

ViolationLS Constraint Based Local Search in CP-SAT

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Constraint-Based Local Search

Constraint Based: inspired by Constraint Programming

Many problems have similar combinatorial structures, don't make users re-implement them!





Constraint-Based Local Search

Local Search: makes local changes to an assignment

Constraints define "how violated" they are in an assignment, solvers first minimize total violation, then the objective.

Constraints typically also define a neighborhood.*



Violation Functions

$$V\left(\sum cx \leq K
ight) = \min\left(\sum cx - K, 0
ight)$$





Feasibility Jump

Feasibility Jump = Single-var moves + Guided Local Search





Feasibility Jump

Feasibility Jump changes one variable at a time

The variable "jumps" to the value that minimizes the **weighted sum** of constraint violations for that variable.

If no moves reduce weighted violation, increase the weight of violated constraints

If feasible, **emit the new solution** and replace objective constraint: **objectiveVar < currentObjectiveValue**



Feasibility Jump

Computing the "Jump Value" is cheap if we assume violation is convex **when changing a single variable**:

$$O\left(\ln(x_{max}-x_{min})\right)$$



Arc vars have domain {0,1}; 1 inflow at A; 1 outflow at E $\begin{array}{c|c}
\hline
A \\
\hline
C \\
\hline
\end{array}$

Weight

Violation

А	В	С	D	Е
1	1	1	1	1
1	0	0	0	1

Score

AB	AC	BD	CD	DE
0	0	-2	-2	0
0	0	0	0	0



Arc vars have domain {0,1}; 1 inflow at A; 1 outflow at E $\begin{array}{c|c} & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & \\ & & & \\ & &$

Weight

Violation

Α	В	С	D	E
2	1	1	1	2
1	0	0	0	1

Score

AB	AC	BD	CD	DE
1	1	-2	-2	1
0	0	0	0	0



Arc vars have domain {0,1}; 1 inflow at A; 1 outflow at E $\begin{array}{c|c} & & & \\ & & & \\ & & & \\ \hline \end{array}$

Weight

Violation

Α	В	С	D	E
2	1	1	1	2
0	1	0	0	1

Score

AB	AC	BD	CD	DE
0	-3	0	0	1
1	0	0	0	0



Arc vars have domain {0,1}; 1 inflow at A; 1 outflow at E Weight

Violation

Α	В	С	D	E
2	1	1	1	2
0	1	0	1	0

Score

AB	AC	BD	CD	DE
0	-3	2	0	0
1	0	0	0	1



Arc vars have domain {0,1}; 1 inflow at A; 1 outflow at E $\begin{array}{c|c} & & & \\ \hline A & & \\ \hline \end{array}$

Weight

Violation

A	В	С	D	E
2	1	1	1	2
0	0	0	0	0

Score

AB	AC	BD	CD	DE
0	-1	0	-1	0
1	0	1	0	1





Multi-Variable Moves

Usually local search changes more than 1 variable at a time!

We'd like a way to find chains of moves automatically, while using the same operations as Feasibility Jump

But I'm lazy: I don't want to write specialized neighbourhoods





Local Search as Planning

Idea: Treat the search for a move as a domain-independent planning problem.

Note: this is just an inspiration, we don't really solve a planning problem!





"Novelty" based search: only expands "novel" states

More structured than random exploration

Polynomial work per search





What makes a state novel?

Some atomic fact is true in the state that has never been true in any prior one





What makes an assignment novel?

A constraint is satisfied that has not been satisfied before?









What makes an assignment novel?

A constraint is violated that has not been violated before

Or (non-discounted) weighted violation is less than any prior assignment



Novelty Jump

How to make "jump if weighted violation decreases" find novel states:

- Discount the weight of satisfied constraints (multiply by epsilon)
- Reset the weight when a constraint becomes violated
- Keep a stack of var changes & backtrack when we have no good moves*
- Clear the stack when sum of (non discounted) scores are positive





Novelty Jump: Why backtrack?

