Implementing incremental and parallel parsing

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In this talk

- Parsing using the CYK algorithm
- Implementing an incremental parser
- Writing dependently typed Haskell code
- ...and a lot of itemized lists

Motivation

- Parallelism everywhere
- Syntax highlighting sucks
- Parsing is costly

We can address all three!

Context-free grammars

- 4-tuple: $G = (V, \Sigma, P, S)$
  - V set of variables
  - Σ set of terminal symbols
  - P productions, recursive rules
  - S start symbol, entrypoint
- Language recognized denoted $L(G)$
- $L(G) = \{w \in \Sigma^* \mid S \overset{*}{\underset{G}{\Rightarrow}} w\}$

CYK algorithm

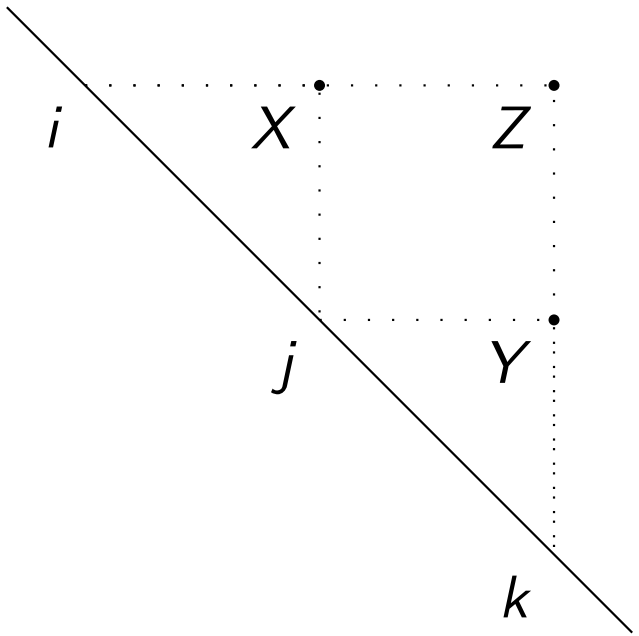
- Cocke, Younger and Kasami (60s)
- Recognition matrix for context-free languages
- Not very efficient, $O(n^3)$

How does it work?

$$W_{i,i+1} = \{A | A ::= S_t[i] \in P\}$$

$$W_{ij} = \sum_{k=i+1}^{j} W_{ik} \cdot W_{kj}$$

$$x \cdot y = \{A | A_0 \in x, A_1 \in y, A ::= A_0 A_1 \in P\}$$



Valiant's algorithm

- Improvement of the CYK algorithm
- Context-free recognition is the same as transitive closure...
- ...which is the same as matrix multiplication...
- ...which in turn we only need to do with boolean matrices.

Matrix multiplication can be done faster than $O(n^3)$ (but not that much faster)

Recent improvement

- Bernardy and Claessen (2013)
- For a lot of input, large parts of the matrices will be empty, in fact so empty that we can optimise based on that.
- New time complexity: $O(log^3\ n)$
- Took care of linear behaviour by using an oracle

Using a lexer

- MSc thesis by Hansson and Hugo
- Input source code as a FingerTree
- Lexing by measuring

Finger trees

- Balanced trees
- Notion of *measuring*

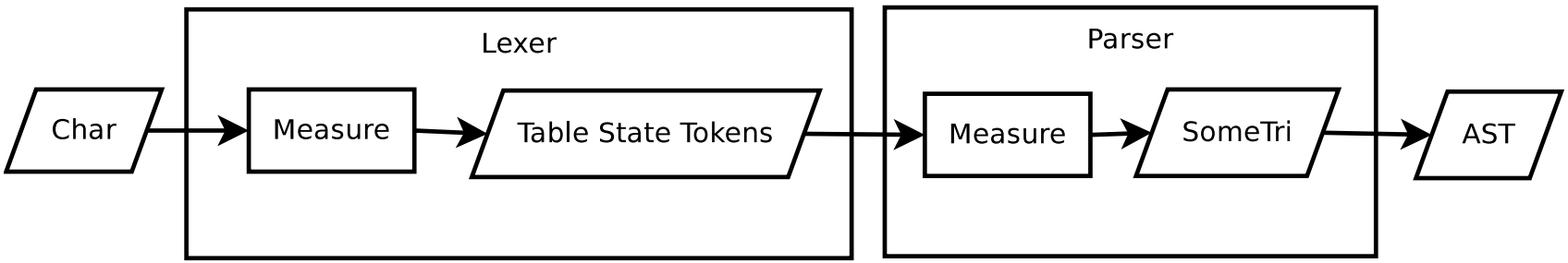
```
class Monoid v ⇒ Measured v a | a → v where
    measure :: a → v
```

Measures are cached at each node in the tree. That, plus the tree structure makes the FingerTree suitable for an incremental approach.

Idea of parsing

- Use the same approach as the lexer!
- Lexer measure Char $\rightarrow$ FingerTree of tokens
- Have the parser measure tokens $\rightarrow$ CYK entries

Pipeline of measures



This is done for every `Char`. Results are combined using `mappend`.

Implementation of matrices

```
data Shape = Bin Shape Shape | Leaf

data Mat :: Shape → Shape → ∗ → ∗ where
  Quad :: !(Mat x1 y1 a) → !(Mat x2 y1 a) →
          !(Mat x1 y2 a) → !(Mat x2 y2 a) →
          Mat (Bin x1 x2) (Bin y1 y2) a
  Zero :: Mat x y a
  One :: !a → Mat Leaf Leaf a
  Row :: Mat x1 Leaf a → Mat x2 Leaf a → Mat (Bin x1 x2) Leaf
  Col :: Mat Leaf y1 a → Mat Leaf y2 a → Mat Leaf (Bin y1 y2)

data SomeTri a where
  T :: Shape' s → Pair (Mat s s a) → SomeTri a
```