

TRIGONOMETRI

1. Rumus Jumlah dan Selisih Sudut

- $\sin(A \pm B) = \sin A \cos B \pm \cos A \sin B$
- $\cos(A \pm B) = \cos A \cos B \mp \sin A \sin B$
- $\tan(A \pm B) = \frac{\tan A \pm \tan B}{1 \mp \tan A \tan B}$

2. Rumus Sudut Rangkap

- $\sin(2A) = 2 \sin A \cos A$
- $\cos(2A) = \cos^2 A - \sin^2 A = 2 \cos^2 A - 1 = 1 - 2 \sin^2 A$
- $\tan(2A) = \frac{2 \tan A}{1 - \tan^2 A}$

3. Rumus Sudut Setengah

- $\sin\left(\frac{A}{2}\right) = \pm \sqrt{\frac{1 - \cos A}{2}}$
- $\cos\left(\frac{A}{2}\right) = \pm \sqrt{\frac{1 + \cos A}{2}}$
- $\tan\left(\frac{A}{2}\right) = \frac{\sin A}{1 + \cos A} = \frac{1 - \cos A}{\sin A}$

4. Rumus Perkalian ke Penjumlahan

- $2 \sin A \cos B = \sin(A + B) + \sin(A - B)$
- $2 \cos A \cos B = \cos(A + B) + \cos(A - B)$
- $-2 \sin A \sin B = \cos(A + B) - \cos(A - B)$

5. Rumus Penjumlahan ke Perkalian

- $\sin A + \sin B = 2 \sin\left(\frac{A+B}{2}\right) \cos\left(\frac{A-B}{2}\right)$
- $\sin A - \sin B = 2 \cos\left(\frac{A+B}{2}\right) \sin\left(\frac{A-B}{2}\right)$
- $\cos A + \cos B = 2 \cos\left(\frac{A+B}{2}\right) \cos\left(\frac{A-B}{2}\right)$
- $\cos A - \cos B = -2 \sin\left(\frac{A+B}{2}\right) \sin\left(\frac{A-B}{2}\right)$

LIMIT FUNGSI

Limit Fungsi

1. Limit di Tak Hingga

- Untuk $\lim_{x \rightarrow \infty} \frac{ax^m + \dots}{px^n + \dots}$
 - Jika $m > n$, hasil = ∞
 - Jika $m = n$, hasil = $\frac{a}{p}$
 - Jika $m < n$, hasil = 0
- Untuk $\lim_{x \rightarrow \infty} (\sqrt{ax^2 + bx + c} - \sqrt{px^2 + qx + r})$
 - Jika $a > p$, hasil = ∞
 - Jika $a < p$, hasil = $-\infty$
 - Jika $a = p$, hasil = $\frac{b-q}{2\sqrt{a}}$

2. Limit Trigonometri Dasar (untuk

$x \rightarrow 0$)

- $\lim_{x \rightarrow 0} \frac{\sin ax}{bx} = \frac{a}{b}$
- $\lim_{x \rightarrow 0} \frac{\tan ax}{bx} = \frac{a}{b}$
- $\lim_{x \rightarrow 0} \frac{\sin ax}{\tan bx} = \frac{a}{b}$