# Robust autonomous landing of fixed-wing UAVs in wind

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Half time report

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#### Problem description

#### Research questions:

- 1. How can sampling-based motion planning techniques be used to generate landing sequences for fixed-wing UAVs?
- 2. How can safe landings be guaranteed when taking wind effects into account?

#### Scope

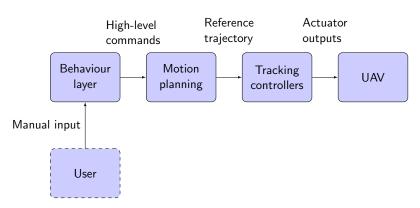


Figure 1: Components of a general autonomous system

#### Kinematic model

$$\dot{x}_{N} = \cos \psi + \cos$$
 (1)  
 $\dot{y}_{E} = \sin \psi + \sin$  (2)  
 $\dot{\psi} = \frac{g}{2} \tan \phi$  (3)

$$\dot{\phi} = f_{\phi}(\phi - \phi^{c}) \tag{4}$$

# Straight path following in wind

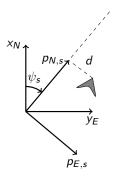


Figure 2: Coordinate frame for straight path following

# Straight path following in wind (contd)

$$\dot{d} \equiv \dot{p}_{E,s} = \sin(\psi - \psi_s) + \sin(-\psi_s)$$

$$\dot{\psi} = \frac{g}{2} \tan \phi$$
(5)

$$d pprox 0$$
,  $\dot{d} pprox 0$  means that  $\sin(\psi - \psi_{s}) + \sin(-\psi_{s}) = 0$  so

$$\equiv -\arcsin\left(\sin(-\psi_s)\right) + \psi_s \tag{7}$$

# Trajectory following controller

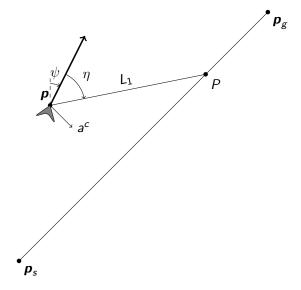


Figure 3:  $L_1$  controller logic

# Trajectory following controller (contd)

$$= \begin{bmatrix} \cos \psi \\ \sin \psi \end{bmatrix} + \begin{bmatrix} \cos \\ \sin \end{bmatrix}$$

$$a^{c} = 2 \frac{V^{2}}{L_{1}} \sin \eta, \quad V = \|\|$$

$$\phi^{c} = \tan^{-1}(a^{c}/g)$$

$$(8)$$

$$(9)$$

## State and action set definitions

$$x = (x_N, y_E, \psi)$$
 (11)  
 $u = (p_{N,g}, p_{E,g})$  (12)

# Closed loop system

$$\dot{\psi} = \frac{a^{c}(x, u)}{}$$
(13)

Physical constraint:  $\dot{\psi} \leq \dot{\psi}_{\text{max}} \Rightarrow$ 

$$\underline{\dot{\psi}}(x,u) = \begin{cases} a^c(x,u)/ & |a^c(x,u)/| \le \dot{\psi}_{\text{max}} \\ \operatorname{sgn}(a^c(x,u)/)\dot{\psi}_{\text{max}} & \text{otherwise} \end{cases}$$
(14)

# Closed loop system (contd)

$$\dot{x} = f(x, u) = \begin{bmatrix} \cos \psi + \cos \\ \sin \psi + \sin \\ \dot{\psi}(x, u) \end{bmatrix}$$
 (15)

#### Motion primitives

- ▶ Different motion primitives for different wind direction
- ▶ Different motion primitives for different wind speeds

# Motion primitives (contd)

Constraints on final course instead of heading where course is defined as

$$\psi_c(x) = \tan^{-1}\left(\frac{\sin\psi + \sin}{\cos\psi + \cos}\right) \tag{16}$$

# Optimal control problem

$$\min_{x(t),u,T} \qquad J = |d(x(T),u)|^2 + |\psi_c(x(T)) - \psi_d|^2 + \int_0^T dt$$
 (17a) subject to 
$$\psi(0) = \qquad \qquad (17b)$$
 
$$\psi_c(x(0)) = 0, \quad |\psi_c(x(T)) - \psi_d| \leq \Delta \psi_{\min} \quad (17c)$$
 
$$\dot{x} = f(x(t),u) \qquad \qquad (17d)$$
 
$$x(t) \in \qquad \qquad (17e)$$
 
$$u \in \qquad (17f)$$

# Optimal control problem (contd)

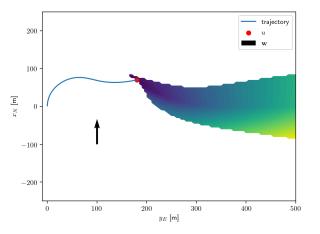


Figure 4: J for = 14 m/s, = 5 m/s, = 0°,  $\psi_d=90^\circ$ 

# Optimal control problem (contd)

Derivative free optimization methods

$$\min_{x \in \mathbb{R}^n} \qquad f: x \to \mathbb{R}$$
 (18a) subject to  $x \in_{feasible}$  (18b) (18c)

Mesh-Adaptive Direct Search (MADS)

## Resulting primitives

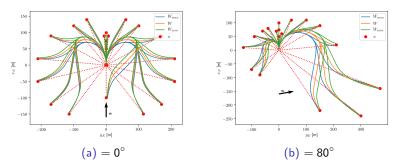


Figure 5: Motion primitives for different wind directions, = 5 m/s

#### Heuristic function

- States defined in inertial frame
- Cost is distance travelled by UAV in air-relative frame
- Not equal to inertial frame distance if  $\neq 0$

