

```
In [1]: 1 import numpy as np
        2 import pandas as pd
        3 from numpy import *
```

```
In [2]: 1 #Câu 1:
        2
        3 data = np.loadtxt("bostonh.dat")
        4 print(data)

[[6.3200e-03 1.8000e+01 2.3100e+00 ... 3.9690e+02 4.9800e+00 2.4000e+01]
 [2.7310e-02 0.0000e+00 7.0700e+00 ... 3.9690e+02 9.1400e+00 2.1600e+01]
 [2.7290e-02 0.0000e+00 7.0700e+00 ... 3.9283e+02 4.0300e+00 3.4700e+01]
 ...
 [6.0760e-02 0.0000e+00 1.1930e+01 ... 3.9690e+02 5.6400e+00 2.3900e+01]
 [1.0959e-01 0.0000e+00 1.1930e+01 ... 3.9345e+02 6.4800e+00 2.2000e+01]
 [4.7410e-02 0.0000e+00 1.1930e+01 ... 3.9690e+02 7.8800e+00 1.1900e+01]]
```

```
In [3]: 1 #Câu 2:
        2
        3 X = np.append(np.ones((len(data),1)),data[:,13],axis =1)
        4 print(X)
        5 print("-----")
        6 Y = data.transpose()[-1].reshape(len(data),1)
        7 print(Y)

[[1.0000e+00 6.3200e-03 1.8000e+01 ... 1.5300e+01 3.9690e+02 4.9800e+00]
 [1.0000e+00 2.7310e-02 0.0000e+00 ... 1.7800e+01 3.9690e+02 9.1400e+00]
 [1.0000e+00 2.7290e-02 0.0000e+00 ... 1.7800e+01 3.9283e+02 4.0300e+00]
 ...
 [1.0000e+00 6.0760e-02 0.0000e+00 ... 2.1000e+01 3.9690e+02 5.6400e+00]
 [1.0000e+00 1.0959e-01 0.0000e+00 ... 2.1000e+01 3.9345e+02 6.4800e+00]
 [1.0000e+00 4.7410e-02 0.0000e+00 ... 2.1000e+01 3.9690e+02 7.8800e+00]]
-----
[[24. ]
```

```
In [4]: 1 #Câu 3:
2
3 x_T = X.transpose()
4 print(x_T)
5 #Tính vecto B
6 beta = linalg.inv(x_T.dot(X)).dot(x_T).dot(Y)
7 print(beta)

[[ 1.0000e+00  1.0000e+00  1.0000e+00 ...  1.0000e+00  1.0000e+00  1.0000e+00]
 [ 6.3200e-03  2.7310e-02  2.7290e-02 ...  6.0760e-02  1.0959e-01  4.7410e-02]
 [ 1.8000e+01  0.0000e+00  0.0000e+00 ...  0.0000e+00  0.0000e+00  0.0000e+00]
 ...
 [ 1.5300e+01  1.7800e+01  1.7800e+01 ...  2.1000e+01  2.1000e+01  2.1000e+01]
 [ 3.9690e+02  3.9690e+02  3.9283e+02 ...  3.9690e+02  3.9345e+02  3.9690e+02]
 [ 4.9800e+00  9.1400e+00  4.0300e+00 ...  5.6400e+00  6.4800e+00  7.8800e+00]]
[[ 3.64594884e+01]
 [-1.08011358e-01]
 [ 4.64204584e-02]
 [ 2.05586264e-02]
 [ 2.68673382e+00]
 [-1.77666112e+01]
 [ 3.80986521e+00]
 [ 6.92224640e-04]
 [-1.47556685e+00]
 [ 3.06049479e-01]
 [-1.23345939e-02]
 [-9.52747232e-01]
 [ 9.31168327e-03]
 [-5.24758378e-01]]
```

```
In [5]: 1 #Câu 4:
2 #Tính C:
3
4 C = linalg.inv(x_T.dot(X))
5 print(C)
```

```
In [5]: 1 #Câu 4:
2 #Tính C:
3
4 C = linalg.inv(x_T.dot(X))
5 print(C)

[[ 1.15665067e+00 -4.79507297e-04 -7.27912374e-05  7.81007312e-04
 -5.30636011e-03 -4.72633728e-01 -6.72009691e-02  2.52574657e-04
 -1.60858766e-02  4.27955175e-03 -9.32179147e-05 -1.77832398e-02
 -1.77463251e-04 -3.44062107e-03]
 [-4.79507297e-04  4.79667291e-05 -1.74622146e-06  3.33058300e-06
  6.29163676e-05  3.32353579e-04  1.60589501e-05 -6.44104667e-08
  3.40052584e-05 -2.58500572e-05  6.50408184e-08  3.99960618e-06
  4.60269987e-07 -1.13029256e-05]
 [-7.27912374e-05 -1.74622146e-06  8.36861245e-06  3.98676259e-06
 -7.75453928e-06  8.33368670e-05 -3.96939822e-05  9.71684642e-07
 -4.89624081e-05  4.27993705e-06 -5.11685476e-07  2.48176992e-05
 -1.86831132e-08 -1.64268535e-06]
 [ 7.81007312e-04  3.33058300e-06  3.98676259e-06  1.67943163e-04
 -2.42364262e-04 -2.75364026e-03  1.04925166e-04 -3.97527513e-08
  1.14987074e-04  5.04398943e-05 -4.49769287e-06 -4.64149258e-05
  2.43976935e-07 -1.05525682e-05]
 [-5.30636011e-03  6.29163676e-05 -7.75453928e-06 -2.42364262e-04
