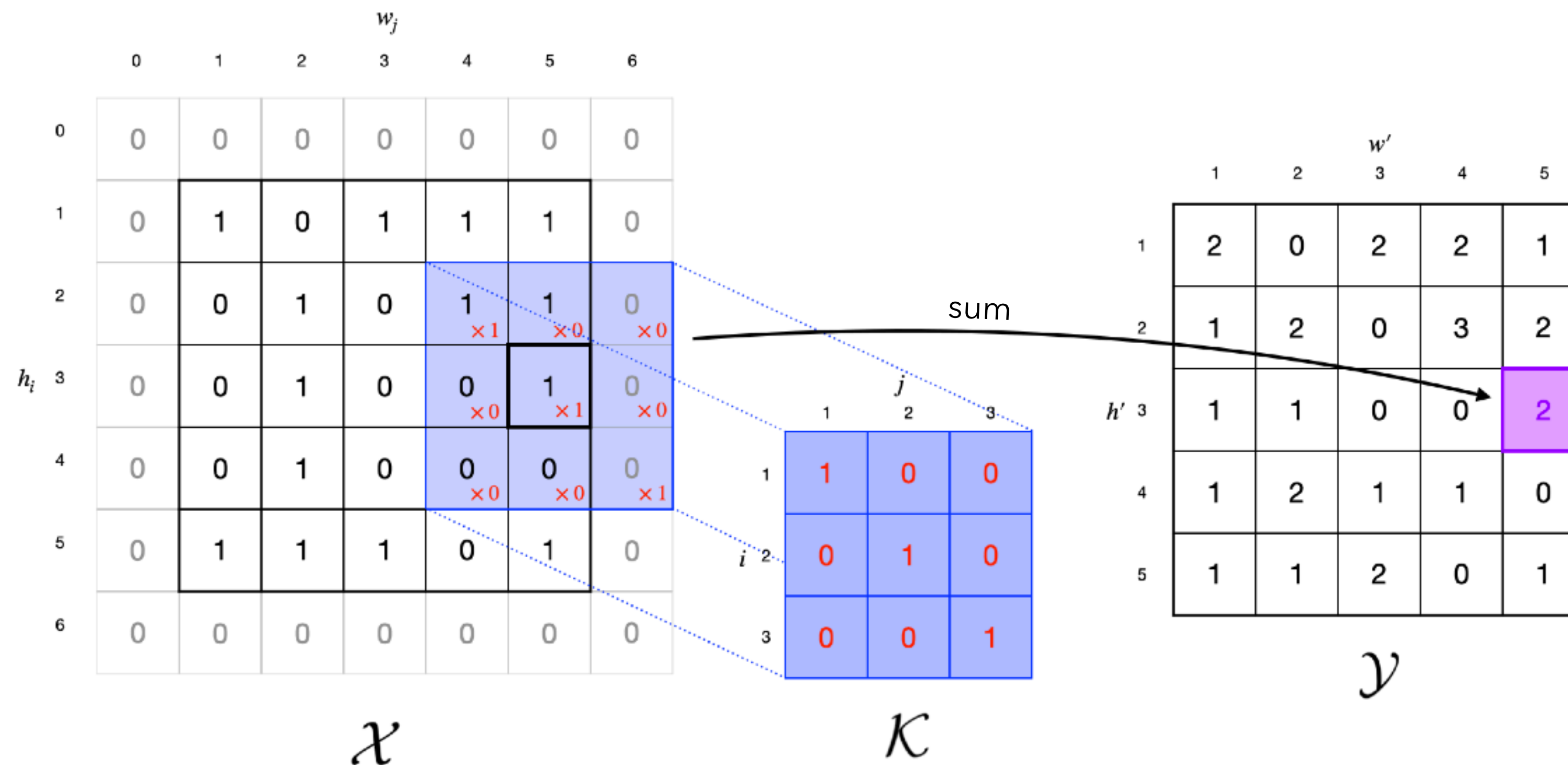


## Method 2

# The Convolution

$$\mathcal{Y}(f', h', w', t) = \sum_{i=1}^{D_F} \sum_{j=1}^{D_H} \sum_{l=1}^{D_W} \sum_{s=1}^S \mathcal{K}(i, j, l, s, t) \mathcal{X}(f_i, h_j, w_l, s)$$



Very simple example for images with only 1 input channel (black / white)

# Compressing the Convolution

$$\mathcal{K}(i, j, l, s, t) = \sum_{r_4=1}^{R_4} \sum_{r_5=1}^{R_5} \mathcal{C}(i, j, l, r_4, r_5) \mathbf{U}^{(4)}(s, r_4) \mathbf{U}^{(5)}(t, r_5)$$

Using this in the convolution:

$$\mathcal{Y}(f', h', w', t) = \sum_{i=1}^{D_F} \sum_{j=1}^{D_H} \sum_{l=1}^{D_W} \sum_{s=1}^S \sum_{r_4=1}^{R_4} \sum_{r_5=1}^{R_5} \mathcal{C}(i, j, l, r_4, r_5) \mathbf{U}^{(4)}(s, r_4) \mathbf{U}^{(5)}(t, r_5) \mathcal{X}(f_i, h_j, w_l, s)$$

Rearranging:

$$\mathcal{Y}(f', h', w', t) = \sum_{r_5=1}^{R_5} \mathbf{U}^{(5)}(t, r_5) \underbrace{\sum_{i=1}^{D_F} \sum_{j=1}^{D_H} \sum_{l=1}^{D_W} \sum_{r_4=1}^{R_4} \mathcal{C}(i, j, l, r_4, r_5) \underbrace{\sum_{s=1}^S \mathbf{U}^{(4)}(s, r_4) \mathcal{X}(f_i, h_j, w_l, s)}_{\mathcal{Q}(f_i, h_j, w_l, r_4)}}_{\mathcal{Q}'(f', h', w', r_5)}$$