

# TRIGONOMETRI

## 1. Rumus Jumlah dan Selisih Sudut

- $\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$
- $\cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$
- $\tan(A \pm B) = \frac{\tan A \pm \tan B}{1 \mp \tan A \tan B}$

## 2. Rumus Sudut Rangkap

- $\sin(2A) = 2 \sin A \cos A$
- $\cos(2A) = \cos^2 A - \sin^2 A = 2 \cos^2 A - 1 = 1 - 2 \sin^2 A$
- $\tan(2A) = \frac{2 \tan A}{1 - \tan^2 A}$

## 3. Rumus Sudut Setengah

- $\sin\left(\frac{A}{2}\right) = \pm \sqrt{\frac{1-\cos A}{2}}$
- $\cos\left(\frac{A}{2}\right) = \pm \sqrt{\frac{1+\cos A}{2}}$
- $\tan\left(\frac{A}{2}\right) = \frac{\sin A}{1+\cos A} = \frac{1-\cos A}{\sin A}$

## 4. Rumus Perkalian ke Penjumlahan

- $2 \sin A \cos B = \sin(A+B) + \sin(A-B)$
- $2 \cos A \cos B = \cos(A+B) + \cos(A-B)$
- $-2 \sin A \sin B = \cos(A+B) - \cos(A-B)$

## 5. Rumus Penjumlahan ke Perkalian

- $\sin A + \sin B = 2 \sin\left(\frac{A+B}{2}\right) \cos\left(\frac{A-B}{2}\right)$
- $\sin A - \sin B = 2 \cos\left(\frac{A+B}{2}\right) \sin\left(\frac{A-B}{2}\right)$
- $\cos A + \cos B = 2 \cos\left(\frac{A+B}{2}\right) \cos\left(\frac{A-B}{2}\right)$
- $\cos A - \cos B = -2 \sin\left(\frac{A+B}{2}\right) \sin\left(\frac{A-B}{2}\right)$

# LIMIT FUNGSI

## Limit Fungsi

### 1. Limit di Tak Hingga

- Untuk  $\lim_{x \rightarrow \infty} \frac{ax^m + \dots}{px^n + \dots}$ 
  - Jika  $m > n$ , hasil =  $\infty$
  - Jika  $m = n$ , hasil =  $\frac{a}{p}$
  - Jika  $m < n$ , hasil = 0
- Untuk  $\lim_{x \rightarrow \infty} (\sqrt{ax^2 + bx + c} - \sqrt{px^2 + qx + r})$ 
  - Jika  $a > p$ , hasil =  $\infty$
  - Jika  $a < p$ , hasil =  $-\infty$
  - Jika  $a = p$ , hasil =  $\frac{b-q}{2\sqrt{a}}$

### 2. Limit Trigonometri Dasar (untuk

$x \rightarrow 0$ )

- $\lim_{x \rightarrow 0} \frac{\sin ax}{bx} = \frac{a}{b}$
- $\lim_{x \rightarrow 0} \frac{\tan ax}{bx} = \frac{a}{b}$
- $\lim_{x \rightarrow 0} \frac{\sin ax}{\tan bx} = \frac{a}{b}$