

12.3

3

$$\begin{aligned}\langle 0, 1, 1 \rangle \cdot \langle -7, 41, -39 \rangle \\ &= 0 + 41 + -39 \\ &= \boxed{2}\end{aligned}$$

13

$$\begin{aligned}\vec{a} &= \langle 1, 1, 1 \rangle \\ \vec{b} &= \langle 1, -2, -2 \rangle \\ \vec{a} \cdot \vec{b} &= \|\vec{a}\| \|\vec{b}\| \cos(\theta)\end{aligned}$$

$$\begin{aligned}\langle 1, 1, 1 \rangle \cdot \langle 1, -2, -2 \rangle \\ &= 1 - 2 - 2 \\ &= -3\end{aligned}$$

$$\begin{aligned}\|\vec{a}\| &= \sqrt{3} \\ \|\vec{b}\| &= 3\end{aligned}$$

$$\begin{aligned}\cos \theta &= \frac{-\sqrt{3}}{3} \\ \theta &= 2.19\end{aligned}$$

$$\begin{aligned}\theta &> \pi/2 \\ \therefore \theta &\text{ is obtuse } \square\end{aligned}$$

19

$$\begin{aligned}\vec{a} &= \langle 0, 3, 1 \rangle \\ \vec{b} &= \langle 4, 0, 0 \rangle \\ \vec{a} \cdot \vec{b} &= \|\vec{a}\| \|\vec{b}\| \cos(\theta)\end{aligned}$$

$$\begin{aligned}\langle 0, 3, 1 \rangle \cdot \langle 4, 0, 0 \rangle \\ &= 0\end{aligned}$$

$$\begin{aligned}\|\vec{a}\| &= \sqrt{10} \\ \|\vec{b}\| &= 2\end{aligned}$$

$$\cos \theta = 0$$

27

$$\begin{aligned}\vec{a} &= \langle 0, 1, 1 \rangle \\ \vec{b} &= \langle 1, -1, 0 \rangle \\ \vec{a} \cdot \vec{b} &= \|\vec{a}\| \|\vec{b}\| \cos(\theta)\end{aligned}$$

$$\begin{aligned}\langle 0, 1, 1 \rangle \cdot \langle 1, -1, 0 \rangle \\ &= -1\end{aligned}$$

$$\|\vec{a}\| = \sqrt{2}$$

$$\|\vec{b}\| = \sqrt{2}$$

$$\cos \theta = \frac{-1}{2}$$

$$\theta = \boxed{2.09}$$

43

$$\begin{aligned} & 2\vec{u} \cdot (3\vec{u} - \vec{v}) \\ &= 6(\vec{u} \cdot \vec{u}) - 2(\vec{u} \cdot \vec{v}) \\ &= 6\|\vec{u}\|^2 - 2(2) \\ &= 6 - 4 \\ &= \boxed{2} \end{aligned}$$

12.4

9

$$\vec{a} = \langle 1, 2, 1 \rangle$$

$$\vec{b} = \langle 3, 1, 1 \rangle$$

$$\begin{aligned} & \langle 1, 2, 1 \rangle \times \langle 3, 1, 1 \rangle \\ &= \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 2 & 1 \\ 3 & 1 & 1 \end{vmatrix} \end{aligned}$$

$$= \langle 1, 2, -5 \rangle \square$$

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$$\begin{aligned} & (\hat{i} - 3\hat{j} + 2\hat{k}) \times (\hat{j} - \hat{k}) \\ &= \langle 1, -3, 2 \rangle \times \langle 0, 1, -1 \rangle \\ &= \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & -3 & 2 \\ 0 & 1 & -1 \end{vmatrix} \\ &= \langle 1, 1, 1 \rangle \end{aligned}$$

$$\begin{aligned} & (\hat{i} - 3\hat{j} + 2\hat{k}) \times (\hat{j} - \hat{k}) \\ &= \hat{k} + \hat{j} + 3\hat{i} - 2\hat{i} \\ &= \hat{i} + \hat{j} + \hat{k} \\ &= \langle 1, 1, 1 \rangle \end{aligned}$$

