Frequency modulation with modulation depth $m_{\rm FM}$ [Hz] at a frequency f [Hz] has the form

$$y(t) = \exp\left\{i\omega t\right\} \exp\left\{i \int_0^t 2\pi \ m_{\rm FM} \ \Re\left\{e^{i2\pi f t'}\right\} \ dt'\right\}$$

where ω [radians/second] is the carrier frequency. We can simply do the integral and get:

 $y(t) = \exp\{i\omega t\} \exp\left\{i \frac{1}{f} m_{\text{FM}} \Re\left\{i e^{i2\pi f t}\right\}\right\}$

which is just phase modulation at frequency f [Hz] with modulation depth $m_{\rm PM}=\left(\frac{i}{f}\right)m_{\rm FM}$ [radians]:

$$\frac{d}{dt} \left(\frac{1}{f} m_{\text{FM}} \sin 2\pi f t \right) = 2\pi \ m_{FM} \cos 2\pi f t$$

The i signifies a phase shift of 90 degrees in the modulation (turning cos to sin).