R Programming as a Part of Bigdata Course Introduction to R language Elements

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R Programming Examples TOC (1)

```
# Filename: 2_R_Programming.R
# Objective:
# Introduction to R language elements and functions.
#
  TABLE OF CONTENTS
#
# 2.0: Enter the main R Language documentation.
# 2.1: Scalar operations and examples on functions.
# 2.2: Vector definitions and operations.
# 2.3: Matrix definitions and vector, matrix operations.
# 2.4: Factors. (Ordinal variables, where only the ordering matters).
# 2.5: Lists - the most general ordered collection of objects, which
         can be of mixed types.
```

R Programming Examples TOC (2)

2.6.8: Plot selected parts of data frame.

2.6.9: Deleting (removing) rows or columns in dataframes.

R Programming Examples TOC (3)

```
# 2.7: Program control structures
# 2.7.1: The if-else condition
# 2.7.2: The for-loop
# 2.7.3: The while-loop
# 2.7.4: The repeat function
# 2.7.5: The function definition.
```

R Programming Examples TOC (4)

```
# 3.1: Example Probability Distributions, Sets, Combinations
      and Permutations
# 3.2: Binomial Distribution
# 3.3: Mean and variance of a set of data.
# 3.4: Set operations, sampling, union, intersection, diffe-
      rence, equal.
# 3.5: Combinations of a set.
# 3.6: Permutations of a set.
# 3.7: Central Limit Theorem (CLT) example with runif(),
      uniform density seed.
# 3.8: Central Limit Theorem (CLT) example with rbinom(),
      binomial distribution seed.
# 3.9: Normal Distribution.
```

Main R Manual and I/O Parameters

Packages, Install and Include in Library

```
> #
> # Install packages needed in this script.
> #
> install.packages("combinat",lib="C:/R_packages")
trying URL
 'https://cran.rstudio.com/bin/windows/contrib/3.2/combinat_0.0-8.zip'
Content type 'application/zip' length 29294 bytes (28 KB)
downloaded 28 KB
package combinat successfully unpacked and MD5 sums checked
The downloaded binary packages are in
C:\Users\jaas\AppData\Local\Temp\Rtmp4gZ46V\downloaded_packages
> library("combinat",lib="C:/R_packages")
Det folgende objekt er maskeret fra package:utils:
    combn
>
```

Scalar operations, Functions, logicals (1)

```
> # 2.1: Examples on scalar operations, functions and logicals
> #
> 10*32
             # Multiply.
Γ1] 320
> (10+2)*5
             # Do not use [10+2]*5. It don't work.
[1] 60
> 2^3
             # Exponent
[1] 8
> 2**4
             # Exponent
Γ1 16
> (2+3i)^2
             # Square a complex number: 4 + 12i - 9 = -5+12i
[1] -5+12i
> 12/3
             # Division
Γ17 4
>
```

Scalar operations, Functions, logicals (2)

```
> #
> # Some constants: pi and e.
> #
> print(pi, digits=15)
[1] 3.14159265358979
> print(exp(1), digits=10)
[1] 2.718281828
>
```

Scalar operations, Functions, logicals (3)

```
> #
> # Some functions, e.g. [Kabacoff, 2015] page 91, Table 5.2
> #
> abs(-4)
[1] 4
> sqrt(2.71^2)
[1] 2.71
> ceiling(15.29)
Γ1 16
> floor(15.29)
[1] 15
> trunc(-1.5)
                                # Truncation towards 0
[1] -1
> round(3.14159265, digits=3)
                                # Round down to 3 decimal places.
[1] 3.142
> signif(3.141592, digits=2) # Signicant digits.
[1] 3.1
```

Scalar operations, Functions, logicals (4)

```
> ac <- c(1,2,5,100)
> median_ac <- median(ac); median_ac</pre>
[1] 3.5
> mean_ac <- mean(ac);mean_ac</pre>
[1] 27
> #
> exp(1)
                # Exponential function of 1, Eulers number e=2.71828
[1] 2.718282
> log(exp(1))
               # Natural logarithm to Eulers number e, which is 1
Γ1 1
> log10(10)
                # Base 10 logarithm to 10 which is 1.
Γ1 1
> log10(1)
               # Base 10 logarithm to 1, which is 0.
Γ1 0
 > \log(3^2, \text{base=3})  # Base 3 logarithm of 9, which is 2, bc 3^2=9.
[1] 2
```

Scalar operations, Functions, logicals (5)

```
> #
> # Constants
> #
> ?NA # NA: Not available/missing value. NA is a reserved word in R.
> is.na(c(1,2,NA)) # Ask if there is an NA in the array.
[1] FALSE FALSE TRUE
> #
> # INF, -INF Numbers out of numerical range.
> ?Inf # Inf is a reserved word in the R.
> 2^1024 # This return an Inf.
[1] Inf
> -2^1024 # This returns an -Inf.
[1] -Inf
> #
> # NaN Not a number.
> ?NaN
> 0/0
          # Notice this is "Not a number"
[1] NaN
> 1/0 # Notice this is Inf
[1] Inf
>
```

Scalar operations, Functions, logicals (6)

```
> #
> # Logicals, relations and set operations.
> #
> z <- 1:5:z
                               # z is a vector.
[1] 1 2 3 4 5
> test_z1 <- (z < 3); test_z1 # Test "less than" on each position.
[1] TRUE TRUE FALSE FALSE FALSE
> test_z2 <- (z == 2); test_z2 # Test "equal to" on each position.
[1] FALSE TRUE FALSE FALSE FALSE
> test_z3 <- (z != 2); test_z3 # Test "not equal to" on each position.
[1] TRUE FALSE TRUE TRUE TRUE
> test_z4 <- (z > 1 \& z < 3); test_z4 # Test "logical AND".
[1] FALSE TRUE FALSE FALSE FALSE
> test_z5 <- (z > 4 \mid z < 1); test_z5 # Test "logical OR".
[1] FALSE FALSE FALSE TRUE
# test membership on each position
> test_z6 <- (z \%in\% c(0,-1,1,5,6,7,8,9,10,100)); test_z6
[1] TRUE FALSE FALSE FALSE TRUE
>
```

Scalar operations, Functions, logicals (7)

```
> #
> # Set operations: union, intersect, setdif
> #
> z1 <- 1:3;z1
[1] 1 2 3
> z2 <- 2:5;z2
[1] 2 3 4 5
> z3 <- union(z1, z2); z3
[1] 1 2 3 4 5
> z4 <- intersect(z1, z2); z4
[1] 2 3
> z5 <- setdiff(z1, z2); z5 # Remove from z1 the elements in z2
Γ1 1
> z6 <- setdiff(z2, z1); z6 # Remove from z2 the elements in z1
[1] 4 5
>
```

Vector Definitions and Operation (1)

```
> # 2.2: Examples on vector definitions and vector operations.
> #
> # Examples on atomic vectors, c.f. [Kabacoff, 2015] page 464.
> # Atomic vectors are arrays of a single type:
> #
      Logical, real, complex, character
> passed <- c(TRUE, TRUE, FALSE, TRUE) # Vector of logicals.
> passed
[1] TRUE TRUE FALSE TRUE
> ages <- c(15, 18, 25, 14, 19); ages # Vector of numericals.
[1] 15 18 25 14 19
> cmplxNums <- c(1+2i, 0+1i, 39+3i, 12+2i) # Vector of numericals.
> cmplxNums
[1] 1+2i 0+1i 39+3i 12+2i
> cmplxNums1 <- c(1, 1i, 39+3i, 12+2i) # "It's ok to skip ..."
> cmplxNums1
[1] 1+0i 0+1i 39+3i 12+2i
>
```

Vector Definitions and Operation (2)

```
> #
        Examples on vector operations, based on
> #
        examples from R Manual display on console using >?c
> #
        and [Kabacoff, 2015] page 22-23.
> #
> a <- c(1:1,7:9); a
                                    # Create array with 4 elements.
[1] 1 7 8 9
> (a1 <- seq(from=3, to= 12, by=2)) #
[1] 3 5 7 9 11
> b <- c(1:5, 10.5, "next"); b # Create array with 7 elements.
[1] "1" "2" "3" "4" "5" "10.5" "next"
> c <- letters[3:5];c
                                    # letters c,d,e
[1] "c" "d" "e"
> #
> # Used with a single argument to drop attributes
> x <- 1:4; x
                               # Create and display x
[1] 1 2 3 4
> v <- c(1:4); v
                              # Same as the immediate former line.
[1] 1 2 3 4
```

