

**Answer all question on the back of this page (or on a separate sheet). Please be as neat as you can. Show all work, including units. Circle your final answer clearly.**

### LAUNCH LOCATION AND FREE $\Delta V$

In the first homework we calculated that you need a  $\Delta V$  of about 8 km/s to orbit the Earth. But that calculation ignored the fact that the Earth rotates (it ignored a lot of other thing like air resistance as well). The rotation of the Earth an can be a source of free  $\Delta V$  if you launch in the correct direction (eastward). How much  $\Delta V$  you get depends on your location on the Earth.

More specifically, it depends on your latitude. The best place to get free  $\Delta V$  is at the equator.

To calculated how fast the Earth is rotating at the equator you need two pieces of data: the total distance around the equator, and the time it takes the Earth rotate  $360^\circ$ .

The distance around the equator is  $2\pi R_E$ , where  $R_E$  is the radius of the Earth ( $R_E = 6,371.14$  km).

The time it takes the Earth to rotate  $360^\circ$  is 23.934472 hours

**1** (5 pts) Calculate the distance around the Earth's equator.

**2** (5 pts) Calculate the time it takes the Earth to rotate in seconds.

**3** (10 pts) Calculate the speed of an object on the Earth's equator. This is the free  $\Delta V$  that the Earth's rotation gives you.

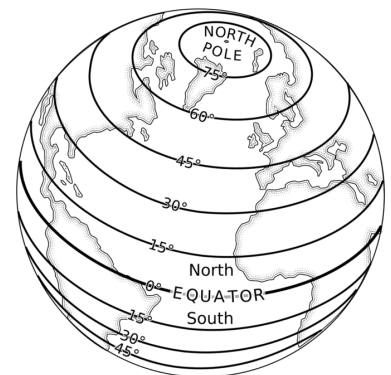
The speed of an object at any latitude can be found by:

$$V_{eq} \cos(\theta)$$

where  $V_{eq}$  is your speed at the equator, and  $\theta$  is your latitude.

**4** (5 pts) The main US launch site is *Cape Canaveral* located at a latitude of  $\theta = 28.5^\circ$ . Calculate the free  $\Delta V$  at Cape Canaveral.

**5** (5 pts) The Russians main launch site is the *Baikonur Cosmodrome* located at a latitude of  $\theta = 45.965^\circ$ . Calculate the free  $\Delta V$  at the Baikonur Cosmodrome.



Make sure your calculator is set to degree mode. If you are using Google be sure to enter `cos(28.5 deg)`.

ASTRONOMY 105

HOMEWORK #3

NAME: \_\_\_\_\_