

Max-Planck Institute for the Science of Light

11.03.2021

Seminar Talk

Topological states in real and synthetic quantum matter

Tobias Grass

ICFO^R

Topology and symmetry

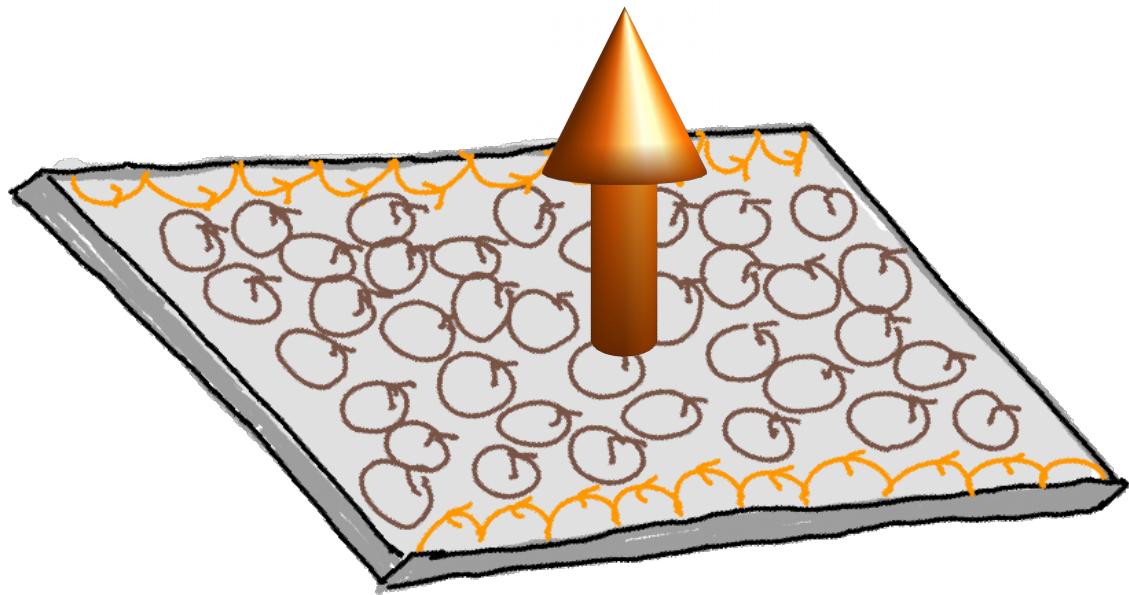
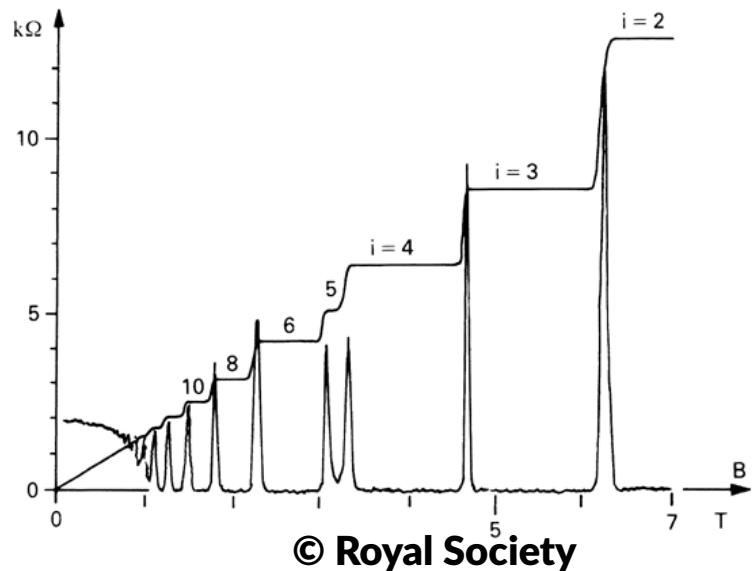


Topology and symmetry



Quantum Hall Systems

Robust transport property:
quantized Hall resistance



Magnetic field defines topology → chiral motion leads to robust edge transport



[von Klitzing, Dorda, Pepper, PRL (1980)]

Topological invariant from band curvature:

$$C = \frac{i}{2\pi} \int d\mathbf{k} \left\langle \frac{\partial u_{\mathbf{k}}^*(\mathbf{r})}{\partial \mathbf{k}} \right| \times \left| \frac{\partial u_{\mathbf{k}}(\mathbf{r})}{\partial \mathbf{k}} \right\rangle$$

Kubo formula:



$$\sigma_H = \frac{e^2}{h} C$$



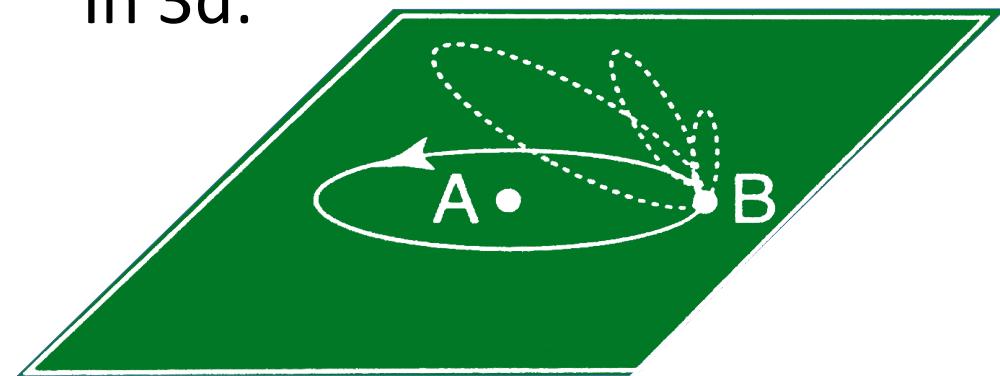
[Thouless, Kohmoto, Nightingale, den Nijs, PRL (1982)]

2016

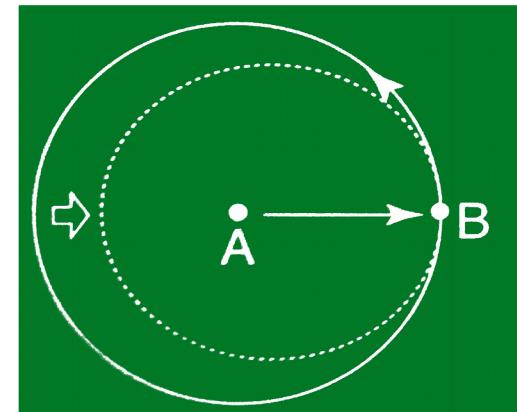
Anyons and non-Abelions

- Topological band structure (in 1d or 2d) + interactions:
→ Emergence of exotic quasiparticle (“anyons”)

In 3d:



In 2d:



Double Exchange = Identity

→ Bosons or Fermions

$$\Psi_{AB} = \pm \Psi_{BA}$$

Double Exchange non-trivial

→ Anyons

$$\Psi_{AB} = \exp(i\theta) \Psi_{BA}$$

- If anyonic states are degenerate, exchange corresponds to rotations within the degenerate space → non-Abelion anyons

Fractional Quantum Hall Effect



Tsui, Stoermer, Laughlin
1998

- Hall conductance $\sigma_H = \frac{e^2}{h} C$ quantized to fractional values:

$C = n \Rightarrow$ Integer Quantum Hall Effect

$n, p, q \in \mathbb{N}$

$C = \frac{p}{q} \Rightarrow$ Fractional Quantum Hall Effect

In general: $C = \nu$ (Landau level filling)

→ integer filling: HUGE single-particle gap

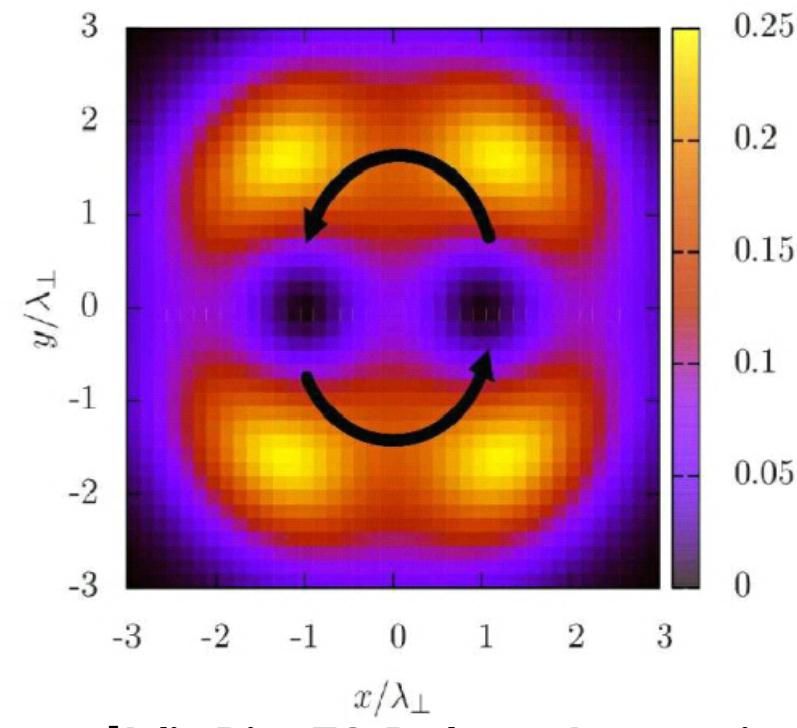
→ fractional filling: NO single-particle gap

- Interactions can yield strongly anticorrelated and gapped states

Examples: Laughlin state, Pfaffian state, ...

- Bulk excitations (e.g. quasiholes) behave like anyons

- Goal: experimental demonstration



[Julia-Diaz, TG, Barberan, Lewenstein,
New J. Phys. 14, 055003 (2012)]

Outline of the talk

- Fractional Quantum Hall physics in synthetic matter:

- Engineering of Hamiltonian

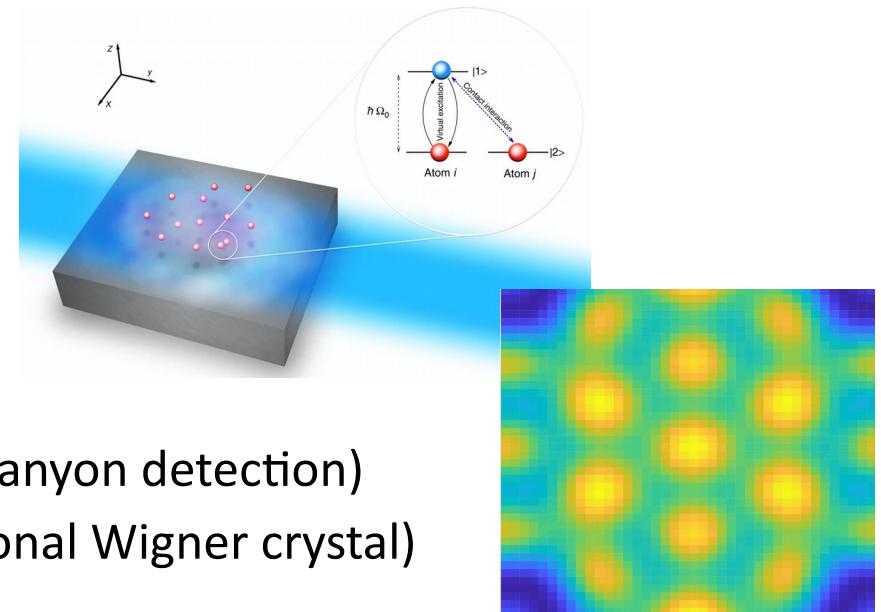
- Synthetic gauge fields

- Preparation of ground state

- Adiabatic scheme

- Reward of these efforts:

- enhanced detection opportunities (anyon detection)
 - engineering of exotic phases (fractional Wigner crystal)



- Fractional Quantum Hall physics in electronic matter:

- Monolayer graphene in B field:

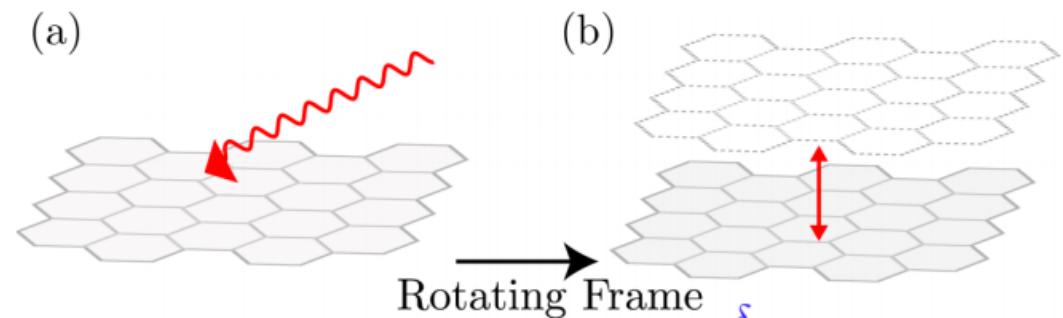
- Laughlin state

- Optical driving:

- synthetic bilayer structure

- Reward:

- non-Abelian Fibonacci anyons



Synthetic FQH matter: preparation

- Fractional Quantum Hall physics in synthetic matter:

- Engineering of Hamiltonian

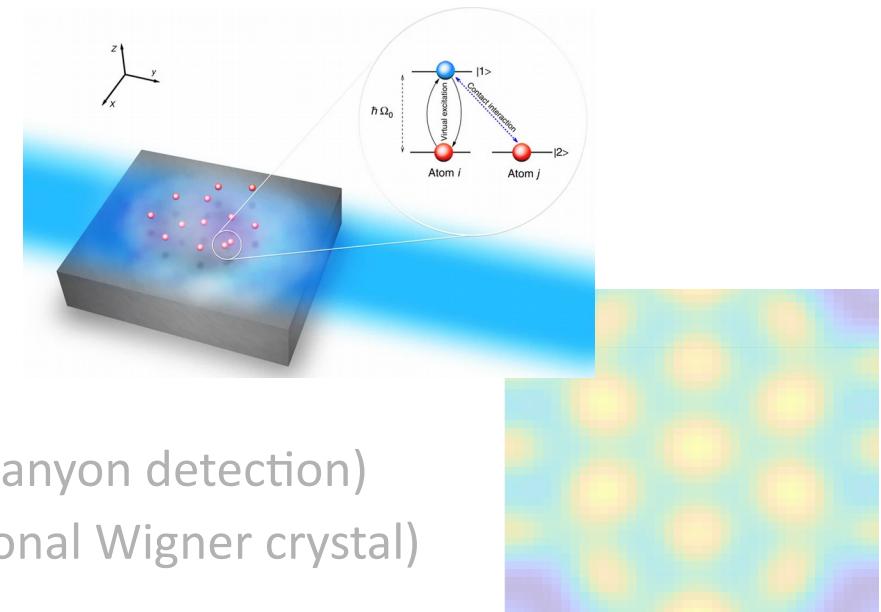
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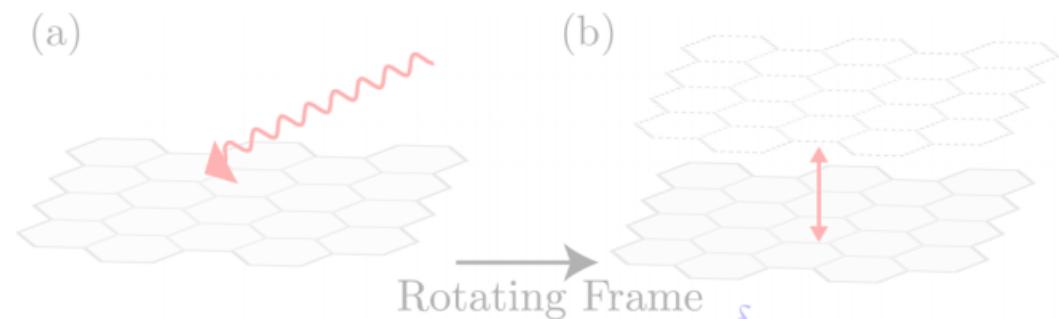
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Synthetic gauge fields

- Mimic effect of magnetic field in charge-neutral systems:
(cold atoms, photons, etc.)

- Optical techniques

Cold atoms in trap:

[Lin,..., Spielman, Nature (2009)]

Cold atoms in lattice:

[Aidelsburger,..., Bloch, PRL (2013)]

[Miyake,...,Ketterle, PRL (2013)]

Coupled resonators:

[Hafezi ...,Taylor, Nat. Phys. (2011)]

Modulated SC qubits:

[Roushan, ..., Martinis, Nat. Phys. (2016)]

Modulated ions:

[TG, ..., Lewenstein, PRA (2018)]

- Mechanical techniques

Optomechanical lattices: [Schmidt,...,Marquardt, Optica (2015)]

[Struck,...,Sengstock, PRL (2012)]

Lattice shaking: [Matthews, ..., Cornell, PRL (1999)]

[Madison,..., Dalibard, PRL (2000)]

Rotating gases: [Abo-Shaeer,..., Ketterle, Science (2001)]

[Gemelke, Sarajlic, Chu, arXiv, (2010)]

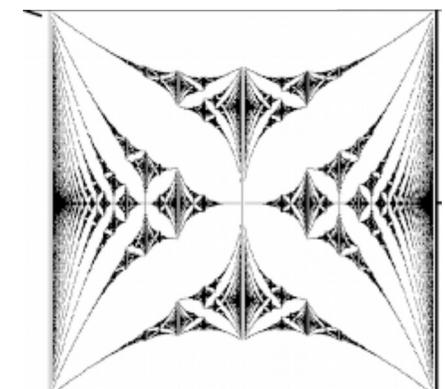
[Clark,...,Simon, Nature (2020)]

Rotating lattices:

Twisted cavities:

- Single-particle physics: edge states, Chern numbers
Hofstadter butterfly, ...

- Many-body physics: would/could support anyons,
but little explored yet!



Preparation of atomic Laughlin droplet

- Ingredients:
 - Interactions ✓ (Contact interaction)
 - Synthetic gauge fields ✓ (Rotation)

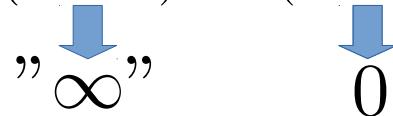
- But:

having the Hamiltonian ≠ having the state

- Way to Laughlin state:

Rotation produces Landau levels spectrum

$$E_{nm} = \hbar [(\Omega + \omega)n + (\Omega - \omega)m] + \text{const.}$$



Rotating faster flattens the Landau levels

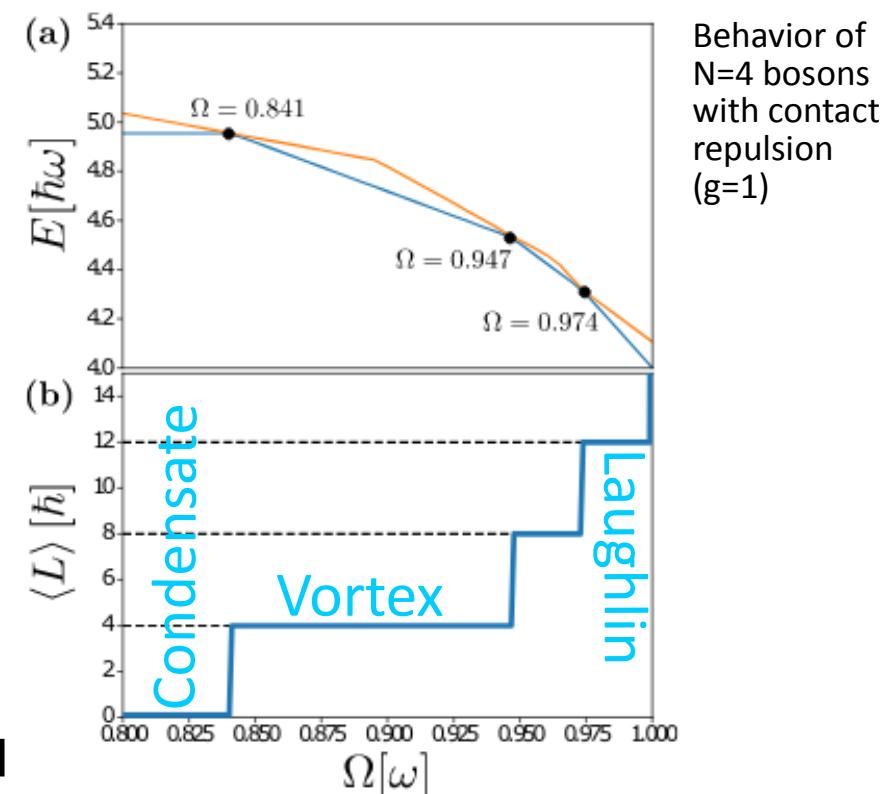


Repulsive interactions in a flat band: strongly anticorrelated ground states (vortices, vortex lattices, FQH states)

[Popp, Paredes, Cirac, PRA (2004)]

[Dagnino, Barberan, Lewenstein, Dalibard, Nat. Phys. (2009)]

[Andrade, Kasper, Lewenstein, Weitenberg, TG, arXiv 2009.08943]



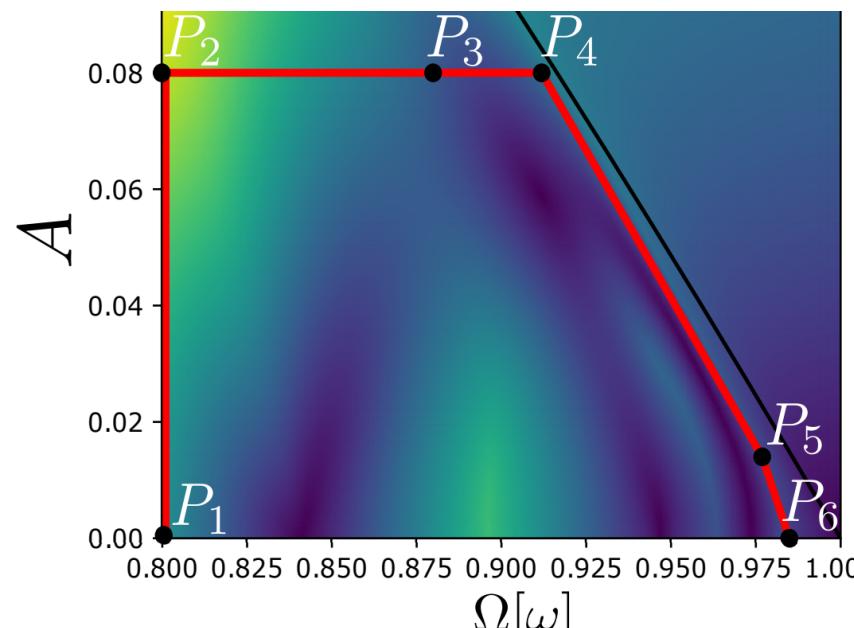
Preparation of atomic Laughlin droplet

- Ingredients:
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- But:

having the Hamiltonian ≠ having the state

- Way to Laughlin: **Adiabatic path via anisotropy-induced gaps**



[Popp, Paredes, Cirac, PRA (2004)]

