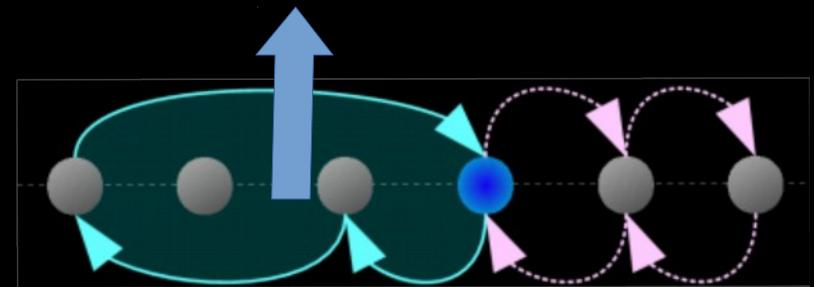
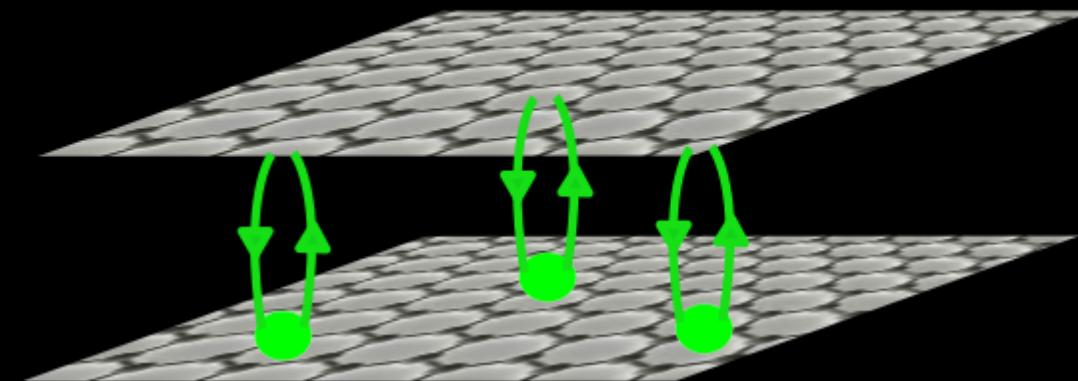


University of Oklahoma
Department of Physics and Astronomy
02/14/2019
Colloquium

Topological Quantum Simulators

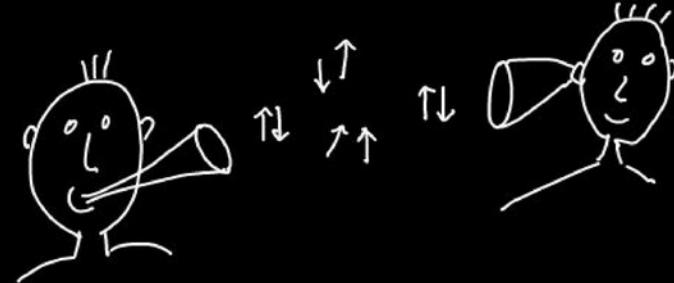


Tobias Grass
Joint Quantum Institute and University of Maryland
College Park, Maryland, USA



Quantum Sensing

**(precision measurements, atomic clocks,
quantum imaging, ...)**



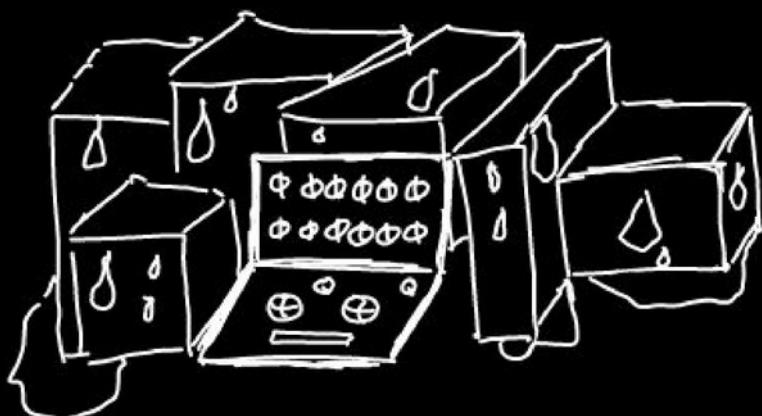
Quantum Communication

(Quantum cryptography, quantum networks,...)

Quantum Technologies

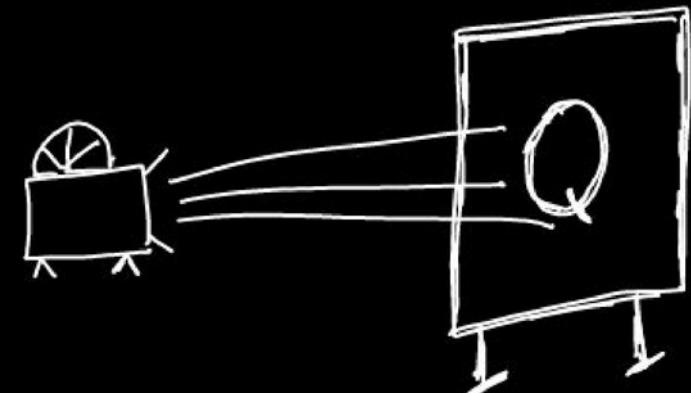
Quantum Computation

(Quantum processor, quantum algorithms, error-correction,...)

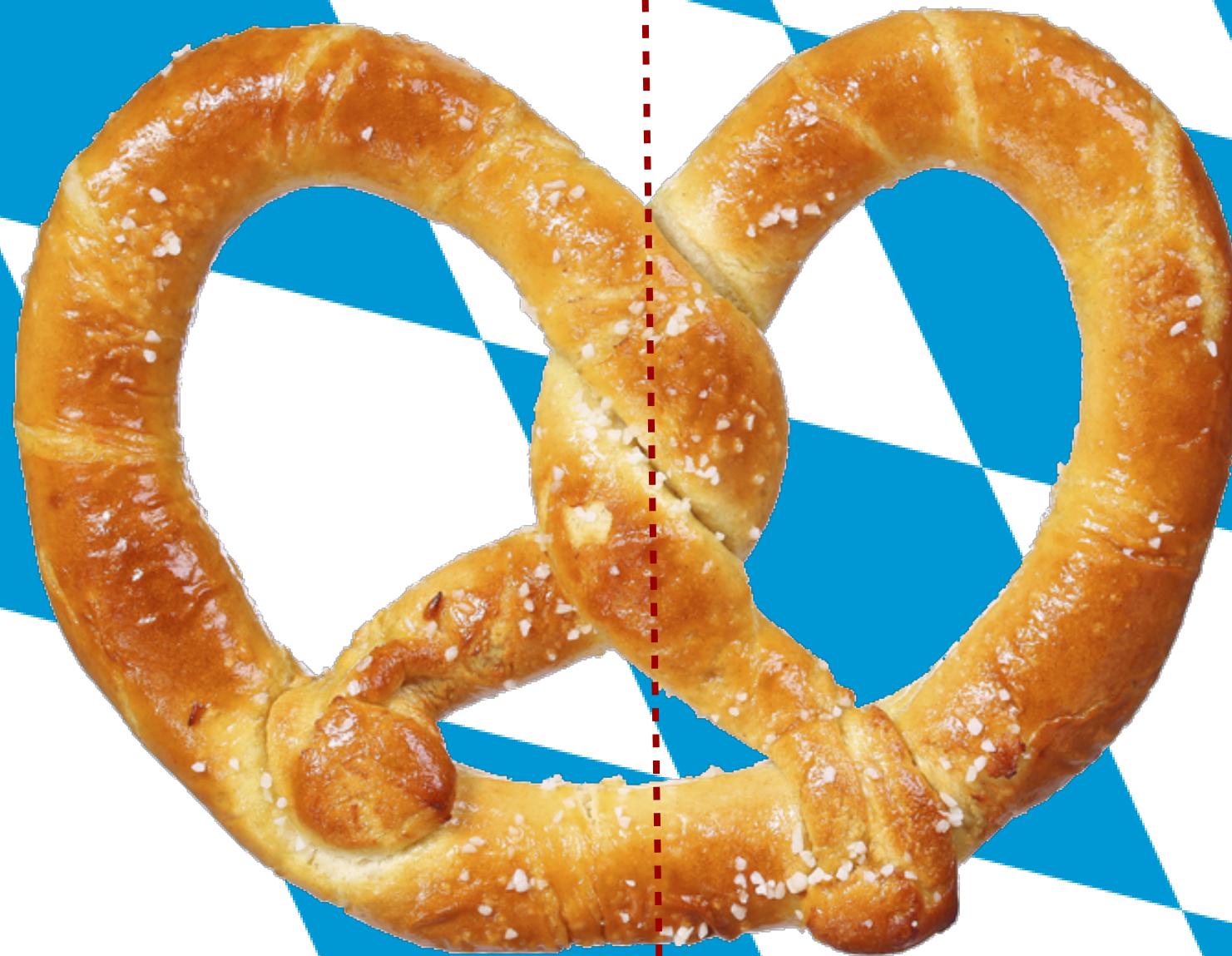


Quantum Simulation

(quantum many-body physics, model solver,
quantum annealing...)

