

# Dissertation draft

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Standard economic theory suggests that retirement annuities should be highly prized by individuals as a way to insure against the risk of late death Yaari (1965). However, in developed countries rates of annuitization are far below the levels that theory predicts. In this paper I test two competing hypotheses for the annuity problem: bequests and pessimistic life expectancy. In most developed countries, individuals are forced to contribute to either a defined benefit or defined contribution pension. A defined benefit pension accumulates throughout your job tenure as Under the coalition government in the UK the law regarding the use of private defined contribution pensions changed. Individuals were no longer forced to annuitise their pension pots and could access them in a variety of ways such as lump sum withdrawals or income drawdown and subsequently the number of annuities sold in the UK dropped precipitously.

Depending on the reason for the lack of annuitization in the UK, the consumption response of retirees to the pension reform will differ. If individuals do not annuitise because of pessimistic life expectancy I will show that their consumption should increase. If, on the other hand, individuals do not annuitise because of a bequest motive, consumption should not change much as a result of the reform. I will solve lifecycle models for both of these cases and simulate consumption decisions with, and without, forced annuitization. I will then use a variety of empirical models to measure the consumption change in early retirement that resulted from the policy reform. The size and magnitude of this change will be indicative of the mechanism causing the annuitization problem.

The importance of retirement policy to individuals in the UK is growing. The number of individuals of pensionable age is expected to grow from 11.9 million in 2020 to 15.2 million in 2045 according to the latest ONS statistics and for every 1000 people of working age there will be 341 of pensionable age in 2045 compared to 280 in 2020 ONS (2020). The increase in absolute and relative numbers of elderly makes retirement policy more important. Moreover, private, defined contribution (DC), pensions are becoming increasingly common and are predicted to grow as current cohorts age Cribb and Karjalainen (2023). Therefore, policies regarding how private pensions can be accessed will have a

larger impact on overall welfare for retirees.

The so called "pensions freedom act" received Royal Assent in December 2014 marked the end of a series of pension reforms carried out by the coalition government between 2010 and 2015. The reform was announced in the Spring budget and made it possible to withdraw money from a private pension pot subject to the marginal rate of income tax that an individual faced. In the June 2010 budget the government made a first reform to the annuitization rules, creating a minimum income requirement above which individuals would not need to annuitise more HMT (2011). However, this was set at £20,000 and therefore few individuals were eligible. The minimum income requirement was scrapped in the 2014 bill finally eliminating the compulsory annuities market. The impact of the reforms on annuity demand has been documented by Cannon et al. (2016). Using data from the Association of British Insurers they show that annuity demand dropped by 75% from its maximum.

## 0.1 Literature review

My paper draws on three main strands of literature. The annuity problem, the retirement saving problem and lifecycle models. **this intro is rubbish**

Yaari (1965) was the first to show that under standard assumptions we would expect individuals to annuitise all of their wealth at retirement to insure against the risk of long life. Since then there has been much literature discussing possible reasons that people do not annuitise. Finkelstein and Poterba (2002) and Finkelstein and Poterba (2004) find evidence of adverse selection, thereby making the 'money's worth' of annuities lower for the general population as opposed to the population of annuitants. However, they also find that theory would still predict annuitization.

Friedman and Warshawsky (1990) show that annuitization decisions can be fully explained by a mixture of bequest motives and actuarially unfair annuities. They solve an augmented life-cycle model with a range of parameters on how severe the rate of return is on the annuity versus market rates. For plausible values they find that individuals would optimally not annuitise much wealth. Similarly to Finkelstein and Poterba (2004), Friedman and Warshawsky (1988) show that there is a significant difference between the life expectancy of annuitants and the general population in the American annuity market but this cannot fully explain the annuitization problem. Only when bequest motives are added to the model can annuitization rates be rationalized.

Lockwood (2012) builds on this and shows that a realistic bequest motive in lifecycle simulations achieves realistic annuitization rates. He solves a simple lifecycle model with bequest motives taken from several recent papers in the literature. The bequest motives he picks therefore match other important aspects of the lifecycle model such as how much

individuals actually bequest and how rich individuals are when they bequest.

Lockwood (2018)

Vidal-Melia and Lejárraga-García (2004) have some interesting results. Need to talk about that.

*There are some more papers to include here. Time to go and have dinner.*

## 1 Data

The main data set I use is the English Longitudinal Study of Ageing (ELSA) Banks et al. (2023). ELSA repeatedly interviews individuals over the age of 50 and asks them a range of questions relating to their income and wealth as well as expectations about the future. Importantly it also includes detailed information pensions including the type of pension that an individual holds when working, thus I am able to distinguish between individuals who have defined benefit and defined contribution pensions. For ease of access I use Harmonized ELSA <sup>1</sup> which ensures that variables are comparable across waves. Since this only includes a subset of the questions in ELSA I also supplement it with variables taken directly from the data.