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[Andrade, Kasper, Lewenstein, Weitenberg, TG, arXiv 2009.08943]



Barbara Andrade
(ICFO)



Valentin Kasper
(ICFO)



Christof
Weitenberg
(Uni Hamburg)



Maciej
Lewenstein
(ICFO)

Synthetic FQH matter: opportunities

- Fractional Quantum Hall physics in synthetic matter:

→ Engineering of Hamiltonian

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→ Preparation of ground state

Adiabatic scheme

→ Reward of these efforts:

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- Fractional Quantum Hall physics in electronic matter:

→ Monolayer graphene in B field:

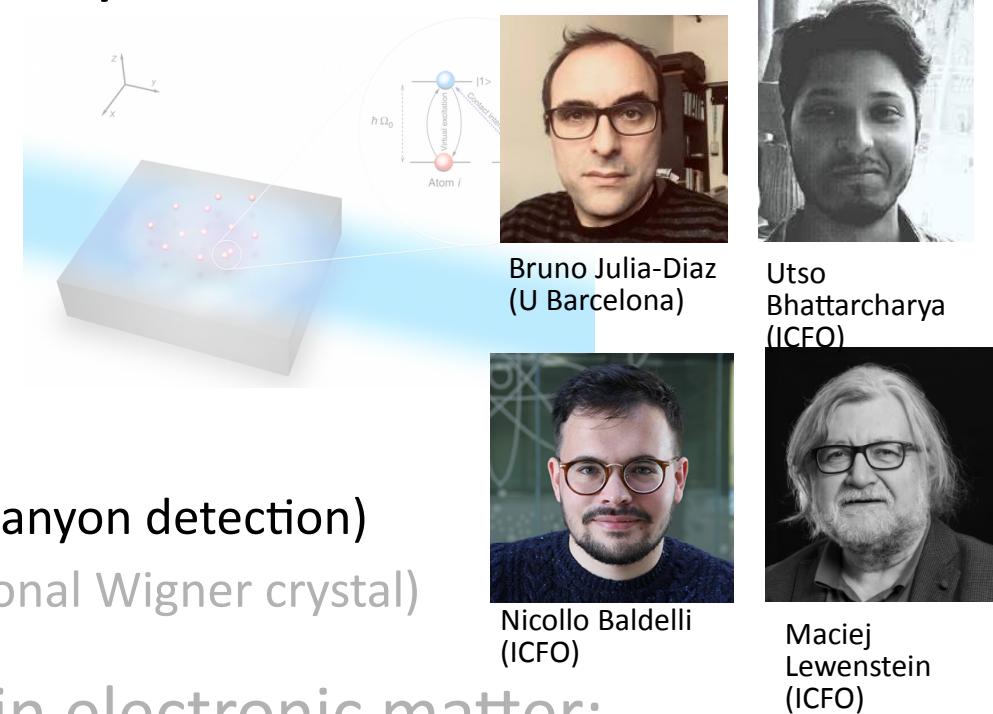
Laughlin state

→ Optical driving:

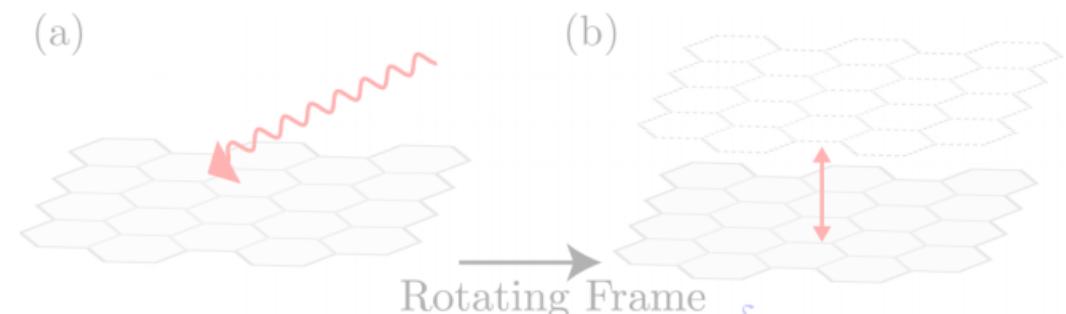
synthetic bilayer structure

→ Reward:

non-Abelian Fibonacci anyons



 Fundación "la Caixa"



Impurities for anyon detection

Probe system with impurity particles binding to anyonic quasiholes

[Zhang, Sreejith, Gemelke, Jain, PRL (2014)]
[Lundholm and Rougerie, PRL (2016)]
[Grusdt, ..., Demler, Nat. Commun. (2016)]
[Yakaboylu and Lemeshko, PRB, (2018)]

- Screening of magnetic field due to the liquid:

$$B^* = B(1 - \nu) \Rightarrow l_B^* = l_B / \sqrt{1 - \nu}$$

- Effective Landau level wave functions for the impurities:

$$\tilde{\varphi}_m(w) \sim w^m \exp \left[-(1 - \nu) \frac{|w|^2}{4l_B^2} \right] \text{ with average angular momentum: } L_m = \frac{m + \nu}{1 - \nu}$$

in contrast to the original wave functions

$$\varphi_m(w) \sim w^m \exp \left[-\frac{|w|^2}{4l_B^2} \right] \text{ with angular momentum: } L_m = m$$

- Can we use impurity angular momentum to trace anyon behavior?

[TG, Julia-Diaz, Baldelli, Bhattacharya, Lewenstein, Phys. Rev. Lett. 125, 136801 (2020)]

Impurities in Abelian liquids

For multiple impurities, the angular momentum reflects the filling of the single-particle levels:

Fermi sea:

$$L_F = \sum_{m=0}^{N_b-1} L_m$$

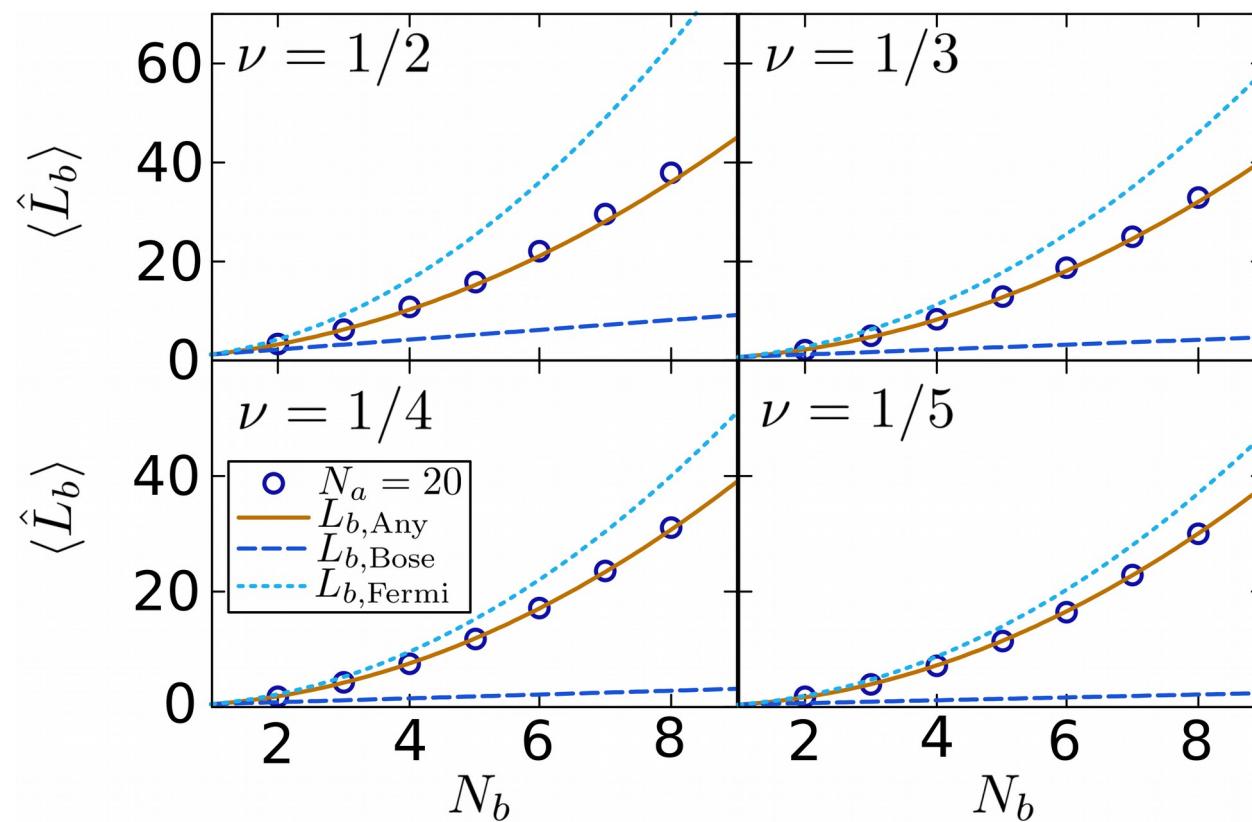
Bose condensate:

$$L_B = N_b L_0$$

Anyon gas:

$$L_A = (1 - \alpha)L_F + \alpha L_B$$

with statistical parameter α



Detection of α :
No braiding or interference needed, only density measurement!