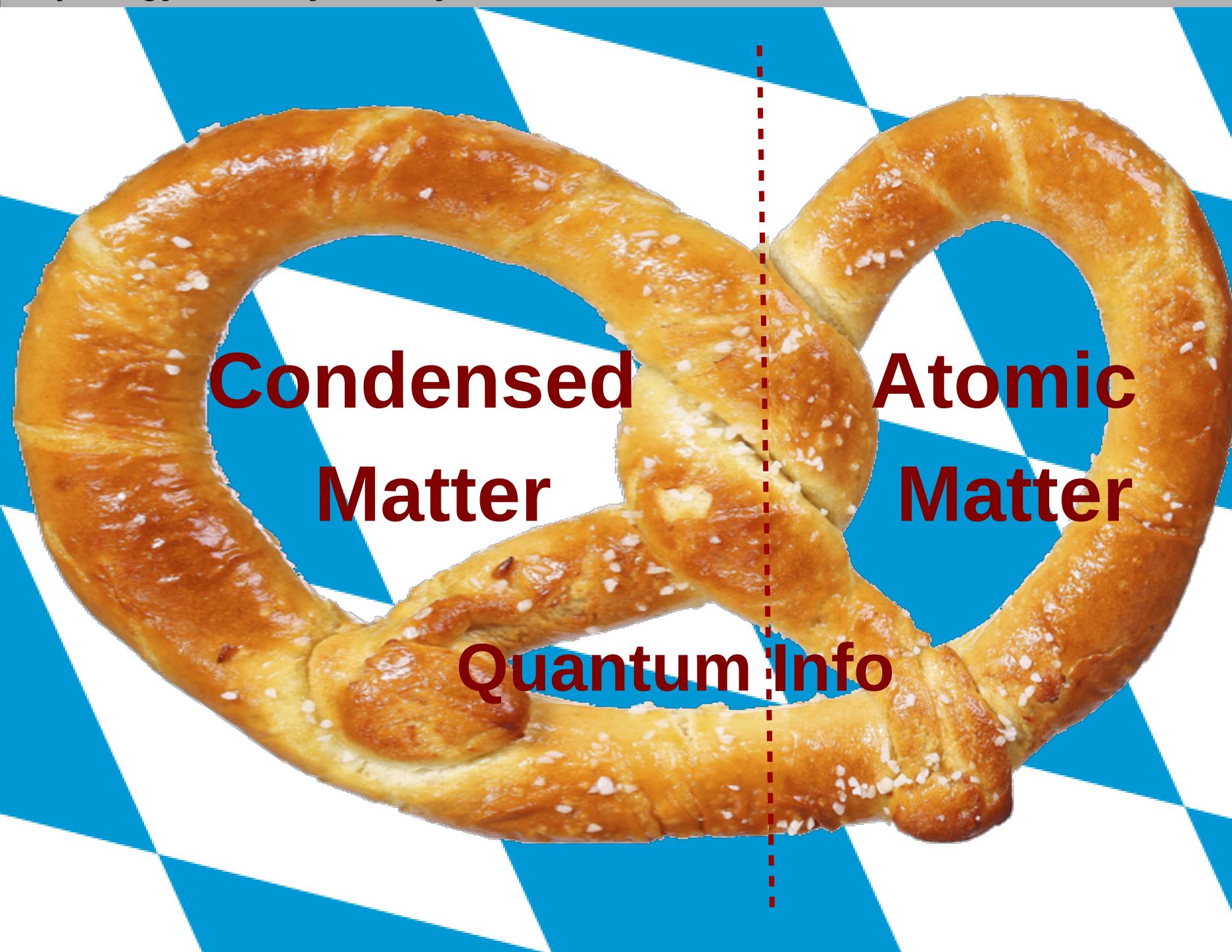


Topology and Symmetry



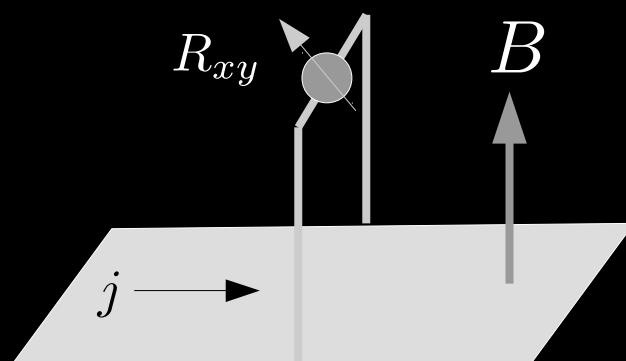
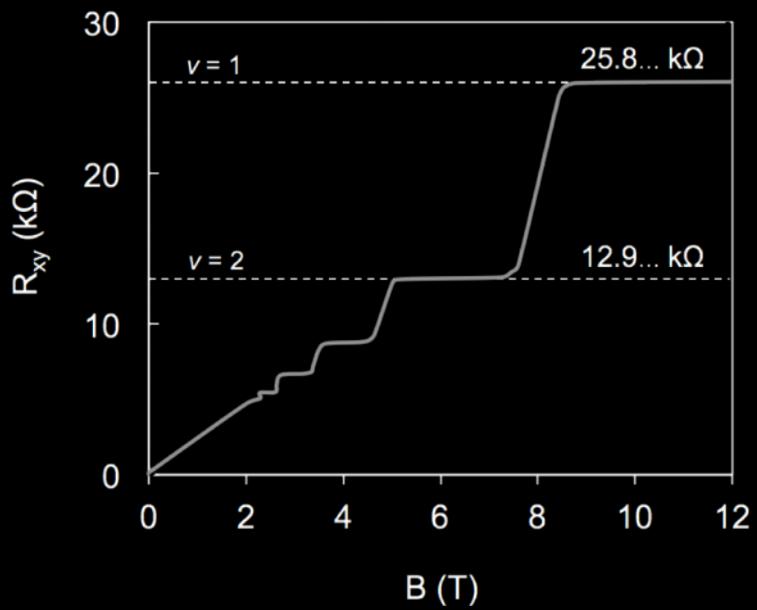
Topology and Symmetry





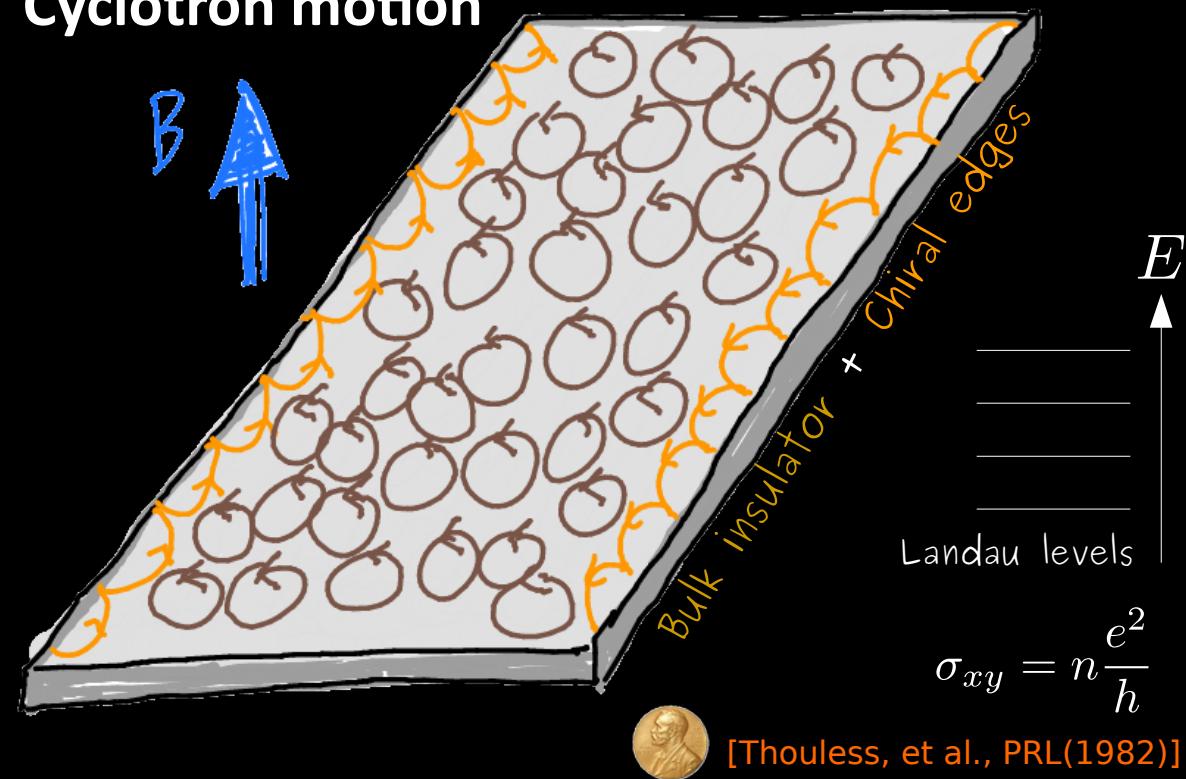
Integer Quantum Hall Effect

Experimental observation: Quantized Hall resistance



[von Klitzing, Dorda, Pepper, PRL (1980)]

2d transport in magnetic field: Cyclotron motion



Experimental systems:



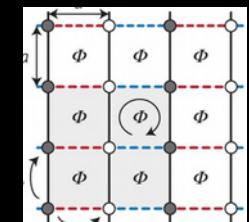
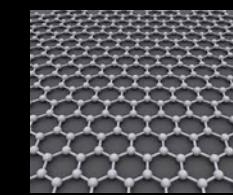
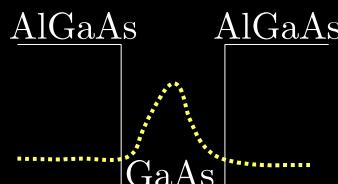
Semiconductors
Quantum Wells



2d materials
(graphene)



Quantum simulators



Fractional Quantum Hall Effect

Remarkable observation: Robust Hall conductances also for fractionally filled Landau levels



[Tsui, Stormer, Gossard, PRL (1982)]

Explanation:

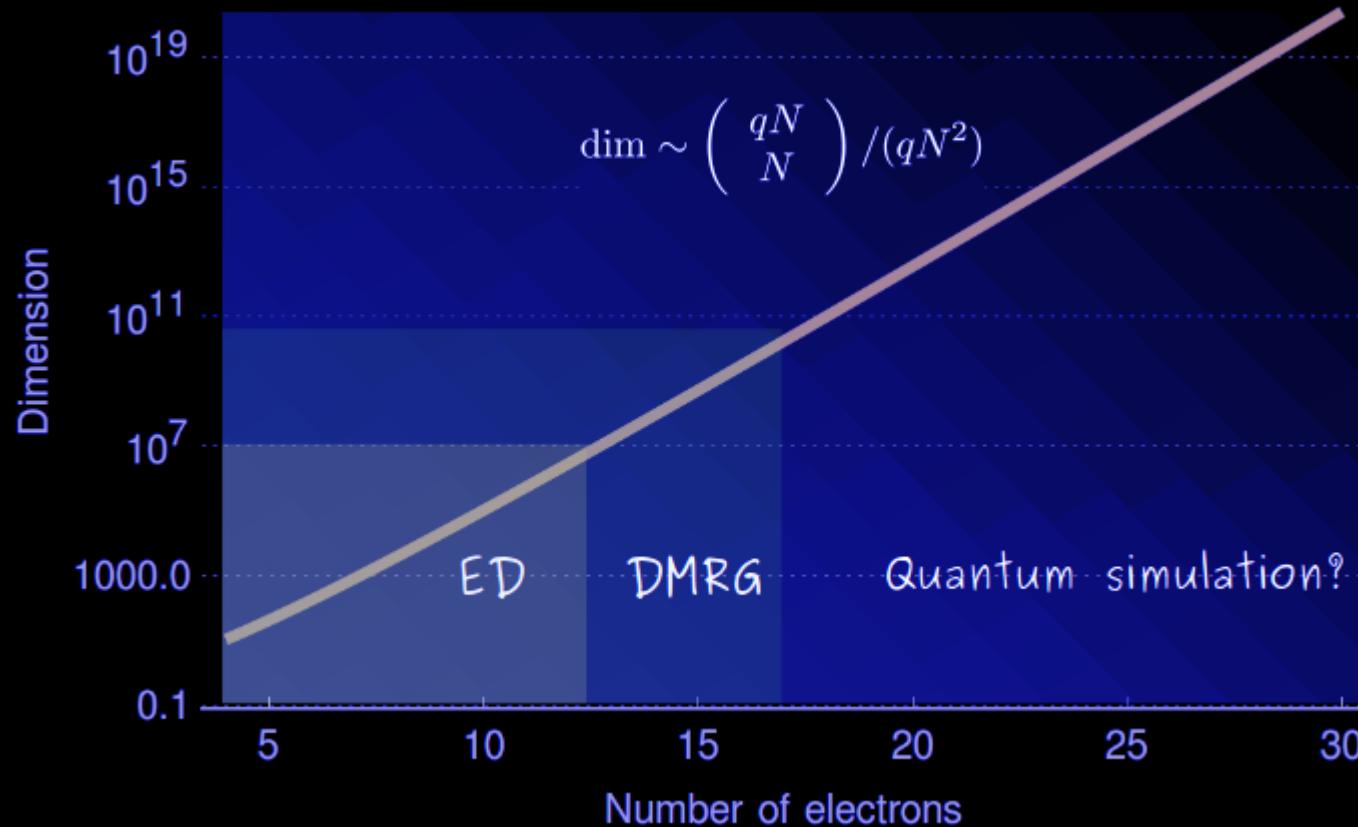
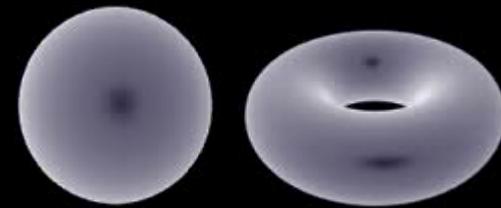
Gapped liquid due to interactions



[Laughlin, PRL (1982)]