## Cost for straight line paths

Assuming that  $\psi_i = \psi_f =:$ 

$$V_{\parallel} = \cos \psi_s(\cos + \cos) + \sin \psi_s(\sin + \sin) \tag{19}$$

$$s_A = \frac{1}{|V_{\parallel}|} \|\boldsymbol{p}_{i+1} - \boldsymbol{p}_i\| \tag{20}$$

# Cost for arbitrary initial and final heading

- ▶ Dubin's path if = 0
- ▶ No analytical solution if  $\neq$  0
- Numerical solutions exist but computationally expensive

## Heuristic Look-Up Table

- ▶ Entries for different values of  $\psi_i$  from 0° to 180°
- Different require new HLUT
- Generated with Dijkstra's Algorithm using motion primitives

# Heuristic Look-Up Table (contd)

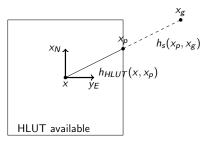


Figure 6: Projection of queries on HLUT

# Heuristic Look-Up Table (contd)

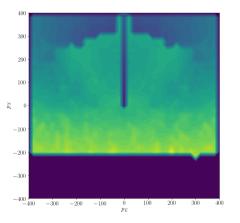


Figure 7: HLUT for  $\psi_f = 0^\circ$ 

# Landing sequences

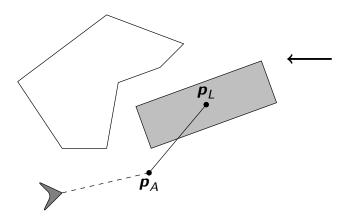


Figure 8: Landing sequence definition

# Landing sequences (contd)

- ▶ Approach: Descend at rate  $\dot{h}$  given by  $\boldsymbol{p}_A$  and  $\boldsymbol{p}_L$
- ▶ Flare: When below altitude , begin descending at fixed rate
- ▶ Has to enter landing area above altitude  $h_A$

# Optimal landing sequence

#### Objectives:

- 1. Land as closely to the center of as possible
- 2. Land against the wind if possible

# Optimal landing sequence (contd)

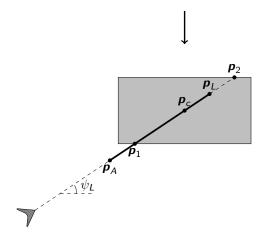


Figure 9: Variables to determine optimal landing sequence

# Optimal landing sequence (contd)

#### Divided into two steps:

- 1. Determine  $\psi_L$
- 2. Determine  $R_a = \| \boldsymbol{p}_A \boldsymbol{p}_2 \|$  and  $R_I = \| \boldsymbol{p}_L \boldsymbol{p}_2 \|$

# Determining approach direction

$$V_L(\psi) = \cos \psi(\cos + \cos) + \sin \psi(\sin + \sin)$$
 (21)

$$R_{\min}(\psi) = V_L(\psi) \frac{h_A - h_A}{\dot{h}_{\max}}$$
 (22)

$$R_{flare}(\psi) = V_L(\psi)$$
 (23)

# Determining approach direction (contd)

 $L(\psi)$ : Line from  ${m p}_1$  in direction  $\psi+180^\circ$  with length K for some K>0

$$\{\psi_L\}_{feas} = \{\psi : (R(\psi) \ge R_{\min}(\psi) + R_{flare}(\psi)) \cap (L(\psi) \notin)\} \quad (24)$$

$$\psi_{L,opt} = \underset{\psi \in \{\psi_L\}_{feas}}{\arg \min} R(\psi) \quad (25)$$

# Determining approach parameters

$$\dot{h} = f(R_a, R_l)$$

$$h(R) = h_0 - R \frac{\dot{h}}{V_L}$$

$$R_c = || \boldsymbol{p}_1 - \boldsymbol{p}_2 ||$$
(26)
$$(27)$$

# Determining approach parameters (contd)

Constraints:

$$h(R_a - 2R_c) \ge h_A \tag{29}$$
  
$$h(R_a - R_{flare} - R_I) = \tag{30}$$

# Determining approach parameters (contd)

$$\min_{R_a,R_l} \qquad J = R_a^2 + \lambda |R_c - R_l|^2 \qquad (31a)$$
 subject to 
$$R_a, R_l \ge 0 \qquad (31b)$$
 
$$\dot{h}(R_a, R_l) \le \dot{h}_{\text{max}} \qquad (31c)$$
 
$$(??)$$
 
$$(??)$$

## System overview

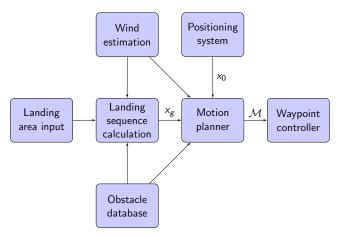


Figure 10: System overview

#### Results

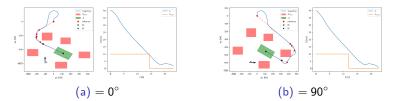


Figure 11: Resulting landing procedures for different wind directions, = 5 m/s

# Results (contd)

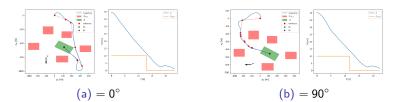


Figure 12: Resulting landing procedures for different wind directions,  $= 5 \ \text{m/s}$ 

#### Possible improvements

- Extend formulation to handle varying winds with the same motion primitive set/HLUT
- Investigate admissibility of heuristic (especially projection)
- Handle wind variations in landing sequence generation
- Estimate wind mean and variance online from measurements