

Report Presentation

EBS 2003: Second-year Project II

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Econometric Analysis

Exploratory Analysis

Cluster Identification

- Origin cluster: Cluster 1
- 4 most frequent destination clusters between 200 and 400km: clusters 12, 15, 186, 208
- Lanes aggregated to (week)daily data with $n=204$ obs. at periodicity 5

Outliers

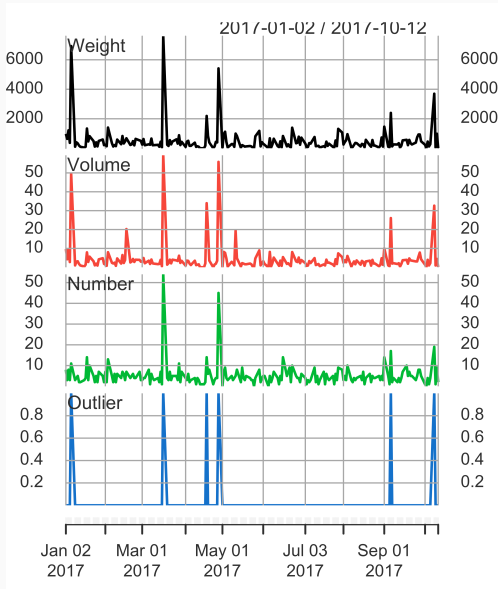
We use a custom function to generate dummy variable columns that are coded 1 for any observation where any of W_t , V_t , or N_t exceed their mean by 2 or more standard deviations, as given for *Weight* by

$$Flag_{Weight,i} = \begin{cases} 1 & \text{if } W_{t,i} \geq \mu_W + 2 \times \sigma_W \\ 0 & \text{else} \end{cases}$$

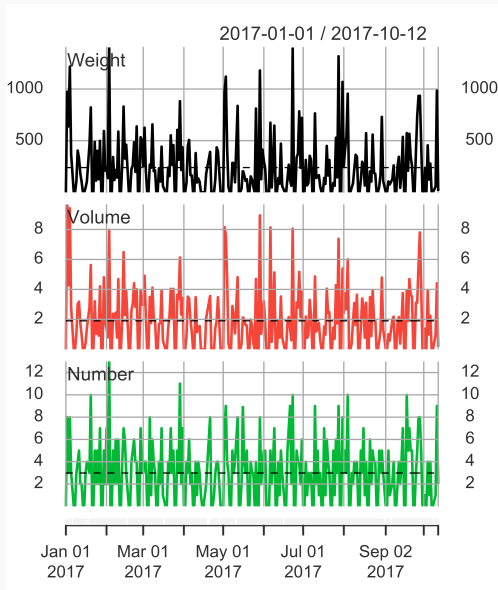
and use these three columns to create a fourth column:

$$Outlier = \begin{cases} 1 & \text{if } Flag_{Weight,i} = 1 \vee Flag_{Volume,i} = 1 \vee Flag_{Number,i} = 1 \\ 0 & \text{if } Flag_{Weight,i} = 0 \wedge Flag_{Volume,i} = 0 \wedge Flag_{Number,i} = 0 \end{cases}$$

Outliers (2)



Stationarity



Baseline Models

$$W_t = \alpha_0 + \alpha_1 \text{Tuesday} + \alpha_2 \text{Wednesday} + \alpha_3 \text{Thursday} + \alpha_4 \text{Friday} \quad (1) \\ + \alpha_5 \text{Outliers} + \epsilon_t$$

$$V_t = \alpha_0 + \alpha_1 \text{Tuesday} + \alpha_2 \text{Wednesday} + \alpha_3 \text{Thursday} + \alpha_4 \text{Friday} \quad (2) \\ + \alpha_5 \text{Outliers} + \epsilon_t$$

$$N_t = \alpha_0 + \alpha_1 \text{Tuesday} + \alpha_2 \text{Wednesday} + \alpha_3 \text{Thursday} + \alpha_4 \text{Friday} \quad (3) \\ + \alpha_5 \text{Outliers} + \epsilon_t$$