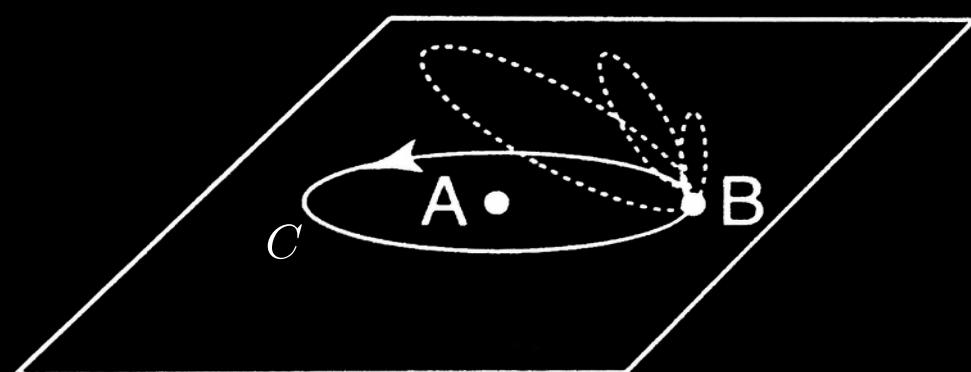
→ Non-perturbative many-body problem

→ Numerical methods: Exact diagonalization, DMRG



Spin-Statistics Theorem: bosons, fermions, anyons

Particle exchange in 3 dimensions:



$$\Psi_{AB} \rightarrow e^{i\gamma(C)} e^{i2\varphi_{\text{stat}}} \Psi_{AB}$$

Topological equivalence between
double-exchange loop and no loop

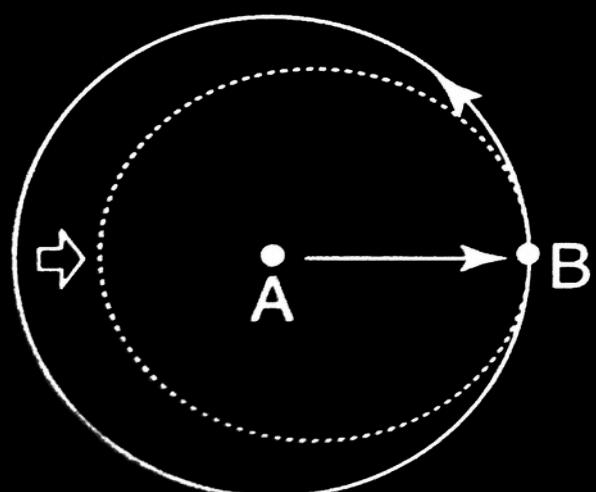
$$e^{i2\varphi_{\text{stat}}} = 1$$

→ Statistical phase restricted:

$$\varphi_{\text{stat}} = 0 : \quad \Psi_{AB} = +\Psi_{BA} \quad \rightarrow \quad \text{bosons}$$

$$\varphi_{\text{stat}} = \pi : \quad \Psi_{AB} = -\Psi_{BA} \quad \rightarrow \quad \text{fermions}$$

Particle exchange in 2 dimensions:



Double-exchange loop cannot be shrunk away

→ Particle exchange can produce an arbitrary phase

$$\Psi_{AB} = e^{i\varphi_{\text{stat}}} \Psi_{BA} \quad \rightarrow \quad \text{anyons}$$

Quasiparticle excitations in FQH systems exhibit anyon statistics!

[Leinaas & Myrheim, Il Nuovo Cimento B (1977)]

Non-Abelian Anyons

Non-Abelian anyons: degenerate states characterized by “fusion rules”

Example: Fibonacci anyons

$$1 \otimes \tau = \tau$$

$$1 \otimes 1 = 1$$

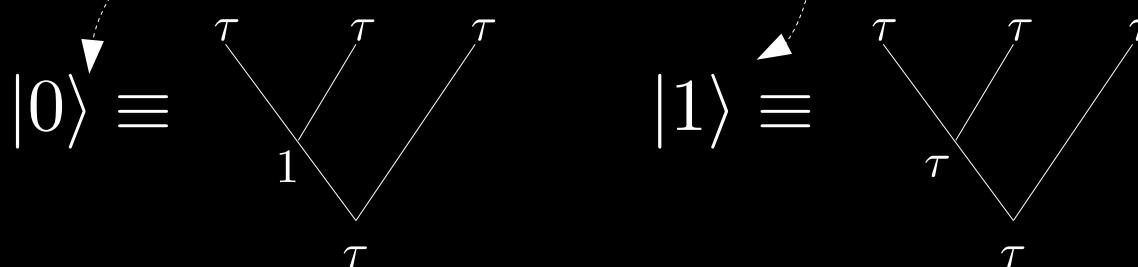
$$\tau \otimes \tau = 1 \oplus \tau$$

\Rightarrow

$$\begin{aligned} \tau \otimes \tau \otimes \tau &= 1 \oplus 2 \cdot \tau \\ \tau \otimes \tau \otimes \tau \otimes \tau &= 2 \cdot 1 \oplus 3 \cdot \tau \\ \tau \otimes \tau \otimes \tau \otimes \tau \otimes \tau &= 3 \cdot 1 \oplus 5 \cdot \tau \\ &\vdots \end{aligned}$$

Number of states which fuse to τ follows Fibonacci series: 1, 2, 3, 5, 8...

Topological qubit:



Topological quantum computing:
Process information by braiding

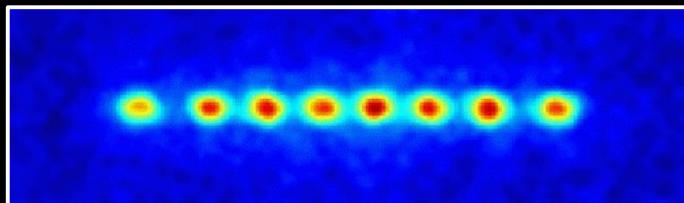


Technically involved

Robust against local noise

THIS TALK: How to engineer Fibonacci phase in graphene!

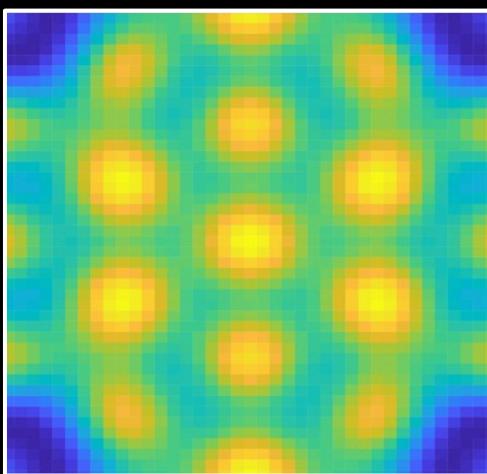
Outline



(1) QUANTUM SIMULATIONS WITH TRAPPED IONS:

Synthetic Hofstadter ladder (IQH system)

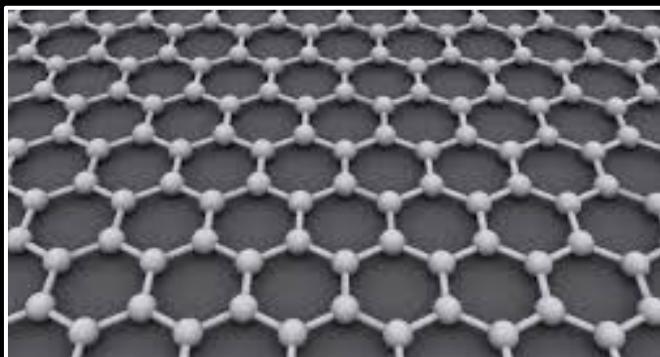
- Microscopic System (individual control)
- Naturally long-ranged interactions
- 1-D



(2) QUANTUM SIMULATION WITH COLD ATOMS:

Fractional Wigner Crystal

- Mesoscopic System
- Long-range interactions through Rydberg dressing



(3) QUANTUM SIMULATION IN REAL MATTER

Non-Abelian Fibonacci phase

- Macroscopic System

(1)

QUANTUM SIMULATION OF TOPOLOGICAL MATTER WITH TRAPPED IONS

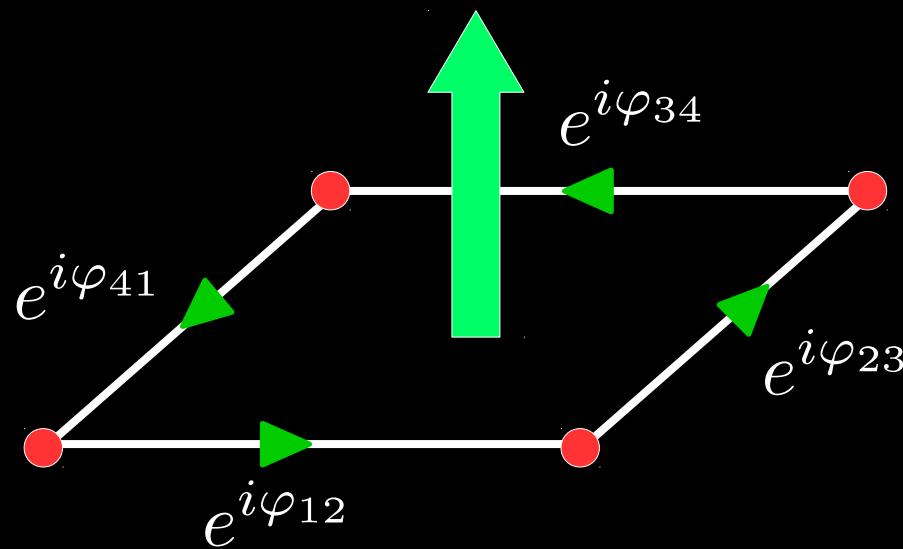
Synthetic Hofstadter ladder
[Grass, Muschik, Celi, Chhajlany, Lewenstein PRA (2015)]

Triangle with flux
[Grass, Celi, Pagano, Lewenstein, PRA (Rapid) (2018)]

Magnetic Flux

Magnetic field → wave function picks up Berry phase when moving along closed loop

$$\Phi = \varphi_{12} + \varphi_{23} + \varphi_{34} + \varphi_{41} \quad (= \text{encircled flux})$$



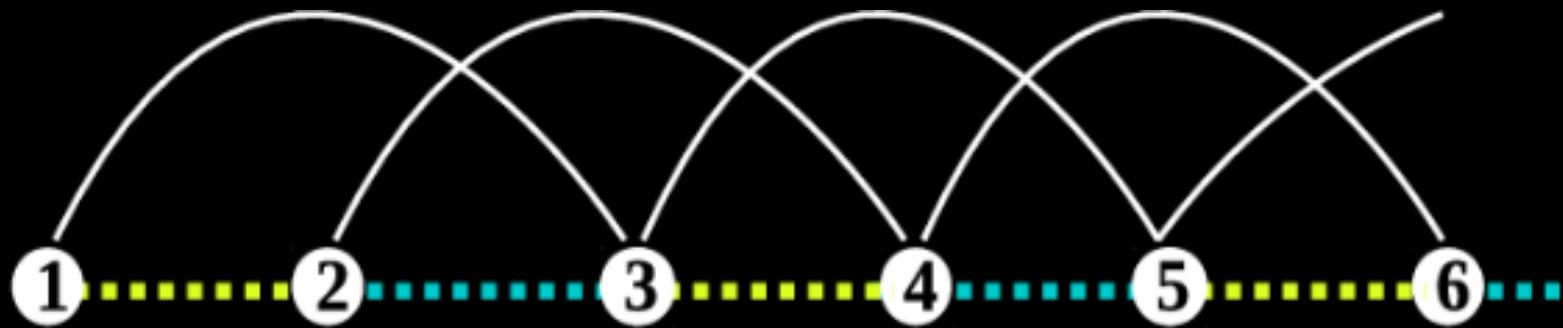
In 1D: Closed loops are along straight lines



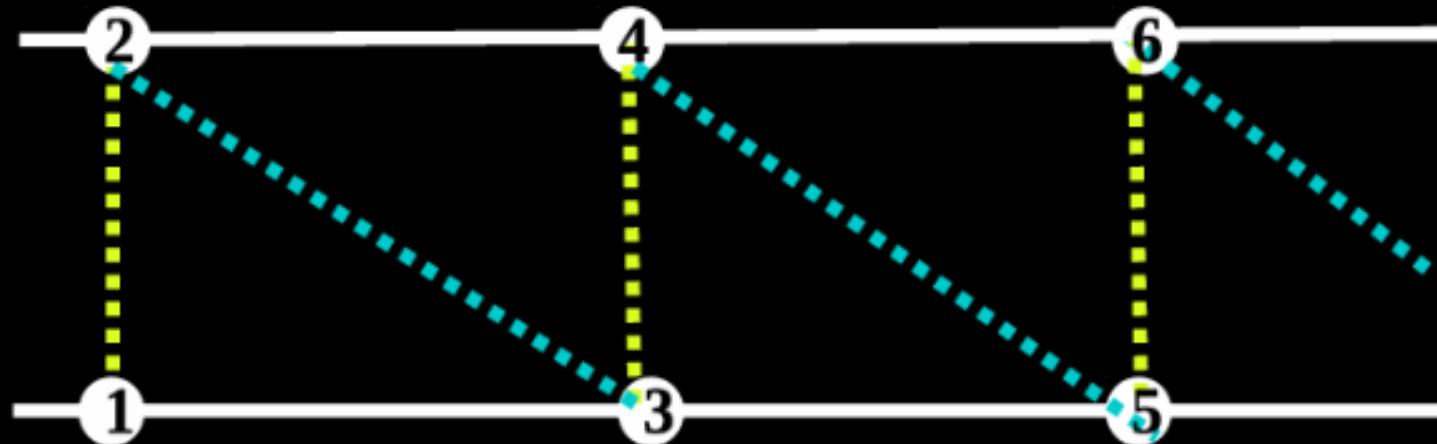
Can we still pick up a non-zero Berry phase?