Impurities in non-Abelian liquids

Hallmarks of non-Abelian liquids:

- Quasihole states are degenerate.
- Sensitivity of braiding phase to the parity of the number of particles in the liquid:

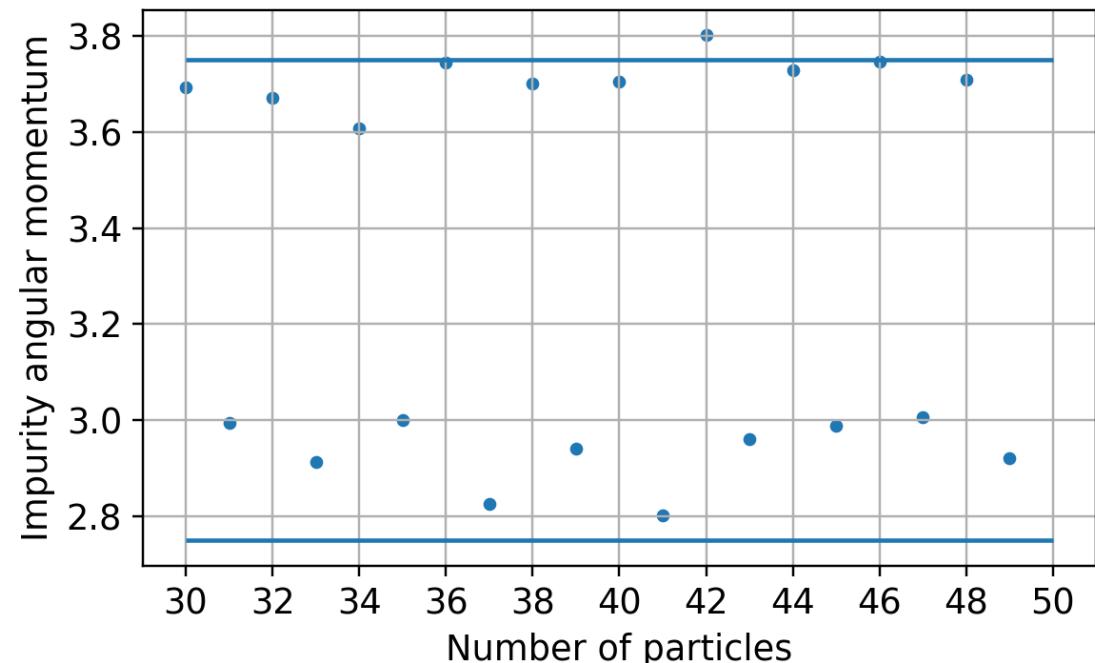
Statistical phase in Pfaffian liquid:

$$\alpha = \frac{\nu}{4} - \frac{1}{8} + \frac{P}{2}$$

[Macaluso, Comparin, Mazza, and Carusotto, PRL (2019)]
[Bonderson, Gurarie, Nayak, PRB (2011)]

Even-odd effect of impurity angular momentum:

[Baldelli, Julia-Diaz, Bhattacharya, Lewenstein, TG, arXiv 2102.02072]



Synthetic FQH matter: opportunities

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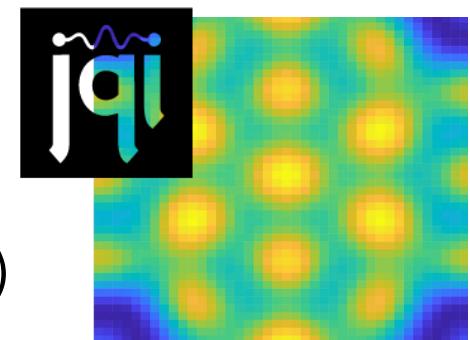
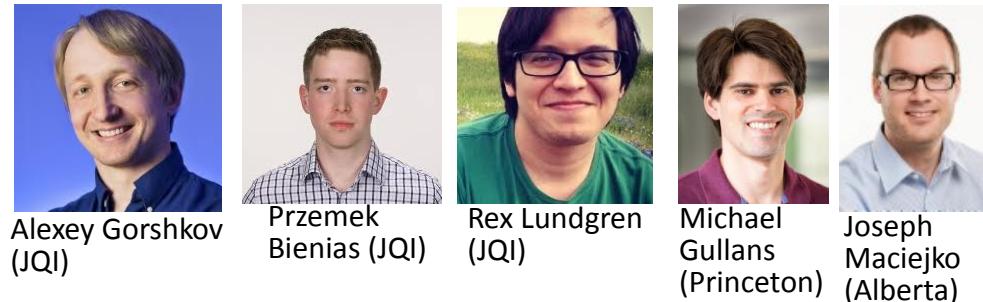
Synthetic gauge fields

→ Preparation of ground state

Adiabatic scheme

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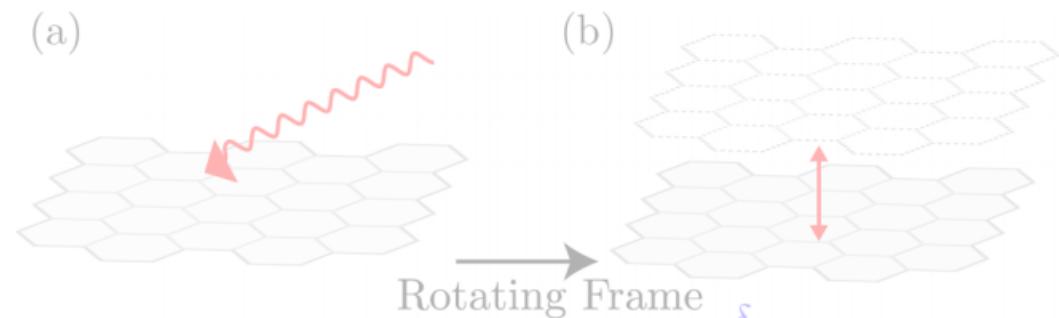
Laughlin state

→ Optical driving:

synthetic bilayer structure

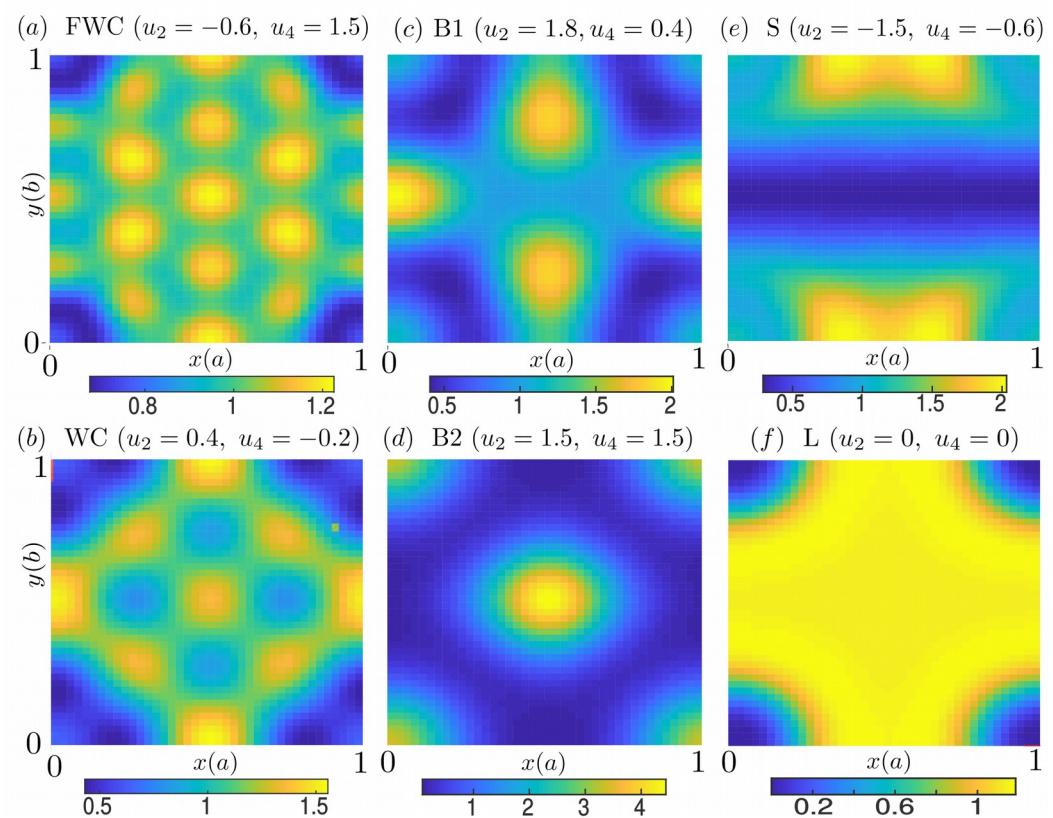
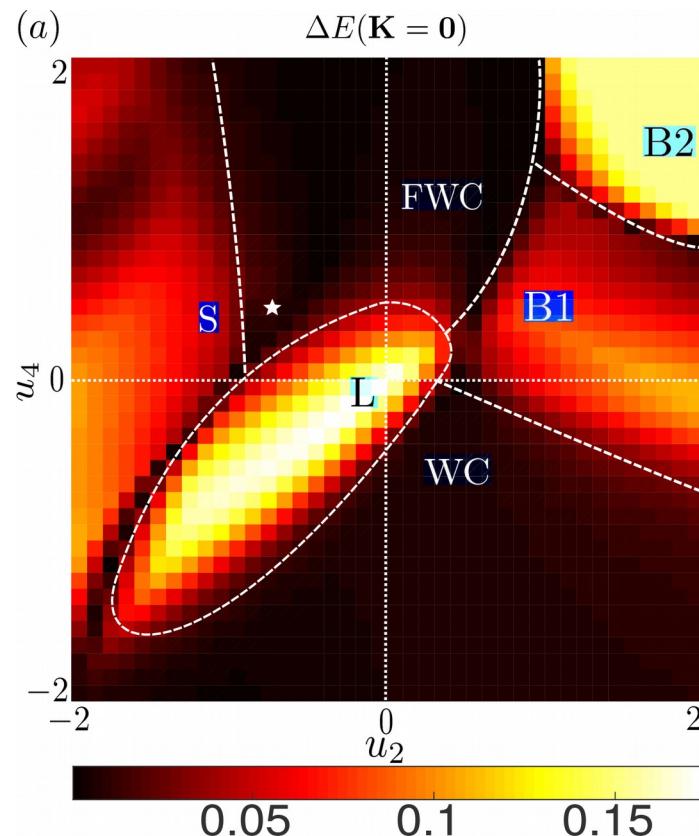
→ Reward:

non-Abelian Fibonacci anyons



Synthetic FQH matter: opportunities

- Interparticle interactions tunable via Rydberg dressing.
- Transition of Laughlin liquid into symmetry-broken phases:



[TG, Bienias, Lundgren, Gullans, Maciejko, Gorshkov, Phys. Rev. Lett. 121, 253403 (2018)]

- Fractional Wigner crystal: Exotic combination of topological order and symmetry-broken order?