Baseline Models: Estimation Results

Table 1: Baseline Regression Results

	<i>Dependent variable:</i>		
	Weight	Volume	Number
tuesday	-21.0671	0.0723	-1.3210
wednesday	67.3354	0.5663	0.8576
thursday	-6.6085	0.8012	-1.3454*
friday	391.4009***	2.7827***	2.3422***
Outlier	4,204.3500***	39.0742***	20.8399***
Constant	280.7378***	2.2310***	4.3698***
Observations	204	204	204
Adjusted R ²	0.7276	0.7910	0.5411
F Statistic (df = 5; 198)	109.4428***	154.6670***	48.8782***

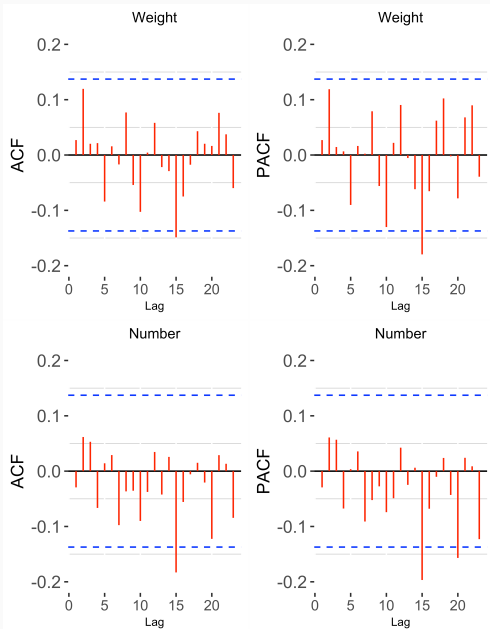
Note:

*p<0.1; **p<0.05; ***p<0.01

Econometric Analysis

SARMA(p,q)(P,Q) Models

SARMA(p,q)(P,Q)[5] Models: Identification



SARMA(p,q)(P,Q)[5] Models: Baseline Results

Table 2: ARMA(0,0)(0,0) Estimation Results

	<i>Dependent variable:</i>		
	Weight	Volume	Number
intercept	280.7378***	2.2310***	4.3698***
Outlier	4,204.3500***	39.0742***	20.8399***
tuesday	-21.0671	0.0723	-1.3210*
wednesday	67.3354	0.5663	0.8576
thursday	-6.6085	0.8012	-1.3454*
friday	391.4009***	2.7827***	2.3422***

Note:

* $p < 0.1$; ** $p < 0.05$; *** $p < 0.01$

SARMA(p,q)(P,Q)[5] Models: Final Specifications

Models automatically selected based on AIC (BIC gives identical results)

Weight : SARMA(0, 0, 0)(2, 0, 1)[5]

Volume : SARMA(0, 0, 0)(0, 0, 0)[5]

Number : SARMA(0, 0, 0)(2, 0, 1)[5]

Table 3: Information Criteria Comparison

	BIC Baseline	BIC Final	AIC Baseline	AIC Final
Weight	15.242	15.281	15.128	15.086
Volume	5.493	5.493	5.379	5.379
Number	5.582	5.619	5.468	5.456

SARMA(p,q)(P,Q)[5] Models: Estimation Results

Table 4: ARMA(p,q)(P,Q) Estimation Results

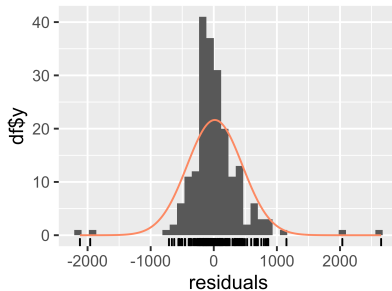
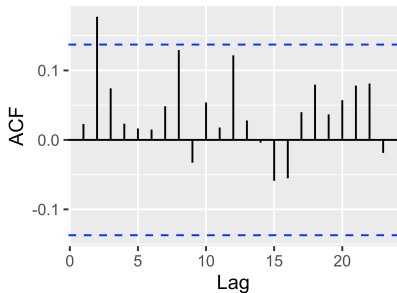
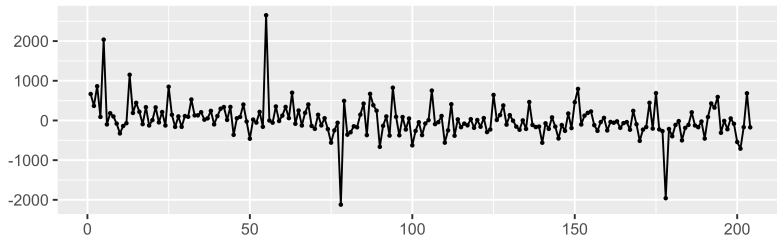
	<i>Dependent variable:</i>		
	Weight	Volume	Number
sar1	0.5582***		0.6363***
sar2	-0.0988		-0.1783**
sma1	-0.7263***		-0.6549***
intercept	282.8321***	2.2310***	4.4237***
Outlier	4,151.9630***	39.0742***	21.0669***
tuesday	-25.5452	0.0723	-1.3545***
wednesday	39.9651	0.5663	0.6840
thursday	-8.1966	0.8012	-1.3919***
friday	380.5566***	2.7827***	2.4926***

