

Computer Vision: Assignment4

Part1:

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- Geometric Equation: $(x-a)^2 + (y-b)^2 = r^2$
- Construct Least Square:

edge points: $X = \begin{bmatrix} x^i & y^i \end{bmatrix}_{n \times 2}$ unknowns: $\bar{U} = \begin{bmatrix} a \\ b \\ r \end{bmatrix}$

- expand geo. eq. to get rid of non-linearity
 $= x^2 - 2ax + a^2 + y^2 - 2by + b^2 - r^2 = 0$

- terms x^2 and y^2 don't vary with a, b, r
 $= \underbrace{-2a}_{P_1} x + \underbrace{-2b}_{P_2} y + \underbrace{a^2 + b^2 - r^2}_{P_3} = 0$

- Introduce: $p_1 = -2a, p_2 = -2b, p_3 = a^2 + b^2 - r^2$

$\begin{bmatrix} x^i & y^i & 1 \end{bmatrix}_{n \times 3} \cdot \begin{bmatrix} p_1 \\ p_2 \\ p_3 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$ $\min_{arg \neq p} \sum_{i=0}^n (\bar{X}^i \cdot \bar{P})^2$

Scanned with CamScanner

Pseudo-code:

$(x, y)^i$: i^{th} edge point

For a:= a_min to a_max:

For b:= b_min to b_max:

For r:= r_min to r_max:

For i:= 1 to n:

If $(x^i - a)^2 + (y^i - b)^2 \sim r^2$:

Acc[a, b, r]++;

Part2:

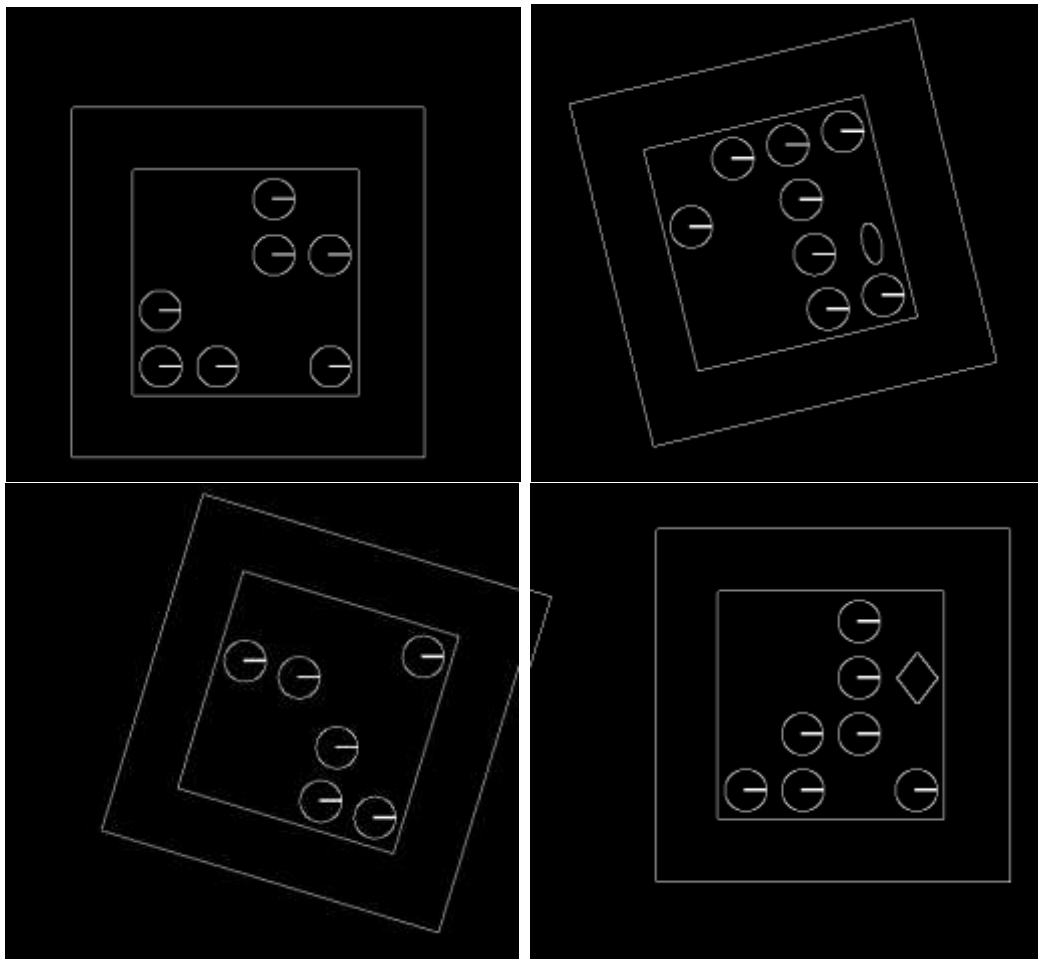
In part1, we write a pseudo-code for the Hough circle detection method, basically we iterate over image with parameters a, b and try all circles with varying the parameter r and count the number of edge points which fits in this equation. I wanted to make my Hough function general for all images. Thus, instead of setting bounds for a, b, and r parameters, Hough function determines itself, and try every (if quantization=1) possible circle within those bounds.

In order to speed-up the algorithm I determined an upper and lower bound for parameters a, b according to the parameter r. Thus, algorithm's logic becomes "try to construct a circle with radius= r^i on center (a', b')".

Hough_circle() function sets upper limit of r according to the $\min(\text{num_row}, \text{num_colm})/2$, since any circle with greater r value, cannot be complete circle. For that reason to speed-up the algorithm, I also divided the marker image 4 equal pieces and examine each of those pieces separately.

Quantization	Run time
3	~3 min.
2	~9.5 min.
1	~80 min.

The function at quantization=2 or quantization=3 works faster but fails to detect all circles, especially the ones in rotated marker. Due to the runtime, I wouldn't recommend quant=1. The result of the run with quantization=1 as follow:



Part3:

In this part, I implemented a general `area_growing()` function and `volume_growing()` function. Those functions call required `get_x_neighbors()` function, then check those neighbors and decide to label 1 or not, according to the given threshold value. Those functions could have realized as recursively, but I did prefer it to realize it iteratively since it can be vectorised in this way, and also “stack overflow” is not a concern for larger NIfTI data (especially with 26-neighborhood).

- **a) 8-neighborhood:**

In this part `get_8_neighbors()` function called inside the `area_growing()` function. This function takes 2D points and returns its 8 neighbors.

- **b) 4-neighborhood:**

In this part `get_4_neighbors()` function called inside the `area_growing()` function. This function takes 2D points and returns its 4 neighbors.

- **c) 26-neighborhood:**

In this part `get_26_neighbors()` function called inside the `volume_growing()` function. This function takes 3D points and returns its 26 neighbors.

- **d) 6-neighborhood:**

In this part `get_6_neighbors()` function called inside the `volume_growing()` function. This function takes 3D points and returns its 6 neighbors.

- **e) Dice score results & Suggestion:**

The performance of 8-neighbors: 0.9037632259828772

The performance of 4-neighbors: 0.8060919096350647

The performance of 26-neighbors: 0.8901082972687553

The performance of 6-neighbors: 0.8909479095412806

Since image/data corrupted by Poisson noise (a random type noise) applying arithmetic mean or geometric mean filters before segmentation operation, may improve result of the segmentation.