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$$\begin{aligned} & (\vec{u} - 2\vec{v}) \times (\vec{u} + 2\vec{v}) \\ &= 2(\vec{u} \times \vec{v}) - 2(\vec{v} \times \vec{u}) \\ &= 4(\vec{u} \times \vec{v}) \\ &= 4\langle 1, 1, 0 \rangle \\ &= \langle 4, 4, 0 \rangle \square \end{aligned}$$

41

$$\vec{v} = \langle 1, 3, 1 \rangle$$

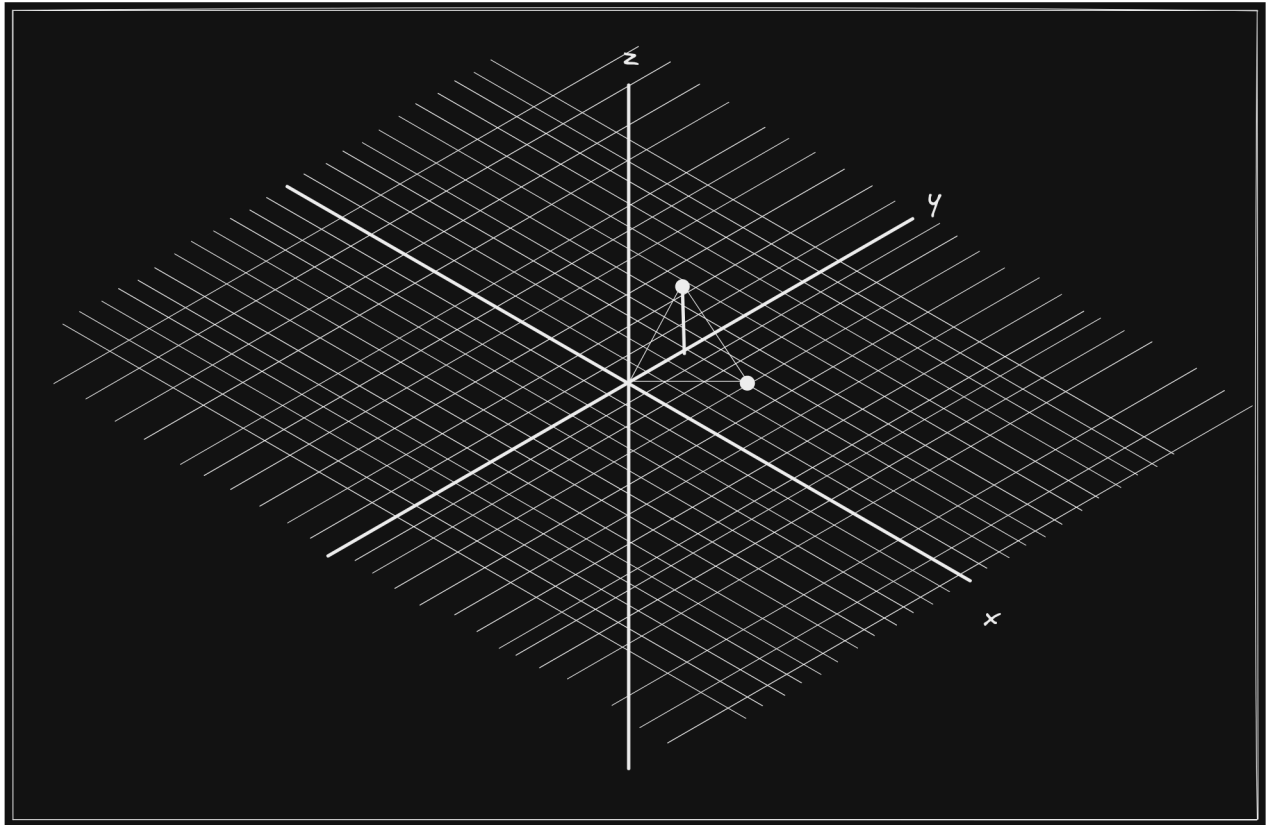
$$\vec{w} = \langle -4, 2, 6 \rangle$$

$$\|\vec{v} \times \vec{w}\| = \left\| \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 3 & 1 \\ -4 & 2 & 6 \end{vmatrix} \right\|$$