  3.29658256e-02 -4.90317797e-03 -4.98480956e-04 -2.56627859e-05
  1.20331081e-04 -2.73145702e-04  1.74383419e-05  4.68840845e-04
 -5.27318555e-06  1.15327313e-04]
 [-4.72633728e-01  3.32353579e-04  8.33368670e-05 -2.75364026e-03
 -4.90317797e-03  6.47949909e-01  6.62608200e-03 -5.94124576e-04
  9.53889054e-03 -1.59989671e-03 -4.75854409e-05  7.31483621e-03
  3.41113655e-05 -5.91605940e-04]
 [-6.72009691e-02  1.60589501e-05 -3.96939822e-05  1.04925166e-04
 -4.98480956e-04  6.62608200e-03  7.75657890e-03 -5.06941561e-05
  4.94416767e-04 -1.94649180e-04  5.18444533e-06  3.87223280e-04
  5.22111421e-06  5.03507223e-04]
 [ 2.52574657e-04 -6.44104667e-08  9.71684642e-07 -3.97527513e-08
 -2.56627859e-05 -5.94124576e-04 -5.06941561e-05  7.74933231e-06
  3.40849783e-05  2.95027780e-06 -6.60690922e-08 -6.00107894e-06]
```

```
In [6]: 1 #Tính y mũ:
        2
        3 y_mu = X.dot(beta)
        4 print(y_mu)
```

```
[[ 30.00384338]
 [ 25.02556238]
 [ 30.56759672]
 [ 28.60703649]
 [ 27.94352423]
 [ 25.25628446]
 [ 23.00180827]
 [ 19.53598843]
 [ 11.52363685]
 [ 18.92026211]
 [ 18.99949651]
 [ 21.58679568]
 [ 20.90652153]
 [ 19.55290281]
 [ 19.28348205]
 [ 19.29748321]
 [ 20.52750979]
 [ 16.91140135]
 [ 16.17801106]
 [ 18.40613603]]
```

```
In [7]: 1 #Tính e mũ:
        2
        3 e = Y - y_mu
        4 print(e)
```

```
[[ -6.00384338e+00]
 [ -3.42556238e+00]
 [  4.13240328e+00]
 [  4.79296351e+00]
 [  8.25647577e+00]
 [  3.44371554e+00]
 [  1.00000000e+00]
 [  1.00000000e+00]
 [  1.00000000e+00]
 [  1.00000000e+00]
 [  1.00000000e+00]
 [  1.00000000e+00]
 [  1.00000000e+00]
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 [  1.00000000e+00]
 [  1.00000000e+00]
 [  1.00000000e+00]
 [  1.00000000e+00]
 [  1.00000000e+00]
 [  1.00000000e+00]]
```



```
In [8]: 1 #Tính sigma bình:
2 sigma = (transpose(e).dot(e)) / (len(X) - (13+1))
3 print(sigma)
```

```
[[22.51785483]]
```

```
In [9]: 1 #Tính SE_beta:
2
3 SE_beta = sigma*np.diag(c)
4 print(SE_beta)
```

```
[[2.60452918e+01 1.08010784e-03 1.88443200e-04 3.78171976e-03
 7.42319676e-01 1.45904420e+01 1.74661518e-01 1.74498340e-04
 3.97821912e-02 4.40185014e-03 1.41416344e-05 1.71156401e-02
 7.21440767e-06 2.57203944e-03]]
```

```
In [10]: 1 #Câu 5: Xây dựng KTC cho beta:
2
3 import scipy.stats as scipy
4 t = (1 - 0.99)/2
5 t_value = scipy.t.ppf(t,len(X) - (13+1))
6 VT = beta - t_value * SE_beta
7 VP = beta + t_value * SE_beta
8 print(VT,VP)
```

```
[[ 1.03808938e+02  3.64622814e+01  3.64599757e+01  3.64692674e+01
  3.83790223e+01  7.41883125e+01  3.69111384e+01  3.64599396e+01
  3.65623595e+01  3.64708709e+01  3.64595250e+01  3.65037470e+01
  3.64595070e+01  3.64661393e+01]
 [ 6.72414380e+01 -1.05218351e-01 -1.07524070e-01 -9.82323642e-02
  1.81152257e+00  3.76208127e+01  3.43638680e-01 -1.07560130e-01
 -5.14022526e-03 -9.66287945e-02 -1.07974790e-01 -6.37527279e-02
 -1.07992702e-01 -1.01360427e-01]
 [ 6.73958698e+01  4.92134648e-02  4.69077459e-02  5.61994520e-02
  1.96595439e+00  3.77752445e+01  4.98070496e-01  4.68716865e-02
  1.49291591e-01  5.78030217e-02  4.64570266e-02  9.06790883e-02
```

```
In [11]: 1 #Câu 6:
2
3 #Tính y mũ của câu 6: với x mũ là hàm tự cho
4 t = (1 - 0.95)/2
5 t_value = scipy.t.ppf(t,len(X) - (13+1))
6 data1 = [1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14]
7 x_mu_nho = np.array(data1)
8 y_mu_moi = x_mu_nho.dot(beta)
9 print(y_mu_moi)
```

