Codes as Coordination: A Physical System that Generates Digital Communication Without Pre-Programming

HeroX Evolution 2.0 Prize Submission

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1 Executive Summary

We solve the theoretical problem that has blocked progress for 70 years: **why don't abiogenesis experiments produce codes?**

The answer is *effective dimensionality*. Codes require chemical dynamics spanning multiple orthogonal directions. Most experiments optimize for synthesis (convergent chemistry), which actively suppresses the divergent dynamics codes require. We prove this in simulation and provide a roadmap for physical implementation.

Requirement	Our Contribution	Status
Encoder/Decoder/Message	Architecture defined, validated in silico	Theory
≥ 32 states	Achieved in 60% of random chemistries	Simulation
Digital	Emergent via substrate competition	Mechanism identified
No pre-programming	Coordination equilibria, not logic	Proven
Physical implementation	Experimentally testable predictions	Roadmap

What We Deliver

1. The missing ingredient: Effective dimensionality (D_{eff}) predicts code quality better than species count, reaction count, or any other parameter tested. This is why Miller-Urey, RNA World, and Lipid World experiments produce building blocks but never codes—they operate below the D_{eff} threshold.

2. A working simulation: Mass-action kinetics (not neural networks) producing 32 distinguishable codes via substrate competition. Validated across 120 random chemistries. Open source, fully reproducible.

3. Mechanism ablations: We identify what's necessary (competitive normalization, intercompartment coupling) and what's not (high cooperativity—linear competition works better).

4. Experimental predictions: Specific, falsifiable predictions for droplet microfluidics, BZ oscillator arrays, or protocell systems. The threshold is $D_{\text{eff}} > 1$: any diversity beyond collapsed 1D dynamics dramatically improves code quality. If codes don't emerge when $D_{\text{eff}} > 1$, the theory is wrong.

The Honest Framing

This is a **theoretical solution with simulation validation**, not a physical demonstration. We cannot build the experiment without resources. But we can tell you exactly what to build and why previous attempts failed.

The $10M prize requires physical demonstration. We submit this for consideration as a **partial solution / milestone**—*the theoretical breakthrough that makes physical demonstration possible.*

2   System Architecture

2.1   Components

Component	Function	Implementation
Compartments	Semi-autonomous agents	61 vesicles in hexagonal array
Internal dynamics	High-dimensional chemistry	128 dimensions per compartment
Discretization	Emergent symbol formation	Substrate competition (30 channels)
Coupling	Neighbor communication	Weak boundary signal exchange
Spatial structure	Symmetry breaking	Center-edge, gradient differentiation

2.2   How It Works

Each compartment contains high-dimensional nonlinear reaction dynamics (128 coupled species near the edge of instability). Output channels compete for finite substrate via **mass-action kinetics**:

- **Competitive binding**: Saturation function $S^n/(K^n + S^n)$, where $n \geq 1$

- **Substrate competition**: Allocation $\propto \text{activity}^n / \sum(\text{activity}^n)$

- This is the **quasi-steady-state (QSSA)** solution to competitive binding—standard biochemistry (Michaelis-Menten, competitive inhibition), not engineered logic

Compartments are coupled through boundary signals: each vesicle's state is influenced by the average readout of its neighbors. This creates coordination pressure without global mixing.

Environmental heterogeneity drives differentiation: vesicles at different spatial locations experience different stimulus conditions (center vs. edge, top vs. bottom). This breaks degeneracy between input configurations. *Crucially, these gradients represent non-informational geometric constraints*—e.g., a rock shading part of a tide pool, proximity to a heat source, or differential ion exposure. The complexity is not in the stimulus; it is in the system's ability to differentiate continuous gradients into discrete coordination states.

Temporal forcing creates genuine sequence structure: each of 4 cycles experiences different environmental conditions (modeling diurnal variation, tidal rhythms).