From Chain to Synthetic Ladder

Chain with nearest and next-nearest neighbor interactions:



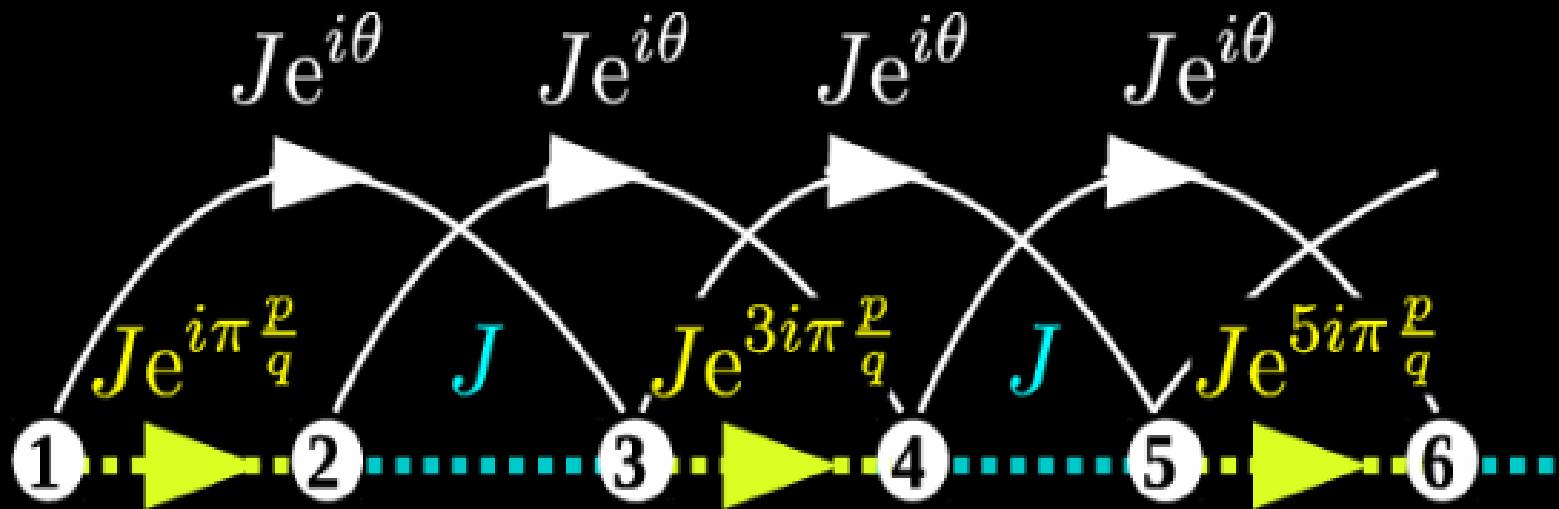
Mapping onto triangular ladder (“synthetic ladder”):



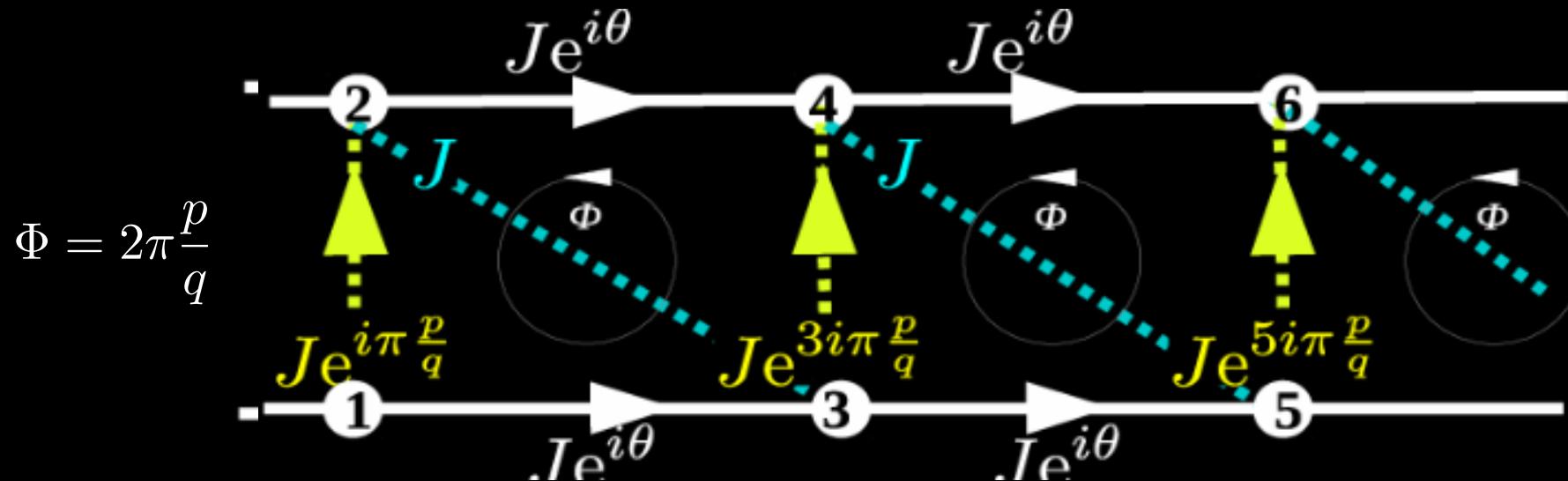
[Grass, Muschik, Celi, Chhajlany, Lewenstein, PRA (2015)]

From Chain to Synthetic Ladder

Chain with nearest and next-nearest neighbor interactions:



Mapping onto triangular ladder (“synthetic ladder”):



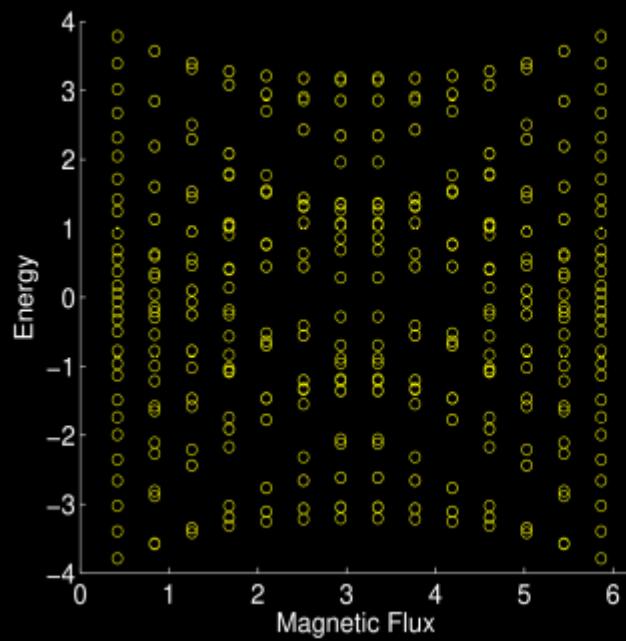
[Grass, Muschik, Celi, Chhajlany, Lewenstein, PRA (2015)]

Hofstadter-like model

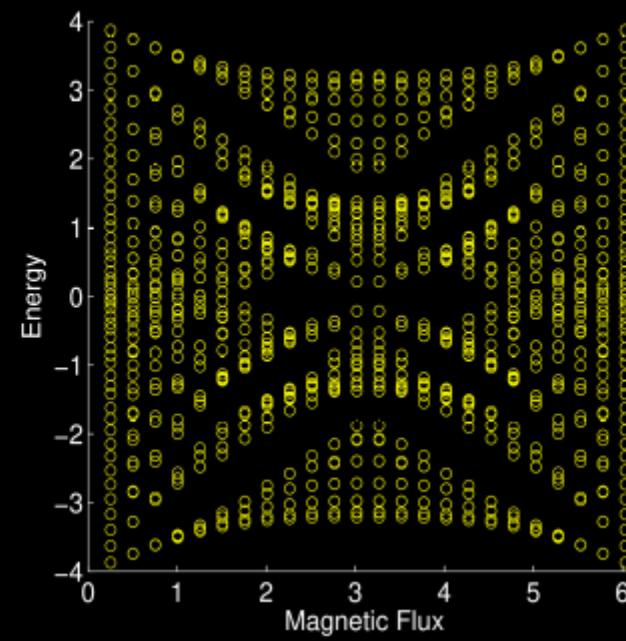
Hofstadter model: Lattice model for integer quantum Hall effect

Famous feature: Fractal energy spectrum → “Hofstadter butterfly”

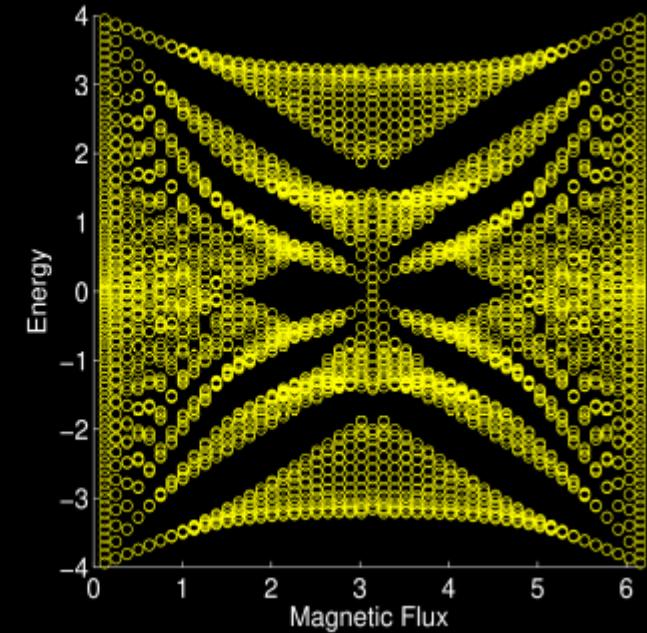
Energy vs. flux per plaquette



N=30



N=50



N=100

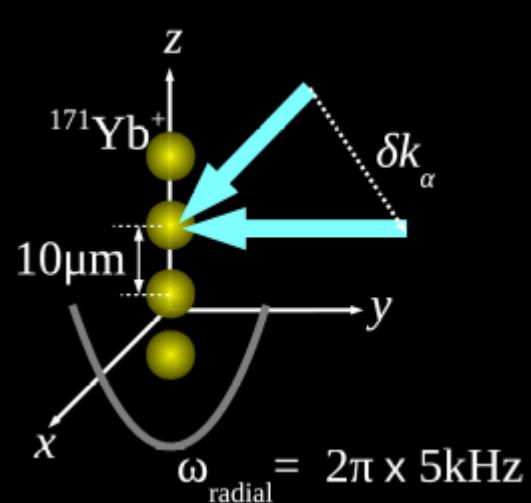
Also: Localized edge states, non-zero Chern numbers, ...