[Xia, Eisenstein, Pfeiffer, West, Nat. Phys. (2011)]
[Samkharadze, ..., Fradkin, Csáthy, Nat. Phys (2016)]

Electronic FQH matter

- Fractional Quantum Hall physics in synthetic matter:

→ Engineering of Hamiltonian

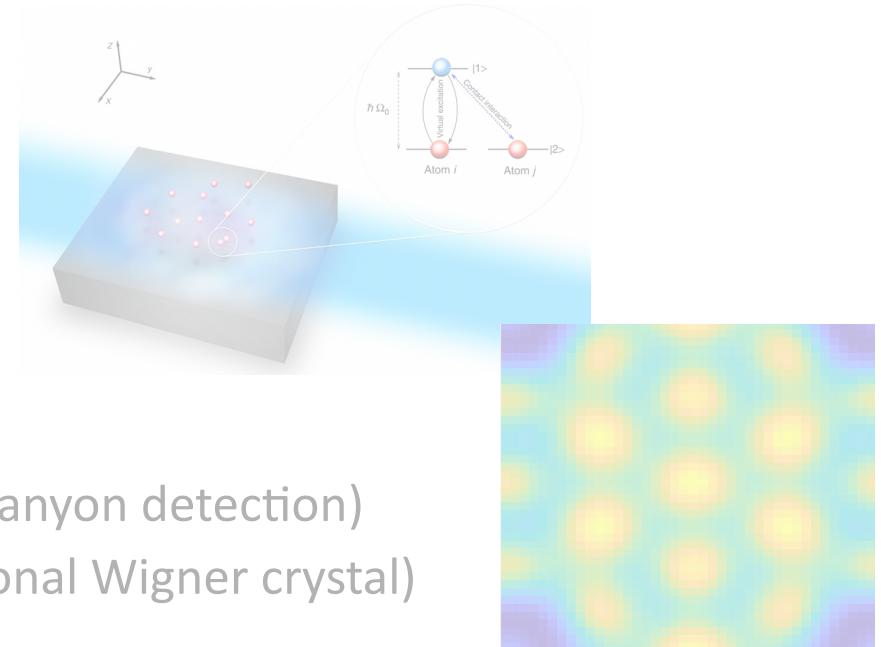
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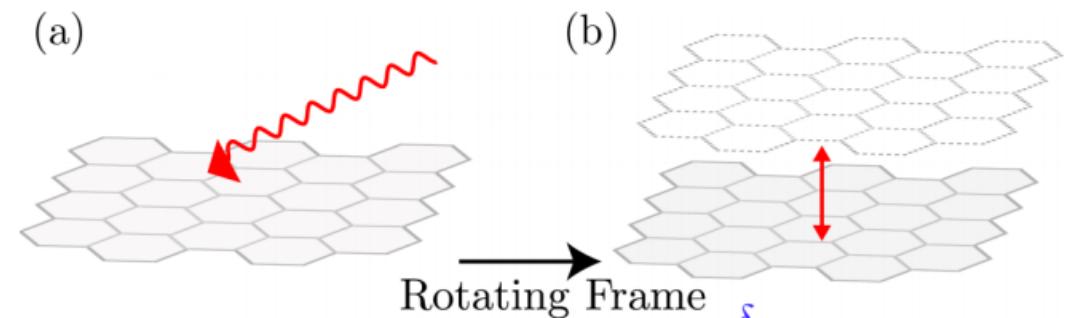
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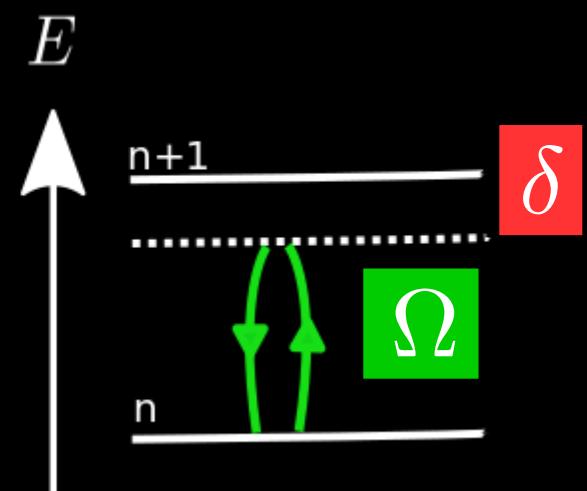
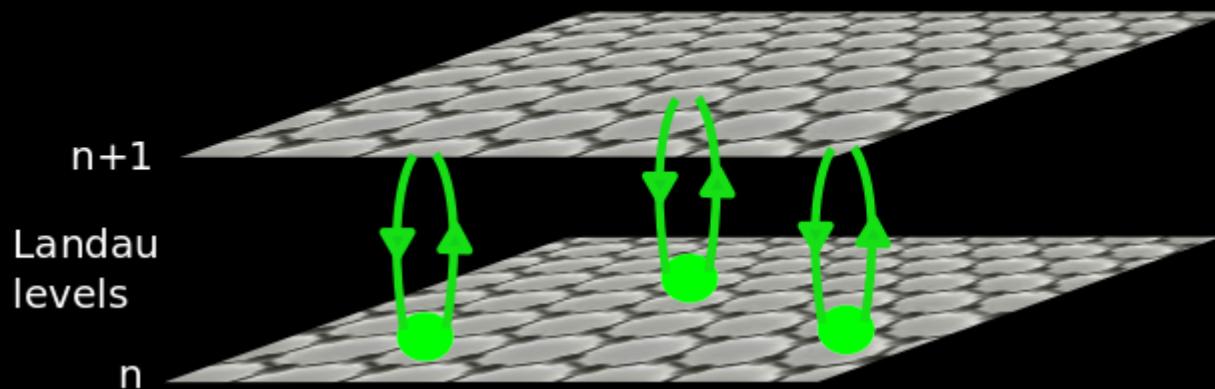
Optical driving in graphene

Optical engineering of electronic Hamiltonians:

- Floquet topological insulator in graphene
- Breaking of time-reversal symmetry through circularly polarized or twisted light

[Oka & Aoki, PRB (2009)]
[McIver, ..., Cavalleri, Nat. Phys. (2020)]
[Bhattacharya, Chaudhary, TG, Lewenstein arXiv:2006.10688]

In quantum Hall regime: Optically coupled Landau levels form synthetic bilayer.



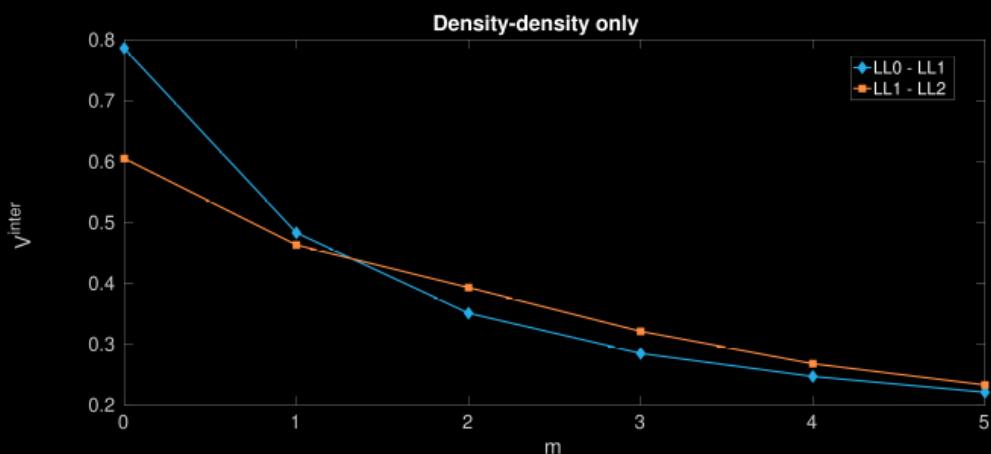
$$H_0 = \sum_m \left[\hbar\delta c_{n+1,m}^\dagger c_{n+1,m} + \hbar\Omega c_{n+1,m}^\dagger c_{n,m} \right] + \text{h.c.}$$

“chemical potential”

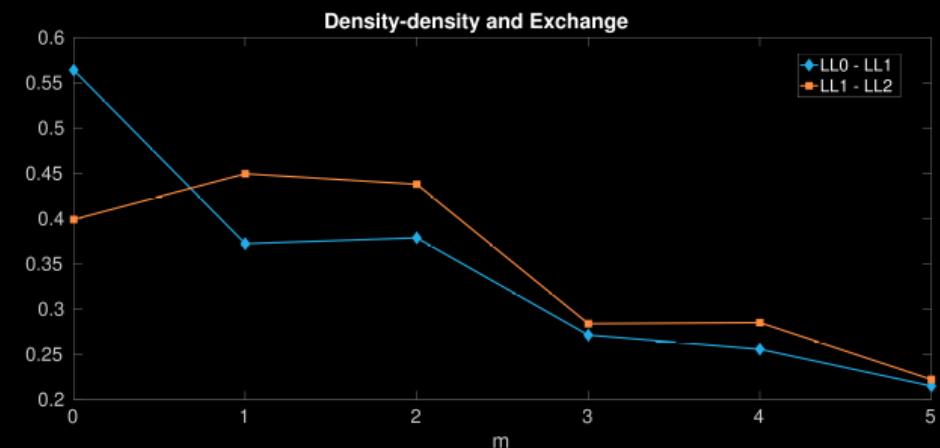
“interlayer tunneling”

Exotic interactions and Fibonacci phase

Synthetic bilayer exhibits exotic structure of Haldane pseudopotentials:



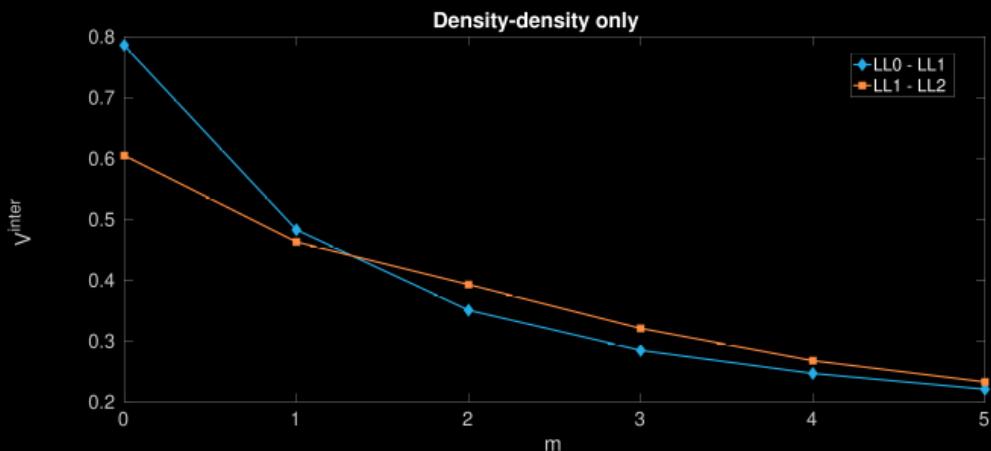
Normal bilayer: Monotonic decay.



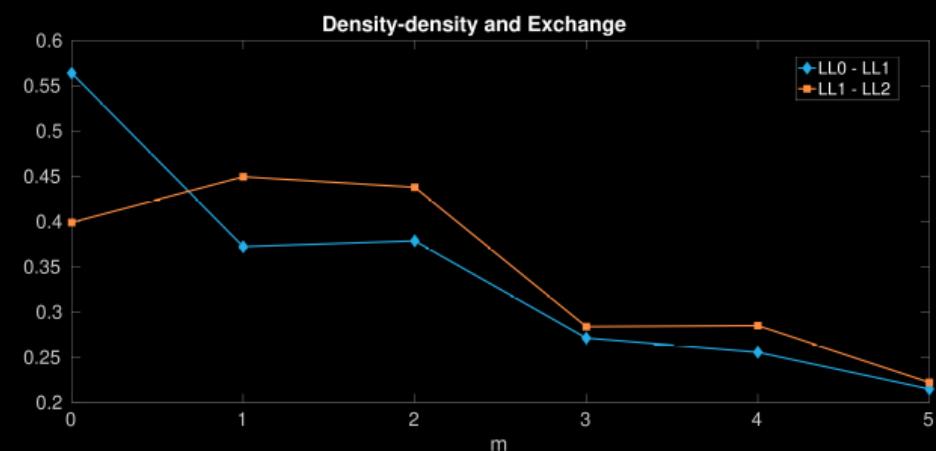
Synthetic bilayer interactions: non-monotonic behavior favoring singlets at $m=0$

Exotic interactions and Fibonacci phase

Synthetic bilayer exhibits exotic structure of Haldane pseudopotentials:



Normal bilayer: Monotonic decay.