Vector Definitions and Operation (3)

```
> # Alternative methods for creating vectors
> a1 <- rep(1:4,2); a1
[1] 1 2 3 4 1 2 3 4
> a2 <- rep(1:4, each=2); a2
                                  #
[1] 1 1 2 2 3 3 4 4
> a3 <- rep(1:4, c(2,2,2,2)); a3 # Same as the former result.
[1] 1 1 2 2 3 3 4 4
> a4 <- c(1,2,3,4, 'bigdata'); a4 # Vector with different types.
        "2"
                       "3"
[1] "1"
                                 "4"
                                           "bigdata"
                                  # All entries becomes type: string.
>
> a5 <- length(a4); a5
                                  # Length of vector
[1] 5
> #
> x < c(1,2,3,4,5,6,7,8) # Create a vector
> x1 < -x[x > 4 \& x < 7]; x1 # All elements with 4 < index < 7
[1] 5 6
```

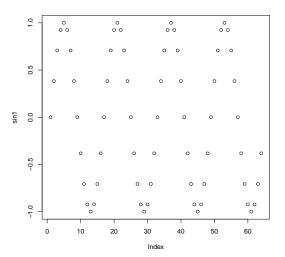
Vector Definitions and Operation (4)

```
> # Assign names to the components of x using the names() function.
> # Check the function of names() using R Manual display on console
> # using >?names
> ?names()
                                # Check manual
> names(x) <- letters[1:4]; x # Assigns the letters a b c d to the
                   d < NA > < NA > < NA > < NA >
        2 3 4 5 6 7
>
                                # 4 components of x.
> c(x)
                                 # The array has names.
              c d \langle NA \rangle \langle NA \rangle \langle NA \rangle \langle NA \rangle
              3 4 5
                              6 7
> as.vector(x)
                                # The vector has no names.
[1] 1 2 3 4 5 6 7 8
```

Vector Definitions and Operation (5)

```
> # Example on a vector argument to a function
> arg1 <- c(0:63)*pi/8; # Generate a vector with pi/8 multiples.
> head(arg1)  # List top of vector arg1
[1] 0.0000000 0.3926991 0.7853982 1.1780972 1.5707963 1.9634954
> sin1 <- sin(arg1);
> head(sin1)  # List top of vector sin1
[1] 0.0000000 0.3826834 0.7071068 0.9238795 1.0000000 0.9238795
> plot(sin1)
> #
> pdf("fig_2_sin1.pdf") # Generate pdf of plot
> par(.opar)
> plot(sin1)
> dev.off()
RStudioGD
> par(.opar)
```

sin()





Matrix Definitions and Vector, Matrix Operations (1)

```
> # 2.3: Examples on matrix definitions and vector, matrix operations.
> #
> # Define a matrix, c.f. [Kabacoff,2015] page 23; display the matrix
> # and check its class and attributes.
> # Notice that the matrix is generated columnwise from a vector 1:N.
> # If generated by rows instead of by columns use the following
> # attribute in the matrix argument: matrix( .... byrow=T)
>
```

Matrix Definitions and Vector, Matrix Operations (2)

```
Now continue from here using by column organisation.
> #
> #
     Notice there is no bycolumn (byrow=FALSE) attribute.
> #
> Nelem <- 32; Nrow <- 4; Ncol <- 8
>
                 # Notice that Nelem = Nrow*Ncol (required).
> # Create a matrix.
> z <- matrix(1:Nelem, nrow=Nrow, ncol=Ncol, byrow=FALSE); z
    [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8]
[1,] 1 5 9 13
                        17
                                 25
                            21
                                      29
[2,] 2 6 10 14 18 22
                                 26 30
[3,] 3 7 11 15 19 23
                                 27 31
[4,] 4
           8 12 16
                        20
                            24
                                 28
                                      32
> class(z)
[1] "matrix"
> attributes(z) # Display the attributes on the console.
$dim
[1] 4 8
> dim(z)
                 # Display the dimension on the console.
Γ17 4 8
> #
```

Matrix Definitions and Vector, Matrix Operations (3)

```
> # Check matrix creation if too few elements.
> # Notice no warning but circular allocation.
> # Create an 4 x 8 matrix.
> z1 <- matrix(1:31, nrow=4, ncol=8, byrow=FALSE); z1
Warning message:
In matrix(1:31, nrow = 4, ncol = 8, byrow = FALSE):
datalength [31] is not sub-multiple or multiple of number of rows [4]
    [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8]
[1,]
      1 5 9 13 17
                            21
                                25 29
[2,] 2 6 10 14 18 22
                                26 30
[3,] 3 7 11 15 19 23
                                27 31
[4,] 4
               12
                   16
                       20
                            24
                                28 1
> #
```

Matrix Definitions and Vector, Matrix Operations (4)

```
> # Get single element in matrix z ("the lower right corner element")
> z[Nrow, Ncol]
[1] 32
> # Get column number 2 in matrix z.
> z[,2]
[1] 5 6 7 8
> # Get row number 3 in matrix z.
> z[3,]
[1] 3 7 11 15 19 23 27 31
> # Get last row
> z[Nrow,]
[1] 4 8 12 16 20 24 28 32
> # Get last column
> z[,Ncol]
[1] 29 30 31 32
```

Matrix Definitions and Vector, Matrix Operations (5)

```
> # Get all rows, except rows 2 and 3
> z[-(2:3),]
    [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8]
[1,] 1 5 9 13
                       17
                           21
                                25
[2,] 4 8 12 16
                       20
                                28 32
                           24
> # Get all columns, except columns no. 1, 2, 3
> z[,-(1:3)]
    [,1] [,2] [,3] [,4] [,5]
[1,] 13 17
              21
                  25
                       29
[2,] 14 18
              22
                 26
                       30
[3,] 15 19 23
                 27
                       31
[4,] 16
          20
              24
                  28
                       32
> #
```

Matrix Definitions and Vector, Matrix Operations (6)

```
> #
> # Transpose matrix z ("Exchange rows and columns") and display
> z_t <- t(z); z_t
     [,1] [,2] [,3] [,4]
[1,]
      1 2
[2,]
       5
[3,] 9
           10
                11
                     12
[4,] 13
           14
                15
                     16
[5,]
     17
           18
                19
                     20
[6,]
      21
           22
                23
                     24
[7,]
      25
           26
                27
                     28
[8,]
      29
           30
                31
                     32
> #
```

Matrix Definitions and Vector, Matrix Operations (7)

```
> # The norm (length) of a vector:
> z2 <- matrix(c(3,4), nrow=2, ncol=1); z2
     [,1]
[1,]
[2,] 4
> length_z2 <- sqrt(t(z2)%*%z2); length_z2
     [,1]
Γ1. ]
> #
> # Multiply a matrix with a scalar, a vector and a matrix
> z2=0.5*z: z2
    [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8]
[1,] 0.5 2.5 4.5 6.5 8.5 10.5 12.5 14.5
[2,] 1.0 3.0 5.0 7.0 9.0 11.0 13.0 15.0
[3,] 1.5 3.5 5.5 7.5 9.5 11.5 13.5 15.5
[4.] 2.0 4.0 6.0 8.0 10.0 12.0 14.0 16.0
>
```

Matrix Definitions and Vector, Matrix Operations (8)

```
> # Create a vector of apropriate size and multiply with matrix z
> v \leftarrow matrix(c(0,0,0,1,0,0,0,0), nrow=8, ncol=1)
> v
     [,1]
[1,]
[2,]
[3,]
[4,]
[5,]
[6,]
[7,]
[8,]
> dim(v)
[1] 8 1
```

