

# Discrete Codes from Continuous Substrates: A Minimal Channel-Capacity Simulation

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## Abstract

We present a minimal simulation demonstrating that discrete symbolic codes emerge spontaneously when continuous data passes through a noisy bandwidth-limited channel. Using a simple autoencoder trained on a 1-D ring manifold embedded in 512-D, we show that neither the dimensional bottleneck nor channel noise alone produces discretization—both ingredients are required for the qualitative transition from continuous to discrete representation. We quantify this transition using the Adjusted Rand Index (semantic preservation) and participation ratio (effective dimensionality). The simulation provides a concrete, reproducible demonstration of how discrete codes can emerge from continuous substrates through information-theoretic constraints, with potential relevance to categorical perception, neural coding, and the emergence of digital information in biological systems.

## 1 Introduction

How do discrete symbols emerge from continuous physical substrates? This question spans cognitive science (how do brains form discrete concepts?), linguistics (how did discrete language emerge?), and origin-of-life research (how did digital genetic information arise from analog chemistry?).

We approach this question computationally, constructing a minimal simulation that exhibits spontaneous discretization. The goal is not to model any specific biological system, but to identify the *sufficient conditions* for code formation—the minimal ingredients that, when combined, produce discrete representations.

Our central finding is that two ingredients are required:

1. A **dimensional bottleneck**: Information must pass through a channel with fewer degrees of freedom than the input
2. **Channel noise**: The transmission is corrupted by stochastic perturbations

Neither alone produces discretization. The bottleneck without noise preserves continuous structure. Noise without a bottleneck leaves room for continuous codes. But together, they force the system into a regime where only discrete codes can reliably transmit information.

This paper describes what we simulated, how we simulated it, and what it might mean.

Table 1: Mapping between simulation components and physics concepts.

Simulation	Physics Analogue	Mathematical Proxy
Input data	Continuous manifold	$S^1$ with $O(2)$ symmetry
Bottleneck ( $k$ )	Degrees of freedom	Embedding dimension
Noise ( $\sigma$ )	Thermal fluctuations	Temperature-like parameter
Loss function	Effective potential	Lyapunov-like objective
Code clustering	Symmetry reduction	$O(2) \rightarrow C_n$

## 2 What We Simulated

### 2.1 The Input: A Continuous Manifold

We need a continuous input space with clear topology. We chose a ring ( $S^1$ )—a 1-dimensional closed manifold—embedded in high-dimensional space:

```
# Generate 2000 points uniformly on a circle
theta = random(0, 2*pi, n_samples=2000)
ring_2d = [cos(theta), sin(theta)]

# Embed in 512 dimensions via random projection
projection = random_orthonormal(2, 512)
data_512d = ring_2d @ projection + noise(0.05)
```

The embedding noise (0.05) is small relative to the ring radius, so the intrinsic  $S^1$  topology is preserved. The input is *continuous*—points can take any value along the ring. There are no discrete categories in the data itself.

For *evaluation only*, we partition the ring into 6 equal sectors and ask: do the learned codes preserve this structure? We treat these sectors as “semantic classes” and measure the Adjusted Rand Index (ARI) between k-means clusters of learned codes and ground-truth sectors. (The choice of  $n = 6$  is for convenience; results are qualitatively similar for 4–8 sectors.)

### 2.2 The Channel: Encoder-Noise-Decoder

The core architecture is a sender-channel-receiver system:

```
# Encoder: compress 512D to k dimensions
code = encoder(input) # code is k-dimensional

# Channel: add Gaussian noise
noisy_code = code + noise(sigma)

# Decoder: reconstruct 512D from noisy code
output = decoder(noisy_code)

# Training objective: minimize reconstruction error
loss = mean_squared_error(input, output)
```

The encoder and decoder are neural networks (3-layer MLPs with ReLU activations). The channel dimension  $k$  and noise level  $\sigma$  are the experimental variables.

The key insight is that the encoder must learn codes that are *robust to noise*. If two nearby codes get confused after noise corruption, the decoder cannot distinguish them, and reconstruction suffers. The only solution is to space codes apart—creating discrete clusters with “safety margins.”

### 2.3 The Metrics

We measure two quantities:

**Semantic Preservation (ARI):** We cluster learned codes via k-means ( $n = 6$ ) and compute the Adjusted Rand Index against the 6-sector ground truth. ARI = 1 means perfect cluster-label agreement; ARI = 0 means agreement no better than chance.