Synthetic bilayer interactions: non-monotonic behavior favoring singlets at $m=0$

→ Synthetic bilayer supports non-Abelian Fibonacci phase.
(candidate for universal topological quantum computing)



Mohammad Hafezi (JQI)



Ze-Pei Cian (JQI)



Areg Ghazaryan (IST Austria)



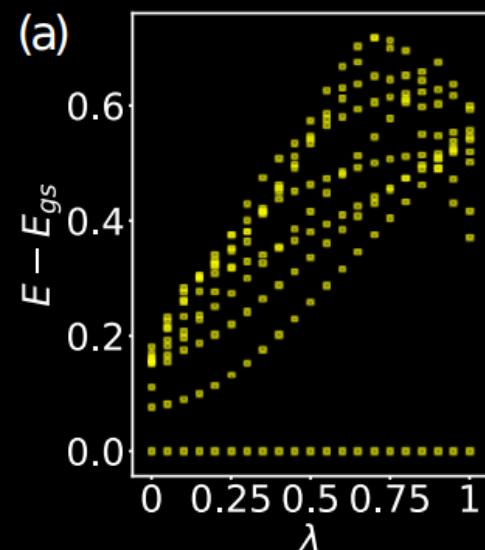
Pouyan Ghaemi (CUNY)



Abolhassan Vaezi (Tehran)



Zhao Liu (Zhejiang)

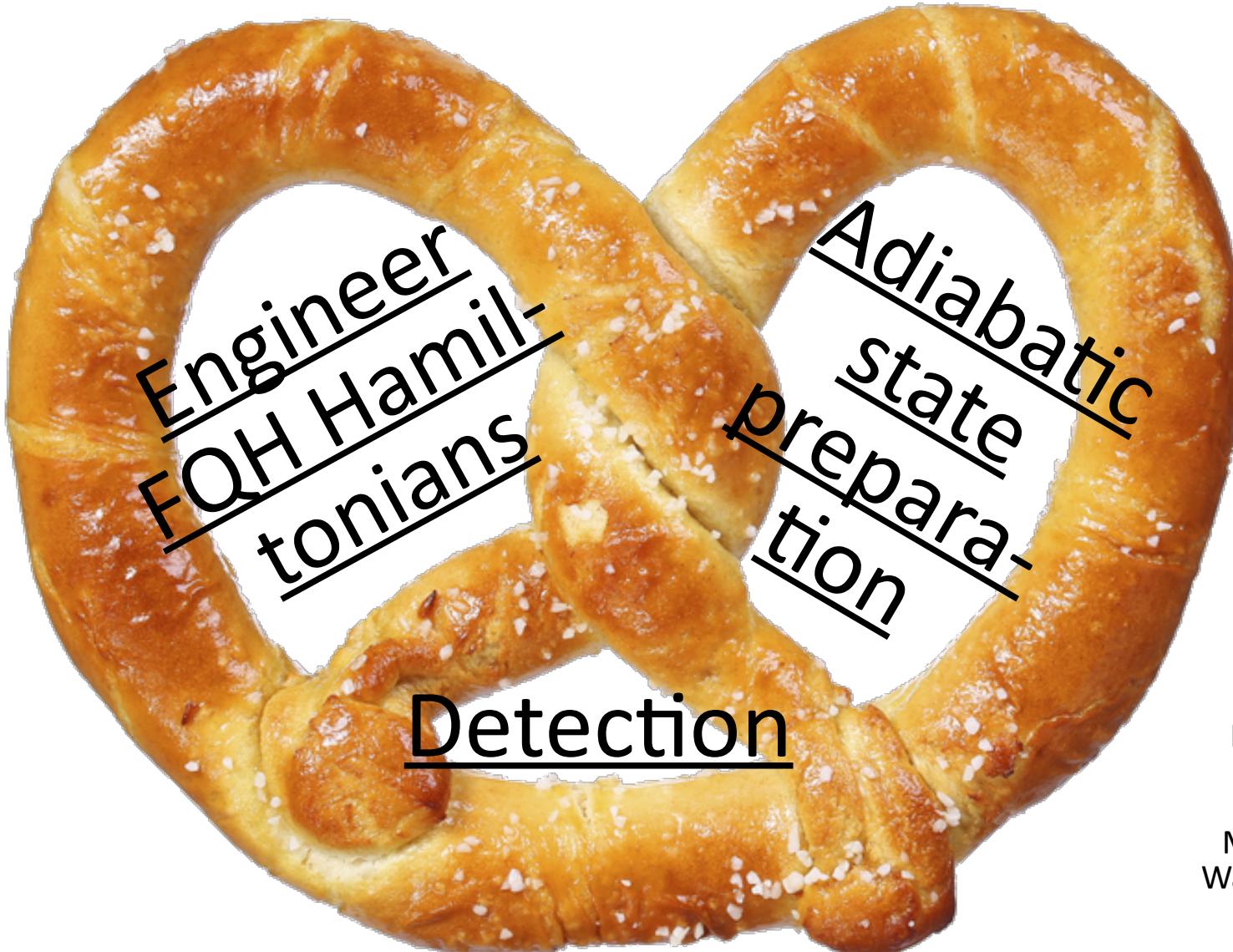


Adiabatic connection
to parent Hamiltonian

[Cian, TG, Vaezi, Liu, Hafezi, Phys. Rev. B 102, 085430 (2020)]

[Ghazaryan, TG, Gullans, Ghaemi, Hafezi, Phys. Rev. Lett. 119, 247403 (2017)]

Thank you!



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Niccolo Baldelli
Utso Bhattacharya
Alexandre Dauphin
Joana Fraxenet
Valentin Kasper
Bernhard Irsigler
Maciej Lewenstein
Debrah Rakshit
Leticia Tarruell

@ JQI/UMD/NIST:
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David Raventos (IFF Madrid)
Christoph Weitenberg (U Hamburg)
Abolhassan Vaezi (Sharif)

Max-Planck Institute for the Science of Light

11.03.2021

Discussion of Plans

Designer Quantum Matter from the Optical Toolbox and more

Tobias Grass

ICFO^R

Research lines

CONDENSED MATTER THEORY MEETS QUANTUM OPTICS

- Floquet Engineering of Many-Body Phases
- Non-linear optics and strongly correlated matter

QUANTUM INFORMATION

- Quantum Algorithms and Machine Learning
- Topological Codes

New Quantum Simulation Platforms

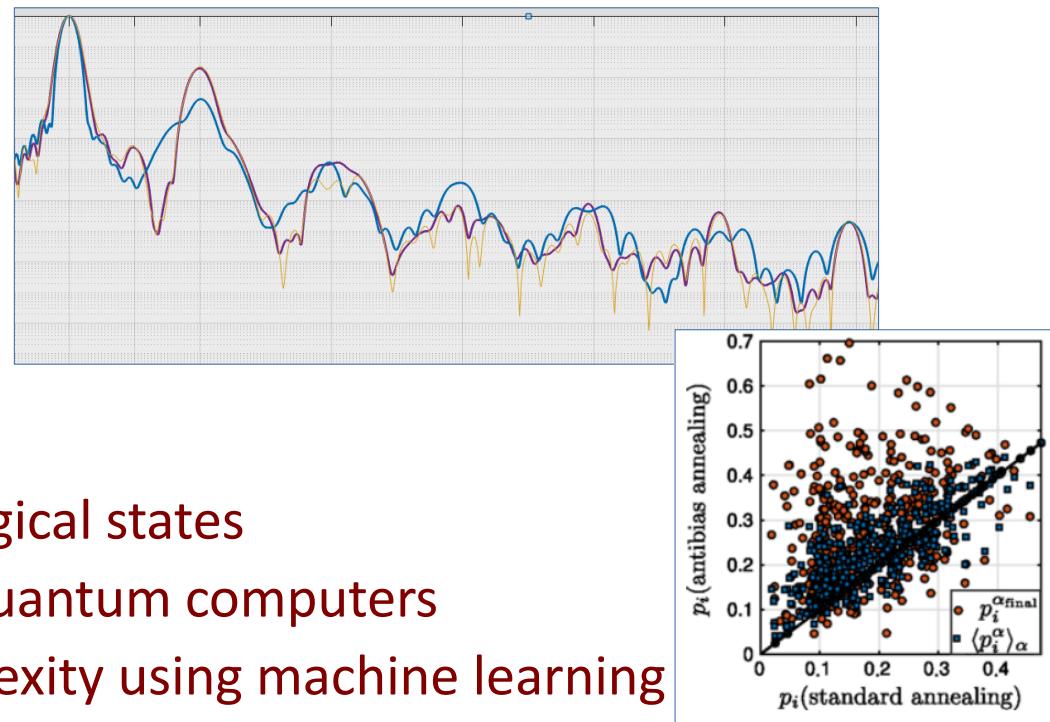
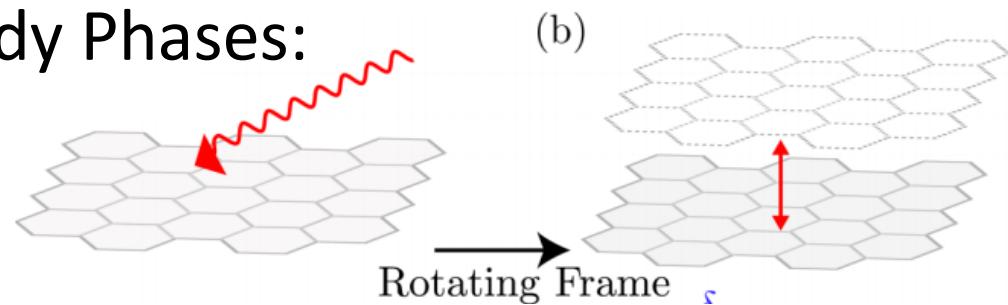
Quantum Materials “on demand”

Detection of Topological Properties

Software for Quantum Computers

List of Topics

- Floquet Engineering of Many-Body Phases:
 - Optical dressing: tunable interactions for electrons
 - N -body interactions?
 - The heating challenge: Tailoring thermalization channels?
 - More structure using structured light: electronic quantum simulators?
- Non-linear optics and strongly correlated matter:
 - High-harmonic spectra from topological matter
 - Exciton-polaritons in topological matter and topological matter out of exciton-polaritons
- Quantum Algorithms:
 - Digital gate preparation of topological states
 - Checks and cheats for adiabatic quantum computers
 - Understand computational complexity using machine learning



Floquet Engineering of Many-Body Phases

▪ Tunable Interactions:

- Coupled Landau levels yields synthetic bilayer with exotic interactions - depending on coupled levels

[Ghazaryan, TG, Gullans, Ghaemi, Hafezi, Phys. Rev. Lett. 119, 247403 (2017)]

- Develop systematic coupling scheme (various LLs , pulse shaping, etc.) for interactions “on demand”

- LL mixing leads to effective N -body interactions

[Sodemann & MacDonald, Phys. Rev. B 87, 245425 (2013)]