Matrix Definitions and Vector, Matrix Operations (9)

```
> # Multiply matrix z and vector v and display the product.
> zv <- z%*%v; zv # Multiply and display.
    [,1]
[1,]
      13
[2,] 14
[3,] 15
[4,] 16
> z
            # Display matrix and verify column and zv.
    [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8]
[1,]
           5 9
                  13
                        17
                             21
                                 25
                                      29
[2,]
                                 26 30
           6 10 14
                        18
[3,] 3 7 11
                  15
                        19
                             23
                                 27 31
[4,]
           8
               12
                    16
                        20
                             24
                                 28
                                      32
```

Matrix Definitions and Vector, Matrix Operations (10)

```
> # Scalar product (inner product, "dot" product) between
> # two vectors w1 and w2.
> w1 <- matrix(c(1,2,3), nrow=3, ncol=1); w1
    [,1]
[1,] 1
[2,] 2
[3,] 3
> w2 <- matrix(c(3,2,1), nrow=3, ncol=1); w2
    [,1]
[1,]
[2,] 2
[3,] 1
> a1 <- sum(w1*w2); a1 # Elementwise product and sum.
Γ1 10
> a2 <- t(w2)%*%w1; a2 # Matrix product of a row (use transpose) and
     [,1]
[1.] 10
                       # a column vector.
```

Matrix Definitions and Vector, Matrix Operations (11)

Matrix Definitions and Vector, Matrix Operations (12)

```
> # Element wise product of two matrices
> A2 <- matrix(c(1,2,3,4,5,6), nrow=2, ncol=3, byrow=TRUE);A2
    [,1] [,2] [,3]
[1,] 1 2 3
[2.] 4 5 6
> A3 <- matrix(c(6,5,4,3,2,1), nrow=2, ncol=3, byrow=TRUE);A3
    [,1] [,2] [,3]
[1,] 6 5 4
[2,] 3 2 1
> A2A3 <- A2*A3;A2A3</pre>
    [,1] [,2] [,3]
[1,] 6 10 12
[2,] 12 10 6
```

Matrix Definitions and Vector, Matrix Operations (13)

```
> # Arrays: matrices with more than 2 dimensions.
> AR1 <- array(data=1:24,dim=c(3,4,2)) # 3 dim with dimensions 3x4x2
> AR1 # Display AR1
, , 1
    [,1] [,2] [,3] [,4]
[1,] 1 4 7 10
[2,] 2 5 8 11
[3,] 3 6 9 12
, , 2
    [,1] [,2] [,3] [,4]
[1,]
      13
          16
              19
                   22
[2,] 14 17
              20 23
[3,] 15
          18
              21
                   24
```

Matrix Definitions and Vector, Matrix Operations (14)

```
> AR2 <- array(1:24,c(3,3,2)) # identical array
> AR2 # Display AR2
, , 1
    [,1] [,2] [,3]
[1,] 1 4 7
[2,] 2 5 8
[3,] 3 6 9
, , 2
    [,1] [,2] [,3]
[1,]
    10
          13 16
[2,] 11
        14 17
[3,] 12
          15
              18
```

Matrix Definitions and Vector, Matrix Operations (15)

```
> # Examples on special vectors and matrices
> # Generate and display a column zero vector of size N=3.
> N <- 3
> zero_c <- matrix(rep(0,N), nrow=N, ncol=1); zero_c</pre>
     [,1]
[1,] 0
[2,] 0
[3.] 0
> #
> # Generate and display a row vector with 1 of size N=3.
> N <- 3
> one_r <- matrix(rep(1,N), nrow=1, ncol=N); one_r</pre>
     [,1] [,2] [,3]
[1,] 1 1 1
>
```

Matrix Definitions and Vector, Matrix Operations (16)

```
> # Generate and display a matrix with zero entries
> MO <- matrix(0, nrow=3, ncol=2); MO
    [,1] [,2]
[1,] 0
[2,] 0 0
[3,] 0 0
> #
> # Generate and display a diagonal matrix
> ?diag()
              # Look into the manual of diag()
> Md \leftarrow diag(c(1,2,3,4,5,6)); Md
    [,1] [,2] [,3] [,4] [,5] [,6]
[1,]
[2,] 0 2 0 0 0
[3,] 0 0 3 0 0
[4,] 0 0 0 4 0
[5,] 0
        0 0 0 5
[6,] 0
                  0
                      0
                          6
> #
```

Matrix Definitions and Vector, Matrix Operations (17)

Matrix Definitions and Vector, Matrix Operations (18)

```
> # Define and exemplify multiplication of matrices MM1 %*% MM2
> # Notice that the number of columns in the leftmost matrix MM1
> # must be equal to the number of rows of rightmost matrix MM2.
> n2row <- n1col; n2col <- 4; # Rows and columsn of rightmost matrix.
> MM1 <- matrix(1:(n1row*n1col),nrow=n1row, ncol=n1col); MM1</pre>
    [,1] [,2] [,3]
[1,] 1 3 5
[2,] 2 4 6
> MM2 <- matrix(1:(n2row*n2col),nrow=n2row, ncol=n2col); MM2
    [,1] [,2] [,3] [,4]
[1,] 1 4 7 10
[2,] 2 5 8 11
[3,] 3 6 9 12
> MM12 <- MM1 %*% MM2; MM12 # F.inst chec manually elements of MM12
    [,1] [,2] [,3] [,4]
[1.]
     22 49
              76 103
[2,] 28 64 100 136
>
```

Matrix Definitions and Vector, Matrix Operations (19)

```
> # Determine the inverse of a quadratic matrix.
> # Create an example quadratic matrix A1
> A1 <- matrix(c(1,2,3,4), nrow=2, ncol=2, byrow=FALSE); A1
    [,1] [,2]
[1,] 1 3
[2,] 2 4
> #
> A1_inv <- solve(A1); A1_inv # Determine and display inverse A1.
    [,1] [,2]
[1,] -2 1.5
[2,] 1 -0.5
> #
> # Check that A1 and A1_inv are inverse by multiplying.
> A1A1_inv <- A1 %*% A1_inv; A1A1_inv
    [,1] [,2]
[1,] 1 0
[2,] 0 1
> # Check also the alternative ordering
> A1_invA1 <- A1_inv %*% A1; A1_invA1</pre>
    [,1] [,2]
[1,] 1 0
[2,] 0
```

Matrix Definitions and Vector, Matrix Operations (20)

Factors (1)

Factors (2)

```
> # Example:
> # Likert scale for representing responses on statements on product.
> # Scale value 5: The customer strongly agree (SA).
> # Scale value 4: The customer agree (A).
> # Scale value 3: The customer is neutral (N).
> # Scale value 2: The customer disagree (D).
> # Scale value 1: The customer strongly disagree (SD).
> # Scale value NA: The customer abstains (AB) from assessing.
> #
> # factor levels: Strongly Agree (SA), Agree (A),
> #
                   Neutral (N),
> #
                   Disagree (D), Strongly Disagree (SD).
> #
```

Factors (3)

```
> survey.vector <- c('A', 'SA', 'N', 'SD', 'A', 'A', 'D')
> survey.vector
[1] "A" "SA" "N" "SD" "A" "A" "D"
> #
> # Assign numerical value to category by ordered list
> #
> survey.factor <- factor(survey.vector, order=TRUE,
                         levels=c('SD','D','N','A','SA'))
+
> #
                         values 1 2 3 4 5
> survey.factor
[1] A SAN SDA A D
Levels: SD < D < N < A < SA
# Check the numerical values of categories.
> (as.numeric(survey.factor))
[1] 4 5 3 1 4 4 2
>
```

Lists (1)

```
> # 2.5: lists - the most general ordered collection of objects,
              which can be of mixed types.
> #
> #
> ?list() # Check manual for the list() function.
> obj1 <- 1:3; obj2 <- c('text1', 'text2', 'text3');</pre>
> Nelem <- 6; Nrow <- 3; Ncol <- 2 # Notice Nelem = Nrow*Ncol (req.)
> obj3 <- matrix(1:Nelem, nrow=Nrow, ncol=Ncol, byrow=FALSE)
> # create a list with 3 objects:
> m1 <- list(name1=obj1, name2=obj2, name3=obj3); m1</pre>
$name1
[1] 1 2 3
$name2
[1] "text1" "text2" "text3"
$name3
    [,1] [,2]
[1,] 1 4
[2,] 2 5
[3,] 3 6
>
```