Note:

*p<0.1; **p<0.05; ***p<0.01

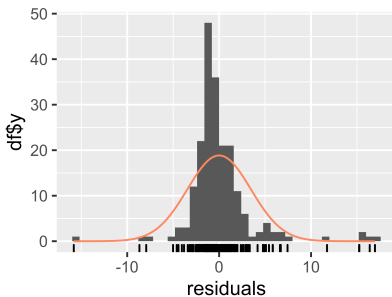
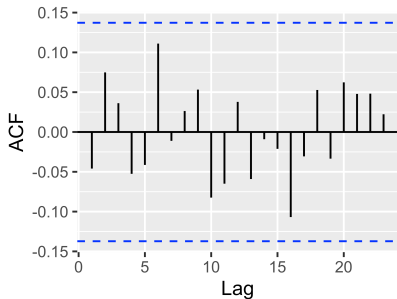
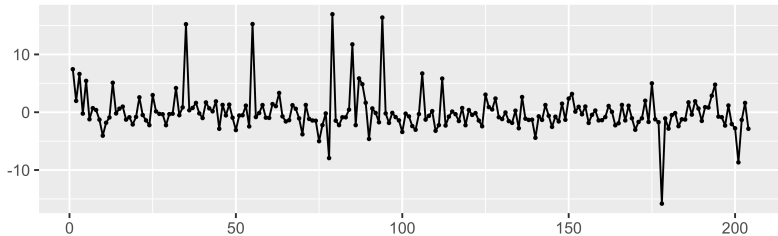
SARMA(p,q)(P,Q)[5] Models: Robustness

Residuals from ARIMA(0,0,0)(2,0,1)[5] with non-zero mean



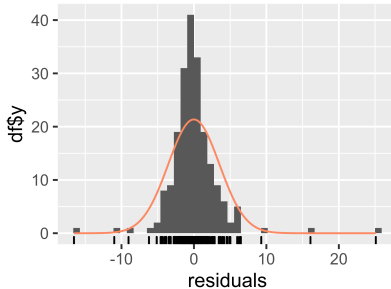
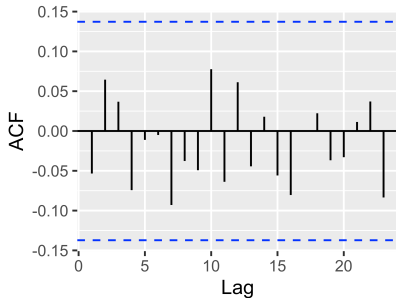
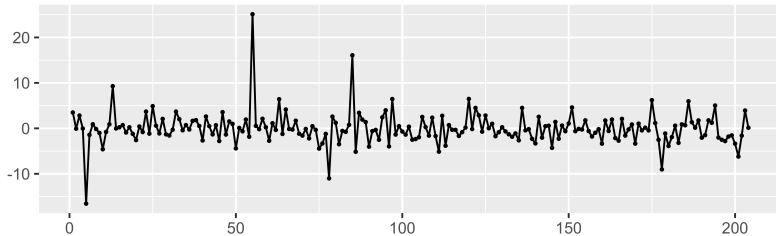
SARMA(p,q)(P,Q)[5] Models: Robustness (2)

Residuals from ARIMA(0,0,0) with non-zero mean



SARMA(p,q)(P,Q)[5] Models: Robustness (3)