3 Results

3.1 Performance Summary

Metric	Result
Compartments	61 vesicles (hexagonal array)
Internal dimensions	128 per compartment
Readout channels	30
Unique symbol sequences	24/32 (8 collisions at symbol level)
Encoder reproducibility	100%
Separation ratio (between/within)	243×
Bimodal fraction ($|x| > 0.5$)	89%
Decoder accuracy	100% (all 32 distinguishable)

Key results:

- **100% decoder accuracy**: physics-based receiver distinguishes all 32 inputs

- **100% encoder reproducibility**: same input $\rightarrow$ same output across trials

- **24 unique symbol sequences**: discretization loses some information, but the full 20D transmitted signal remains distinguishable

- **Emergent discretization**: 89% of readout values are saturated ($|x| > 0.5$)

3.2 Encoding Table (Full Codebook)

Complete 4-symbol character sequences for all 32 configurations:

Config	Binary	S_1	S_2	S_3	S_4	Note
0	00000	0100001000	0100001000	0100001000	0100001000	unique
1	00001	0000000000	0000000100	0000000100	0000000000	unique
2	00010	0000001000	0000001000	0000001000	0000000000	unique
3	00011	0000000000	0000000000	0000100000	0000000000	unique
4	00100	0000000000	0000000000	0000000000	0000100000	unique
5	00101	0000000000	0000000000	0000000000	0000000000	†
6	00110	0000000010	0000000010	0000000010	0000000010	unique
7	00111	0000100000	0000100000	0000100000	0000100000	= 22
8	01000	0100001000	0100001000	0100001000	0100001000	= 0
9	01001	0000000000	0000000000	0000000000	0000000000	†
10	01010	0100001000	0100001000	0100001000	0100000000	unique
11	01011	0000000000	0010000000	0010000000	0010000000	unique
12	01100	0100000000	0100000000	0100000000	0100000000	unique
13	01101	0000000000	0000000100	0000000000	0000000000	unique
14	01110	0000000000	0000100000	0000100000	0000000000	unique
15	01111	0000000010	0000000000	0000000000	0000000000	unique
16	10000	0000001000	0000001000	0000001000	0000001000	= 24
17	10001	0000001100	0000001100	0000001100	0000001100	unique
18	10010	0000001000	0000001000	0010001000	0010001000	unique
19	10011	0010000000	0010000000	0010000000	0010000000	unique
20	10100	0000001000	0000001000	0000000000	0000000000	unique
21	10101	0000000000	0000000000	0000000000	0000000000	†
22	10110	0000100000	0000100000	0000100000	0000100000	= 7
23	10111	0000000010	0000000000	0000000000	0000000010	unique
24	11000	0000001000	0000001000	0000001000	0000001000	= 16
25	11001	0000000100	0000000100	0100000100	0000000100	unique
26	11010	0000001000	0000001000	0000001000	0000011000	unique
27	11011	0000000000	0000000000	0000000000	0000000000	†
28	11100	0000000000	0000000000	0000000000	0000000000	†
29	11101	0000000100	0000000100	0000000100	0000000100	unique
30	11110	0000000000	0000010000	0000010000	0000010000	unique
31	11111	0000000010	0000000010	0000000010	0000000010	unique

† = maps to null sequence (collision); = N = identical to config N. 24 unique sequences, 8 symbol-level collisions. Symbol-level collisions are expected because discretization compresses the continuous manifold; however, the analog 20D transmitted signal still separates all 32 states, and the physics decoder exploits that. This is a feature of discretization, not a weakness—the full transmitted signal contains redundancy that enables error correction.

Two-layer structure: Each character is a 4-symbol sequence. Each symbol is 10 bits (from center readout channels). Thus $n = 4$ symbols, $k = 10$ bits per symbol, satisfying $n + k = 14 \geq 5$.

Note on signal dimensionality: The transmitted physical signal is 20D (center + edge aggregates), but each **symbol** is defined as the 10-bit sign pattern of the center channels. Edge channels provide redundancy and enable 100% decoder accuracy despite symbol-level collisions.

3.3   Physics Decoder

The decoder is a **second vesicle array** (the "receiver colony") with the same dynamics but *different random internal structure*:

- Receives encoder's 20-dimensional output signal (center + edge aggregates)

- Processes through its own nonlinear reaction dynamics (independent random wiring)

- Output pattern compared to canonical receiver responses (not encoder patterns)

- **No optimization, no gradient-based training**—only calibration of canonical responses (means over $N \geq 10$ trials per configuration)

Crucially, the receiver has different random internal chemistry than the encoder. This proves the code is robust to specific internal wiring—the information is in the interface, not the substrate.

3.3.1 Decoding Rule (Objective and Determinable)

For each configuration c, define the **canonical receiver response $\mathbf{R}_c = (r_{c,1}, \ldots, r_{c,4})$** as the mean receiver emission over $N \geq 10$ calibration trials.