Lists (2)

```
> # Accessing list objects individually through indexing
> m1[[1]]  # The same as m1$name1
[1] 1 2 3
> m1[['name1']] # The same as m1$name1
[1] 1 2 3
> m1[[2]]  # The same as m1$name2
[1] "text1" "text2" "text3"
> m1[[2]][2]  # 2'nd list object element no. [2]
[1] "text2"
> m1[[3]]
              # The same as m1$name3
    [,1] [,2]
[1,] 1 4
[2,] 2 5
[3,] 3 6
> m1[[3]][3,2] # 3'nd list object element no. [3,2]
Γ17 6
>
```

Lists (3)

```
#
> m1$name1[2]  # The same as obj1[2]
[1] 2
> m1$name2[3]  # The same as obj2[3]
[1] "text3"
> m1$name3[2,2]  # The same as obj3[2,2]
[1] 5
```

Lists (4)

```
> # Further examples on defining and applying lists.
> # Ref. [Kabacoff, 2015] page 30.
> #
> # Using the example [Kabacoff, 2015] page 31, demonstrates ex. of
> # a list with: string, numeric vector, matrix and character vector.
> g <- "first list"
> h <- c(25,26,18,39)
> j <- matrix(1:10, nrow=5) # By-column as byrow=F (default)
> k <- c("one","two","three")
> newlist <- list(title=g,ages=h,j,k)</pre>
```

Lists (5)

>

```
> newlist <- list(title=g,ages=h,j,k)</pre>
> newlist
$title
[1] "first list"
$ages
[1] 25 26 18 39
[[3]]
    [,1] [,2]
[1,] 1 6
[2,] 2 7
[3,] 3 8
[4,] 4
         9
[5,] 5
           10
[[4]]
[1] "one" "two"
                 "three"
```

Lists (6)

```
> # Refer to the second object in the list, by index [2]
> newlist[[2]]
[1] 25 26 18 39
> # Refer to the second object in the list, by name ["ages"]
> newlist[["ages"]]
[1] 25 26 18 39
> # Refer to the second named component
> newlist$ages
[1] 25 26 18 39
> # Refer to the first named component.
> newlist$title
[1] "first list"
```

Dataframes (1)

Dataframes (2)

```
> # In the following is an example on a data frame for the represen-
> # tation of heterogeneous data from an example on user assessments
> # of products. The example contains the following operations:
> # - create a data frame.
> # - Insert a new variable in a data frame.
> # - Merge two sets of observations for the same set of variables.
    - Identifying missing values in a data frame.
> #
    - Excluding missing values in preparation for analysis.
> #
    - Grouping observations, example into age groups:
> #
      Teen (13-19), Young (20-39), MidAged (40-69),
> #
      MidAgeP (70-79), Old (80-).
> # - Sorting observations according to one variable.
> # - Plot selected parts of data frame.
>
```

Dataframes (3)

```
> # 2.6.1: Create a data frame -----
> #
> # Create a data frame which contains a mixture of numerical and
> # character values, exemplified by customer assessment of two
> # products, using a Likert scale for the product assessment.
> #
> # Create a data frame which contains a mixture of numerical and
> # character values, exemplified by customer assessment of two
> # products, using a Likert scale for the product assessment.
> #
> # The Likert scale used for assessing a statement about the product:
> # Scale value 5: The customer strongly agree (SA).
> # Scale value 4: The customer agree (A).
> # Scale value 3: The customer is neutral (N).
> # Scale value 2: The customer disagree (D).
> # Scale value 1: The customer strongly disagree (SD).
> # Scale value NA: The customer abstains (AB) from assessing.
> #
```

Dataframes (4)

```
> # There are two products, denoted Product 1 and Product 2.
> # Each customer assessment is labeled with the customer gender.
> # Each customer register the customer age.
> # Each customer assesses the correctness of each of 3 statements
> #
       about the product:
> #
     S1: The product is useful.
> #
     S2: The product price is acceptable.
> #
     S3: The customer will, without hesitation, recommend the product
> #
          to a person known well by the customer.
> #
   In the present example there are 8 customers.
> #
> # Now build a data frame for representing the above assessments on
> # the two products: Product 1 and Product 2.
>
```

Dataframes (5)

```
> # The products 1 or 2 assessed by the customer 1 to 8.
> Prod_no <- c(1,1,2,1,2,1,2,2)
> # F: Female and M: Male.
> Gender <- c("F","F","M","F","M","F","M")
> Age <- c(37,81,57,79,17,18,67,45)  # The customers ages
> S1 <- c(4,3,2,5,NA,3,5,5)  # Assessments of Statement S1.
> S2 <- c(3,4,1,4,3,NA,1,1)  # Assessments of Statement S2.
> S3 <- c(4,3,2,5,3,3,4,5)  # Assessments of Statement S3.
> # Create dataframe.
> Assessments <- data.frame(Prod_no, Gender, Age, S1, S2, S3)</pre>
```

```
# Display the values in the complete data frame.
> Assessments
 Prod_no Gender Age S1 S2 S3
             F 37 4 3 4
2
             F 81 3 4 3
3
             M 57 2 1 2
4
             F 79 5 4 5
5
             M 17 NA 3 3
6
             M 18 3 NA 3
             F 67 5 1 4
8
             M 45 5 1 5
> Assessments$Prod_no # Display the product numbers, assessed.
[1] 1 1 2 1 2 1 2 2
> Assessments$Gender # Display the customer gender.
[1] FFMFMMFM
Levels: F M
> Assessments$Age  # Display the customers age.
[1] 37 81 57 79 17 18 67 45
> Assessments$S1
                 # Display customer replies for Statement 1.
[1] 4 3 2 5 NA 3 5 5
> Assessments$S2
                     # Display customer replies for Statement 2.
[1] 3 4 1 4 3 NA
                     1 1
> Assessments$S3
                     # Display customer replies for Statement 3.
[1] 4 3 2 5 3 3 4 5
>
```

Dataframes (7)

```
> # 2.6.2: Insert a new variable in a data frame -----
> #
> # Example: Extend the Assessments dataframe with one more question
> #
            S4 by inserting a new column S4 in the dataframe.
> #
> # S4: The product design is attractive.
> #
> S4 \leftarrow c(5, 3, 1, 4, 3, 4, 5, NA)
> ?transform() # Look into the manual
> Assessments_1 <- transform(Assessments, S4=S4)</pre>
> Assessments_1
 Prod_no Gender Age S1 S2 S3 S4
       1
             F 37 4 3 4 5
             F 81 3 4 3 3
          M 57 2 1 2 1
3
          F 79 5 4 5 4
4
5
          M 17 NA 3 3 3
6
         M 18 3 NA 3 4
           F 67 5 1 4 5
8
             M 45 5 1 5 NA
```

Dataframes (8)

```
> # ... alternative solution using cbind()
      (Bind a new column to the dataframe).
> Assessments_2 <- cbind(Assessments, S4)
> Assessments_2
 Prod_no Gender Age S1 S2 S3 S4
            F 37 4 3 4 5
            F 81 3 4 3 3
      2 M 57 2 1 2 1
            F 79 5 4 5 4
5
            M 17 NA 3 3 3
6
        M 18 3 NA 3 4
          F 67 5 1 4 5
8
            M 45 5 1 5 NA
> #
```

Dataframes (9)

```
> # 2.6.3: -------
> # Merge two sets of observations for the same variables.
> # Insert additional rows with observations in a data frame
> # and generate a new extended dataframe.
> # Notice: In this example the observations from one loca-
> #
           tion are just repeated at the other location.
> #
> # Create assessments for one location denoted A.
> Assessments_location_A <- Assessments
> # Create assessments for one other location B.
> Assessments_location_B <- Assessments
> # One dataframe with all observations.
> Assessments_all <- rbind(Assessments_location_A, +</pre>
                                  Assessments_location_B
> #
```

Dataframes (10)