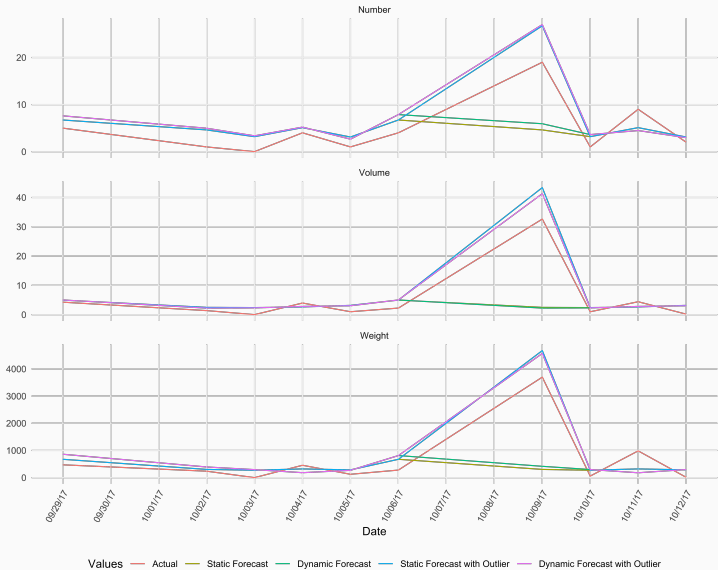
Residuals from ARIMA(0,0,0)(2,0,1)[5] with non-zero mean



Econometric Analysis

In-Sample Forecasting

Forecasting: In-Sample Accuracy



Forecasting: In-Sample Accuracy (2)

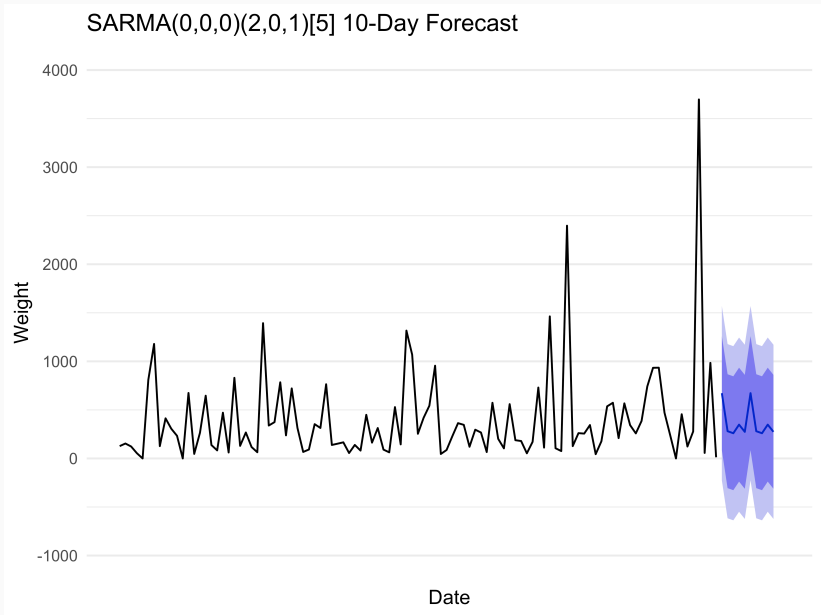
Table 5: RMSE of Forecast Models

	Weight	Volume	Number
Static Forecast	1113.878	9.721	5.171
Dynamic Forecast	1104.308	9.781	5.021
Static with Outlier	428.418	3.886	3.469
Dynamic with Outlier	468.031	3.281	3.810