Discounted score can be positive, but real score negative (which is the point)!

If we commit such a move we may not find our way back.

This would be an interesting metaheuristic, but not a compound move.

This interferes with GLS rather than complements it



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Novelty Example

Arc vars have domain {0,1}; 1 inflow at A; 1 outflow at E

Weight

Violation

Α	В	С	D	E
1	ε	ε	ε	1
1	0	0	0	1

Score

AB	AC	BD	CD	DE
1-ε	1-ε	-2ε	-2ε	1-ε
0	0	0	0	0



Novelty Example

Arc vars have domain {0,1}; 1 inflow at A; 1 outflow at E $\begin{array}{c|c} & & & \\ \hline A & & \\ \hline \end{array}$

Weight

Violation

A	В	С	D	E
1	1	3	1	1
0	1	0	0	1

Score

AB	AC	BD	CD	DE
0	-1-ε	1-ε	-2ε	1-ε
1	0	0	0	0



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Novelty Example

Arc vars have domain {0,1}; 1 inflow at A; 1 outflow at E $\begin{array}{c|c} & & & \\ & & & \\ \hline & & & \\ \hline \end{array}$

Weight

Violation

Α	В	С	D	E
1	1	3	1	1
0	0	0	1	1

Score

AB	AC	BD	CD	DE
0	-1-ε	0	1-ε	2
1	0	1	0	0



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Novelty Example

Arc vars have domain {0,1}; 1 inflow at A; 1 outflow at E $\begin{array}{c|c}
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A \\
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\hline
\end{array}$

Weight

Violation

Α	В	С	D	E
1	1	ε	1	1
0	0	0	0	0

Score

AB	AC	BD	CD	DE
0	-1-ε	-2	-1-ε	0
1	0	1	0	1



Is Novelty Jump always better?

No! But you don't have to pick!

ViolationLS:

- If there is a new better solution from some other worker:
 - Set incumbent to the new solution
 - Randomly pick Novelty Jump or Feasibility Jump
- Do some iterations
- Repeat



Results

Solver	ViolationLS	Feasibility Jump	Yuck	fzn-oscar-cbls
ViolationLS	-	650.6	652.28	734.64
Feasibility Jump	182.00	-	523.84	617.24
Yuck	209.52	268.96	-	435.72
fzn-oscar-cbls	101.96	135.36	147.6	-

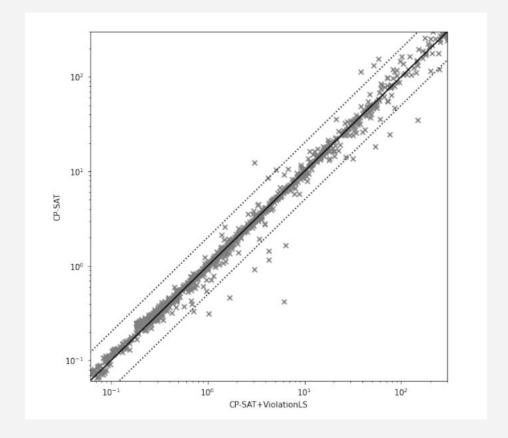
#instances (of 1216) where ViolationLS beats Yuck

#instances where column solver beats row (1216 mzn challenge instances)
Using 8 cores, except fzn-oscar-cbls which is single-threaded
Averaged over 5 seeds per solver



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Results



Solve time of CP-SAT with and without ViolationLS 60.5% faster; 39.5% slower



Results

CP- SAT +	ViolationLS	Feasibility Jump	Baseline
ViolationLS	-	609.20	659.04
Feasibility Jump	588.36	-	651.80
Baseline	538.32	545.48	-

#instances where column solver beats row (1216 mzn challenge instances)
Using 8 cores





Conclusions

- CBLS makes a powerful primal heuristic for a state-of-the-art CP solver
- Efficiently implemented, generic LS moves can beat constraint-specific ones
- Novelty is a good exploration criterion that integrates well with GLS

