

Crop-yielding Prediction using Neural Network for Stochastic Differential Equation Parameters Estimation

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Abstract

Crops-yielding prediction is a multi-variant random dynamic and computationally expensive problem. This project employs a collection of stochastic differential equations (SDE) in Itô form using an artificial neural network (ANN) to predict the parameters of the stochastic differential equation of the chaotic time series of wheat yielding daily, monthly, and yearly. We aim to build a novel and unique stochastic wheat model that gives the best prediction based on SDE parameter estimation. The project will define new SDE parameters that can accurately be estimated in SDE using a neural network under specific noise level regimes to predict the crop yielding. The dataset used is the European Commission's MARS Crop Yield Forecasting System (MCYFS) including spring barley, potato, grain maize, and sunflower. The historical data are in daily and yearly scales.

Research Objective

High-performance wheat-yielding prediction model for large-scale data by using the stochastic approach with machine learning in parameter estimation, which reduces the computational time compared to a traditional and deep neural network that has many overfitting issues due to unbalanced data.

Research Output

In conducting this study, we will accomplish the following specific deliverables:

- Novel Crop SDE model that can predict crop yielding and a specific number of parameters with new drift and diffusion functions.

Introduction

Crop yielding prediction is a complex problem. It is considered a multi-variant random dynamic system because it has hundreds of factors based on weather, soil type, genotype, and phenotype variations. Those variations include almost thousands of factors. Due to data scaling, this large data multi-variant is computationally expensive using traditional or deep machine learning because it has thousands of genotype, phenotype, and environment variable features. These invariant and hidden factors are similar to stock exchange rate prediction.

Research Method

Parameter Estimation

Given a one-dimension time-homogeneous SDE:

$$dX = \mu(X; \theta)dt + g(X; \theta)dW \quad (1)$$

the task is to estimate the parameter θ from a sample of $(N+1)$ observations X_0, X_1, \dots, X_n of the process at known times t_0, t_1, \dots, t_n . In the statement of equation (1), dW is the differential of the Wiener process (Brownian motion), $\mu(X; \theta)$ is the instantaneous drift, and $g(X; \theta)$ is the instantaneous diffusion.

Crop SDE Model

The SDE model will propose new functions for the drift and diffusion SDE parts. The output model is evaluated by Euler and Stratonovich methods.

Research Activities

Activity	Timeline
Implementing the SDE model based on small testing data using Python	1-3 months
Tuning the model by adding parameters and functions	1-3 months
Implementing NN that changes the parameters based on the output performance	2-3 months
Optimize the ANN hyper-parameters, the SDE functions, and number of yielding on real datasets	1-2 months

Table 1: Activity and timeline

Skills Required

Advanced math, Stochastic Differential Equations.

References

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