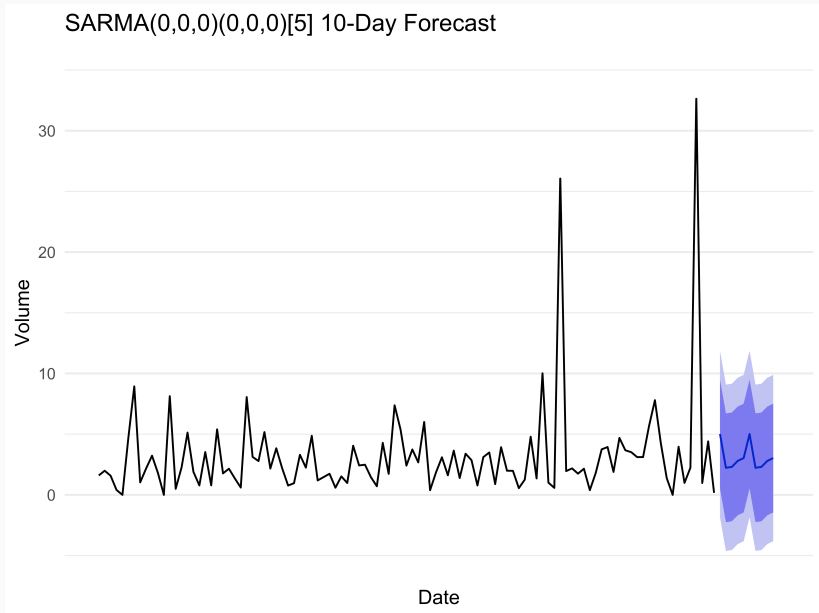
Econometric Analysis

Out-Of-Sample Forecasting

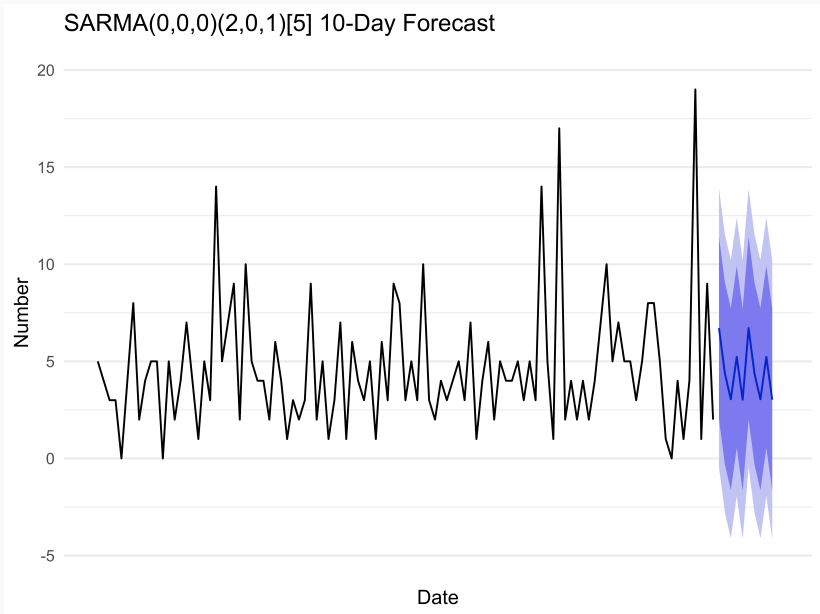
Forecasting: Out-of-Sample



Forecasting: Out-of-Sample (2)



Forecasting: Out-of-Sample (3)



Vehicle Routing

Program Structure

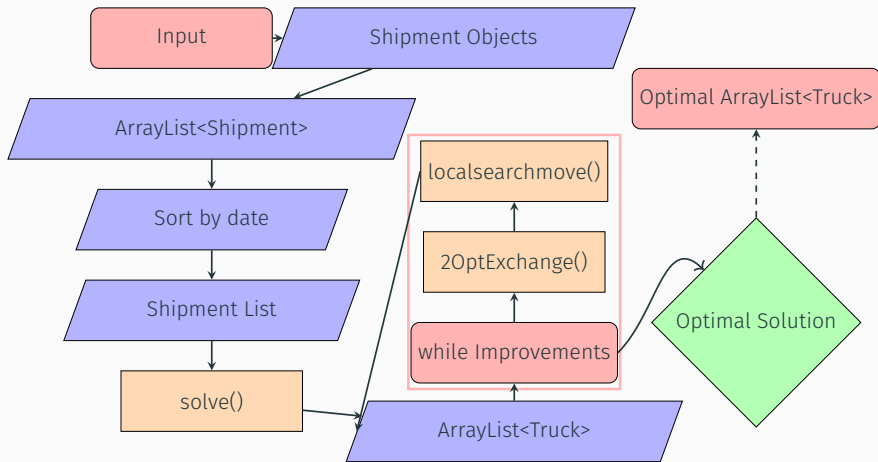
Objects

```
1 public class Shipment {  
2     private final Date PDate;  
3     private final double Weight;  
4     private final double Volume;  
5     private final double OriginClusterLat;  
6     private final double OriginClusterLong;  
7     private final Customer customer;  
8 }  
9  
10 public class Customer {  
11     private double lat;  
12     private double lon;  
13     private final String ID;  
14     private int numShip = 0;  
15 }
```