> Assessments_all

	Prod_no	${\tt Gender}$	Age	S1	S2	S3	
1	1	F	37	4	3	4	
2	1	F	81	3	4	3	
3	2	M	57	2	1	2	
4	1	F	79	5	4	5	
5	2	M	17	NA	3	3	
6	1	M	18	3	NA	3	
7	2	F	67	5	1	4	
8	2	M	45	5	1	5	
9	1	F	37	4	3	4	
10	1	F	81	3	4	3	
11	2	M	57	2	1	2	
12	1	F	79	5	4	5	
13	2	M	17	NA	3	3	
14	1	M	18	3	NA	3	
15	2	F	67	5	1	4	
16	2	M	45	5	1	5	
`							

Dataframes (11)

```
> # 2.6.4: Identifying missing values in a data frame -----
> #
> # Example: Identify the observations (rows) in the data
> #
            frame with missing values.
> #
> ?is.na()
                                    # Manual for is.na()
> Missing <- is.na(Assessments_1[,4:7]) # Check 4 columns
> Missing
             S2 S3
                        S4
[1,] FALSE FALSE FALSE
[2,] FALSE FALSE FALSE FALSE
[3,] FALSE FALSE FALSE
[4,] FALSE FALSE FALSE FALSE
[5,] TRUE FALSE FALSE FALSE
[6,] FALSE TRUE FALSE FALSE
[7,] FALSE FALSE FALSE
[8,] FALSE FALSE TRUE
```

Dataframes (12)

```
> # 2.6.5:
> # Remove missing values from dataframe before analysis.
> #
> ?na.omit()
> # Exclude those data frame rows (observations) with NA.
> Assessments_2 <- na.omit(Assessments_1)</pre>
> Assessments 2
 Prod_no Gender Age S1 S2 S3 S4
         F 37 4 3 4 5
       1 F 81 3 4 3 3
3
      2 M 57 2 1 2 1
   1 F 79 5 4 5 4
      2 F 67 5 1 4 5
```

Dataframes (13)

```
> # 2.6.6: Grouping observations into age groups:
> #
           Teen, Young, MidAged, MidAgeP, Old
> # Teen (13-19), Young (20-39), MidAged (40-69),
       MidAgeP (70-79), Old (80-)
> #
> # Include the age categories in a new variable.
> #
> Assessments$AgeCat[Assessments$Age >= 13 &
       Assessments$Age <= 19] <- "Teen"
> Assessments$AgeCat[Assessments$Age >= 20 &
       Assessments$Age <= 39] <- "Young"
> Assessments$AgeCat[Assessments$Age >= 40 &
       Assessments$Age <= 69] <- "MidAge"
> Assessments$AgeCat[Assessments$Age >= 70 &
       Assessments$Age <= 79] <- "MidAgeP"
> Assessments$AgeCat[Assessments$Age >= 80] <- "Old"
```

Dataframes (14)

```
> Assessments
              # Display Assessments with age categories.
 Prod_no Gender Age S1 S2 S3 AgeCat
                37
                   4 3 4
                           Young
             F 81 3 4 3
                              01d
3
             M 57
                   2 1
                           MidAge
4
             F 79 5 4 5 MidAgeP
5
                17 NA
                      3 3
                             Teen
6
             M 18 3 NA 3
                             Teen
             F 67 5 1
                           MidAge
8
                45 5 1
                           MidAge
```

Dataframes (15)

```
> # 2.6.7:
> # Sorting observations in dataframe accd. to one variable
> #
> ?order() # Display the manual for the function order().
> # Reuse the data frame with product assessments and sort
      according to the customer age.
> # The products assessed by the customers.
> Prod no <- c(1.1.2.1.2.1.2.2)
> # F: Female and M: male.
> Gender <- c("F","F","M","F","M","M","F","M")</pre>
> Age <- c(37,81,57,79,17,18,67,45) # The customers ages
> S1 <- c(4,3,2,5,NA,3,5,5) # Assessments of Statement S1.
> S2 <- c(3,4,1,4,3,NA,1,1) # Assessments of Statement S2.
> S3 \leftarrow c(4,3,2,5,3,3,4,5) # Assessments of Statement S3.
> # Create the data frame.
> Assessments <- data.frame(Prod_no, Gender, Age, S1, S2, S3)
```

Dataframes (16)

> Assessments # Display the values in the total data frame.

```
      Prod_no
      Gender
      Age
      S1
      S2
      S3

      1
      1
      F
      37
      4
      3
      4
      3

      2
      1
      F
      81
      3
      4
      3

      3
      2
      M
      57
      2
      1
      2

      4
      1
      F
      79
      5
      4
      5

      5
      2
      M
      17
      NA
      3
      3

      6
      1
      M
      18
      3
      NA
      3

      7
      2
      F
      67
      5
      1
      4

      8
      2
      M
      45
      5
      1
      5
```

> Assessments_sorted <-

Assessments[order(Assessments\$Age),]

> Assessments_sorted

 Prod_no
 Gender
 Age
 S1
 S2
 S3

 5
 2
 M
 17
 NA
 3
 3

 6
 1
 M
 18
 3
 NA
 3

 1
 1
 F
 37
 4
 3
 4

 8
 2
 M
 45
 5
 1
 5

 3
 2
 M
 57
 2
 1
 2

 7
 2
 F
 67
 5
 1
 4

 4
 1
 F
 79
 5
 4
 5

 2
 1
 F
 81
 3
 4
 3

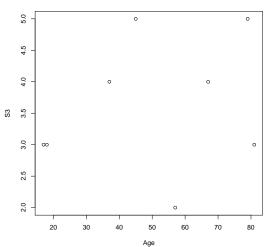
Dataframes (17)

Dataframes (18)

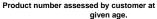
```
> par(.opar)
> with(Assessments, {
   Assessments
   pdf(file = "fig_2_Assessments.pdf")
   plot(Age,S3);title(main = "S3: Customer rec. of prod.")
  dev.off()
 par(.opar)
   pdf(file = "fig_2_Assessments_2.pdf")
   plot(Age,Prod_no); title(main = "Product number assessed
+
                      by customer at given age.")
+
   dev.off()
   par(.opar)
+ })
```

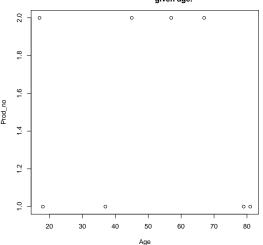
Dataframes (19)

S3: Customer recommendation of products.



Dataframes (20)





Dataframes (21)

```
> # 2.6.9: Delete (remove) rows or columns in dataframes.
> #
> x1 <- c("(r1, c1)", "(r2, c1)", "(r3, c1)", "(r4, c1)")
> x2 <- c("(r1, c2)", "(r2, c2)", "(r3, c2)", "(r4, c2)")
> x3 <- c("(r1, c3)", "(r2, c3)", "(r3, c3)", "(r4, c3)")
> xx <- data.frame(x1,x2,x3) # Form data frame.
> xx
       x1 x2
                         x3
1 (r1, c1) (r1, c2) (r1, c3)
2 (r2, c1) (r2, c2) (r2, c3)
3 (r3, c1) (r3, c2) (r3, c3)
4 (r4, c1) (r4, c2) (r4, c3)
>
```

Dataframes (22)

```
> # Remove row 2 from xx, generate xx1 and verify.
> xx1 <- xx[-2,] # Remove row 2.
> head(xx1)
           # Check that row 2 is removed.
       x1 x2 x3
1 (r1, c1) (r1, c2) (r1, c3)
3 (r3, c1) (r3, c2) (r3, c3)
4 (r4, c1) (r4, c2) (r4, c3)
> head(xx) # ... for comparison.
       x1
            x2 x3
1 (r1, c1) (r1, c2) (r1, c3)
2 (r2, c1) (r2, c2) (r2, c3)
3 (r3, c1) (r3, c2) (r3, c3)
4 (r4, c1) (r4, c2) (r4, c3)
```

Dataframes (23)

```
> # Remove col 2 from xx, generate xx2 and verify.
> xx2 <- xx[,-2] # Remove col. 2.
> head(xx2) # Check that col 2 is removed.
       x1
             x3
1 (r1, c1) (r1, c3)
2 (r2, c1) (r2, c3)
3 (r3, c1) (r3, c3)
4 (r4, c1) (r4, c3)
> head(xx) # ... for comparison.
       x1 x2
                         x.3
1 (r1, c1) (r1, c2) (r1, c3)
2 (r2, c1) (r2, c2) (r2, c3)
3 (r3, c1) (r3, c2) (r3, c3)
4 (r4, c1) (r4, c2) (r4, c3)
>
```