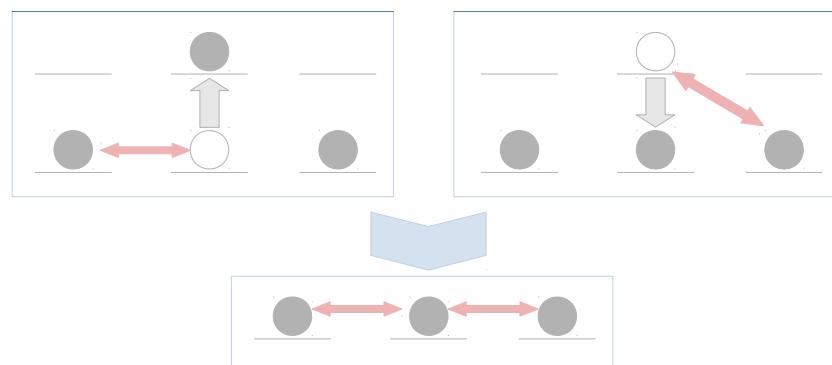
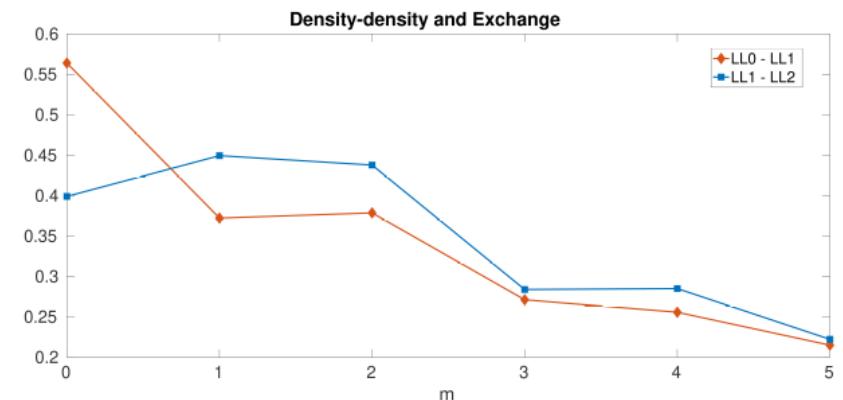
Even weak terms are relevant in some systems (e.g. 5/2 state)

[Pakrouski, Peterson, Jolicoeur, Scarola, Nayak, Troyer, Phys. Rev. X 5, 021004 (2015)]

▪ Heating is bottleneck of Floquet engineering. Include thermalization!

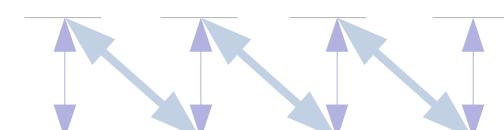
- Simulate open system dynamics (e.g. quantum jump method)

▪ Further topics: SSH model, twisted bilayer, twisted light,...



[Seetharam et al., Phys. Rev. X 5, 041050 (2015)]

[D'Alessio & Rigol, Phys. Rev. X 4, 041048 (2014)]



Topology in topology: Coupled Landau levels form SSH chain.

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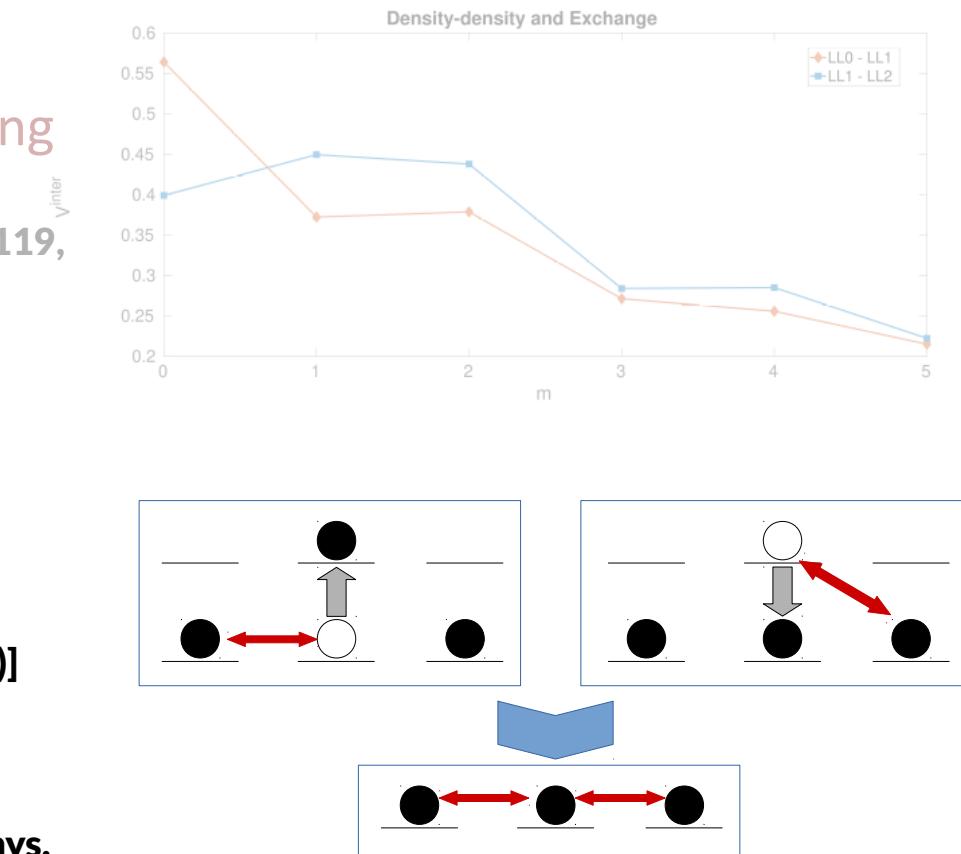
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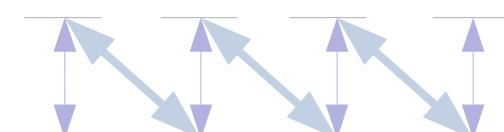
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[Sodemann & MacDonald, Phys. Rev. B 87, 245425 (2013)]

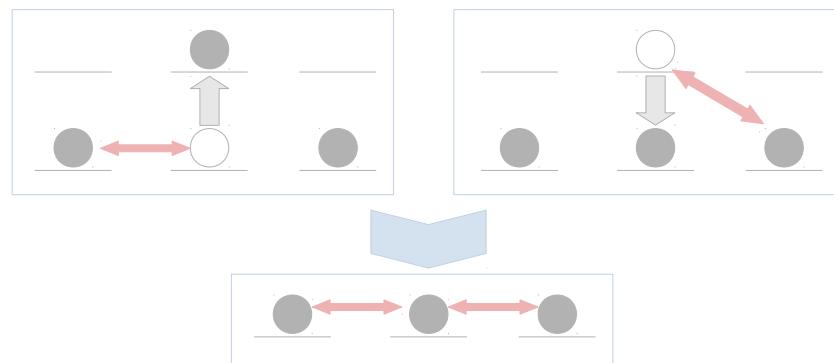
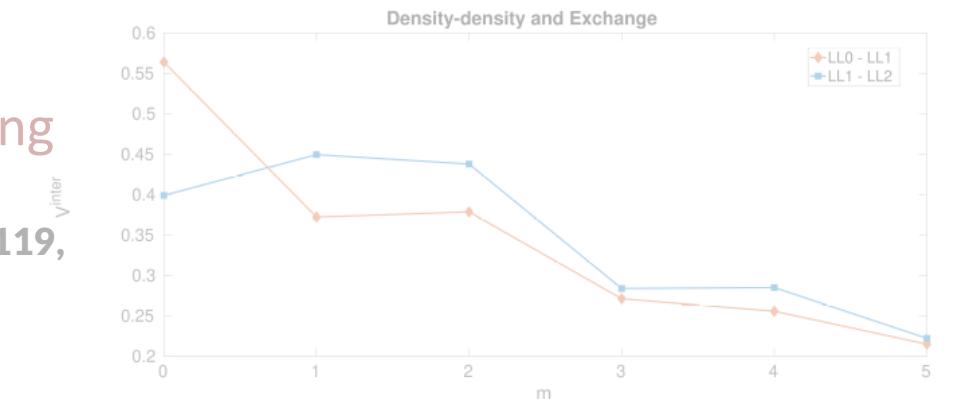
Even weak terms are relevant in some systems (e.g. 5/2 state)

[Pakrouski, Peterson, Jolicoeur, Scarola, Nayak, Troyer, Phys. Rev. X 5, 021004 (2015)]

▪ Heating is bottleneck of Floquet engineering. Include thermalization!

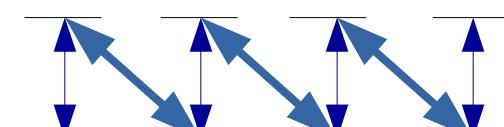
- Simulate open system dynamics (e.g. quantum jump method)

▪ Further topics: SSH model, twisted bilayer, twisted light,...



[Seetharam *et al.*, Phys. Rev. X 5, 041050 (2015)]

[D'Alessio & Rigol, Phys. Rev. X 4, 041048 (2014)]



Topology in topology: Coupled Landau levels form SSH chain.

Non-linear Optics meets Correlated Matter

■ High-harmonic generation

- Well established in atomic systems, getting “popular” also in condensed matter

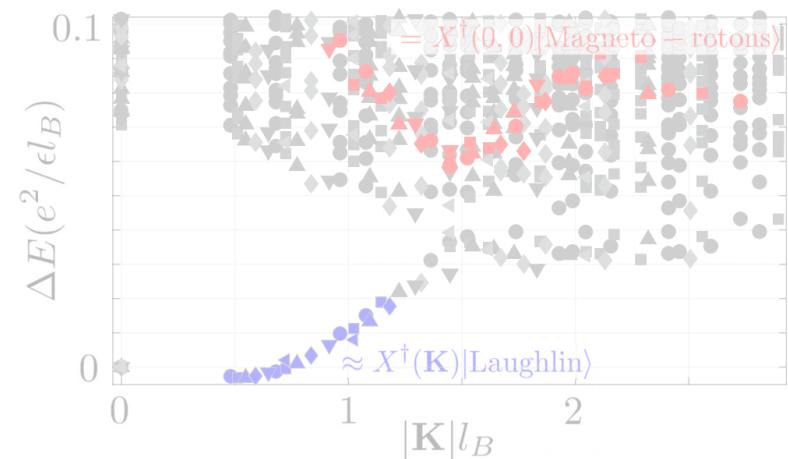
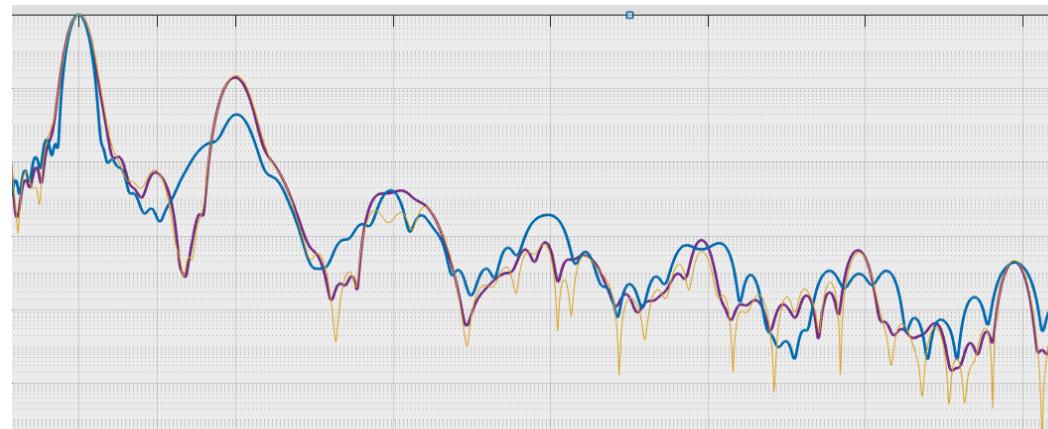
[Ghimire and Reis, Nat. Phys. 15, 10 (2019)]

- Detection of topology via HHG
- [A. Chacon et al., Phys. Rev. B 102, 134115 (2020)]

- Signatures of anyons?
 - Kitaev chain (quadratic model)
 - Interacting models
- Signature of superconductivity?
 - HHG spectra of cuprates
 - Light-induced superconductivity

■ Excitonic systems

- Exciton-polaritons in FQH systems – theoretical model for interactions?
- Excitons bound to quasiparticles: Anyon detection via impurities?
- Many-body phases of excitons: strong interactions, artificial gauge fields,...?