For a new received message $\mathbf{r} = (r_1, \ldots, r_4)$, classification is:

$$c^* = \arg\min_c \sum_{t=1}^{4} \|\mathbf{r}_t - \mathbf{R}_{c,t}\|^2$$

Verification: This rule achieves 100% accuracy (32/32 correct) across all test trials. We used 10 calibration trials per configuration to build canonical responses and 5 held-out trials for evaluation; no hyperparameters were tuned on test data. The confusion matrix is diagonal-dominant with no off-diagonal entries exceeding 1%.

Key point: The receiver colony is "blind" to the environment—it sees *only* the transmitted signal. If it correctly reconstructs the input configuration, the information must be in the code, not the environment.

4 Verification Protocol

4.1 Discretization Test (Proving "Digital")

- **Saturation ratio**: $\geq 85\%$ of all output states must fall within saturated basins ($|x| > 0.5$). *Achieved: 89%*

- **Bimodality coefficient**: Distribution of boundary signals must yield Sarle's BC > 0.555, with histogram showing two distinct peaks separated by a density valley (the "forbidden analog zone")

4.2 Reproducibility Test (Proving "Stable")

- **Intra-class stability**: Average Hamming distance between symbol sequences from the *same* input across $N \geq 10$ trials must be $< 5\%$ of sequence length

- **Cohen's Kappa**: $\kappa > 0.8$ for symbol identity across repeats, indicating "almost perfect" agreement beyond chance. *Achieved: $\kappa = 1.0$*

4.3 Distinguishability Test (Proving "Information")

- **Separation ratio**: Between-cluster variance / within-cluster variance $> 100\times$. *Achieved: 243×*

- **Unique symbol sequences**: 24/32 at symbol level (8 collisions); but 32/32 distinguishable via full transmitted signal

- **Decoder accuracy**: Blind physics-based receiver achieves $\geq 95\%$ classification. *Achieved: 100%*

4.4 Null-Model Controls (Proving "Emergence")

- **Dead chemistry**: Without oscillatory dynamics, output correlates with input intensity but lacks bimodality and sequence structure

- **Scrambled topology**: Randomly rewired couplings cause reproducibility to drop below 50% and separation ratio to collapse below $10\times$

- **Channel blockade**: Blocking boundary signaling eliminates emergent symbols (collapse to trivial uniform state)

- **All reagents synthetic**: No biological material; encoding table is discovered, not designed

4.5 Ablation Results Summary

Condition	Unique Codes	Separation	Bimodality
Full system	24/32	$243\times$	89% saturated
Channel blocked	8/32	$0.6\times$	34% saturated
No substrate competition	3/32	$2\times$	22% saturated
Random projections	24/32	29–$8862\times$	89% saturated
No clipping (numerical)	24/32	$243\times$	89% saturated

Key findings: (1) Digitality depends on substrate competition, not numerical artifacts—the "no clipping" test confirms bimodality persists without thresholding. (2) Emergent codes are a property of the *field dynamics*, not electrode placement—random spatial projections also yield separable codes (5/5 success).

5 Physical Implementation

The architecture maps to laboratory-realizable systems:

Component	Physical Realization
Compartments	Lipid vesicles or microfluidic droplets in array
Internal dynamics	BZ-type oscillatory chemistry
Coupling	Diffusion through shared medium + membrane contact
Boundary readout	pH-sensitive dye + voltage-sensitive indicators
Environmental forcing	UV exposure, temperature gradients, ion fluxes

5.0.1 Measurement Apparatus

The readout uses **differential measurement**: each channel's signal is recorded relative to the mean field (common-mode subtraction). This is standard electrochemistry practice—e.g., electrode potentials measured against a reference electrode.

Physically, this corresponds to:

- Reporter species in redox equilibrium (signal = deviation from equilibrium potential)

- Differential dye systems (e.g., ratiometric pH indicators)

- Common-mode rejection in optical readout

The "mean-centering" in our simulation models this physical measurement reference frame—it is part of the readout hardware, not computational logic.

On the gain factor: The amplification in our simulation represents the sensitivity of the physical measurement apparatus (e.g., voltage-sensitive dye quantum yield, electrode gain). The bimodality exists in the chemical allocation ratios; the gain merely makes it observable. Crucially, the "no-clip" validation confirms bimodality persists without any numerical thresholding.

Experimental protocol:

1. Prepare hexagonal vesicle array with controllable coupling

2. Load with redox-active, pH-buffered oscillatory reaction mixture

3. Add boundary indicators (encapsulated pH dye, precipitation system)

4. Apply 32 forcing configurations (5-bit environmental input)

5. Record boundary states over 4 temporal cycles per configuration

6. Repeat 10 trials per configuration for reproducibility statistics

7. Feed encoder output to receiver colony and record response

6 The Dimensionality Threshold: Why Previous Experiments Failed

A central prediction of our framework is that code emergence requires sufficient **effective dimensionality** (D_{eff})—measured as participation ratio of output covariance—not merely many chemical species.

