Diagnosing Strong Interactions via Signatures of Non-Markovian Dynamical Feedback on an Impurity Spin



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Background

We investigate the free induction decay of an impurity spin, embedded within a strongly correlated material, as the central process of a nuclear magnetic resonance.

Korringa law: relaxation rate of a nuclear spin embedded within a Fermi-gas is proportional to the temperature [1-2].

$$\frac{1}{T_1} \sim T$$

Based on Markovian approximation: The bath has no memory of prior interaction with impurity spin.

Power-law modification of Korringa relation is known for strong interactions within bath.

This neglects temporal correlations in the initial jointcoherent dynamics, which lead to an appreciable slip in relaxation amplitude at short times [3].

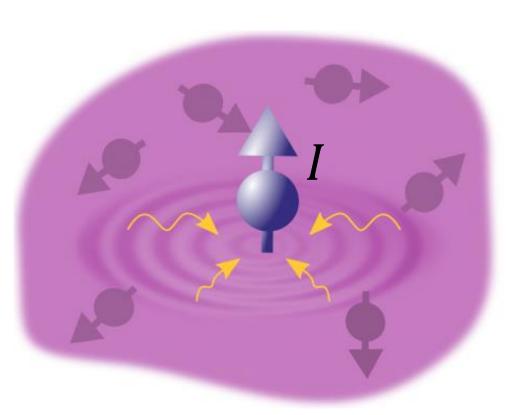
Is there a dynamical signature of strong interactions in the short term? What is the fate of the initial slip in amplitude?

Methodology

Impurity spin embedded within a bath

$$H = H_0 + H_I + H_{int}$$

$$H_{int} = AI \cdot S_0$$

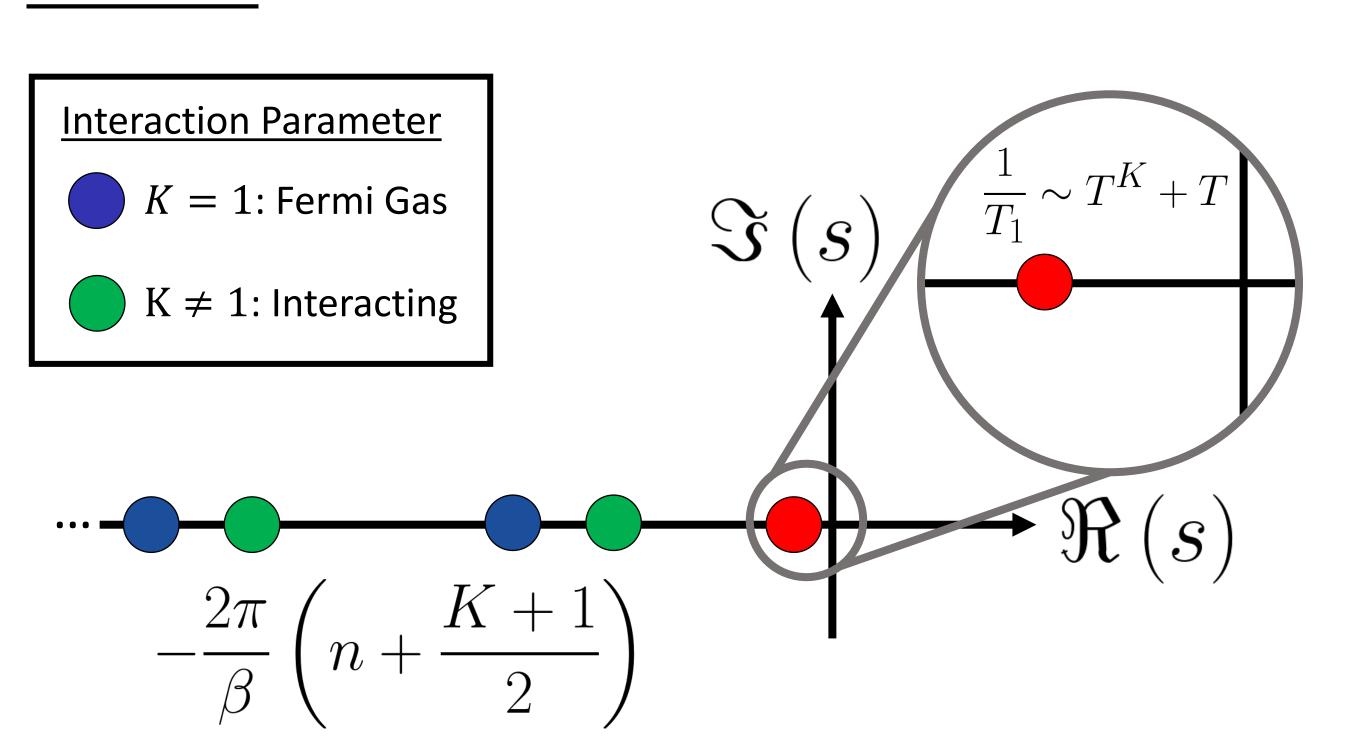


We use Luttinger liquid as model of a strongly correlated quantum wire $(v = \sigma, \rho)$

$$\mathcal{H}_{\nu} = u_{\nu} K_{\nu} (\nabla \theta_{\nu})^2 + \frac{u_{\nu}}{K_{\nu}} (\nabla \phi_{\nu})^2$$

