A positivity preservation property of Runge-Kutta based convolution quadratures

Lehel Banjai a and Christian Lubich b

 a Heriot-Watt University, Edinburgh, UK b University of Tübingen, Germany

Recently the two authors together with F.-J. Sayas have used a positivity preservation property of low order convolution quadratures to analyse a fully discrete FEM/BEM coupling in the time domain. Here we extend this positivity property to A-stable Runge-Kutta based methods, hence allowing for higher order approximations. The proof requires an adaptation of M. Crouzeix's proof of von Neumann's theorem as given in E. Hairer, G. Wanner, Solving Ordinary Differential Equations, II.

As an application of the result we consider a boundary integral formulation of a scattering problem with a non-linear impedance boundary condition and its Radau IIA based time-discretization.