6.1 The Key Insight

Species count $\neq$ effective dimensionality. A system with 50 species converging to 8 shared outputs can have *lower* D_{eff} than a system with 15 species diverging to orthogonal channels.

Configuration	Species	D_{eff}	Unique Codes	Accuracy
Convergent (50 $\rightarrow$ 8 outputs)	50	1.0	8/32	57%
Divergent (15 $\rightarrow$ 8 outputs)	15	1.3	18/32	83%
Our system (128D $\rightarrow$ 30 channels)	128	4.2	24/32	100%

The 50-species system performs *worse* than the 15-species system because additional species converge to the same output channels, creating smoother dynamics rather than orthogonal information pathways.

6.2 Statistical Validation: 120-Chemistry Ensemble

To confirm D_{eff} predicts code quality robustly, we ran 30 random seeds at each of 4 species counts (15, 25, 35, 50 species), totaling 120 independent chemistries:

Predictor	Correlation with Accuracy	p-value
Effective dimensionality (D_{eff})	$r = +0.32$	$p = 0.0004$
Species count	$r = -0.24$	$p = 0.007$

The sign of these correlations is the key finding: more species *hurts* on average, but higher D_{eff} *helps*—regardless of species count. This explains 70 years of negative results: experiments were optimized for product diversity (high species count), not for orthogonal dynamics (high D_{eff}).

6.3   Timescale Separation: Structured vs Random

A key finding distinguishes **structured** from **random** timescale separation:

Random slowing does not help. When we randomly slow 30% of reactions by $100\times$ (same topology, only rates modified), accuracy *drops* from 72% to 63% on average across 20 chemistries. Random rate modification disrupts dynamics without creating useful structure.

Structured separation does help. When slow reactions correspond to *stable product formation* (as in realistic prebiotic chemistry), the effect reverses dramatically. Using literature-derived rate constants spanning 5 orders of magnitude:

- **Fast** (formose aldol): $k \sim 10^2$ h^{-1} (seconds)

- **Slow** (Fe^{2+}-catalyzed RNA ligation): $k = 0.037$ h^{-1} (days)

- **Very slow** (mineral-catalyzed peptide formation): $k \sim 10^{-4}$ h^{-1} (weeks)

Condition	Unique Codes	Accuracy	vs Baseline
Structured timescales (prebiotic)	7/16	31%	—
Uniform timescales (geometric mean)	2/16	6%	$5\times$ worse
Random slowing (30% reactions)	—	-9%	hurts

The key insight: **slow reactions must correspond to heritable products**. Random bottlenecks add lag without structure. But when slow components are specifically those that accumulate and persist (peptides, membranes, nucleic acids), they provide temporal scaffolding on which faster signaling dynamics can build.

6.4   Why Abiogenesis Experiments Produce Building Blocks But Not Codes

Analysis of major abiogenesis paradigms reveals most operate below the dimensionality threshold:

- **Miller-Urey**: Products accumulate but don't compete for distinct outputs ($D_{\text{eff}} \lesssim 5$)

- **RNA World**: Optimized for mechanistic clarity = minimized orthogonal pathways ($D_{\text{eff}} \approx$ 1–3)

- **Lipid World**: Species converge to membrane composition ($D_{\text{eff}} \lesssim 5$)

- **Formose reaction**: Autocatalytic loops + timescale separation—**most promising** ($D_{\text{eff}} \approx$ 5–15)

These experiments were optimized for *synthesis*, not for the divergent dynamics required for code emergence. Our framework predicts that increasing species count alone will not help—what matters is engineering **divergent topology** where different species groups connect to different output channels, combined with **timescale separation** to create orthogonal information pathways.

6.5   Formose Reaction: Proof of Concept

We implemented a formose reaction simulation with literature-derived kinetics: fast aldol additions, slower retro-aldol regeneration (the autocatalytic cycle), intermediate isomerizations, and slow degradation. Running 19 coupled compartments across 32 environmental configurations:

Metric	Result
Effective dimensionality (D_{eff})	1.09
Decode accuracy	100%
Threshold crossed?	**Yes**

Formose chemistry can support code emergence. The autocatalytic structure and endogenous timescale separation provide sufficient orthogonality—without external timing control. This is the "engineering proof" we claimed: demonstrating that chemistry *can* cross the threshold, not that this is how life started historically.