Dataframes (24)

```
> # Remove consequtive rows.
> xx3 < -xx[-2:-3,] # remove row 2 and 3.
> head(xx3) # Check that row 2 and 3 are deleted.
       x1 x2 x3
1 (r1, c1) (r1, c2) (r1, c3)
4 (r4, c1) (r4, c2) (r4, c3)
> head(xx) # ... for comparison.
       x1 x2
                       x3
1 (r1, c1) (r1, c2) (r1, c3)
2 (r2, c1) (r2, c2) (r2, c3)
3 (r3, c1) (r3, c2) (r3, c3)
4 (r4, c1) (r4, c2) (r4, c3)
```

Dataframes (25)

R function

```
> # 2.7.5: Define an R function returning cubes
          of a sequence of integers, here
> #
          cubes of 2, 3 and 4.
> #
> #
> arg1 <- 2; arg2 <- 4;
> newfunction <- function(arg1, arg2){  # Define function.
+ cubes <- (arg1:arg2)^3
+ return(cubes)
+ }
> result <- newfunction(arg1,arg2)</pre>
                                       # Apply function.
> result
                                        # Display result.
[1] 8 27 64
```

Probability Distributions, Sets, Combinations and Permutations (1)

```
> # 2.8: Example Probability Distributions, and
> #
       Sets, Combinations and Permutations.
> #
> # 2.8.1: Bionomial Distribution, mean and variance.
> #
> ?dbinom()
                # Check manual the Binomial Distribution
> #
> # Plot the binomial distribution function for n=1, p=03
> par(.opar)
> x1 <- dbinom(0:1,size=1,prob=0.3)
> barplot(x1,names.arg = c(0,1))
> title(main="Binominal distribution with n=1, p=0,3")
> par(.opar)
>
```

Probability Distributions, Sets, Combinations and Permutations (2)

```
> #
> x2 <- dbinom(0:2,size=2,prob=0.3)
> barplot(x2,names.arg = c(0:2))
> title(main="Binominal distribution with n=2, p=0,3")
> par(.opar)
> #
> x5 <- dbinom(0:5,size=5,prob=0.3)
> barplot(x5,names.arg = c(0:5))
> title(main="Binominal distribution with n=5, p=0,3")
> par(.opar)
> #
> x10 <- dbinom(0:10,size=10,prob=0.3)
> barplot(x10,names.arg = c(0:10))
> title(main="Binominal distribution with n=10, p=0,3")
> par(.opar)
```

Probability Distributions, Sets, Combinations and Permutations (3)

```
> x25 <- dbinom(0:25,size=25,prob=0.3)
> barplot(x25,names.arg = c(0:25))
> title(main="Binominal distribution with n=25, p=0,3")
> par(.opar)
> #
> x100 <- dbinom(0:100,size=100,prob=0.3)
> barplot(x100,names.arg = c(0:100))
> title(main="Binominal distribution with n=100, p=0,3")
> par(.opar)  # Restore default settings before continuing.
```

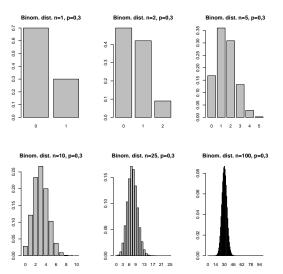
Probability Distributions, Sets, Combinations and Permutations (4)

```
> # Plot binomial distributions in a single plot with
> # 2 rows and 3 columns.
> par(mfrow=c(2,3)) # 2 rows and 3 columns.
> barplot(x1,names.arg = c(0,1))
> title(main="Binom. dist. n=1, p=0,3")
> barplot(x2,names.arg = c(0:2))
> title(main="Binom. dist. n=2, p=0,3")
> barplot(x5,names.arg = c(0:5))
> title(main="Binom. dist. n=5, p=0,3")
> barplot(x10,names.arg = c(0:10))
> title(main="Binom. dist. n=10, p=0,3")
> barplot(x25,names.arg = c(0:25))
> title(main="Binom. dist. n=25, p=0,3")
> barplot(x100,names.arg = c(0:100))
> title(main="Binom. dist. n=100, p=0,3")
> par(.opar)
```

Probability Distributions, Sets, Combinations and Permutations (5)

```
> # save single plot into pdf file in the working directory.
> # Format 2 rows, 3 columns.
> pdf(file = "fig_2_barplot_binom.pdf")
> par(mfrow=c(2,3))
                            # 2 rows and 3 columns.
> barplot(x1,names.arg = c(0,1))
> title(main="Binom. dist. n=1, p=0,3")
> barplot(x2,names.arg = c(0:2))
> title(main="Binom. dist. n=2, p=0,3")
> barplot(x5,names.arg = c(0:5))
> title(main="Binom. dist. n=5, p=0,3")
> barplot(x10,names.arg = c(0:10))
> title(main="Binom. dist. n=10, p=0,3")
> barplot(x25,names.arg = c(0:25))
> title(main="Binom. dist. n=25, p=0,3")
> barplot(x100,names.arg = c(0:100))
> title(main="Binom. dist. n=100, p=0,3")
> par(.opar)
> dev.off()
RStudioGD
```

Probability Distributions, Sets, Combinations and Permutations (6)



Probability Distributions, Sets, Combinations and Permutations (7)

```
> # 2.8.2 Examples of mean and median value of set of numbers.
> #
> x <- c(1:10,50);x
 [1] 1 2 3 4 5 6 7 8 9 10 50
> ?mean()
                                    # Check manual.
> x_mean <- mean(x); x_mean</pre>
[1] 9.545455
> ?median()
                                    # Check manual.
> x_median <- median(x); x_median # Why is the xmedian= 6?
[1] 6
> #
> # Examples of variance and standard deviation.
> #
> ?var()
                                  # Check manual.
> x_var <- var(x); x_var
[1] 188.2727
> ?sd()
                                  # Check manual.
> x_sd <- sd(x); x_sd
[1] 13.72125
>
```

Probability Distributions, Sets, Combinations and Permutations (8)

```
> # 2.8.3: Recap set operations,
> # sampling, union, intersect, difference,
> #
> ?union()  # Check manual for set operations.
> ?intersect()
> ?setdiff()
> ?setequal()
> ?sort()  # Check manual.
> ?sample()  # Check the random sampling function.
> #
```

Probability Distributions, Sets, Combinations and Permutations (9)

```
> # sample: Select randomly 9 values from the set 1:20.
> x <- c(sort(sample(1:20, 9)), NA); x
 [1] 2 4 6 8 14 16 17 19 20 NA
> # sample: Select randomly 7 values from the set 3:23.
> y <- c(sort(sample(3:23, 7)), NA); y
[1] 3 10 11 12 14 15 16 NA
> xy_union <- union(x, y); xy_union
 [1] 2 4 6 8 14 16 17 19 20 NA 3 10 11 12 15
> xy_intersect <- intersect(x, y); xy_intersect
[1] 14 16 NA
> xy_setdiff <- setdiff(x, y); xy_setdiff
[1] 2 4 6 8 17 19 20
> yx_setdiff <- setdiff(y, x); yx_setdiff
[1] 3 10 11 12 15
> xy_setequal <- setequal(x, y); xy_setequal</pre>
[1] FALSE
```

Probability Distributions, Sets, Combinations and Permutations (10)

```
> # 2.8.4: Combinations and Permutations.
> #
> # Generate all combinations of two letters from a,b,c,d.
> # Notice that when generating combinations: the order does not
> # matter. This means that the combinations a,b and b,a does only
> # count for one.
> ?combn() # Check manual
```