**Effective Dimensionality (Participation Ratio):**

$$PR = \frac{(\sum_i \lambda_i)^2}{\sum_i \lambda_i^2} \quad (1)$$

where  $\lambda_i$  are eigenvalues of the code covariance matrix. PR = 1 for data collapsed to a line; PR  $\approx d$  for variance spread evenly across  $d$  orthogonal directions. This serves as a coarse measure of effective embedding dimension.

## 3 The Control Experiment

Our main result comes from a simple control experiment. We ask: what *causes* the discretization?

Table 2: Control experiment: both bottleneck AND noise required for clustering.

Condition	Bottleneck ( $k$ )	Noise ( $\sigma$ )	Result
Bottleneck only	2	0	Continuous ring
Noise only	32	0.5	Continuous ring
<b>Both</b>	<b>2</b>	<b>0.5</b>	<b>Discrete clusters</b>

Figure 1 shows this visually. The top row tells a linear story:

1. **The Input:** A perfect continuous ring (color = angular position  $\theta$ )
2. **Bottleneck Only:** Compressed to  $k = 2$  with no noise—ring topology preserved
3. **Bottleneck + Noise:** Compressed to  $k = 2$  with  $\sigma = 0.5$ —discrete clusters emerge

The bottom row shows that increasing  $k$  (with noise held constant) restores continuous representation. At  $k = 32$ , there is enough “room” in the channel for the ring to survive despite noise.

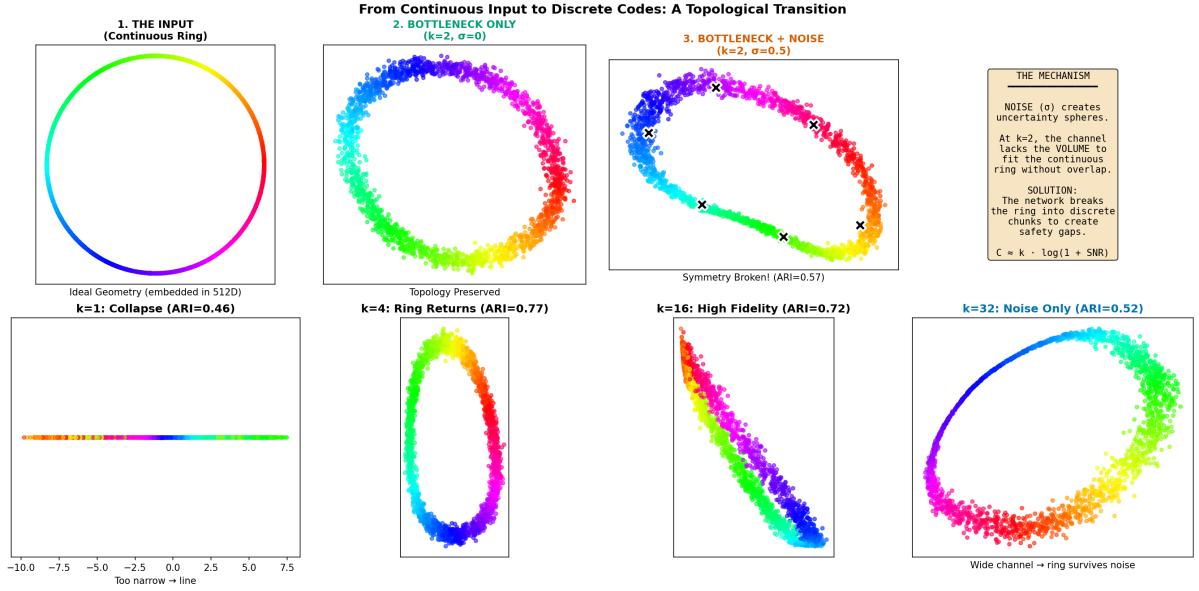


Figure 1: **Visual proof of the two-ingredient hypothesis.** Top row: (1) Continuous input ring, (2) bottleneck alone preserves topology, (3) bottleneck + noise  $\rightarrow$  discrete clusters. Black X's mark learned centroids (k-means). Bottom row: As channel dimension  $k$  increases, ring structure returns despite noise ( $\sigma = 0.5$  throughout).