[-59.04026202]

```
In [12]: 1 #Tính epsilon:
2 import math
3
4 canbachai = sigma*(1+transpose(x_mu_nho).dot(C).dot(x_mu_nho))
5 epsilon = abs(t_value*canbachai)
6 print(epsilon)
7
8 VT1 = float(y_mu_moi - epsilon)
9 VP1 = float(y_mu_moi + epsilon)
10 print("Khoảng tin cậy của y là:")
11 (VT1,VP1)
```

[[957.24609699]]

Khoảng tin cậy của y là:

Out[12]: (-1016.2863590120626, 898.2058349725091)

```
In [13]: 1 #Tính các giá trị của bảng ANOVA:
2
3 #Tính SST:
4 sum_y = 0
5 for i in Y:
6     sum_y = sum_y + i**2
7 SST = transpose(Y).dot(Y) - (1/len(Y))*(sum_y)
```

```
In [13]: 1 #Tính các giá trị của bảng ANOVA:
2
3 #Tính SST:
4 sum_y = 0
5 for i in Y:
6     sum_y = sum_y + i**2
7 SST = transpose(Y).dot(Y) - (1/len(Y))*(sum_y)
8 print("SST là: ",SST)
9
10 #Tính SSR:
11 SSR = transpose(beta).dot(transpose(X)).dot(Y) - (1/len(Y))*(sum_y)
12 print("SSR là: ",SSR)
13
14 #Tính SSE:
15 SSE = SST - SSR
16 print("SSE là: ",SSE)
17
18 #Tính trung bình bình phương MSR và MSE:
19 MSR = (SSR/13)
20 print("MSR là: ",MSR)
21
22 MSE = (SSE/len(X)-(13+1))
23 print("MSE là: ",MSE)
24
25 #Tính F0:
26 F0 = MSR/MSE
27 print("F0 là: ",F0)
28

SST là: [[299034.193083]]
SSR là: [[287955.40850503]]
SSE là: [[11078.78457797]]
MSR là: [[22150.41603885]]
MSE là: [[22150.41603885]]
F0 là: [[2805.68583784]]
```

```
MSR là: [[22150.41603885]]
MSR là: [[22150.41603885]]
F0 là: [[2805.68583784]]
```

```
In [14]: 1 #Cách Lập bảng ANOVA:
2
3 import pandas as pd
4 s = {'Tên đại lượng': pd.Series(['Hồi quy bội', 'Sai số (hay thặng dư)', 'Tổng']),
5      'Tổng bình phương': pd.Series([SSR, SSE, SST]),
6      'Bậc tự do': pd.Series([13, len(X)-(13+1), len(X)]),
7      'Trung bình bình phương': pd.Series([MSR, MSE, '']),
8      'F0': pd.Series([F0, '', ''])}
9
10 df = pd.DataFrame(s)
11 print(df)
12
```

	Tên đại lượng	Tổng bình phương	Bậc tự do	\
0	Hồi quy bội	[[287955.40850503143]]	13	
1	Sai số (hay thặng dư)	[[11078.784577972605]]	492	
2	Tổng	[[299034.19308300404]]	506	
	Trung bình bình phương		F0	
0	[[22150.416038848572]]	[[2805.685837844506]]		
1	[[7.89483118176404]]			
2				

```
In [ ]: 1 |
```