$$= \|\langle 16, -10, 14 \rangle\|$$

$$= \sqrt{552} \square$$

47



$$\vec{P} = \langle 3, 3, 0 \rangle$$

$$\vec{Q} = \langle 0, 3, 3 \rangle$$

$$\frac{\|\vec{P} \times \vec{Q}\|}{2} = \left\| \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 3 & 3 & 0 \\ 0 & 3 & 3 \end{vmatrix} \right\|/2$$

$$= \|\langle 9, -9, 9 \rangle\|/2$$

$$= \sqrt{243}/2$$

$$= 7.79 \square$$

12.5

17

$$(0, 0, 0)$$

$$4x - 9y + z = 3 + C$$

$$0 = 3 + C$$

$$C = -3$$

$$4x - 9y + z = 0 \quad \square$$

21

$$P = (2, -1, 4)$$

$$Q = (1, 1, 1)$$

$$R = (3, 1, -2)$$

$$ax + by + cz = C$$

$$\begin{cases} 2a - b + 4c = C \\ a + b + c = C \\ 3a + b - 2c = C \end{cases}$$

Let $c=1$

$$= \begin{cases} a = C/2 + b/2 - 2 \\ b = C/3 + 2/3 \\ C = 19/4 \end{cases}$$

$$= \begin{cases} a = 3/2 \\ b = 9/4 \\ c = 1 \\ C = 19/4 \end{cases}$$

$$3x/2 + 9y/4 + z = 19/4$$

$$6x + 9y + 4z = 19 \quad \square$$

27a

$$\vec{r}_1(t_1) = \langle t_1, 2t_1 - 1, t_1 - 3 \rangle$$

$$\vec{r}_2(t_2) = \langle 4, 2t_2 - 1, -1 \rangle$$

$$\begin{cases} t_1 = 4 \\ 2t_1 - 1 = 2t_2 - 1 \\ t_1 - 3 = -1 \end{cases}$$

$$\begin{cases} t_1 = 4 \\ t_1 = t_2 \\ t_1 = 2 \end{cases}$$

Since there is no pair of t_1 and t_2 such that $\vec{r}_1(t_1) = \vec{r}_2(t_2)$, the lines will never equal at any time and therefore do not intersect.

27b

$$\vec{r}_1(t_1) = \langle 3t_1, 2t_1 + 1, t_1 - 5 \rangle$$

$$\vec{r}_2(t_2) = \langle 4t_2, 4t_2 - 3, -1 \rangle$$

$$\begin{cases} 3t_1 = 4t_2 \\ 2t_1 + 1 = 4t_2 - 3 \\ t_1 - 5 = -1 \end{cases}$$

$$\begin{cases} t_1 = 4t_2/3 \\ t_1 = 2t_2 - 2 \\ t_1 = 4 \end{cases}$$

$$\begin{cases} t_1 = 4 \\ t_2 = 3 \\ t_1 = 4 \end{cases}$$

$$\vec{P} = \langle 12, 9, -1 \rangle$$

Since the vectors are equal when $t_1 = 4$ and $t_2 = 3$, lines intersect.