[Grass, Muschik, Celi, Chhajlany, Lewenstein, PRA (2015)]

Quantum simulations with ions

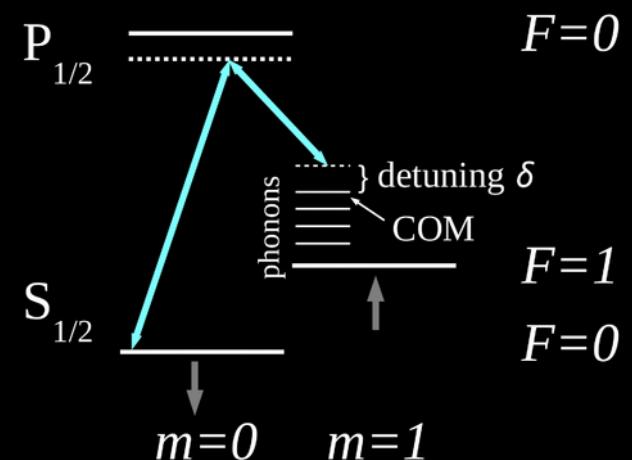
Engineering spin-spin interactions

[Porras, Cirac, PRL (2004)]



$$H_{\text{eff}} = \sum J_{ij} \sigma_j^x \sigma_i^x$$

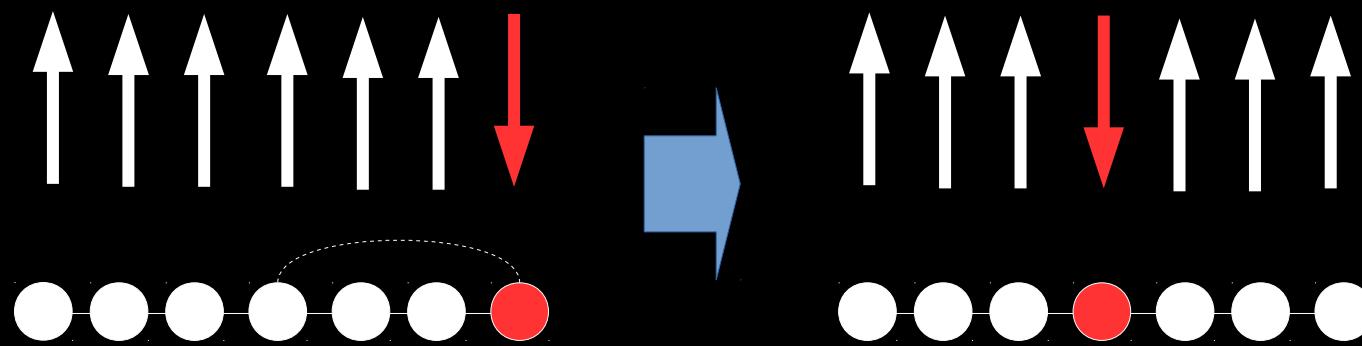
2nd order perturbation theory for spin-phonon model (i.e. virtual phonons)



Early experiments:

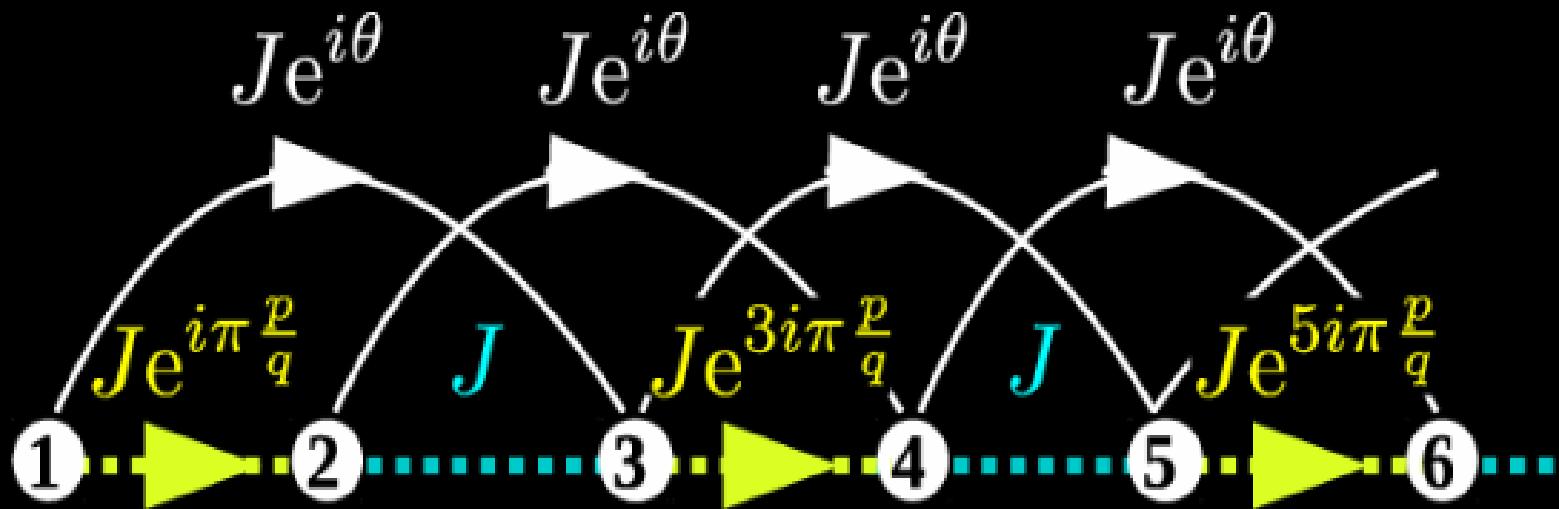
[Friedenauer, Schmitz, Glueckert, Porras, Schaetz, Nat. Phys (2008)] [Kim, Chang, Islam, Korenblit, Duan, Monroe, PRL (2009)]

Equivalence spin flip \leftrightarrow hopping:

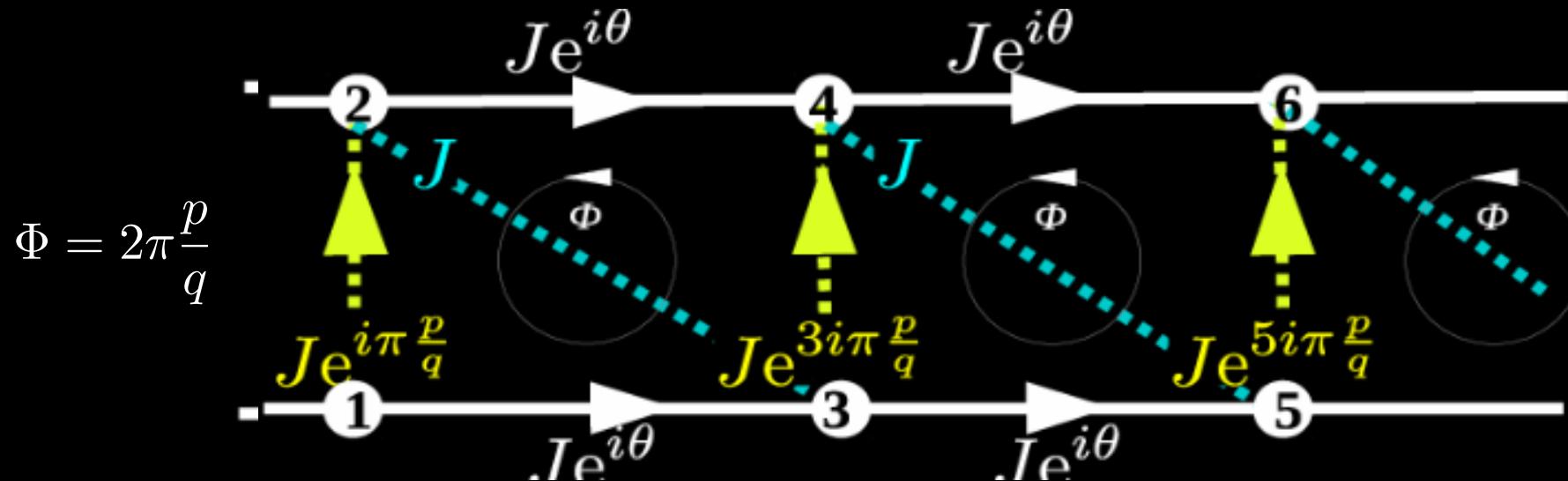


From Chain to Synthetic Ladder

Chain with nearest and next-nearest neighbor interactions:



Mapping onto triangular ladder (“synthetic ladder”):



[Grass, Muschik, Celi, Chhajlany, Lewenstein, PRA (2015)]

Complex-valued J_{ij} : Floquet engineering

Periodic driving to engineer gauge potentials

[Cold atom experiments: Pisa (Arimondo), Hamburg (Sengstock), MIT (Ketterle), Munich (Bloch), Zurich (Esslinger)...]

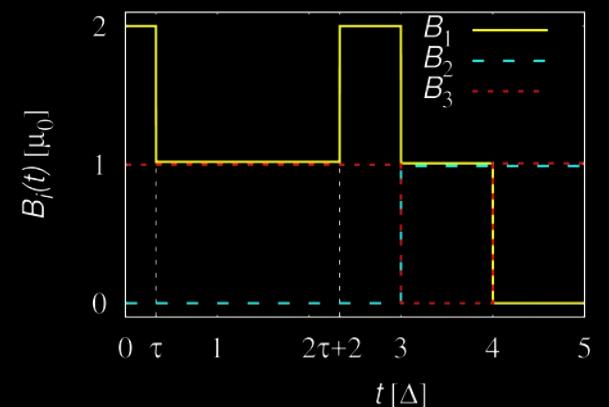
Recipe for spin chain (XY model):

Add “shaken” field: $H(t) = H_{\text{XY}} + \sum_i B_i(t) \sigma_i^z$ with $H_{\text{XY}} = \sum_{i < j} J_{ij} (\sigma_i^+ \sigma_j^- + \text{h.c.})$

Gauge transform
(Floquet basis): $U(t) = e^{-i \sum_i \chi_i(t) \sigma_i^z}$ with $\chi_i(t) = \int_0^t dt' B_i(t')$

In new basis,
average over
shaking period: $H_{\text{eff}} = \sum_{i < j} J_{ij}^{\text{eff}} (\sigma_i^+ \sigma_j^- + \text{h.c.})$ where $J_{ij}^{\text{eff}} = \frac{\bar{J}_{ij}}{T} \int_0^T dt e^{2i[\chi_i(t) - \chi_j(t)]}$

Effective Hamiltonian is again XY model,
with renormalized interaction
parameters



[Grass, Muschik, Celi, Chhajlany, Lewenstein, PRA (2015)]

[Grass, Celi, Pagano, Lewenstein, PRA Rapid (2018)]

Effective model of the effective model...

Spin-phonon model + driving



Effective spin chain + driving



Effective spin chain w/ flux

$$\Phi = \pi/2$$

Good fidelity

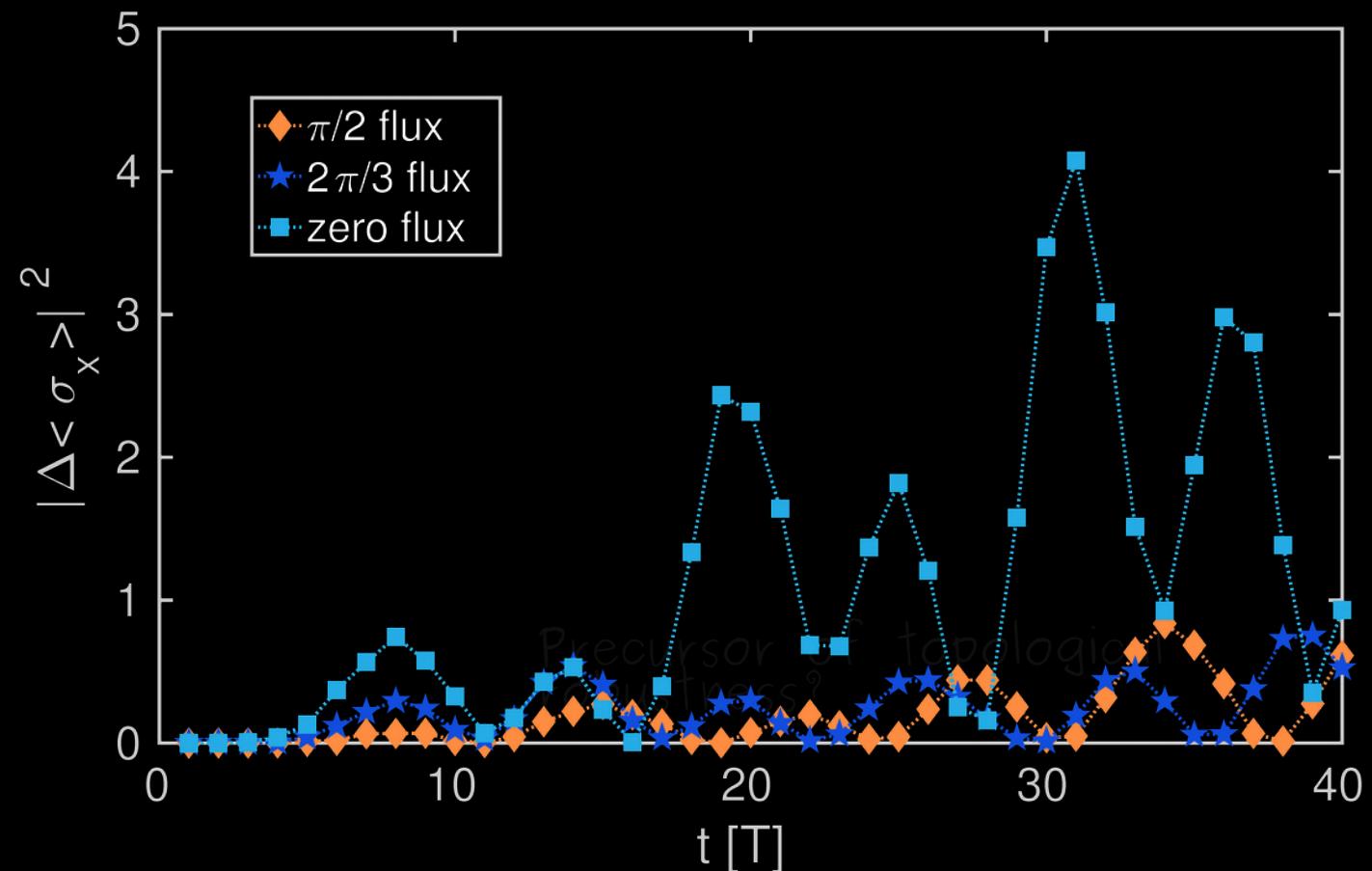
$$\Phi = 0$$

Low fidelity

Onset of
topological
robustness?

