

i: B

ii: A

21

a: D

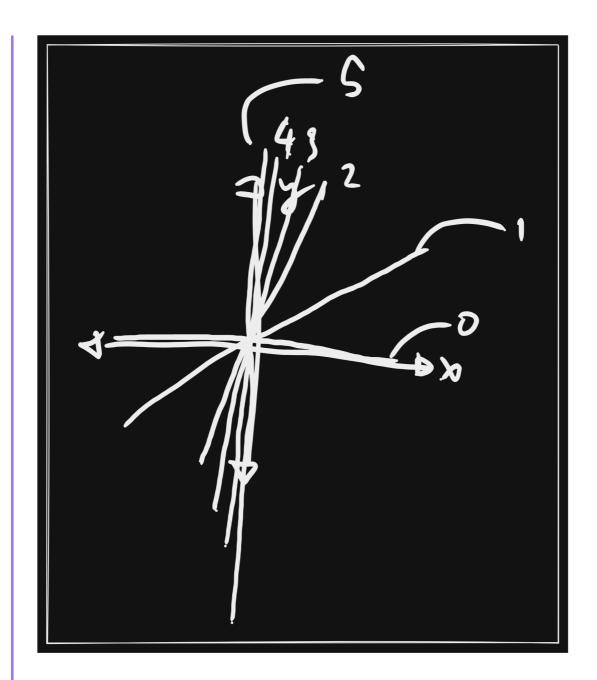
b: C

c: E

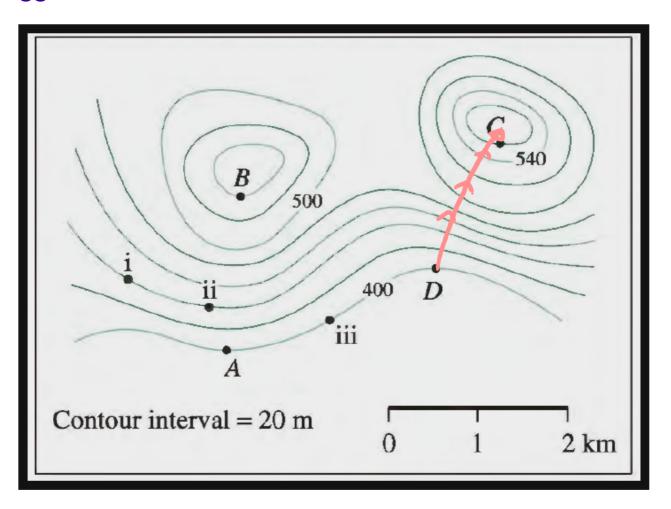
d: B

e: A

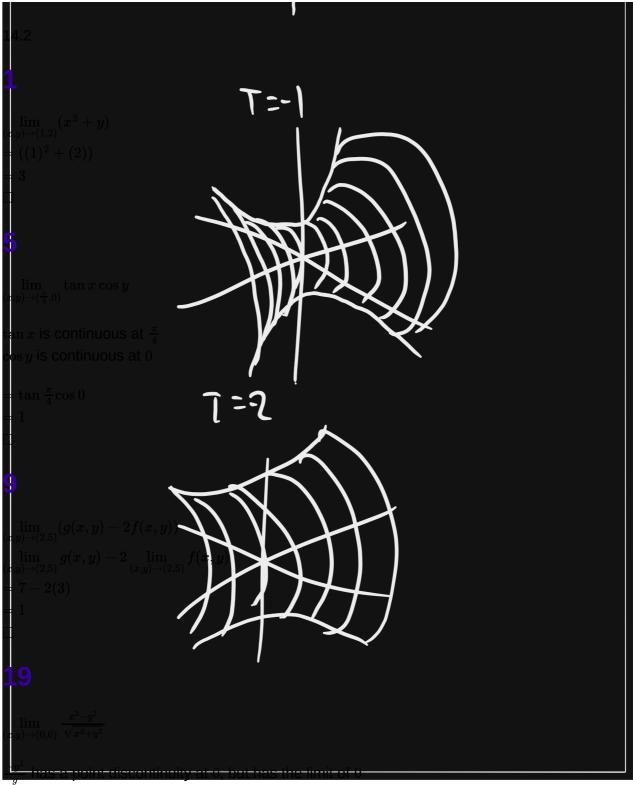
f: F











 $\frac{x^2}{x}$ has a point discontinuity at 0, but also has the limit of 0

= 0

23

$$\lim_{(x,y,z)\to(0,0,0)} \frac{x+y+z}{x^2+y^2+z^2}$$

 $\frac{z}{z^2}$ is not continuous at 0, and the limit does not exist, with the positive limit approaching ∞ and the negative limit approaching $-\infty$

 $\frac{y}{y^2}$ is not continuous at 0, and the limit also does not exist and has the same one-sided limits

as z

 $\frac{x}{x^2}$ has the same properties as y and z

Limit from	Value
+z	∞
-z	$-\infty$
+y	∞
-y	$-\infty$
+x	∞
-x	$-\infty$

Three of these six directional limits do not equal the other three limits, therefore the limit does not exist

31

$$\lim_{(x,y)\to(3,4)}\frac{1}{\sqrt{x^2+y^2}}$$

 $\frac{1}{\sqrt{x^2+16}}$ is continuous at 3, with the value of 1/5 $\frac{1}{\sqrt{9+y^2}}$ is continuous at 4, with the value of 1/5

= 1/5

41

$$\lim_{(x,y)\to(0,0)} \frac{x^2+y^2}{\sqrt{x^2+y^2+1}-1}$$

 $\frac{y^2}{\sqrt{y^2+1}-1}$ has a point discontinuity at 0, but $\lim \frac{y^2}{y^2+1} = \frac{2y}{y^2+1}$