## 4 The Transition

Figure 2 shows how semantic preservation varies with channel dimension  $k$ . There are three regimes:

1.  $k = 1$ : **Topological collapse.** The ring is forced onto a line. Adjacent points on the ring may map to distant points on the line. The  $S^1$  topology is destroyed.
2.  $k \approx k_c$ : **Critical capacity.** Discrete codes emerge that optimally preserve semantic structure. The system “discovers” that a small number of well-separated clusters is the best way to use the limited channel.
3.  $k \gg k_c$ : **Continuous preservation.** With sufficient bandwidth, the ring can be transmitted continuously. Noise is present but doesn’t force discretization.

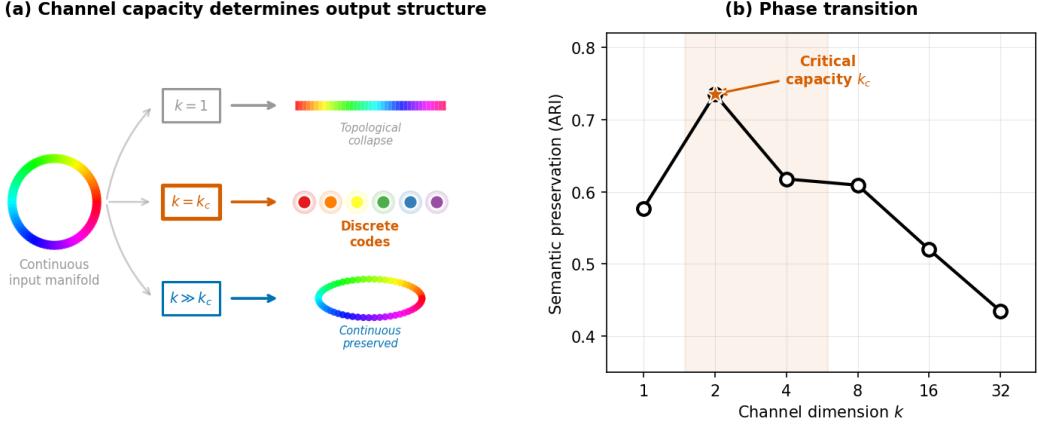


Figure 2: **Qualitative transition in code structure.** (a) Schematic showing three regimes. (b) Semantic preservation (ARI vs. 6-sector ground truth) as function of channel dimension  $k$ . Peak near  $k_c \approx 2$ . Noise  $\sigma = 0.5$  throughout.

In the learned representation, there is a clear topology-changing transition: for  $k = 1$  the ring maps to a line, at intermediate  $k$  to well-separated clusters, and for large  $k$  back to a continuous ring-like manifold. In the language of symmetry, this corresponds to a reduction from the continuous  $O(2)$  rotational symmetry of the input ring to a discrete  $C_n$  point-group symmetry in code space.

We can define an order parameter for this transition as the silhouette score of the code distribution, or equivalently the ARI with respect to equal-sector partitions. This order parameter is near zero for  $k = 1$  (collapsed) and  $k \gg k_c$  (continuous), and peaks at intermediate  $k$  where discrete clustering is strongest.

*Note:* We use “transition” rather than “phase transition” advisedly. In a strict thermodynamic sense, phase transitions occur in the infinite-size limit where singularities appear in the free energy. Our finite neural network exhibits a sharp crossover or bifurcation, not a true thermodynamic phase transition. The symmetry-breaking language describes the *representation-level* structure, not a thermodynamic equilibrium.

## 5 The Mechanism: Capacity Constraints

Why does discretization occur? The intuition comes from **sphere packing** and **channel capacity**.

### 5.1 Geometric Picture

Channel noise smears each code point into an “uncertainty region” of characteristic scale  $\sim \sigma$ . If two codes are closer than this scale, their uncertainty regions overlap, and the decoder cannot reliably distinguish them.

The question becomes: how many well-separated codes can coexist in a  $k$ -dimensional channel? This is related to the classical sphere-packing problem [Conway and Sloane, 1999]. For fixed noise scale and code amplitude, only a finite number of non-overlapping regions fit in low-dimensional space.

### 5.2 Information-Theoretic Picture

The Shannon–Hartley theorem [Shannon, 1948] gives the capacity of an additive white Gaussian noise (AWGN) channel:

$$C \propto k \cdot \log_2(1 + \text{SNR}) \quad (2)$$

where  $k$  is the number of channel uses (dimensions) and SNR is the signal-to-noise ratio. The *logarithm* of the number of distinguishable codewords scales with this capacity.