First approximation:
Problematic for strong driving

Second approximation:
Problematic for weak driving



[Grass, Celi, Pagano, Lewenstein, PRA Rapid (2018)]

(2)

QUANTUM SIMULATION OF TOPOLOGICAL MATTER WITH COLD ATOMS

Synthetic gauge fields through laser dressing

[Julia-Diaz, Dagnino, Guenther, Grass, Barberan, Lewenstein, Dalibard, PRA (2011)]

Non-Abelian spin singlet phases in bosonic FQH system

[Grass, Julia-Diaz, Barberan, Lewenstein, PRA (Rapid) (2012)]

Engineering fermionic Laughlin state through confinement-induced resonance

[Julia-Diaz, Grass, Dutta, Lewenstein, Nat. Commun. (2013)]

Integer quantum Hall phase of bosons

[Grass, Raventos, Lewenstein, Julia-Diaz, PRB (2014)]

Fractional Wigner crystal through Rydberg dressing

[Grass, Bienias, Gullans, Lundgren, Maciejko, Gorshkov, PRL (2018)]

Synthetic gauge fields

Atoms: Electro-neutrality = insensitivity to magnetic fields

Synthesize the effect of a magnetic field:

- rotation (Coriolis force \leftrightarrow Lorentz force)
- laser-dressing (imprinted Berry phase)
- laser-assisted tunneling (in optical lattices)
- Floquet engineering (complex hopping term)

Experimentally achieved phases:

- vortices and vortex lattices

[Matthews, Anderson, Haljan, Hall, Wieman, and Cornell, PRL (1999)]

[(*) Abo-Shaeer, Raman, Vogels, Ketterle, Science (2001)]

...

- integer quantum Hall phases (Hofstadter model)

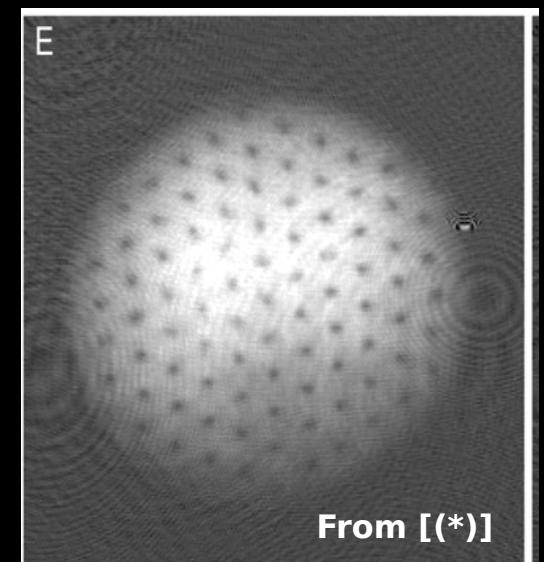
[(**) Aidelsburger, ..., Bloch & Goldman, Nat. Phys. (2015)]

[Stuhl, ..., Spielman, Science (2015)]

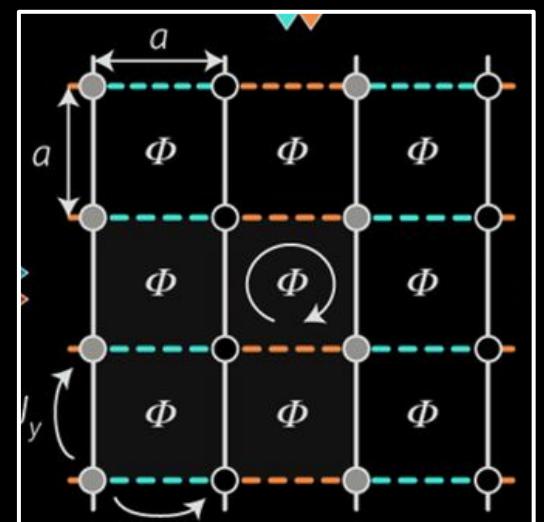
[Mancini, ..., Fallani, Science (2015)]

...

Still outstanding: Synthesis of fractional quantum Hall phase



From [(*)]

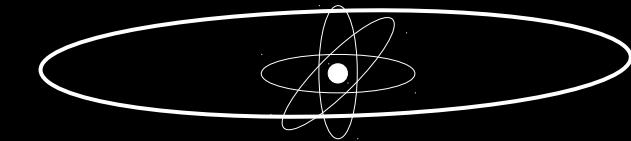


From [(**)]

Engineering interactions by Rydberg dressing

GOAL: Engineer long-ranged atom-atom interactions

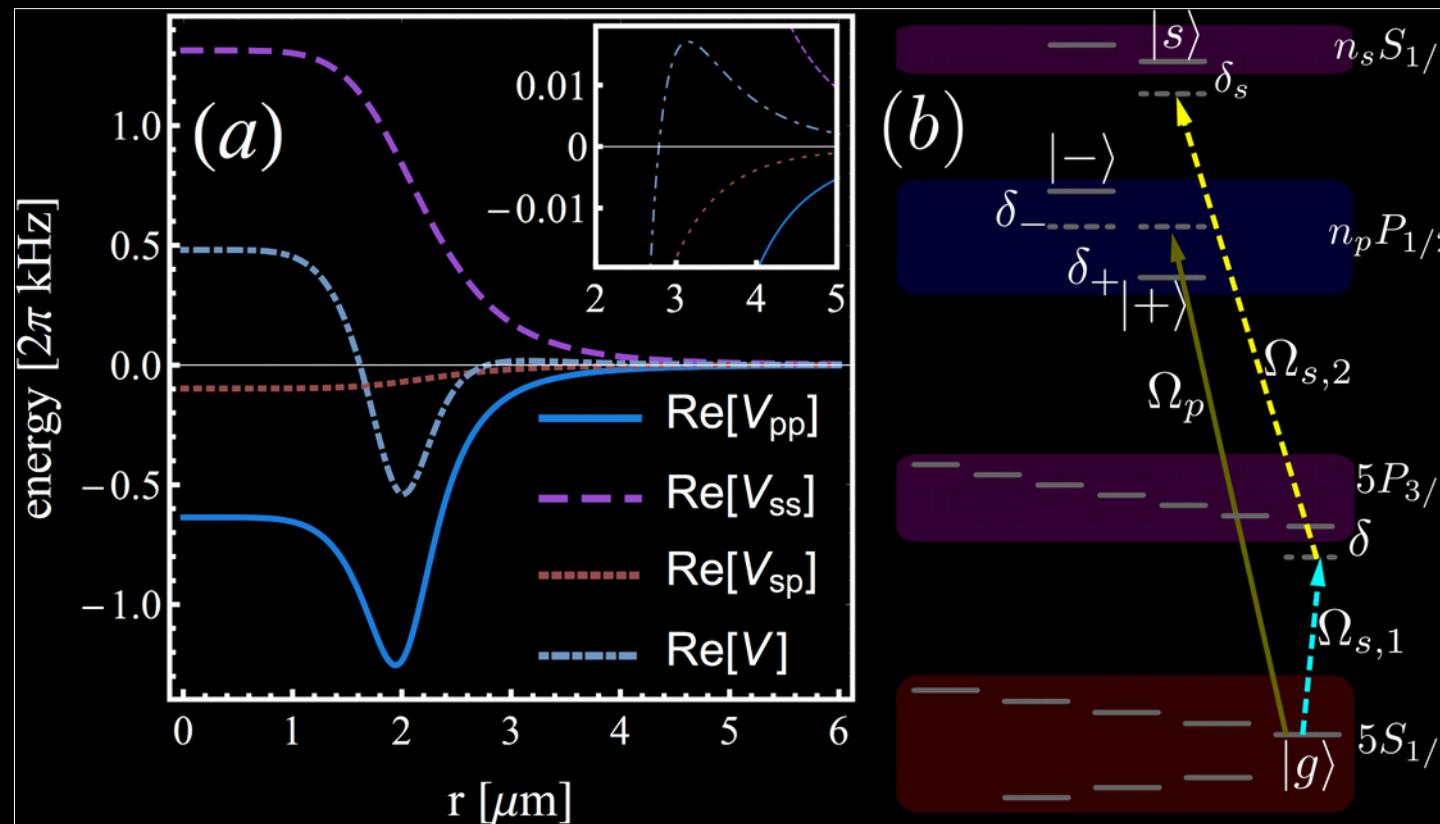
HOW: Using Rydberg states (van der Wals interactions)



Short-lived => only Rydberg **dressing**

[Jau, Hankin, Keating, Deutsch, Biedermann, Nat. Phys. (2016); Zeiher,..., Bloch, Gross, Nat. Phys. (2016)]