$$\vec{r}_1(t_1) = t_1 \langle 3, 2, 1 \rangle + \langle 0, 1, -5 \rangle$$

$$\vec{r}_2(t_2) = t_2 \langle 4, 4, 0 \rangle + \langle 0, -3, -1 \rangle$$

$$\vec{N} = \langle 3, 2, 1 \rangle \times \langle 4, 4, 0 \rangle$$

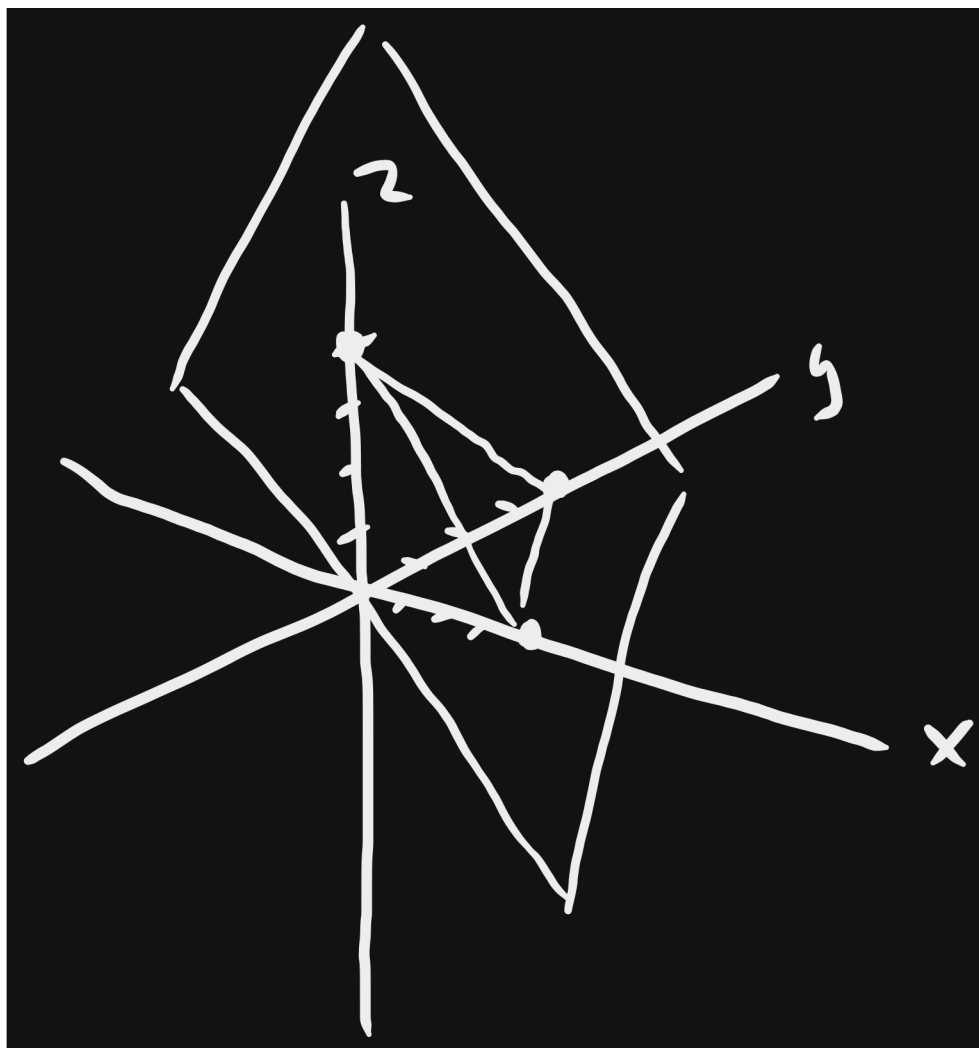
$$= \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 3 & 2 & 1 \\ 4 & 4 & 0 \end{vmatrix}$$

$$= \langle -4, 4, 4 \rangle$$

$$-4(x - 12) + 4(y - 9) + 4(z + 1) = 0$$

$$-4x + 4y + 4z = -16 \quad \square$$

33



57

$$\vec{a} = \langle 1, 0, 1 \rangle$$

$$\vec{b} = \langle -1, 1, 1 \rangle$$

$$\begin{aligned}\vec{a} \times \vec{b} &= \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 0 & 1 \\ -1 & 1 & 1 \end{vmatrix} \\ &= -1 - 2 + 1 \\ &= -2\end{aligned}$$

$$\begin{aligned}\vec{a} \times \vec{b} &= \|\vec{a}\| \|\vec{b}\| \cos(\theta) \\ \cos\theta &= -2/(\sqrt{2} * \sqrt{3}) \\ \theta &= 2.26 \square\end{aligned}$$