3 - **EOM**

PHYS 122-119B Lab 3b: EOM

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PHYS 122-119B
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Lab 3a: EOM (Charge to Mass Ratio of the Electron)
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1 Abstract

The purpose of this lab is to confirm the established value for $\frac{e}{m}$ in electrons through the usage of Heimholz coils and their expected field effect on electrons.

$\frac{e}{m}$ Source	Value
Expected	$1.75882017 \pm 0.00000007 imes 10^{11} \; rac{C}{kg}$
Current	$(4\pm1) imes10^9~rac{C}{kg}$
Voltage	$(1.2\pm0.3) imes10^{11}~rac{C}{kg}$

2 Theory

2.1 Constants

$$rac{e}{m}=1.75882017\pm0.00000007 imes10^{11}rac{C}{kg}$$
 Expected value of e/m $\mu_0=4\pi imes10^{-7}rac{Tm}{A}$ Heimholz constant

Mass of an electron mSpeed of an electron v

Velocity \vec{v}

 \vec{B} Magnetic Field

 \vec{B} Magnitude of the Magnetic Field

 $ec{e}$ Magnitude of the charge of an electron

 $ec{I}_C$ Current

 \vec{R} Radius of beam

 \vec{V} Heimholz coil input voltage

rRadius of Heimholz coil

NNumber of turns in Heimholz coil

2.2 Formulae

Given the relation between potential difference and kinetic energy of an electron, along with the lorenz force of the Heimholz coils, we are able to find a value for $\frac{e}{m}$ given V, B, and R.

Then, we are able to use the known magnetic force of a Heimholz coil in order to find the value of $\frac{e}{m}$ in terms of μ_0 , N, I_C , r, V, R

$$\frac{1}{2}mv^2 = eV$$
 Definition of Kinetic Energy (2.2.1)

$$ec{F} = -e(ec{v} imes ec{B}) \qquad ext{Lorenz force of magnetic field} \qquad \qquad (2.2.2)$$

$$ec{F} = -e(ec{v} imes ec{B})$$
 Lorenz force of magnetic field (2.2.2) $evB = rac{mv^2}{B}$ Centripetal Equation (2.2.3)

$$\frac{eBR}{m} = v Solve for v (2.2.4)$$

$$v = \sqrt{\frac{2eV}{m}}$$
 From 2.2.1 (2.2.5)

$$\frac{eBR}{m} = \sqrt{\frac{2eV}{m}}$$
 From 2.2.4 (2.2.6)

$$\frac{e(BR)^2}{m} = 2V Solving for e/m (2.2.7)$$

$$\frac{e}{m} = \frac{2V}{(BR)^2}$$
 Solve for e/m (2.2.8)

$$B = \frac{8\mu_0 NI_C}{5r\sqrt{5}}$$
 Heimholz Equation (2.2.9)

$$\frac{e}{m} = \left(\frac{r}{\mu_0 R N I_C}\right)^2 \frac{5^3 V}{2^5}$$
 From 2.2.8 (2.2.10)

2.2.1 Formula for relation between current and radius

$$\frac{e}{m} = \left(\frac{r}{\mu_0 R N I_C}\right)^2 \frac{5^3 V}{2^5}$$
 From 2.2.10 (2.2.1.1)

$$\frac{1}{R} = \frac{\mu_0 N}{r} \sqrt{\frac{2^5 \frac{e}{m}}{5^3 V}} I_C$$
 Relate R and I (2.2.1.2)

$$y = ax$$
 Linear relationship (2.2.1.3)

$$y=ax$$
 Linear relationship $(2.2.1.3)$ $y=rac{1}{R}; a=rac{\mu_0 N}{r}\sqrt{rac{2^5rac{e}{m}}{5^3V}}; x=I_C$ With constants $(2.2.1.4)$

$$\frac{e}{m} = \left(\frac{ar}{\mu_0 N}\right)^2 \frac{5^3 V}{2^5} \qquad \text{Solve for e/m} \qquad (2.2.1.5)$$

We can then calculate our errors in $x, y, \frac{e}{m}$

$$\delta_y = \frac{1}{R^2} \delta_R \tag{2.2.1.6}$$

$$\delta_x = \delta_{I_C}$$
 (2.2.1.7)

$$\delta_{\frac{e}{m}} = 2\sqrt{\left(\frac{\delta_N}{N}\right)^2 + \left(\frac{\delta_a}{a}\right)^2 + \left(\frac{\delta_r}{r}\right)^2 + \left(\frac{\delta_V}{2V}\right)^2} \frac{e}{m}$$
(2.2.1.8)