We do not attempt a precise calibration here. The point is qualitative: for fixed  $k$  and  $\sigma$ , capacity is finite, so only a finite number of well-separated codes can coexist. For our parameters ( $k = 2$ ,  $\sigma = 0.5$ ), we empirically observe  $\sim 6$  clusters. We do not claim the theory uniquely predicts “6”—only that a small integer number of clusters is natural in this regime.

The network doesn’t “know” about sphere packing or Shannon capacity; it discovers these constraints through gradient descent on reconstruction error.

## 6 What Gets Preserved

When compressing from 512 dimensions to  $k$  dimensions, what does the encoder choose to preserve?

Figure 3 shows that the encoder learns to preserve **high-variance directions**—essentially the top principal components of the input. The ring lives primarily in the first 2 PCs (we verified that  $PC1 \approx \cos\theta$  and  $PC2 \approx \sin\theta$  by plotting against  $\theta$ ), and these are what the encoder captures.

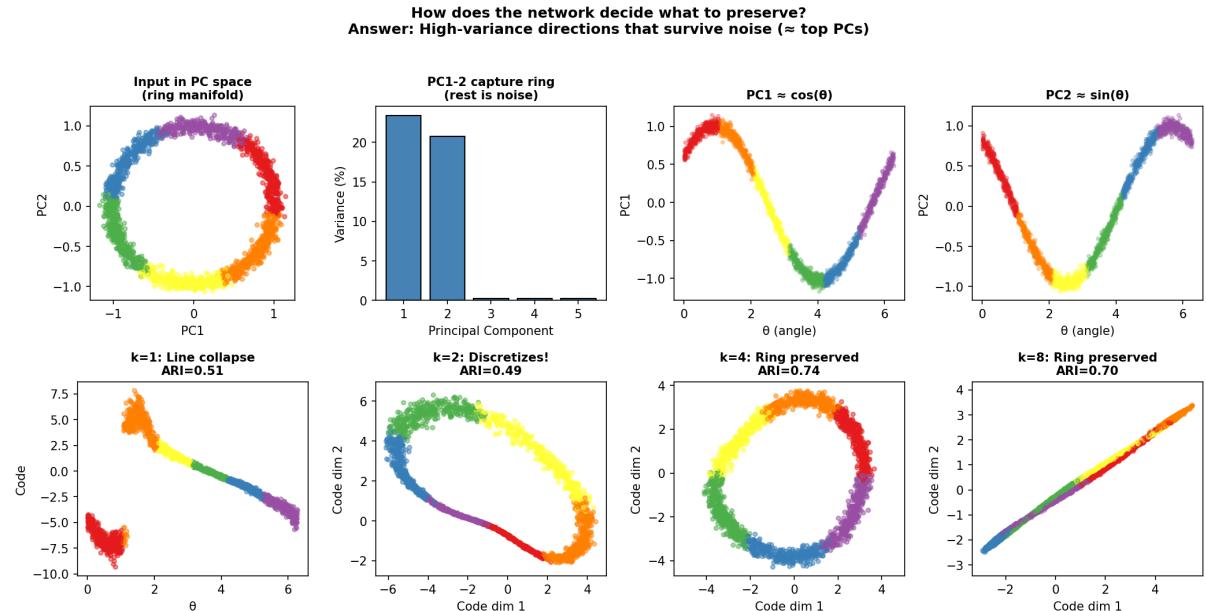


Figure 3: **What gets preserved.** Top: Input effectively lives in a 2-D linear subspace (PC1–2 capture the ring; higher PCs are embedding noise). The generative manifold is  $S^1$  (1-D), but it requires 2 linear dimensions to embed without self-intersection. Bottom: Encoder learns to preserve these high-variance directions. At  $k = 2$  with noise, discretization occurs.

This makes intuitive sense: high-variance directions carry the most information about input structure. Low-variance directions (the remaining 510 dimensions of embedding noise) are discarded as uninformative.

In the limit of a linear encoder/decoder and small noise, the optimum is PCA. Here the nonlinearity (ReLU) allows genuine topology changes—the “tearing” of the continuous ring into discrete clusters when capacity is insufficient.