We analyse decay and oscillation modes of impurity spin in Laplace space, dynamics recovered via contour integral.

$$\rho_I(s)$$
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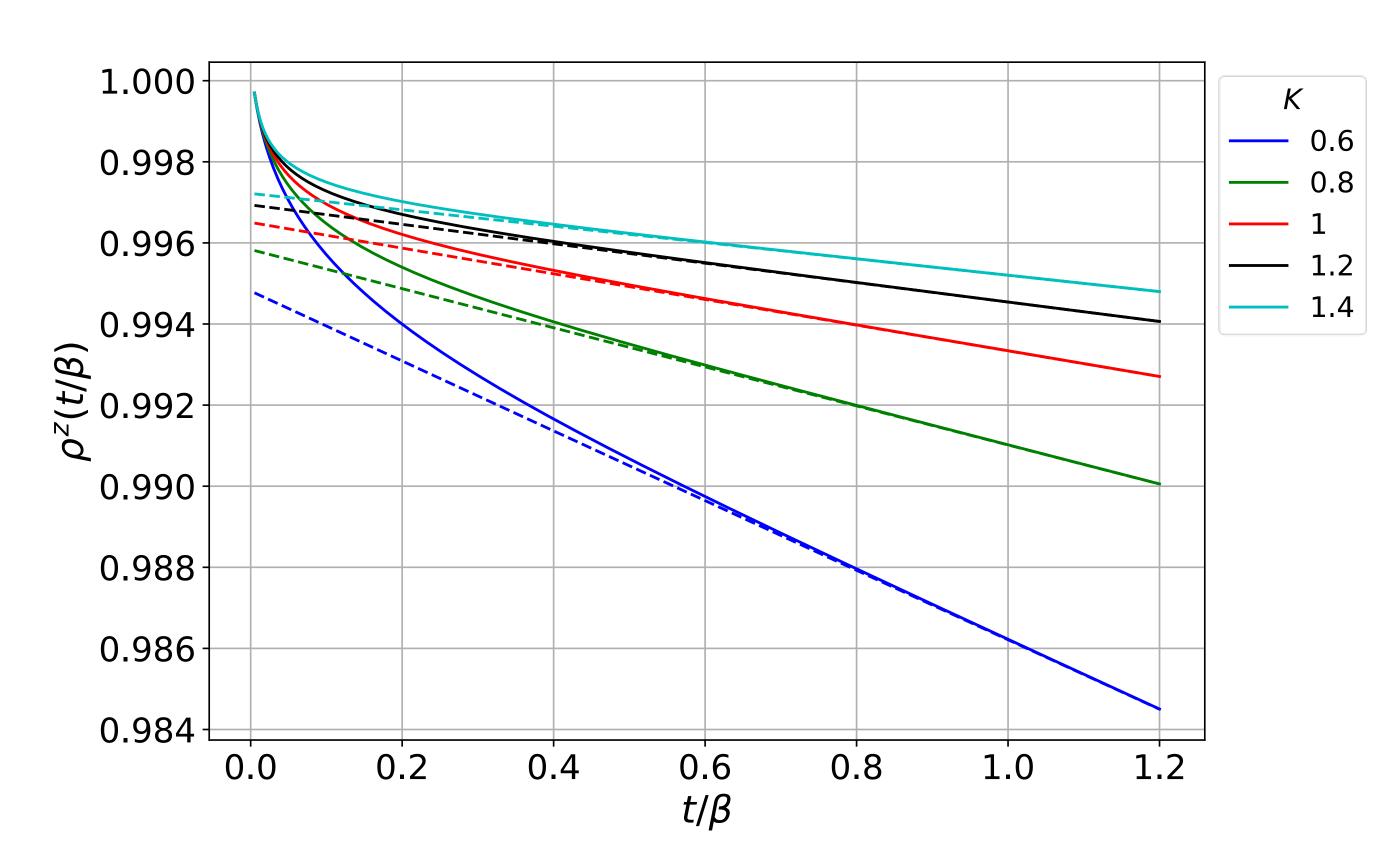