$$\lim_{y\to 0} \frac{2y}{y(y^2+1)^{-1/2}}$$

$$=\lim_{y o 0}rac{2}{(y^2+1)^{-1/2}}$$

And the same is true for x, meaning the original limit is also 2

= 2

14.3

$$z = \frac{x}{y}$$

$$\frac{\partial}{\partial x} = \frac{1}{y}$$

$$\frac{\partial}{\partial y} = \frac{-x}{y^2}$$

$$z = \cos \frac{1-x}{y}$$

$$\frac{\partial}{\partial x} = \frac{1}{y} \sin \frac{1-x}{y}$$

$$\frac{\partial}{\partial y} = \frac{x-1}{y^2} \sin \frac{1-x}{y}$$

$$z=e^{-x^2-y^2} \ rac{\partial}{\partial x}=-2xe^{-x^2-y^2} \ rac{\partial}{\partial y}=-2ye^{-x^2-y^2}$$

$$Q=rac{L}{M}e^{-Lt/M} \ rac{\partial L}{\partial L}=(rac{-Lt}{M^2}+rac{1}{M})e^{-Lt/M} \ rac{\partial }{\partial M}=(rac{-L}{M^2}+rac{L^2t}{M^3})e^{-Lt/M} \ =rac{L(Lt-M)}{M^3}e^{-Lt/M} \ rac{\partial }{\partial M}=rac{-L^2}{M^2}e^{-Lt/M}$$

$$egin{aligned} f(x,y) &= x \ln(y^2) \ rac{\partial}{\partial y} &= rac{2x}{y} \ rac{\partial^2}{\partial^2 y} &= rac{-2x}{y^2} \ rac{\partial^2}{\partial^2 y}(2,3) &= rac{-4}{9} \end{aligned}$$

$$f(u,v) = \cos(u+v^2) \ rac{\partial}{\partial u} = -\sin(u+v^2) \ rac{\partial^2}{\partial^2 u} = -\cos(u+v^2)$$

$$rac{\partial^3}{\partial^2 u \partial v} = 2 v \sin(u + v^2)$$