## 7 Extension: Stochastic Resonance

Our framework provides a geometric interpretation of the **stochastic resonance** (SR) phenomenon—where adding noise can *improve* signal detection [Gammaitoni et al., 1998].

In the classical SR picture, a subthreshold periodic signal in a bistable potential is optimally detected at intermediate noise, which enables barrier crossing. Here, the “potential wells” are code basins learned by the autoencoder, and ambiguity arises from signals lying near decision boundaries.

Consider an ambiguous signal sitting exactly on the boundary between two code clusters. In low-noise conditions, the dynamics are confined to the low-dimensional manifold of learned codes—the signal is “trapped” on the decision boundary.

Adding noise allows the system to explore the ambient high-dimensional embedding space. The signal can fluctuate perpendicular to the boundary, enabling escape into the correct attractor basin by moving *around* the confusion region in high-D space rather than being stuck on a low-D saddle.

Figure 4 demonstrates this SR-like behavior:

- At zero noise, ambiguous signals are trapped on boundaries → poor decoding
- At intermediate noise, the system can escape to correct basins → peak accuracy
- At high noise, random walk dominates → decoding degrades

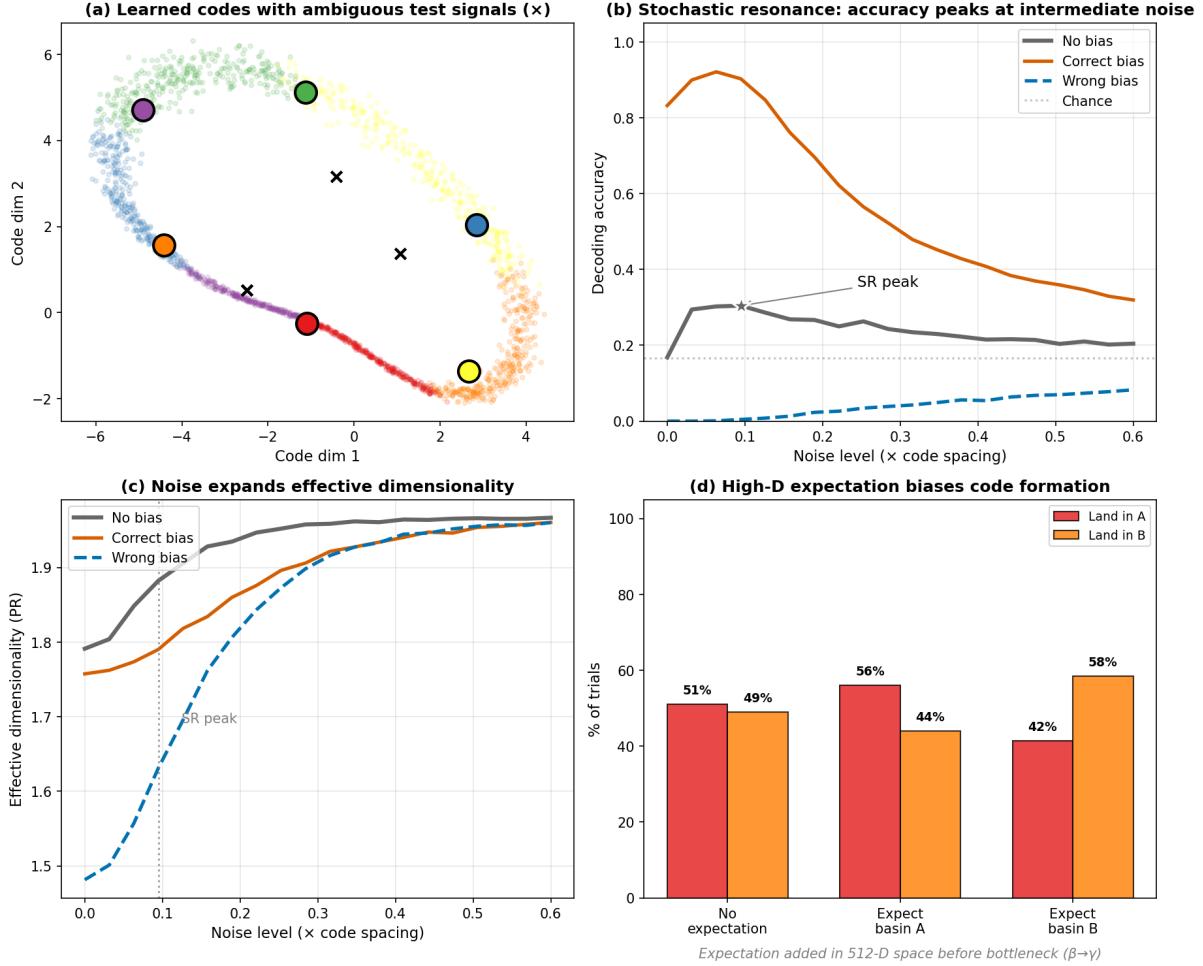


Figure 4: **SR-like behavior and expectation bias.** (a) Learned codes (colored centroids) and ambiguous test signals ( $\times$ , positioned near decision boundaries). (b) Decoding accuracy peaks at intermediate noise—the hallmark SR curve. The star marks the SR peak for the unbiased condition. (c) Effective dimensionality (participation ratio) increases monotonically with noise, reflecting expansion into the ambient 512-D space. (d) Expectation-biased SR: a high-dimensional expectation signal added in 512-D input space (before the bottleneck) biases which basin ambiguous inputs land in. Expectation effectively tilts the potential landscape, widening the basin of attraction for the expected code.

This reframes SR in geometric terms: the ambiguous signal is trapped on a low-dimensional saddle (the decision boundary). Noise does not merely add energy for barrier-crossing; it restores rank to the covariance matrix, allowing system trajectories to utilize the full dimensionality of the ambient space ( $N = 512$ ) to bypass the bottleneck-induced constriction ( $k = 2$ ). Optimal performance occurs when noise is sufficient to escape boundaries but not so large as to cause random wandering.

