

1

Convert the following unsigned numbers

$$3527_8 = ?_2 = ?_{16}$$

$$10101001_2 = ?_{10}$$

$$10101101111001_2 = ?_{16}$$

$$105_{10} = ?_2$$

$$412_{10} = ?_8$$

$$101000.01_2 = ?_{10}$$

✓ Answer ✓

$$3527_8 = 011|101|010|111_2 = 011101010111_2 = 0111|0101|0111_2 = 757_{16}$$

$$10101001_2 = 1 + 8 + 32 + 128_{10} = 169_{10}$$

$$10101101111001_2 = 0010|1011|0111|1001_2 = 2B79_{16}$$

$$105_{10} = 64 + 32 + 8 + 1_{10} = 1101001_2$$

$$412_{10} = 256 + 128 + 16 + 8 + 4_{10} = 110|011|100_2 = 634_8$$

$$101000.01_2 = 0.25 + 8 + 32_{10} = 40.25_{10}$$

2

Indicate whether there is an overflow for the following operations where all the numbers are in two's complement form

$$10010100 + 10010101$$

$$01000011 + 10010001$$

✓ Answer

$$10010100 + 10010101 = 100101001$$

Yes, since both of the leading digits are high, this leads the output to be too large to store in 8 bits, making it overflow to 9. Truncating it to 8 bits will make it have an inaccurate answer.

$$01000011 + 10010001 = 11010100$$

No, since only one leading digit is high and there is no carry over from the previous bit, there is no overflow.

3

Perform the following operations by first representing the decimal numbers in two's complement number system. (Hint: the subtraction will become addition). Use 6 bits to represent the numbers.

$$14 - 15 = ?$$

$$12 - 10 = ?$$

$$24 - 6 = ?$$

$$8 - 22 = ?$$

✓ Answer

$$\begin{aligned} 14 - 15 &= (8 + 4 + 2) - (8 + 4 + 2 + 1) \\ &= 001110_2 - 001111_2 = 001110_2 + 110001_2 = 111111_2 \end{aligned}$$

$$\begin{aligned} 12 - 10 &= (8 + 4) - (8 + 2) \\ &= 001100_2 - 001010_2 = 001100_2 + 110110_2 = 000010_2 \end{aligned}$$

$$\begin{aligned} 24 - 6 &= (16 + 8) - (4 + 2) \\ &= 011000_2 - 000110_2 = 011000_2 + 111010_2 = 010010_2 \end{aligned}$$

$$\begin{aligned} 8 - 22 &= (8) - (16 + 4 + 2) \\ &= 001000_2 - 010110_2 = 001000_2 + 101010_2 = 110010_2 \end{aligned}$$

4

Complete the following table so that each row is the same number in four different representations.

For binary numbers, use six bits.

Decimal	Signed Magnitude	Two's Complement	One's Complement
-14			
	110110		

Decimal	Signed Magnitude	Two's Complement	One's Complement
		010011	
			110111

✓ Answer ✓

Decimal	Signed Magnitude	Two's Complement	One's Complement
-14	101110	110010	110001
-22	110110	101010	101001
19	010011	010011	010011
-8	101000	111000	110111

5

Add the following unsigned numbers:

$$9B4C_{16} + 12E3_{16} = ?$$

$$234_8 + 436_8 = ?$$

✓ Answer

$$9B4C_{16} + 12E3_{16} = AD2F_{16} + 0100_{16} = AE2F_{16}$$

$$234_8 + 436_8 = 662_8 + 010_8 = 672_8$$