Probability Distributions, Sets, Combinations and Permutations (11)

```
> a1 <- combn(letters[1:4], 2); a1
   [,1] [,2] [,3] [,4] [,5] [,6]
[1.] "a" "a" "a" "b" "c"
[2,] "b" "c" "d" "c" "d" "d"
> # ... now try two digit combinations from the digits 0:9
> a2 <- combn(0:9, 2);a2
   [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] ...
[1,] 0 0 0 0 0 0 0 0 1 ...
[2,] 1 2 3 4 5 6 7 8 9 2...
   [,16] [,17] [,18] [,19] [,20] [,21] [,22] [,23] ...
[1.] 1 1 2
                   2 2 2 2 ...
[2,] 8 9 3 4 5 6 7 8...
   [,30] [,31] [,32] [,33] [,34] [,35] [,36] [,37] ...
[1,]
    3 4 4 4 4 4 5 5...
[2,]
    9 5 6 7 8 9 6 7...
   [,44] [,45]
[1,] 7
[2,] 9
```

Probability Distributions, Sets, Combinations and Permutations (12)

```
> a2_size <- dim(a2); a2_size</pre>
[1] 2 45
> a2_comb_count <- a2_size[2]; a2_comb_count</pre>
[1] 45
> #
> # Check the number of combinations of r out of n.
      comb_r_n = n!/(r!*(n-r)!) notice that 0!=1
> comb 2 10 <- factorial(10)/(factorial(2)*factorial(10-2))</pre>
> comb_2_10
Γ1  45
> #
> ?factorial()
                              # Check n! the factorial function.
```

Probability Distributions, Sets, Combinations and Permutations (13)

```
> # 2.8.5: Generate all permutations of the numbers 0:3.
> # Notice fort permulations: the the order does
> # matter. This means 0,1,2,3 and 1,0,2,3 are different
> # and each contribute with one to the total count of
> # the number of permutations.
> a3 <- permn(c(0:3));a3 # Generate a list with permutations.
[[1]]
[1] 0 1 2 3
[[2]]
[1] 0 1 3 2
[[3]]
[1] 0 3 1 2
[[4]]
[1] 3 0 1 2
```

Probability Distributions, Sets, Combinations and Permutations (14)

```
[[5]]
[1] 3 0 2 1
[[6]]
[1] 0 3 2 1
[[7]]
[1] 0 2 3 1
[[8]]
[1] 0 2 1 3
[[9]]
[1] 2 0 1 3
[[10]]
[1] 2 0 3 1
[[11]]
[1] 2 3 0 1
```

Probability Distributions, Sets, Combinations and Permutations (15)

```
[[12]]
[1] 3 2 0 1
[[13]]
[1] 3 2 1 0
[[14]]
[1] 2 3 1 0
[[15]]
[1] 2 1 3 0
[[16]]
[1] 2 1 0 3
[[17]]
[1] 1 2 0 3
[[18]]
[1] 1 2 3 0
```

Probability Distributions, Sets, Combinations and Permutations (16)

```
[[19]]
[1] 1 3 2 0
[[20]]
[1] 3 1 2 0
[[21]]
[1] 3 1 0 2
[[22]]
[1] 1 3 0 2
[[23]]
[1] 1 0 3 2
[[24]]
[1] 1 0 2 3
```

Probability Distributions, Sets, Combinations and Permutations (17)

```
> a3_class <- class(a3); a3_class
[1] "list"
> a3_length <- length(a3); a3_length
[1] 24
> #
> # Check number of permutations against the formula
> # for number of permulations of a set of distinct elements
> #
> perm_4 <- factorial(4);perm_4
[1] 24
> # Notice, as expected perm_4=4!=4*3*2*1=24
>
```

Probability Distributions, Sets, Combinations and Permutations (18)

```
> # 2.8.6: Central Limit Theorem (CLT) eg. with
              runif() uniform density seed.
> #
> #
> # The Central Limit Theorem:
> # The mean of a set of independent, identically distributed
> # (iid) random variables where mean and variance exist, will
> # approximate a normal distribution for increasinbg set size.
> #
> ?runif # Check manual for generator for random uniform distrib.
> #
> Nr <- 5000 # Repeat all experiments Nr times.
>
> x1_1 <- replicate(Nr, {</pre>
+ mm <- runif(1)
+ sum(mm)
+ })
>
```

Probability Distributions, Sets, Combinations and Permutations (19)

```
> x1_2 <- replicate(Nr, {</pre>
    mm <- runif(2)
+ sum(mm)
+ })
>
> x1_4 <- replicate(Nr, {
    mm <- runif(4)
+ sum(mm)
+ })
>
> x1_6 <- replicate(Nr, {</pre>
   mm <- runif(6)
+ sum(mm)
+ })
>
> x1_10 <- replicate(Nr, {
    mm <- runif(10)
  sum(mm)
+ })
```

Probability Distributions, Sets, Combinations and Permutations (20)

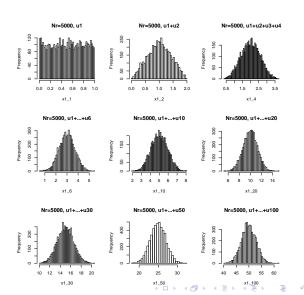
```
> x1_20 <- replicate(Nr, {
   mm <- runif(20)
+ sum(mm)
+ })
>
> x1_30 <- replicate(Nr, {
   mm <- runif(30)
+
   sum(mm)
+ })
>
> x1_50 <- replicate(Nr, {
   mm <- runif(50)
   sum(mm)
+
+ })
>
> x1_100 <- replicate(Nr, {
   mm <- runif(100)
   sum(mm)
+ })
>
```

Probability Distributions, Sets, Combinations and Permutations (21)

```
par(.opar)
            # Restore original parameters.
par(mfrow=c(3,3)) # Figure with 3 rows and 3 columns.
hist(x1_1, breaks=50, main="Nr=5000, u1")
hist(x1_2, breaks=50, main="Nr=5000, u1+u2")
hist(x1_4, breaks=50, main="Nr=5000, u1+u2+u3+u4")
hist(x1_6, breaks=50, main="Nr=5000, u1+...+u6")
hist(x1_10, breaks=50, main="Nr=5000, u1+...+u10")
hist(x1_20, breaks=50, main="Nr=5000, u1+...+u20")
hist(x1_30, breaks=50, main="Nr=5000, u1+...+u30")
hist(x1_50, breaks=50, main="Nr=5000, u1+...+u50")
hist(x1_100, breaks=50, main="Nr=5000, u1+...+u100")
par(.opar)
dev.off()
```

Probability Distributions, Sets, Combinations and Permutations (22)





Probability Distributions, Sets, Combinations and Permutations (23)

```
> # save plot into file in the working directory.
> pdf(file = "fig_2_CLT_unif.pdf")
> par(.opar)
                        # Restore original parameters.
> par(mfrow=c(3,3)) # 3 rows and 3 columns.
> hist(x1_1, breaks=50, main="Nr=5000, u1")
> hist(x1_2, breaks=50, main="Nr=5000, u1+u2")
> hist(x1_4, breaks=50, main="Nr=5000, u1+u2+u3+u4")
> hist(x1_6, breaks=50, main="Nr=5000, u1+...+u6")
> hist(x1_10, breaks=50, main="Nr=5000, u1+...+u10")
> hist(x1_20, breaks=50, main="Nr=5000, u1+...+u20")
> hist(x1_30, breaks=50, main="Nr=5000, u1+...+u30")
> hist(x1_50, breaks=50, main="Nr=5000, u1+...+u50")
> hist(x1_100, breaks=50, main="Nr=5000, u1+...+u100")
> par(.opar)
> dev.off()
null device
1 >
```

Probability Distributions, Sets, Combinations and Permutations (24)

```
> # 2.8.7: Central Limit Theorem (CLT) example with rbinom()
> #
           binomial density seed.
> #
> # The Central Limit Theorem:
    The mean of a set of independent, identically distributed
> #
> #
    (iid) random variables where mean and variance exist, will
> # approximate a normal distribution for increasing set size.
> #
> #
> ?rbinom() # Check manual for generator for random binomial
> #
                distributions.
> #
> Nr <- 5000  # Repeat all experiments Nr times.
              # Probability of sucess.
> p=0.5
> #
> x1_1 <- replicate(Nr, {</pre>
+ mm <- rbinom(1, size=1, prob=p)
+ sum(mm)
+ })
```

