

$$\gamma(t) = (\gamma_x(t), \gamma_y(t)) \quad (1)$$

where  $\gamma_x$  and  $\gamma_y$  are defined after the following discussion.

- Planar or Space?: Planar  
Since the curve is planar, its torsion = 0
- This curve, despite having a fairly complicated equation, can be understood as a combination of 5 clones of a single spiral curve. I find it interesting because, well of its beauty. Further, I devised a method (algorithm) to combine various curves into a single curve, using what I call a cropping function, which may result in large equations, but it achieves its objective without much difficulty. This was the first curve I created using the said algorithm, thus the interest.
- For any given t, only one of the summation terms is non-zero.
- The curvature is the same as that of the ‘base’ curve, provided it’s defined at that point.
- The cropping function is the one that uses Ceiling and Floor functions, and it essentially ‘selects’ which curve to plot.

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<sup>1</sup>This term has been coined by me.

$$\begin{aligned}
\gamma_x(t) = & (\lceil m(t - ((0)\alpha)) \rceil)(\lfloor m(-t + (1\alpha)) \rfloor + 1) \\
& (\cos((0)2\pi/5) \\
& ((t - (0)\alpha)) \\
& (1.2^{(t-(0)\alpha)}) \cos((t - (0)\alpha))) \\
& - \sin((0)2\pi/5) \\
& ((t - (0)\alpha) \\
& (1.2^{(t-(0)\alpha)}) \sin((t - (0)\alpha))) \\
& + (\lceil m(t - ((1)\alpha)) \rceil)(\lfloor m(-t + (2\alpha)) \rfloor + 1) \\
& (\cos((1)2\pi/5) \\
& ((t - (1)\alpha)) \\
& (1.2^{(t-(1)\alpha)}) \cos((t - (1)\alpha))) \\
& - \sin((1)2\pi/5) \\
& ((t - (1)\alpha) \\
& (1.2^{(t-(1)\alpha)}) \sin((t - (1)\alpha))) \\
& + (\lceil m(t - ((2)\alpha)) \rceil)(\lfloor m(-t + (3\alpha)) \rfloor + 1) \\
& (\cos((2)2\pi/5) \\
& ((t - (2)\alpha)) \\
& (1.2^{(t-(2)\alpha)}) \cos((t - (2)\alpha))) \\
& - \sin((2)2\pi/5) \\
& ((t - (2)\alpha) \\
& (1.2^{(t-(2)\alpha)}) \sin((t - (2)\alpha))) \\
& + (\lceil m(t - ((3)\alpha)) \rceil)(\lfloor m(-t + (4\alpha)) \rfloor + 1) \\
& (\cos((3)2\pi/5) \\
& ((t - (3)\alpha)) \\
& (1.2^{(t-(3)\alpha)}) \cos((t - (3)\alpha))) \\
& - \sin((3)2\pi/5) \\
& ((t - (3)\alpha) \\
& (1.2^{(t-(3)\alpha)}) \sin((t - (3)\alpha))) \\
& + (\lceil m(t - ((4)\alpha)) \rceil)(\lfloor m(-t + (5\alpha)) \rfloor + 1) \\
& (\cos((4)2\pi/5) \\
& ((t - (4)\alpha)) \\
& (1.2^{(t-(4)\alpha)}) \cos((t - (4)\alpha))) \\
& - \sin((4)2\pi/5) \\
& ((t - (4)\alpha) \\
& (1.2^{(t-(4)\alpha)}) \sin((t - (4)\alpha)))
\end{aligned} \tag{2}$$

$$\begin{aligned}
\gamma_y(t) = & (\lceil m(t - ((0)\alpha)) \rceil)(\lfloor m(-t + (1\alpha)) \rfloor + 1) \\
& (\sin((0)2\pi/5) \\
& ((t - (0)\alpha)) \\
& (1.2^{(t-(0)\alpha)}) \cos((t - (0)\alpha))) \\
& + \cos((0)2\pi/5) \\
& ((t - (0)\alpha) \\
& (1.2^{(t-(0)\alpha)}) \sin((t - (0)\alpha))) \\
& + (\lceil m(t - ((1)\alpha)) \rceil)(\lfloor m(-t + (2\alpha)) \rfloor + 1) \\
& (\sin((1)2\pi/5) \\
& ((t - (1)\alpha)) \\
& (1.2^{(t-(1)\alpha)}) \cos((t - (1)\alpha))) \\
& + \cos((1)2\pi/5) \\
& ((t - (1)\alpha) \\
& (1.2^{(t-(1)\alpha)}) \sin((t - (1)\alpha))) \\
& + (\lceil m(t - ((2)\alpha)) \rceil)(\lfloor m(-t + (3\alpha)) \rfloor + 1) \\
& (\sin((2)2\pi/5) \\
& ((t - (2)\alpha)) \\
& (1.2^{(t-(2)\alpha)}) \cos((t - (2)\alpha))) \\
& + \cos((2)2\pi/5) \\
& ((t - (2)\alpha) \\
& (1.2^{(t-(2)\alpha)}) \sin((t - (2)\alpha))) \\
& + (\lceil m(t - ((3)\alpha)) \rceil)(\lfloor m(-t + (4\alpha)) \rfloor + 1) \\
& (\sin((3)2\pi/5) \\
& ((t - (3)\alpha)) \\
& (1.2^{(t-(3)\alpha)}) \cos((t - (3)\alpha))) \\
& + \cos((3)2\pi/5) \\
& ((t - (3)\alpha) \\
& (1.2^{(t-(3)\alpha)}) \sin((t - (3)\alpha))) \\
& + (\lceil m(t - ((4)\alpha)) \rceil)(\lfloor m(-t + (5\alpha)) \rfloor + 1) \\
& (\sin((4)2\pi/5) \\
& ((t - (4)\alpha)) \\
& (1.2^{(t-(4)\alpha)}) \cos((t - (4)\alpha))) \\
& + \cos((4)2\pi/5) \\
& ((t - (4)\alpha) \\
& (1.2^{(t-(4)\alpha)}) \sin((t - (4)\alpha)))
\end{aligned} \tag{3}$$