## 7.1 Expectation-Biased Stochastic Resonance

The SR phenomenon described above assumes *isotropic* noise—random fluctuations with no preferred direction. But in systems with top-down predictions, the noise need not be isotropic. We propose **expectation-biased stochastic resonance** (EBSR): the same SR dynamics, but with noise biased toward an expected code.

This maps naturally onto drift-diffusion dynamics. In Langevin form:

$$d\mathbf{x} = -\nabla U(\mathbf{x}) dt + \mathbf{F}_{\text{bias}} dt + \sigma d\mathbf{W} \quad (3)$$

where  $U(\mathbf{x})$  is the effective potential (learned by the decoder),  $\mathbf{F}_{\text{bias}}$  is the expectation-induced drift toward a predicted code, and  $\sigma d\mathbf{W}$  is the stochastic noise term. The expectation term breaks the symmetry of the potential landscape, effectively tilting the basin of attraction so that noise preferentially kicks the state into the expected code.

In discrete form for our simulation:

$$\mathbf{z}_{t+1} = \mathbf{z}_t + \eta \boldsymbol{\xi}_t + \beta \mathbf{b} \quad (4)$$

where  $\boldsymbol{\xi}_t \sim \mathcal{N}(0, I)$  is isotropic noise (scaled by  $\eta$ ),  $\mathbf{b}$  is a unit vector pointing toward the expected code centroid, and  $\beta$  controls the strength of expectation bias.

Figure 4(d) demonstrates this in our simulation. Crucially, we add expectation not in the low-dimensional code space, but in the original 512-dimensional input space—before the bottleneck. This models the key biological intuition: top-down signals (e.g., from higher cortical areas) enter the system at the high-dimensional stage and bias which code emerges after dimensional collapse. The expectation effectively widens the basin of attraction for the target code while narrowing it for competitors.

The results show that expectation reliably biases which basin ambiguous inputs land in. When the expectation matches the true category, accuracy improves; when it mismatches, systematic errors occur.

**The evolutionary argument.** Stochastic resonance is widespread in biological sensory systems—it appears to be a “free” consequence of noisy, threshold-based neural circuits [Gammaitoni et al., 1998]. Similarly, top-down predictions are ubiquitous in cortex. Given that both mechanisms exist independently, *not* combining them would leave performance on the table. We therefore suggest that EBSR is not merely possible but likely: any system that already exploits SR for signal detection, and that has access to top-down expectations, would naturally evolve to bias its noise toward predicted outcomes.

