

Methods description

Task – separate the free and flat models

step 01 - Bounding Box Ratio = Measuring Thickness

What is bounding box?

- A bounding box is the smallest 3D box that completely encloses a 3D object.
- Just like wrapping the 3D model tightly in a rectangular box.

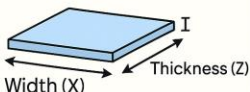
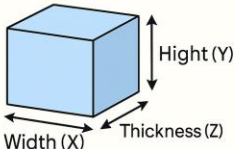
How does it work?

1. For each 3D model we should calculate its **bounding box**.
2. Means we measure **length, width, and height(thickness)** of the box.
3. Calculate the **ratio** of the **smallest dimension to the largest dimension**.

$$\text{ratio} = \text{largest side} / \text{smallest side}$$

4. If **ratio = small**, then it is **thin and likely flat**.
5. If **ratio = large**, then it is **more volumetric → free model**.

$$\text{ratio} = \text{smallest side} / \text{biggest side}$$

Flat Models	Free Models
 ratio < 0,1	 otherwise

Example:

Flat model: A 3D printed coaster might have dimensions

100×100×2 mm → ratio = $2/100 = 0.02$ → very flat.

Free model: A figurine of a cat might have dimensions

50×30×80 mm → ratio = $30/80 = 0.375$ → not flat.

```
if not isinstance(mesh, trimesh.Trimesh):
    continue # skip multi-part meshes

# --- Step 1: Bounding box ratio ---
extents = mesh.bounding_box.extents
min_dim = min(extents)
max_dim = max(extents)
ratio = min_dim / max_dim
```

extents → gives the **length, width, and height (Thickness)** of the bounding box.

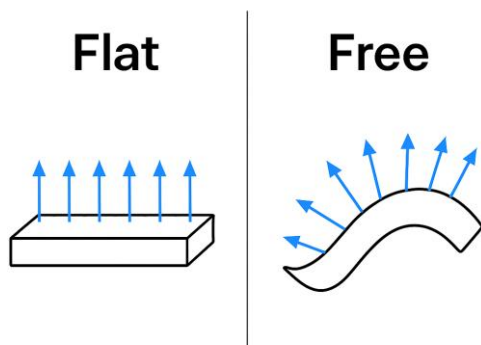
Example: If a model's box is 10×2×1 (length×width×height), extents = [10, 2, 1].

min_dim / max_dim → calculates the **ratio of the smallest dimension to the largest dimension**.

Step 02 - Surface Normal Alignment – Measuring Flatness of Surfaces

Every 3D model is made of **tiny flat triangles**.

What is a Normal?



- Every small triangle that makes up a 3D model has a **normal**.
- A **normal** is like a **tiny arrow sticking straight out** from the triangle.
- It shows **which direction that part of the surface is facing**

1. Average Normal

In this take the mean of all normals

$$\text{avg_normal} = \frac{1}{N} \sum_{i=1}^N \mathbf{n}_i$$

- \mathbf{n}_i = normal vector of each triangle.
- Normalize it (make it length = 1) → gives a **reference direction**. [A reference direction is a single, consistent direction used as a baseline to compare other directions.]

2. Dot Product

Measure similarity between vectors.

$$\mathbf{A} \cdot \mathbf{B} = |\mathbf{A}| |\mathbf{B}| \cos \theta$$

- θ = angle between vectors.
- If $\cos \theta \approx 1$ → vectors point almost the same direction.
- If $\cos \theta \approx 0$ → perpendicular.
- If $\cos \theta \approx -1$ → opposite.

3. Alignment Check

`aligned_ratio = np.mean(alignment > normal_threshold)`

`alignment > normal_threshold` → counts triangles whose normals are mostly aligned with the average normal.

`np.mean(...)` → calculates the fraction of aligned triangles.

Example:

- $\text{aligned_ratio} = 0.95 \rightarrow 95\%$ of faces point in the same direction \rightarrow flat surface.
- $\text{aligned_ratio} = 0.3 \rightarrow$ many faces point different ways \rightarrow free surface.

How it works?

1. Each triangle in the mesh has a **normal vector** perpendicular to its surface.
2. Calculate the **average normal** for the whole model.
 - Values close to **1** \rightarrow triangle is aligned with the average \rightarrow flat region.
 - Values close to **0** \rightarrow triangle is perpendicular \rightarrow curved surface.
4. Calculate the **aligned ratio**: the fraction of triangles aligned with the average normal.
5. If **most triangles are aligned** ($>80\%$), the model is considered **flat**.

Step 3: Combined

- **Bounding box ratio** \rightarrow finds thin models.
- **Surface normal alignment** \rightarrow finds flat surfaces.
- **Both together** \rightarrow robust classification: thin and flat models vs free-form models.