Findings

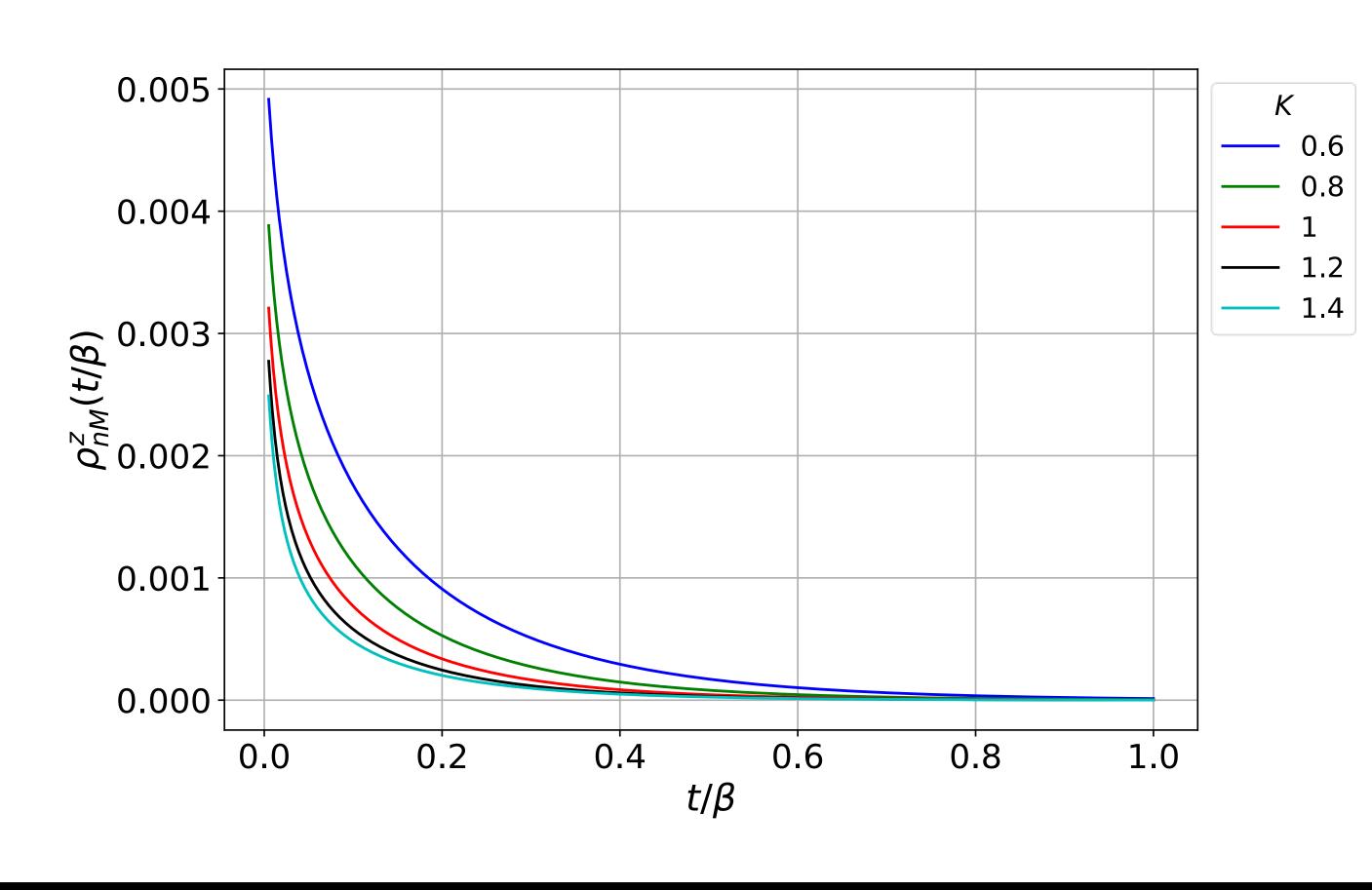
Full recovery of modified Korringa law through Markov mode.

Additional infinite sequence of non-Markov modes, from dynamical feedback of bath on spin. Retention of Fermi-gas modes.

Splitting of modes gives **classification** of of repulsive (K < 1) and attractive (K > 1) interactions.



Modification of initial slip amplitude and lifetime, a new dynamical signature of strong interactions.



Outlook

- Distil the difference in dynamical signatures between various correlated systems.
- Integrate this into a modern formulation of magnetic resonance forgoing standard high-temperature approximations, allowing for a robust description of strongly-correlated materials.

References

- [1]: Slichter, CP. (1990). Principles of Magnetic Resonance. Springer.
- [2]: Korringa, J. (1950). Physica, 16(7-8):601–610.
- [3]: Matern, S., Loss, D., Klinovaja, J., & Braunecker, B. (2019). Physical Review B, 100(13).