Objects (2)

```
1 public class Truck {  
2     private double currentWeight = 0;  
3     private double currentVolume = 0;  
4     private final int truckId;  
5     private final ArrayList<Shipment> shipments = new  
        ArrayList<>();  
6     private ArrayList<Customer> route = new ArrayList<>();  
7 }
```

Execution Flowchart



Vehicle Routing

Local Search

Code Listing: Nearest Neighbour Heuristic

```
1 Let  $S \neq \emptyset$  be the set of shipments,  $C \neq \emptyset$  the set of customers;  
2 Let  $T = \{t_1\}$  be the set of trucks;  
3 while  $S \neq \emptyset$  do  
4     Take  $t \in T$ ;  
5     Let  $c = \text{minDistCustomer}(t)$ ;  
6     for  $s \in S$  do  
7         Take  $s \in S$ ;  
8         if  $s.\text{customer} = c$  AND no constraints violated then  
9             add( $s, t$ ),  $S = S \setminus \{s\}$ ;  
10            add( $c, \text{Route}(t)$ );  
11         else if constraints violated then  
12              $T = T \cup \{t_{\text{new}}\}$ ;  
13             break;
```

Code Listing: 2-Opt-Exchange

```
1 Take  $t \in T$  a truck in the set of trucks;
2 Let  $R = \text{Route}(t)$ ,  $bd = \text{distance}(R)$ ;
3 Let  $newd = 0$ ;
4 while foundImprovement do
5     for  $1 \leq i < |R| - 2$  do
6         for  $i + 1 \leq j < |R| - 1$  do
7              $newR = \text{reverse}(R, i, j)$ ;
8              $newd = \text{distance}(newR)$ ;
9             if  $newd < bd$  then
10                  $bd = newd$ ;
11                  $R = newR$ ;
```

Code Listing: Local Search Move

```
1 Take  $t_1, t_2 \in T$ , where  $t_1 \neq t_2$  are trucks;  
2 Let  $R_1 = \text{Route}(t_1)$ ,  $R_2 = \text{Route}(t_2)$ ,  $bd = \text{distance}(R_1 + R_2)$ ;  
3 while foundImprovement do  
4   for  $1 \leq i < |R_1| - 1$  do  
5     for  $1 \leq j < |R_2| - 1$  do  
6       Let  $c = R_2[j]$  gets customer in route 2 at position  $j$ ;  
7       Let  $\text{new}R_1 = R_1 \cup \{c\}$  at position  $i$ ;  
8       Let  $\text{new}R_2 = R_2 \setminus \{c\}$ ;  
9       if  $\text{distance}(\text{new}R_1 + \text{new}R_2) < bd$  AND no constraints  
10        are violated then  
11           $bd = \text{totalDistance}(\text{new}R_1 + \text{new}R_2)$ ;  
12          Move all shipments with customer  $c$  from  $t_2$  to  $t_1$ ;  
           $R_1 = \text{new}R_1, R_2 = \text{new}R_2$ ;
```

Vehicle Routing

Results

Results

```
1 Date #10: 24/07/2017
2 Total cost of the feasible basic solution: 1493.39 EUR
3 Truck #1: Weight: 15.8/22 Volume: 78.77/82
4 Route: Cluster > FR2055 > FR1207 > FR2006 > FR321 > FR34 >
      FR178 > FR4710 > FR5000 > FR3307 > FR743 > FR47 >
      FR813 > FR3601 > FR2834 > FR1890 > FR953 > FR >
      Cluster
5
6 Truck #2: Weight: 3.6/22 Volume: 62.24/82
7 Route: Cluster > FR > Cluster
8
9 Truck #3: Weight: 2.5/22 Volume: 38.34/82
10 Route: Cluster > FR2754 > FR2845 > FR144 > FR3236 > FR2672
      > FR3191 > FR849 > FR226 > Cluster
11
12 Optimal Total cost : 1491.58 EUR
13 Number of trucks used: 3
14 Method executed in 6 milliseconds, of which
15 Obtaining the feasible basic solution took 2 ms
16 Optimizing the basic solution took 4 ms
```

Questions?