This yields a three-ingredient model of biological code formation:

$$\text{Bottleneck} + \text{Noise} + \text{Predictions} \rightarrow \text{Expectation-biased discrete codes}$$

## 8 Speculative Implications

The simulation is deliberately minimal and agnostic about biophysical details. The points below are *speculative connections*, not claims that this specific architecture underlies any particular system.

### 8.1 Categorical Perception

Humans perceive continuous stimuli as discrete categories—colors, phonemes, facial expressions [Harnad, 1987]. If sensory information must pass through bandwidth-limited neural pathways (due to metabolic constraints, synaptic noise, or architectural bottlenecks), discretization of the kind demonstrated here could contribute to categorical perception.

### 8.2 Beta-Gamma Coupling and Ephaptic Fields

A speculative but intriguing application concerns the interface between oscillatory field dynamics and neural spiking. Consider the beta-gamma coupling observed in cortex [Lundqvist et al., 2016, Miller et al., 2018]: beta oscillations ( $\sim 15\text{--}30$  Hz) modulate the amplitude of nested gamma oscillations ( $\sim 30\text{--}100$  Hz), which in turn coordinate spike timing. Extracellular fields generated by neural activity can, in turn, influence nearby neurons through ephaptic coupling [Anastassiou et al., 2011].

A common interpretation treats beta as “simple” (low-dimensional) because it is slow. We suggest an alternative: low-frequency oscillations can support *more* spatial modes (higher effective dimensionality) precisely because they vary slowly enough for complex spatial patterns to be sustained. Gamma, being faster, acts as a bandwidth-limited channel—a bottleneck that compresses the high-dimensional beta/field structure into a lower-dimensional but higher-information-density code. Spikes then provide a further discretization step.

In this view, the cascade is:

$$\text{Beta field (high-}D\text{)} \rightarrow \text{Gamma (low-}D, \text{high info)} \rightarrow \text{Spikes (discrete codes)}$$

Each arrow represents a noisy, capacity-limited interface of the kind simulated here. The “code formation” we demonstrate—discretization via bottleneck + noise—may thus occur at multiple stages: first at the beta-to-gamma transition (field compression), and again at the gamma-to-spike transition (neural discretization).

Crucially, this interpretation connects directly to EBSR: if beta oscillations carry top-down predictions as high-dimensional spatial patterns, then beta-gamma coupling *is* expectation-biased stochastic resonance. The beta field provides the “expectation” signal that enters the system before the gamma bottleneck, biasing which discrete code emerges. In this picture, the brain is performing SR on itself—using slow oscillations to shape the noise statistics of fast oscillations, thereby implementing prediction-guided code formation.

This inverts the standard interpretation and suggests that slow oscillations are not simple carriers but high-dimensional prediction signals from which discrete neural codes crystallize.

### 8.3 The Measurement Problem

This framework raises a deep epistemological issue: if high-dimensional field dynamics are the substrate from which discrete codes crystallize, then *measurement itself is dimensional collapse* [Todd, 2025a]. When we record from electrodes, we are not observing the high-dimensional field—we are observing the output of a code formation process. The electrode is another bottleneck.

This may explain why neuroscience has historically focused on spikes and discrete codes: they are what survives measurement. The continuous, high-dimensional field dynamics—if they carry the “interesting” computation—are precisely what our instruments cannot access without collapsing. Claims about such high-dimensional substrates may be fundamentally difficult to falsify using measurements that necessarily discretize.

The problem generalizes beyond neuroscience. In any system where high-dimensional energy flows into low-dimensional codes—protein folding, gene regulation, immune recognition, ecological dynamics—we face the same issue. We measure the codes (the outputs), not the high-dimensional processes that formed them. The simulation presented here operates entirely in the measurable regime (we have full access to the 512-D input and the  $k$ -D codes), but it may serve as a window into dynamics that, in physical systems, occur “upstream” of observation.

### 8.4 Symbol Emergence in Language

Discrete tokens are fundamental to language. Our simulation illustrates one mechanism by which discretization can emerge without explicit symbolic machinery—through the interaction of compression and noise. This might inform theories of language evolution, though many other factors are surely involved.

### 8.5 Digital Information in Biology

Life uses digital information (genetic sequences) despite operating in an analog chemical medium. Noise and capacity constraints may have played a role in the emergence of discrete coding in

early self-replicating systems [Walker and Davies, 2013, Deacon, 2011], though this remains highly speculative.