ELSA also includes questions on expenditures. In particular individuals are asked how much they consume on a range of broad categories.

I also use life tables from the UK’s Office for National Statistics. These give us risk of death for each age group. I adjust them to make death certain at age 110 as is common in the literature. I transform these so that I have risk of death conditional on being a given age since this is what is used in the life cycle simulations.

To illustrate the effect the reform had on sales of annuities in the UK I obtained product data from the Financial Conduct Authority. These track the sale of different financial products overtime including data on annuity sales.

To calculate subjective life expectancies I follow O’Dea and Sturrock (2023). Individuals are asked “What are the chances that you will live to be age X or more?” where X changes depending on the age of the interviewee. If individuals were under 65 then X was 75, if individuals were 66 and older they were asked the age that was 11 to 15 years older than them and is a multiple of 5. From wave three respondents were also asked “What are the chances that you will live to be age 85 or more?” if they were under 70. As most

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<sup>1</sup>”This analysis uses data or information from the Harmonized ELSA dataset and Codebook, Version G.2 as of July 2021 developed by the Gateway to Global Aging Data. The development of the Harmonized ELSA was funded by the National Institute on Aging (R01 AG030153, RC2 AG036619, R03 AG043052). For more information, please refer to <https://g2aging.org/>.”

recent retirees are under 70 we therefore have two data points. I carry out the following procedures: drop any individuals who think it is more likely they reach an older age than a younger age since; add, as a third data point their objective chance of reaching 110 according to the ONS life tables; fit these three points to a Weibull distribution using non-linear least squares. Then I create subjective survival tables.

**I could go into more detail here? Maybe I should. Add equation etc**

## 2 Methodology

I first solve a modified retirement lifecycle model. The problem that retirees face is as follows. Every period retirees solve:

$$V_t(a_t, y) = \max_{a_{t+1}, c_t} \{u(c_t) + p_t B(a_{t+1}) + \beta(1 - p_t)V_{t+1}(a_{t+1}, y)\}$$

subject to their budget constraint

$$c_t = a_t(1 + r) - a_{t+1} + y$$

where  $a_t$  are asset holdings in time  $t$ ,  $y$  is constant income for all periods and  $r$ . Income can come either from state pensions, defined benefit pension plans or purchased annuities.

$$u(c_t) = \frac{c_t^{1-\sigma}}{1-\sigma}$$

In some specifications retirees can leave bequests, I use the bequest function from Lockwood (2012).

$$B(a_t) = \left(\frac{m}{1-m}\right)^\sigma \frac{\left(\frac{m}{1-m}c_0 + a_t\right)^{(1-\sigma)}}{1-\sigma}$$

Where  $b_t$  is the amount left at death,  $m$  is a measure of bequest motive strength and  $c_0$  is a minimum amount of consumption that individuals want. **Check this**

First, I discretise the state space. I create a grid from 500 to 50,000 incrementing by 500 for income and 1000 to 500,000 incrementing by 1000 for financial assets. I solve the retirees problem using backward induction. At age 110 there is certainty of death so any leftover assets are carried over into the next period and bequested. This means that the value at the end of the final period is either 0 (if we do not allow a bequest motive) or the value of bequests. I then take this value function and solve an individuals final period problem, choosing assets next period (i.e. those to bequest) and how much to consume.

Using the optimal policy function in the last period, I calculate the value of the last period, which the utility function and the value function evaluated at the maximum.

This is then used in the problem the year before that. I repeat this process back to the age of retirement to obtain optimal consumption amounts for each year of retirement and associated value functions.

To simulate the ELSA data I solve this retirement problems for each new retiree in the data set dependent on their objective probability of death each period. I estimate with subjective life expectancies and objective life expectancies, I also estimate the model both with and without a bequest motive which was picked to fit the unforced real annuity rates seen in the data. I then estimate several empirical models with the simulated data.

In retirees first year of retirement I allow them to choose to annuitise some of their wealth. In practical terms this is moving down the asset grid but up the income grid and seeing if the value of being in that position is better than where the individual is currently. To calculate this trade-off I calculate the annual annuity payment that follows from a given annuity cost. I calculate this using objective life tables from the ONS using the following equation:

$$Ann = \delta * C * \left[ \sum_{t=Retage}^{110} \frac{1 - p_{t|Retage}}{(1 + r)^{t-Retage}} \right]^{-1}$$

Where  $C$  is the one-off payment,  $\delta$  is a factor that controls the 'money's worth' of annuity and  $p_{t|Retage}$  is the probability of death at age  $t$  conditional on being age  $Retage$ . So individuals can move  $C$  on the asset grid for gaining  $Ann$  on the income grid for the rest of their lives.