Probability Distributions, Sets, Combinations and Permutations (25)

```
> x1_2 <- replicate(Nr, {</pre>
    mm <- rbinom(1, size=2, prob=p)
+ sum(mm)
+ })
>
> x1_4 <- replicate(Nr, {
    mm <- rbinom(1, size=4, prob=p)
+ sum(mm)
+ })
>
> x1_6 <- replicate(Nr, {</pre>
+ mm <- rbinom(1, size=6, prob=p)
+ sum(mm)
+ })
>
> #
> x1_10 <- replicate(Nr, {
    mm <- rbinom(1, size=10, prob=p)
    sum(mm)
                                  4ロト 4部ト 4 恵ト 4 恵ト 恵 め90℃
+ })
```

Probability Distributions, Sets, Combinations and Permutations (26)

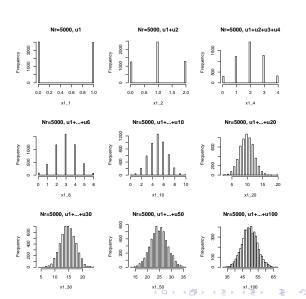
```
> x1_20 <- replicate(Nr, {
   mm <- rbinom(1, size=20, prob=p)
   sum(mm)
+ })
>
> x1_30 <- replicate(Nr, {
   mm <- rbinom(1, size=30, prob=p)
  sum(mm)
+ })
>
> x1_50 <- replicate(Nr, {
   mm <- rbinom(1, size=50, prob=p)
   sum (mm)
+ })
>
> x1_100 <- replicate(Nr, {
 mm <- rbinom(1, size=100, prob=p)
  sum(mm)
+ })
>
```

Probability Distributions, Sets, Combinations and Permutations (27)

```
> # save plot into file in the working directory.
> pdf(file = "fig_2_CLT_binom.pdf")
> par(opar)
               # Restore original parameters.
> par(mfrow=c(3,3)) # Figure with 3 rows and 3 columns.
> hist(x1_1, breaks=50, main="Nr=5000, u1")
> hist(x1_2, breaks=50, main="Nr=5000, u1+u2")
> hist(x1_4, breaks=50, main="Nr=5000, u1+u2+u3+u4")
> hist(x1_6, breaks=50, main="Nr=5000, u1+...+u6")
> hist(x1_10, breaks=50, main="Nr=5000, u1+...+u10")
> hist(x1_20, breaks=50, main="Nr=5000, u1+...+u20")
> hist(x1_30, breaks=50, main="Nr=5000, u1+...+u30")
> hist(x1_50, breaks=50, main="Nr=5000, u1+...+u50")
> hist(x1_100, breaks=50, main="Nr=5000, u1+...+u100")
> par(opar)
> dev.off()
null device
```

Probability Distributions, Sets, Combinations and Permutations (28)

+



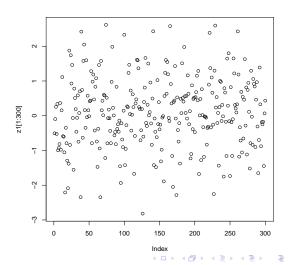
Probability Distributions, Sets, Combinations and Permutations (29)

```
> # 2.8.8: The standard normal probability density function,
> #
          mean=0, spread=1, variance=1.
> #
> ?rnorm() # Check manual for normal distribution.
> Ns=100000 # Number of samples.
> mean <- 0; sd <- 1
> # generate vector of std., normal distributed samples.
> z1 <- rnorm(Ns, mean, sd)
> (class(z1)) # Check which class attribute.
[1] "numeric"
> par(.opar)
> plot(z1[1:300]) # Plot the first 300 samples.
> par(.opar)
> pdf(file = "fig_2_Std_norm_z1().pdf")
> plot(z1[1:300])  # Plot the first samples to pdf file.
> dev.off()
RStudioGD
> par(.opar)
```

Probability Distributions, Sets, Combinations and Permutations (30)

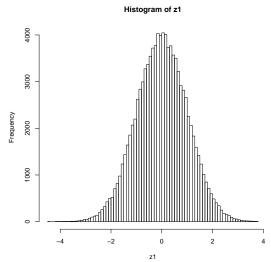
Probability Distributions, Sets, Combinations and Permutations (31)

+



Probability Distributions, Sets, Combinations and Permutations (32)

+



Probability Distributions, Sets, Combinations and Permutations (33)

> #

```
# Arguments for density/distribution function below.
> x < - seq(-3,3,0.1)
> # density
> d1 <- dnorm(x, mean = 0, sd = 1) # Generate density function.
> str(d1)
                # Check structure of d1.
num [1:61] 0.00443 0.00595 0.00792 0.01042 0.01358 ...
> # distribution
> p1 <- pnorm(x, mean = 0, sd = 1, lower.tail = TRUE, log.p = FALSE)
> #
> plot(x,d1, main="Std. normal density function, dnorm(), m=0, sd=1")
>dev.off()
RStudioGD
> plot(x,p1, main="Std. normal dist. function, pnorm(), m=0, sd=1")
>dev.off()
RStudioGD
```

Probability Distributions, Sets, Combinations and Permutations (33)

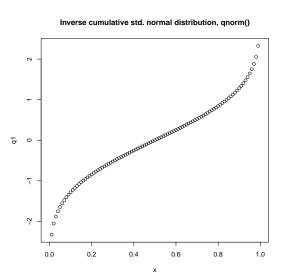
```
> # Plot to pdf files
> pdf(file = "fig_2_5_Std_Norm_Density.pdf")
> plot(x,d1, main="Std. normal density function, dnorm(), m=0, sd=1")
> dev.off()
RStudioGD
> par(.opar)
> pdf(file = "fig_2_6_Std_Norm_Distribution.pdf")
> plot(x,p1, main="Std. normal dist. function, pnorm(), m=0, sd=1")
> dev.off()
RStudioGD
> par(.opar)
```

Probability Distributions, Sets, Combinations and Permutations (34)

```
?qnorm()  # Quantile function.
x<-seq(0,1,0.01)
q1 <- qnorm(x, mean=0, sd=1)
plot(x,q1, main="Inverse cumulative std. normal dist., qnorm()")
par(.opar)
#
# Plot to pdf files
pdf(file = "fig_2_Inv_Std_Norm_Cumulative.pdf")
plot(x,q1, main="Inverse cumulative std. normal distrib., qnorm()")
dev.off()
par(.opar)</pre>
```

Probability Distributions, Sets, Combinations and Permutations (35)

+



Probability Distributions, Sets, Combinations and Permutations (36)

```
> # Values for q such that P(q>limit) for 0.5%, 1%, 2.5%, 5%
> #
                                              10%, 25%, 50%.
> # NOTICE: lower.tail = FALSE => the upper tail is used (one sided).
> #
> (q_0.005 <- qnorm(0.005, mean=0, sd=1, lower.tail=FALSE))</pre>
[1] 2.575829
> (q_0.01 <- qnorm(0.01, mean=0, sd=1,lower.tail=FALSE))</pre>
[1] 2.326348
> (q_0.025 <- qnorm(0.025, mean=0, sd=1, lower.tail=FALSE))</pre>
[1] 1.959964
> (q_0.05 <- qnorm(0.05, mean=0, sd=1,lower.tail=FALSE))</pre>
[1] 1.644854
> (q_0.1 <- qnorm(0.1, mean=0, sd=1, lower.tail=FALSE))</pre>
[1] 1.281552
> (q_0.25 <- qnorm(0.25, mean=0, sd=1,lower.tail=FALSE))</pre>
[1] 0.6744898
> (q_0.50 <- qnorm(0.5, mean=0, sd=1, lower.tail=FALSE))</pre>
[1] 0
```

Probability Distributions, Sets, Combinations and Permutations (37)

```
> #
> # The -1.96, 1.96 limits for 95% in two sided std. normal
> # distribution.
> # Cut off the left 2.5% and the right 2.5% of the
> # density function, thus giving the interval [-1.96, 1.96].
> # Use the qnorm()
> a <- 0.05
> (thres_005= qnorm(1-a/2))
[1] 1.959964
>
```

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