2.2.2 Formula for relation between voltage and radius

$$\frac{e}{m} = \left(\frac{r}{\mu_0 R N I_C}\right)^2 \frac{5^3 V}{2^5}$$
 From 2.2.10 (2.2.2.1)

$$R = \left(rac{r}{\mu_0 N I_C}
ight) \sqrt{rac{5^3}{2^5 rac{e}{m}}} \sqrt{V} \qquad \qquad ext{Relate R and V} \qquad \qquad (2.2.2.2)$$

$$y = ax$$
 Linear relationship (2.2.2.3)

$$y=ax$$
 Linear relationship $y=ax$ Linear relationship $y=R; a=\left(\frac{r}{\mu_0 N I_C}\right) \sqrt{\frac{5^3}{2^5 \frac{e}{m}}}; x=\sqrt{V}$ With constants $(2.2.2.4)$

$$\frac{e}{m} = \left(\frac{r}{a\mu_0 NI_C}\right)^2 \frac{5^3}{2^5} \qquad \text{Solve for e/m} \qquad (2.2.2.5)$$

We can then calculate our errors in $x,y,\frac{e}{m}$

$$\delta_y = \delta_R \tag{2.2.2.6}$$

$$\delta_x = \frac{1}{2\sqrt{I}_C} \delta_{I_C} \tag{2.2.2.7}$$

$$\delta_{\frac{e}{m}} = 2\sqrt{\left(\frac{\delta_N}{N}\right)^2 + \left(\frac{\delta_a}{a}\right)^2 + \left(\frac{\delta_r}{r}\right)^2 + \left(\frac{\delta_{I_C}}{I_C}\right)^2} \frac{e}{m}$$
 (2.2.2.8)

3 Procedure

3.1 Materials

- 1. Heimholz coil, with:
 - Power supply
 - II. Ammeter
- 2. Electron gun, with:

- Power supply
- II. Volt meter

3.2 General Setup

- 1. Position the electron gun
 - I. Within the Heimholz coil
 - II. Pointed tangentially to the coils
 - III. Around 5cm offset into the coil
- 2. Turn on the Heimholz coil to 1A
- 3. Turn on the electron gun to 150V
- 4. Turn off the lights and observe the electron beam
- 5. Rotate the Heimholz coils until the electron beam is circular and not helical
- 6. Take a baseline measurement of the radius of the beam
- 7. Vary the amperage within safe bounds
 - 1. Note down the change in the radius of the beam
- 8. Set the amperage to the lowest while the beam is still visible
- 9. Vary the voltage within safe bounds
 - 1. Note down the change in the radius of the beam

3.3 General Data manipulation

- 1. Calculate x, y from equations 2.2.1.4 and 2.2.2.4
 - L. Calculate its error with equations 2.2.1.6, 2.2.1.7, 2.2.2.6, and 2.2.2.7
- 2. Since we know x, y should relate linearly due to equations 2.2.1.2 and 2.2.2.2
- 3. Linearly relate x, y for the two variances in order to regress for its slope
- 4. Calculate $\frac{e}{m}$ given the slope (a) using equations 2.2.1.5 and 2.2.2.5
 - L. Calculate its error with equations 2.2.1.8 and 2.2.2.8
- 5. Compare our values of $\frac{e}{m}$ with the current widely accepted value and decide if we disprove or fail to disprove the current standard

4 Analysis

4.1 Current vs. Radius

With the following constants:

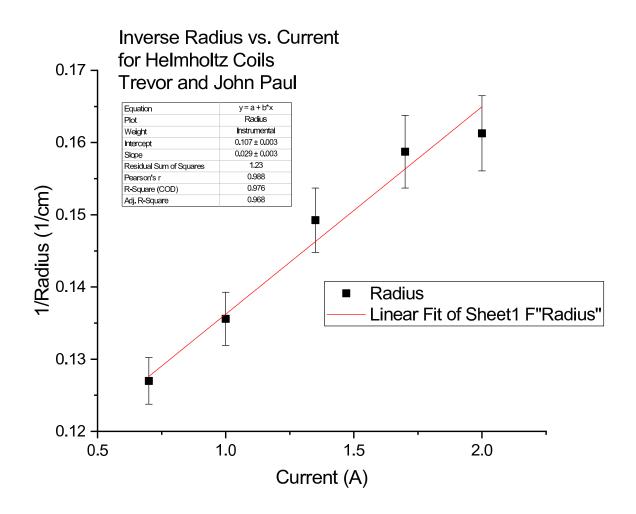
Constant	Value
r	$0.158\pm0.005~m$

Constant	Value
N	130
V	$150\pm 2~V$

When varying radius, we obtained the following transformed data:

Current	Radius
A	cm^{-1}
0.7 ± 0.01	0.127 ± 0.003
1 ± 0.01	0.136 ± 0.004
1.35 ± 0.01	0.149 ± 0.004
1.7 ± 0.01	0.159 ± 0.005
2 ± 0.01	0.161 ± 0.005

Graphing this data, we obtain the following graph:



Property	Value
Equation	y=ax+b
a	$0.029\pm0.003~rac{1}{cmA}$

Property	Value
b	$0.107\pm0.003~rac{1}{cm}$
r^2	0.976

This leaves us with $a=0.029\pm0.003$ to calculate $\frac{e}{m}$ from.

$$rac{e}{m}=(4\pm1) imes10^9~rac{C}{kg}$$

4.2 Voltage vs. Radius

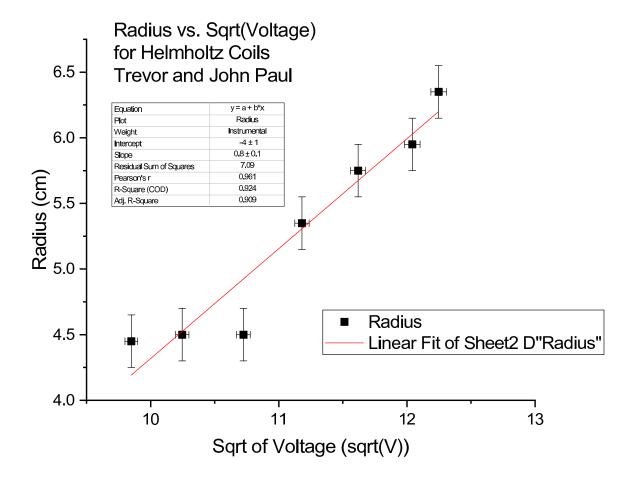
With the following constants:

Constant	Value
r	$0.158\pm0.005~m$
N	130
I_C	$0.70\pm0.01~A$

When varying radius, we obtained the following transformed data:

Voltage	Radius
\sqrt{V}	cm
9.85 ± 0.05	4.5 ± 0.2
10.25 ± 0.05	4.5 ± 0.2
10.72 ± 0.05	4.5 ± 0.2
11.18 ± 0.06	5.4 ± 0.2
11.62 ± 0.06	5.8 ± 0.2
12.04 ± 0.06	6 ± 0.2
12.25 ± 0.06	6.4 ± 0.2

Graphing this data, we obtain the following graph:



Property	Value
Equation	y = ax + b
a	$0.8 \pm 0.1 \; rac{cm}{\sqrt{V}}$
b	$-4\pm1~cm$
r^2	0.924

This leaves us with $a=0.8\pm0.1$ to calculate $\frac{e}{m}$ from.

$$rac{e}{m} = (1.2 \pm 0.3) imes 10^{11} \; rac{C}{kg}$$

5 Conclusion

The purpose of this lab is to confirm the established value for $\frac{e}{m}$ in electrons through the usage of Heimholz coils and their expected field effect on electrons.

We have obtained two different values for $\frac{e}{m}$ by varying Voltage and Current in our Heimholz setup.

$\frac{e}{m}$ Source	Value
Expected	$1.75882017 \pm 0.00000007 imes 10^{11} rac{C}{kg}$

$\frac{e}{m}$ Source	Value
Current	$(4\pm1) imes10^9~rac{C}{kg}$
Voltage	$(1.2\pm0.3) imes10^{11}~rac{C}{kg}$

For the value we got for our varying current, we got an incredibly imprecise and inaccurate answer, to within two orders of magnitude from our expected result. Due to extremely low accuracy, we fail to accept nor reject current theoretical understanding.

For the value we got for our varying voltage, we got a result that is remarkably close to the expected solution, to within $1.5\ SD$ of the expected result. We fail to reject current theoretical knowledge through this result.

I believe a large source of error for our current variance would be due to a low number of sample points and possibly interference from the glass bowl on our last data point, that we did not believe was being interfered with until we saw the plot.

As for the varying voltage, I think a low certainty in our radius measurement could be a large source of error, even if we got a fairly close result to the expected cknowledgements and Info

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Lab Partner: John Paul Magbitang Lab Manual: Lab 3 EOM PHYS 122

6.1 References

Driscoll, D., *General Physics 2: Electricity and Magnetism Lab Manual*, "Charge to Mass Ratio of the Electron".