## 8.6 Relation to Thermodynamics

One might ask how this relates to Landauer’s principle, which bounds the energy cost of bit erasure [Landauer, 1961, Bennett, 1982]. Our simulation has no explicit energy model, so we cannot make direct thermodynamic claims.

However, a thermodynamic reinterpretation is natural: treat the reconstruction loss as an effective potential  $U(\mathbf{c})$  and the channel noise variance as proportional to temperature ( $\sigma^2 \propto k_B T$ ). The system then minimizes an effective free energy  $F = \langle U \rangle - TS$ , where  $S$  is the entropy of the code distribution. Discretization would correspond to the formation of a small number of deep basins in the effective potential, each with a finite catchment volume in code space. At fixed channel capacity, increasing temperature (noise) favours coarse, robust basins over fine-grained structure.

In this picture, the stochastic resonance phenomenon becomes standard barrier-crossing dynamics: noise provides the thermal energy to escape local minima and explore the potential landscape. The “information” emerges when the system settles into a basin—the uncertainty collapses, and the basin identity carries  $\log_2 n$  bits. This collapse is a natural candidate for the “projection” event where thermodynamic costs are paid [Todd, 2025b].

A key insight from recent work on biological thermodynamics is that continuous high-dimensional substrates can defer the Landauer cost of bit erasure until dimensional projection occurs [Todd, 2025b]. In our simulation, the encoder-decoder system operates analogously: information exists as continuous correlations in the high-D input, and the thermodynamic “payment” would occur at the bottleneck where dimensional collapse forces discretization. This suggests that the code formation process we demonstrate may be energetically favored precisely because it defers projection until capacity constraints make it inevitable.

We have not developed this thermodynamic model here; doing so properly would require specifying the potential landscape, computing Kramers rates for basin transitions, and tracking entropy production along trajectories. This is a natural direction for future work, connecting to stochastic thermodynamics and the physics of biological information processing.

## 9 Relation to Prior Work

The results connect to several established frameworks:

**Rate-distortion theory and vector quantization** [Cover and Thomas, 2006]: Our encoder-decoder system minimizes distortion subject to a rate constraint (channel capacity). At low rates, the optimal solution involves quantization—precisely the discrete codes we observe.

**Information bottleneck** [Tishby et al., 2000]: The bottleneck principle frames representation learning as extracting minimal sufficient statistics. Our simulation provides a concrete visualization of what happens geometrically when the bottleneck is tight.

**What’s new here:** The explicit topology-change picture (ring  $\rightarrow$  line/clusters/ring), the use of PR and ARI to track geometry and semantics, and the SR-like dimensionality story.

## 10 Limitations

This simulation is deliberately minimal:

- **Static data:** We use a fixed manifold, not dynamical or temporal structure
- **Gaussian noise:** Real channels have more complex noise statistics

- **Feedforward architecture:** Biological systems have recurrence and feedback
- **Single manifold:** The input is a simple ring; real data has more complex topology
- **No explicit physics:** There is no energy function or thermodynamic model

These limitations define the scope. Extending to time-series, recurrent architectures, and explicit energy models is future work.

## 11 Reproducibility

The simulation is implemented in Python using PyTorch. Code and figures are available at <https://github.com/todd866/code-formation>. Key parameters:

- Input: 2000 points, 512 dimensions, ring manifold ( $S^1$ )
- Encoder/Decoder: 3-layer MLP, 256 hidden units, ReLU activation
- Training: Adam optimizer, 150 epochs, MSE loss
- Critical experiment:  $k = 2$ ,  $\sigma = 0.5$

Random seeds are fixed for reproducibility. Running `python code_formation.py` generates all figures.

## 12 Conclusion

We have presented a minimal simulation demonstrating the emergence of discrete codes from continuous substrates when information passes through a noisy, capacity-limited channel. The key finding is that **both** a dimensional bottleneck **and** channel noise are required—neither alone suffices.

The mechanism is geometrically intuitive: noise creates uncertainty regions around each code point, and limited channel capacity means only a finite number of well-separated codes can coexist. The network discovers this constraint through gradient descent, producing discrete clusters with safety margins.

This illustrates one concrete mechanism by which symbol-like discrete codes can emerge from continuous substrates under capacity and noise constraints. Whether analogous mechanisms operate in biological systems—in perception, memory, language, or molecular information—remains an open and fascinating question.

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