FREUD AND SUB-RANGE FREUD POLYNOMIALS AND THEIR ZEROS

Walter Gautschi

Abstract

Freud and sub-range Freud polynomials are orthogonal with respect to the weight function $w(t) = |t|^{\mu} \exp(-|t|^{\nu})$, $\mu > -1$, $\nu > 0$, supported on the whole real line $\mathbb R$ resp. on strict subintervals thereof. The zeros of these polynomials are studied here as functions of ν and shown, analytically and empirically by computation, to collectively increase or decrease on appropriate intervals of the variable ν .