[S. Ravets et al., Phys. Rev. Lett. 120, 057401 (2018)]
[TG, Cotlet, İmamoğlu, Hafezi, Phys. Rev. B 101, 155127 (2020)]

[Kwon et al., Phys. Rev. Lett. 122, 045302 (2019)]
[Sanvitto et al., Nat. Phys. 6, 527 (2010)]
[Lackner, ..., Hoefling, Schneider, arXiv 2102.09565]

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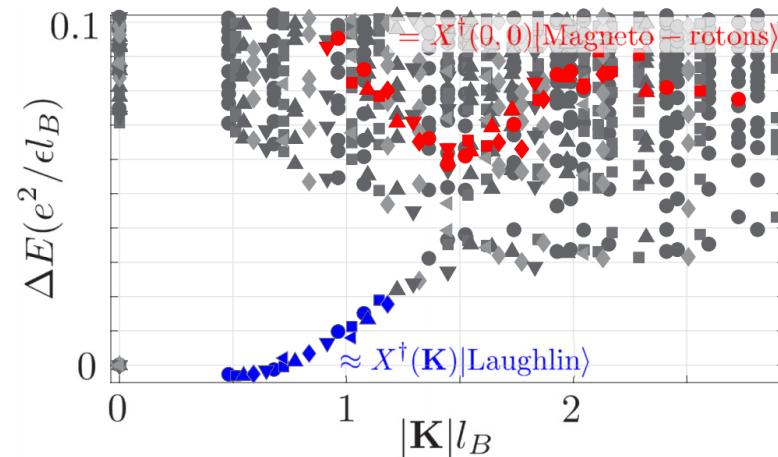
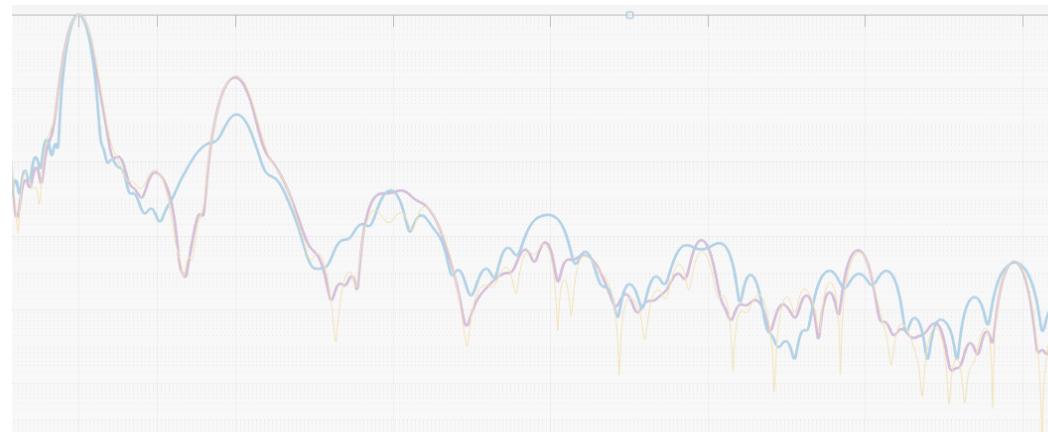
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Quantum Algorithms

▪ Quantum Annealing

→ Bottleneck: Closing of gap

[Altshuler, Krovi, Roland, PNAS 107 12446 (2010)]

→ Bias field can lead to significant improvements

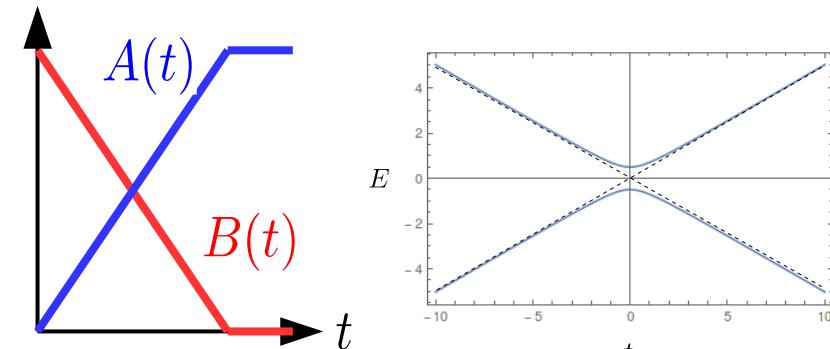
[TG, Phys. Rev. Lett. 123, 120501 (2019)]

→ Dynamical phase transitions: Hints for critical field strength through quench experiments?

→ Reinforcement learning?

[Bukov et al., Phys. Rev. X 8, 031086 (2018)]

[Foesel et al., Phys. Rev. X 8, 031084 (2018)]



$$H(t) = A(t)H_{\text{problem}} + B(t)H_{\text{driver}}$$

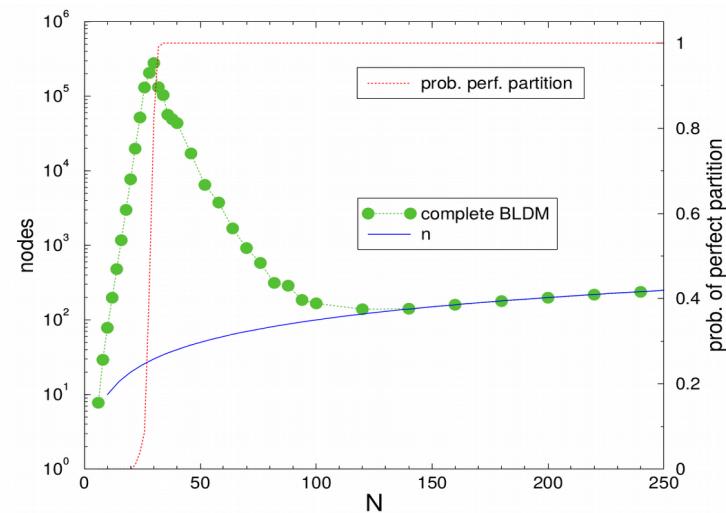
▪ Understanding computational complexity

→ Phase transitions of computational complexity

[Mertens, Phys. Rev. Lett. 81, 4281 (1998)]

→ Expectation: There are more subtle patterns which characterize the hard instances

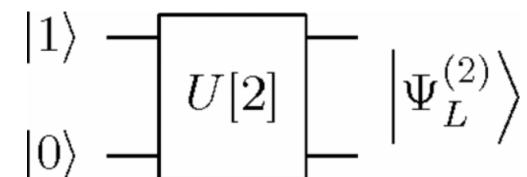
→ Idea: Use machine learning to identify them.



→ Gate preparation of topological qubits

[J. I. Latorre, V. Picó, and A. Riera Phys. Rev. A 81, 060309 (2010)]

[Rahmani et al. PRX QUANTUM 1, 020309 (2020)]



My group

- Currently:

2 PhD students



Nicollo Baldelli
since 2019



Barbara Andrade
since 2020

1 Post-Doc

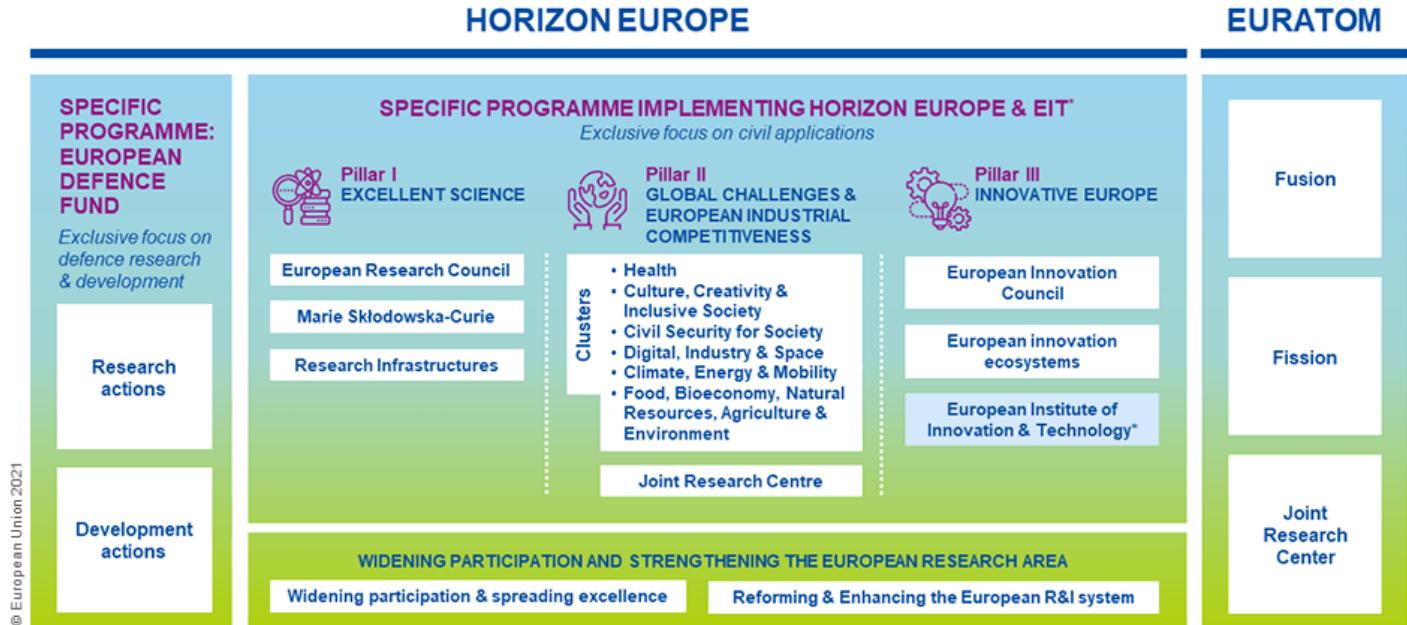


Bernhard Irsigler
since 2021

- Next steps:

- Local students?
- New hires?
- Funding?

- Network:



Lewenstein, Chang, Biegert, Bachtold, Tarruell, Wall...
Julia-Diaz, Barberan, Celi, ...



Hafezi, Gorshkov, Weitenberg, Sengstock
Solomon, Davoudi,...



Universität Hamburg
DER FORSCHUNG | DER LEHRE | DER BILDUNG



Pagano Imamoglu