APPLICATION: Atomic quantum Hall system with tunable pseudopotentials



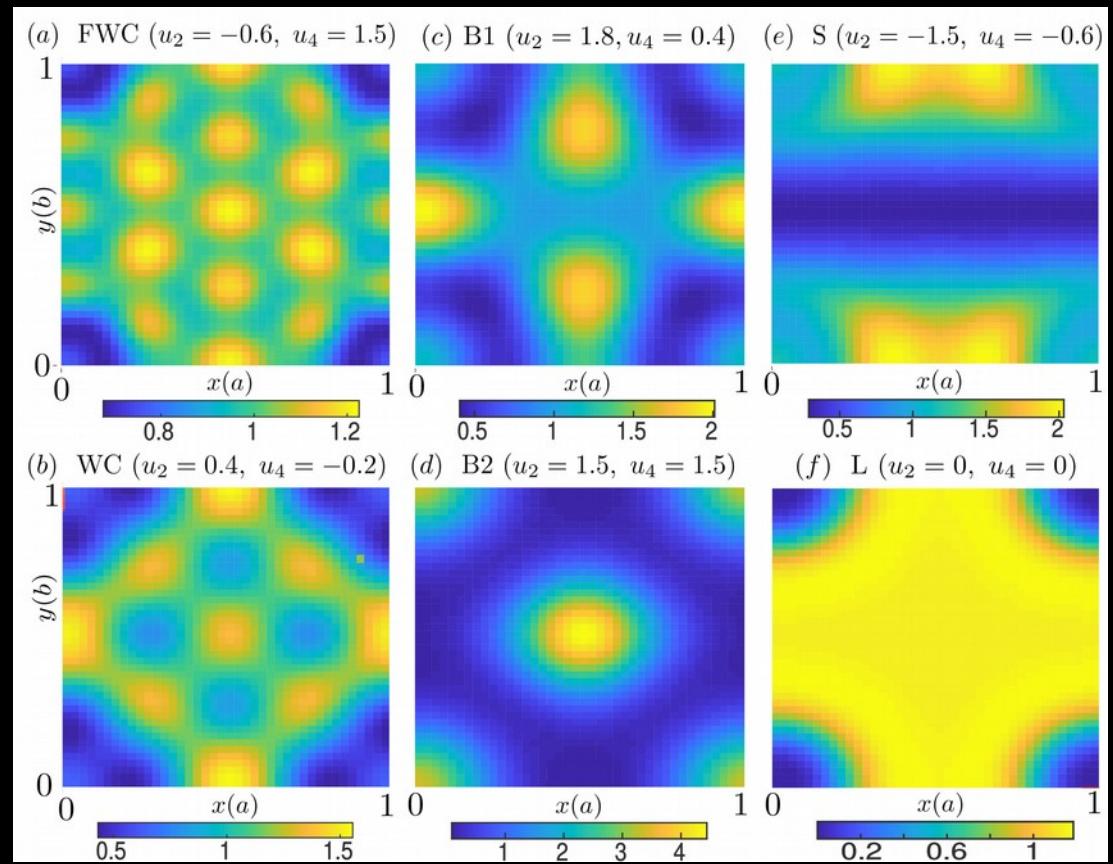
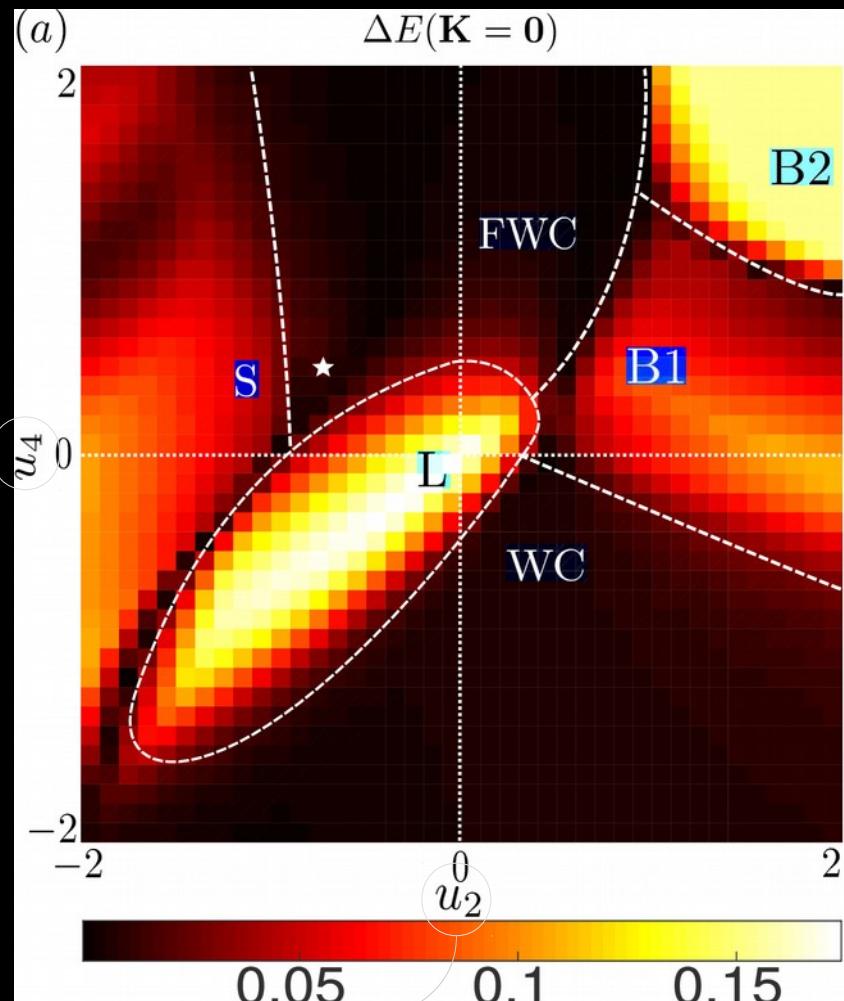
Combined s- and p- state dressing
for enhanced flexibility

Tunable via
principal quantum
numbers,
detuning, Rabi
frequencies

[Grass, Bienias, Gullans, Lundgren, Maciejko, Gorshkov, PRL (2018)]

Phase diagram of bosonic atoms

Landau level filling $v=1/2$: Laughlin liquid and what else?



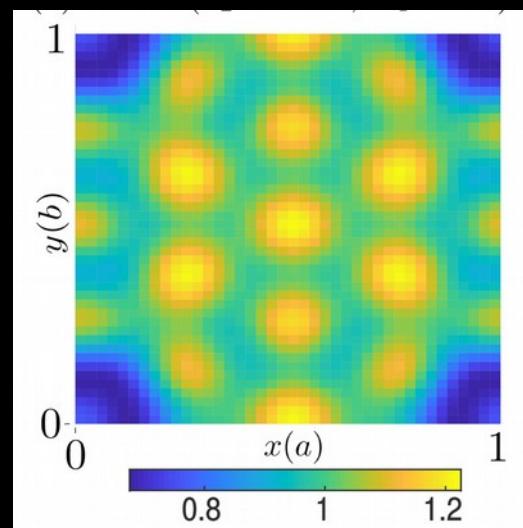
2-body correlation functions (on torus):
Symmetry-broken phases

→ u_2 and u_4 are pseudopotentials: interaction strength at fixed relative angular momentum $2\hbar$ and $4\hbar$

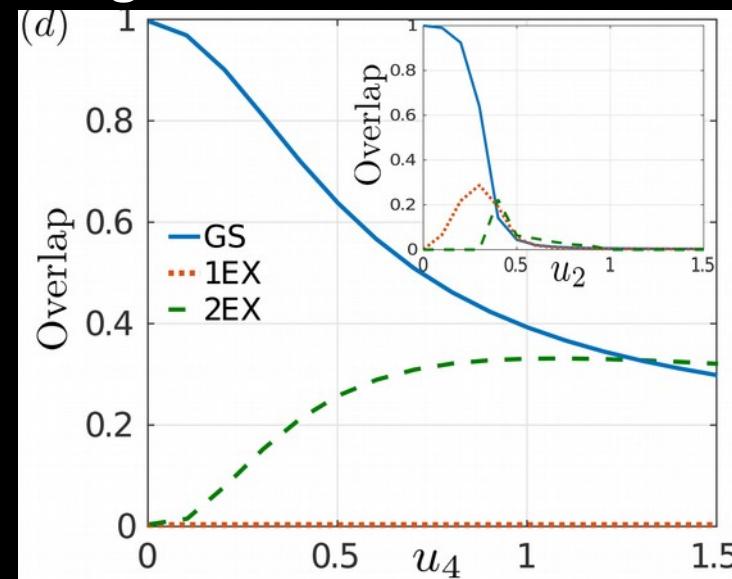
[Grass, Bienias, Gullans, Lundgren, Maciejko, Gorshkov, PRL (2018)]

Fractional Wigner Crystal

Crystal structure with $2N$ peaks:
formed by fractionalized bosons?



Wave-function overlap with
Laughlin state



Coexistence of topological order and symmetry-broken order?

Nematic FQH – Experiments:

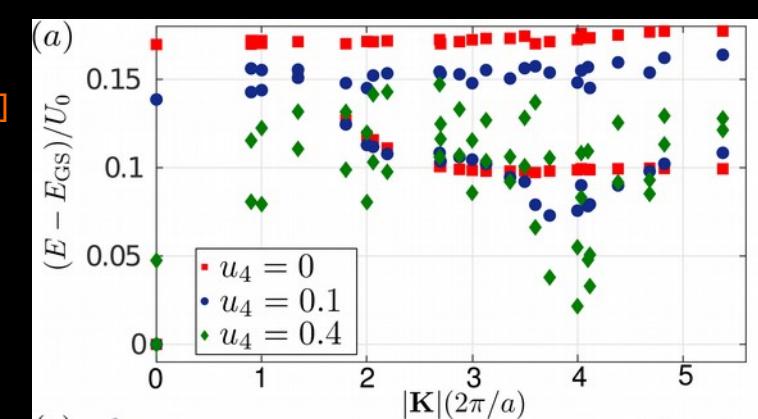
[Xia, Eisenstein, Pfeiffer, West, Nat. Phys. (2011)]

[Samkharadze, Schreiber, Gardner, Manfra, Fradkin, Csáthy, Nat. Phys (2016)]

Explanation through softening of a
collective mode (magnetoroton)?

[Maciejko, Hsu, Kivelson, Park, Sondhi, PRB (2013)]

[You, Cho, Fradkin, PRX, (2014)]



[Grass, Bienias, Gullans, Lundgren, Maciejko, Gorshkov, PRL (2018)]

(3)

QUANTUM SIMULATION OF TOPOLOGICAL MATTER WITH SOLID-STATE SYSTEMS

Engineering of non-Abelian phase in synthetic bilayer graphene

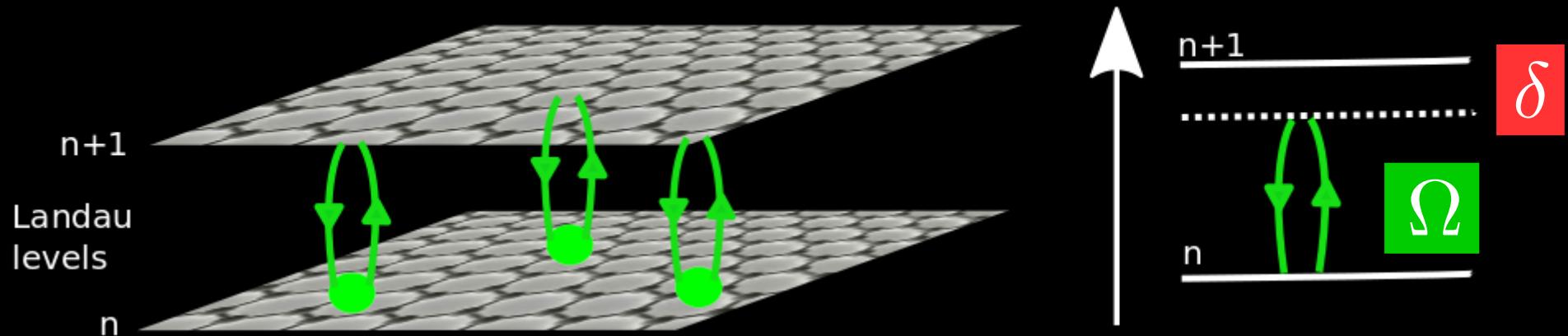
[Ghazaryan, Grass, Gullans, Ghaemi, Hafezi, PRL (2017)]

Creation of anyons by light-matter interactions:

[Grass, Gullans, Bienias, Zhu, Ghazaryan, Ghaemi, Hafezi, PRB (2018)]

Synthetic graphene bilayer

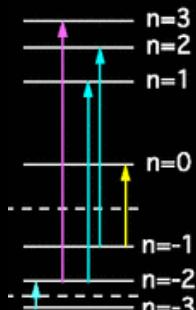
Optically coupled Landau levels:



$$H_0 = \sum_m [\hbar\delta c_{n+1,m}^\dagger c_{n+1,m} + \hbar\Omega c_{n+1,m}^\dagger c_{n,m}] + \text{h.c.}$$

“chemical potential” “interlayer tunneling”

[Ghazaryan, Grass, Gullans, Ghaemi, Hafezi, PRL (2017)]



