MATH 508 Challenge problem #7

Turn in no later than Apr. 12 for credit

First, prove that if Γ is a simple closed curve enclosing domain D, then

$$\int_{\Gamma} \overline{z} \, dz = 2i (\text{area of } D).$$

Then find a way to generalize this result to the case when Γ is not closed; i.e. it runs from z_a to z_b .