### 3 Empirical models

In this section I outline the key empirical models I run with both the simulated consumption data from the lifecycle models and with the real data from ELSA. I then see which lifecycle model better fits the consumption response that happened as a result of the pension reform.

I use a regression discontinuity design where I compare the consumption of recent retirees after the policy reform to recent retirees before the policy reform. The individuals who retired in 2014 and later were not forced to annuitise their defined contribution pension. The key assumption implicit in regression discontinuities is that nothing else changes at the time of the jump apart from the policy of interest. And that the policy occurs without individuals predicting it. The policy change was widely seen as a surprise by the media and financial planners, some of whom in fact complained that they had not been consulted enough. **How can I justify no other jumps at the jump**

Retirement year is the running variable and individuals are treated if retirement year is greater than 2013 and less than 2016. I consumption of individuals up to 2 years into retirement so that the sample size is larger. So if someone retired in 2014 and had consumption data in 2014 and 2016 I include both values. An individual is considered not treated if they retire before 2013 and after 2011. One benefit of using ELSA is that it includes data on pension type for individuals who are working. Therefore, I can differentiate between individuals who have a defined contribution pension and those who have a defined benefit contribution. To account for the fact that the reform only impacted individuals who had accumulated defined contribution pension pots I interact the treatment dummy with an indicator variable signalling whether the individual had ever held a DC pension pot.

The estimating equation is therefore

$$Cons_{it} = \gamma X_{it} + \beta PostReformDC_{it} + \epsilon$$

And  $X_{it}$  is a set of controls including financial wealth etc

The ta

### 3.1 Rough plan

- Intro

1. I think Eric French wrote something about population that I could use in then intro to say why it is important.
2. "Latest data from HM Revenue Customs (published in April) showed more than £45bn has been taken from pots since 2015." <https://www.ftadviser.com/pensions/2022/0/freedoms-were-they-really-a-good-idea/>
3. Add bit about DC/DB pensions in the intro. Also talk about heterogeneity across countries. Some countries want to move towards more annuitisation. This annual review is a good source of info Banks and Crawford (2022)

- Lit review

- Models

- Empirical

1. Diff in diff
2. RDD
3. Matching?

4. can I use anything I learnt in panel? In some sense the decision to annuitise is a discrete choice problem so I could use something from there.
- Conclusion

## References

- Banks, J., G. D. Batty, J. Breedvelt, K. Coughlin, R. Crawford, M. Marmot, J. Nazroo, Z. Oldfield, N. Steel, A. Steptoe, M. Wood, and P. Zaninotto (2023). English longitudinal study of ageing: Waves 0-9, 1998-2019; elsa. Technical Report 38th Edition, UK Data Service.
- Banks, J. and R. Crawford (2022). Managing retirement incomes. *Annual Review of Economics* 14(1), 181–204.
- Cannon, E., I. Tonks, and R. Yuille (2016). The effect of the reforms to compulsion on annuity demand. *National Institute Economic Review* 237(1), R47–R54.
- Cribb, J. and H. Karjalainen (2023, June). How important are defined contribution pensions for financing retirement? Technical report, The Institute for Fiscal Studies, London.
- Finkelstein, A. and J. Poterba (2002). Selection effects in the united kingdom individual annuities market. *The Economic Journal* 112(476), 28–50.
- Finkelstein, A. and J. Poterba (2004). Adverse selection in insurance markets: Policyholder evidence from the u.k. annuity market. *Journal of Political Economy* 112(1), 183–208.
- Friedman, B. M. and M. Warshawsky (1988). *Annuity Prices and Saving Behavior in the United States*. University of Chicago Press.
- Friedman, B. M. and M. J. Warshawsky (1990). The cost of annuities: Implications for saving behavior and bequests. *The Quarterly Journal of Economics* 105(1), 135–154.
- HMT (2011, July). Finance act 2011. Technical report, House of Commons, London.
- Lockwood, L. M. (2012). Bequest motives and the annuity puzzle. *Review of Economic Dynamics* 15(2), 226–243.
- Lockwood, L. M. (2018, September). Incidental bequests and the choice to self-insure late-life risks. *American Economic Review* 108(9), 2513–50.
- O’Dea, C. and D. Sturrock (2023, 03). Survival pessimism and the demand for annuities. *The Review of Economics and Statistics* 105(2), 442–457.

- ONS (2020, January). National population projections: 2020-based interim. Technical report, Office for National Statistics. Accessed: 2021-07-08.
- Vidal-Melia, C. and A. Lejárraga-García (2004). Demand for life annuities from married couples with a bequest motive. Public economics, University Library of Munich, Germany.
- Yaari, M. E. (1965). Uncertain lifetime, life insurance, and the theory of the consumer. *The Review of Economic Studies* 32(2), 137–150.