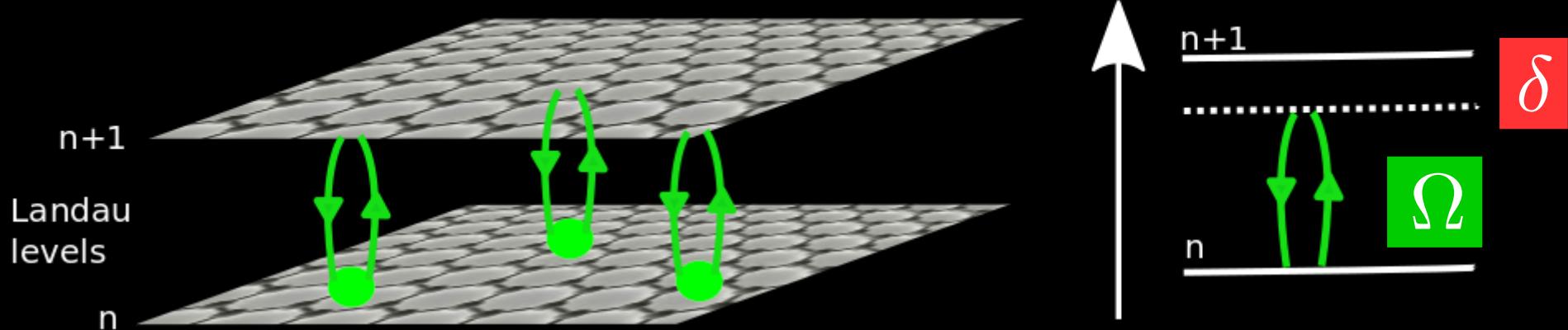
Selection rule for Landau level coupling in graphene:

$$n \leftrightarrow \pm n \pm 1 \quad (\text{B}=10 \text{ Tesla} \rightarrow \text{near-IR transitions})$$

[Jiang, ..., Kim, Stormer, PRL (2007)]

Synthetic graphene bilayer

Optically coupled Landau levels:



$$H_0 = \sum_m \left[\hbar\delta c_{n+1,m}^\dagger c_{n+1,m} + \hbar\Omega c_{n+1,m}^\dagger c_{n,m} \right] + \text{h.c.}$$

“chemical potential” “interlayer tunneling”

[Ghazaryan, Grass, Gullans, Ghaemi, Hafezi, PRL (2017)]

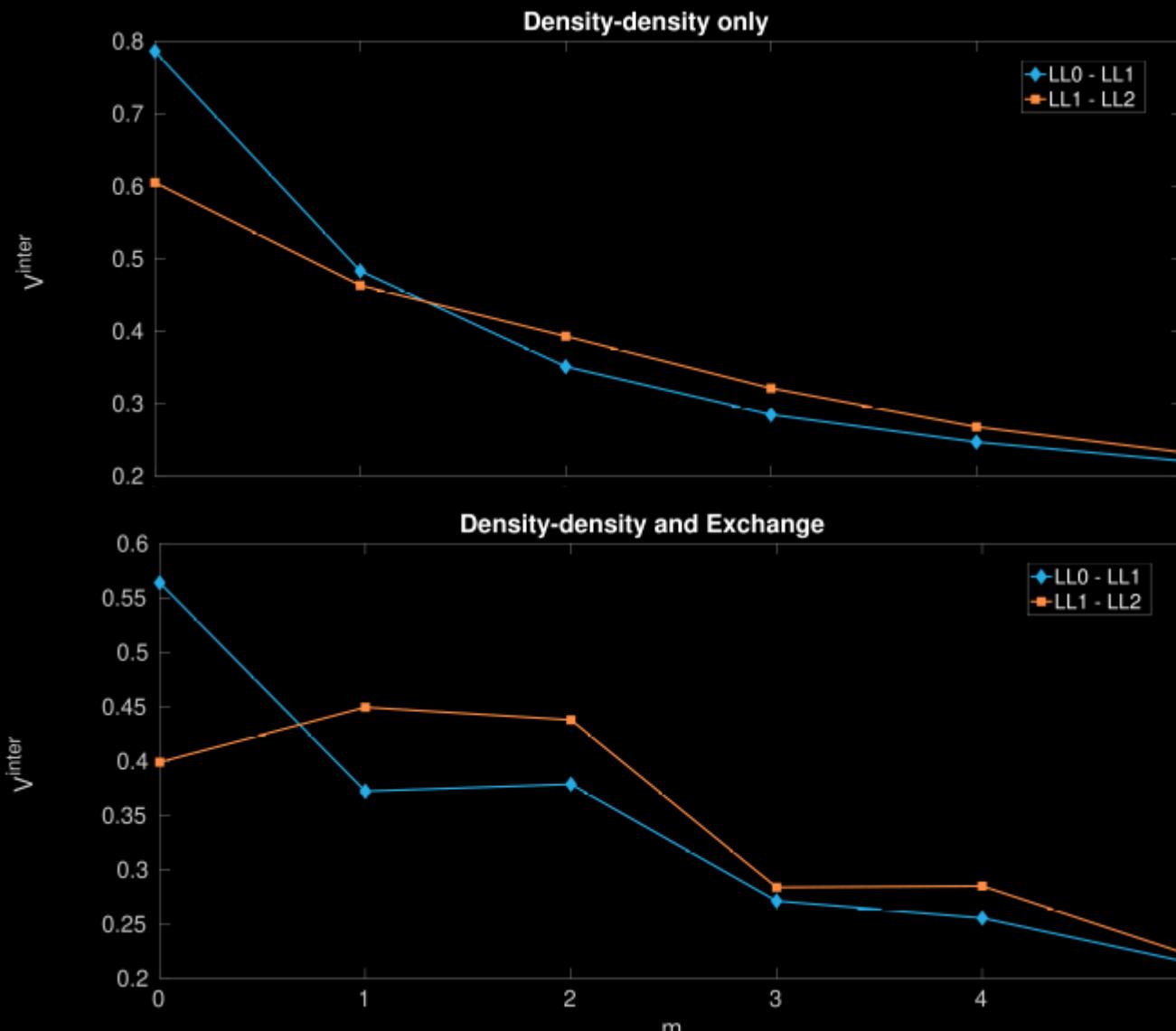
Real vs. synthetic

- Tunable parameters
- Exotic interactions

	Real bilayer	Synthetic bilayer
Density-density $\Psi_i^\dagger(z_1)\Psi_j^\dagger(z_2)\Psi_j(z_2)\Psi_i(z_1)$	YES	YES
Exchange $\Psi_i^\dagger(z_1)\Psi_j^\dagger(z_2)\Psi_i(z_2)\Psi_j(z_1)$	NO	YES

Interactions on synthetic bilayer

Haldane pseudopotentials: Expand interaction in terms of their strength for fixed relative angular momentum m



[Ghazaryan, Grass, Gullans, Ghaemi, Hafezi, PRL (2017)]

Generic behavior:
Monotonic decay
with m

Synthetic bilayer
interactions:
Non-monotonic
behavior →
favoring singlets at
 $m=0$

Identification of the phase: Fibonacci?

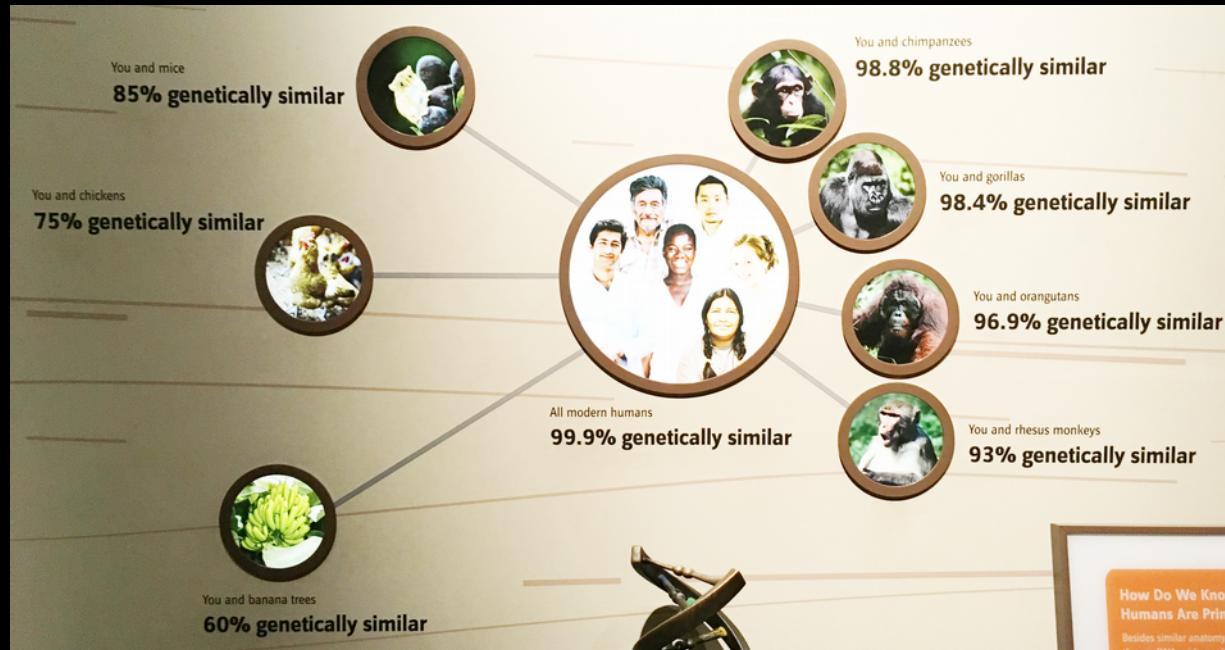
Ground state overlaps:
(at filling 2/3)

“No” overlap with:

- Halperin states (113, 330)
- Composite Fermions
- Intra-layer Pfaffian

“Larger” overlap with:

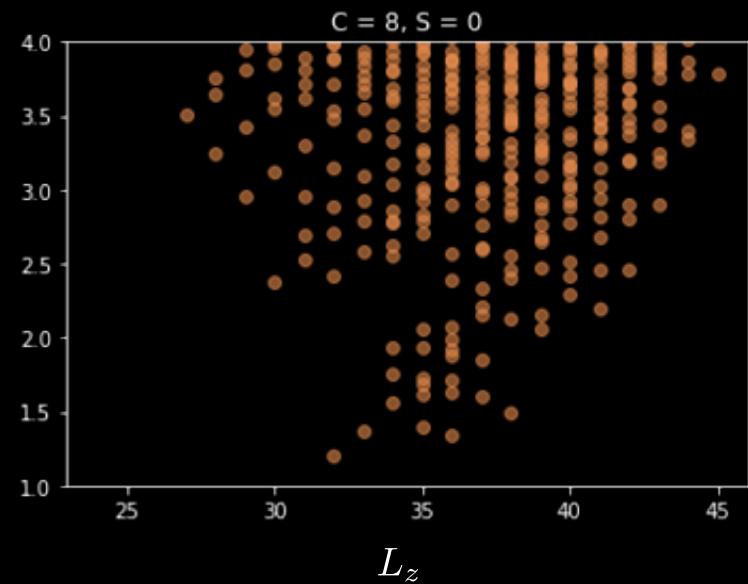
- Inter-layer Pfaffian
- Fibonacci phase



Topological “quantum numbers”:

- Ground state degeneracies on torus
- Edge state counting: 1,1,3,6,...

Conclusion:
Synthetic bilayer likely
to host Fibonacci anyons



Entanglement spectrum for 16 electrons on sphere
(DMRG result by Ze-Pei Cian)

Summary

Quantum Simulation:

- Use light-matter interaction to synthesize features of interest
- Matter can be solid (with some intrinsic features) or atomic (featureless)

Ions: Synthetic Hofstadter ladder

- Floquet-engineered fluxes in 1D geometry
- Microscopic onset of topological protection

Atoms: Fractional Quantum Hall system

- tunable pseudopotentials through Rydberg dressing
- Fractional Wigner Crystal

Graphene: Fibonacci anyon phase

- synthetic bilayer through light-matter interactions
- exotic interlayer interactions

Collaborators

Theory:

Mohammad Hafezi (JQI)



Zepei Cian (JQI)



Guanyu Zhu (IBM)



Alexey Gorshkov (JQI)



Przemek Bienias (JQI)



Rex Lundgren (JQI)



Michael Gullans (Princeton)



Pouyan Ghaemi (City College N.Y.)



Areg Ghazaryan (City College N.Y.)



Maciej Lewenstein (ICFO)



Alessio Celi (Innsbruck)



Ravindra Chhajlany (Poznan)



Christine Muschik (Waterloo)



Experiments::

Glenn Solomon (JQI)



Bin Cao (JQI)



Olivier Gazzano (Paris)

Tobias Huber (Wuerzburg)



Guido Pagano (JQI)

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Thank you!