

Functional Programming

Tutorial 1: Evaluating expressions

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What is the Tutorial for?

- Bridge between lecture and practicals
- Asking your questions
- Getting ready for practicals by making exercises together



Hints

- Download templates from Brightspace
- Start ghci with your .hs files.



Questions?



Evaluating expressions

Given the following definitions:

`square :: Integer → Integer`

`square x = x * x`

`smallest :: Integer → Integer → Integer`

`smallest x y = if x ≤ y then x else y`

Evaluate: `smallest (square 2) (square 3)`.



Evaluating expressions

Given the following definition:

`compute :: Integer → Integer → Integer`

`compute x y = let a = x - y`

`b = x + y`

`in (a + 1) * (b + 2)`

Evaluate: `compute 4 2`.



Evaluating twice

double $x = x * x$

twice $f\ x = f\ (f\ x)$

a) Evaluate twice double 3 by hand.

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- b) What is the type of twice?



Evaluating twice

`double x = x * x`

`twice f x = f (f x)`

- a) Evaluate `twice double 3` by hand.
- b) What is the type of `twice`?
- c) Why does this allow that `twice` can be applied to itself?



Evaluating with GHCi



Twice as a lambda expression

An alternative definition of twice builds on λ -expressions.

$\text{twice}' = \lambda f \rightarrow \lambda x \rightarrow f (f x)$

a) Evaluate $\text{twice}' (+ 1) 0$ and $\text{twice}' \text{twice}' (* 2) 1$.



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An example of applying this rule:

$(\lambda x \rightarrow x + x) 47$



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$\Rightarrow 47 + 47$

$\Rightarrow 94$

