /= 2;
        }
    }
}
```