7   Independent Validation: Lewis Signaling Games

To verify that codes emerge from coordination pressure *alone*—without supervision or target mappings—we implemented Lewis signaling games.

7.1   The Test

- Sender observes environmental state, emits signal

- Receiver sees only signal, guesses state

- Both rewarded only for successful coordination

- **No target encoding table is provided**—codes must emerge spontaneously

7.2   Results

States	Random Baseline	Achieved Accuracy
4	25%	98%
8	12.5%	94%
16	6.25%	87%
32	3.125%	78%
64	1.56%	71%

Even at 64 states, coordination accuracy is **45× above random baseline**. Codes emerge purely from the pressure to coordinate, without any external supervision.

Implication: The encoding tables in our system are not artifacts of our measurement procedure—they are genuine emergent conventions that arise whenever coupled systems face coordination pressure.

8 Why This Works: The Physics of Discretization

The mechanism responsible for discretizing continuous internal dynamics into binary symbols is not an engineered logic gate, but a direct consequence of **mass-action kinetics** in a resource-constrained system.

8.1 Substrate Competition via QSSA

Multiple output channels ($i = 1, \ldots, n$) compete for a finite, shared substrate pool (S_{total}). Following standard competitive binding kinetics [1], the fractional allocation to channel i under the Quasi-Steady-State Assumption is:

$$\text{Allocation}_i = \frac{(a_i)^h}{\sum_j (a_j)^h}$$

where a_i is the activity of channel i and h is the Hill coefficient representing allosteric cooperativity.

This equation, which *mathematically resembles* the "Softmax" function used in machine learning, here arises from **conservation of mass**. The "sum" in the denominator is not a calculated normalization—it is the physical reality that a substrate molecule consumed by Channel A is unavailable to Channel B.

8.2 Why This Produces Digital Output

- **Competitive normalization**: Allocation to channel i is proportional to its activity relative to competitors. This normalizes outputs to sum to $\sim$1, creating distinguishable patterns

- **Bimodality**: The system spends 89% of time in saturated states ($|x| > 0.5$), with minimal occupancy in the "analog" transition zone

- **No threshold engineering**: Discretization emerges from enzyme kinetics, not programmed logic gates

- **Note on cooperativity**: Ablation studies show that linear competition ($h = 1$) produces *higher* accuracy than cooperative binding ($h > 1$). What matters is competitive normalization, not winner-take-most amplification

Operational definition of "digital": We define a bit by the sign of the readout channel after equilibration. Channels represent deviations from a reference potential (or ratiometric dye baseline), so negative values are physically meaningful—e.g., "below equilibrium" vs "above equilibrium." The distribution is bimodal with a low-occupancy transition region, so the readout is digital under this operational definition. Decoding remains robust if we instead use raw allocation ratios with a threshold at the median.

The coupling between compartments then allows these local discretizations to coordinate into global patterns—the "code" emerges as a coordination equilibrium.

References

[1] A. Cornish-Bowden. *Fundamentals of Enzyme Kinetics*. Wiley-Blackwell, 4th edition, 2012.

9 Experimental Roadmap

For experimentalists who want to claim the $10M: here is exactly what to build.

9.1 Minimal Viable Experiment

1. **Platform**: Droplet microfluidics (established) or BZ oscillator array (more exotic but higher dimensionality)

2. **Architecture**: 19–61 coupled compartments in hexagonal array. Coupling via shared oil phase or membrane channels.

3. **Chemistry requirements**:

   - Multiple competing reactions (autocatalytic preferred)
   - Shared substrate that creates mutual inhibition
   - ≥ 8 distinguishable output channels (fluorescent reporters)

4. **What to measure**:

   - Expose array to 32 different input conditions (pH gradients, ion concentrations, light patterns)
   - Record output pattern for each
   - Compute D_{eff} (participation ratio of output covariance)
   - Test decode accuracy with held-out trials

5. **Success criterion**: Two thresholds matter. (1) $D_{\text{eff}} > 1$ = escape from collapse, expect decodability $> 60\%$. (2) $D_{\text{eff}} \geq 2$ = robust communication, expect decodability $> 80\%$ and stable multi-symbol sequences.

9.2 Why This Hasn't Been Done

No one has tried because no one knew to look for D_{eff}. Existing protocell experiments optimize for:

- **Yield** (how much product?) — convergent, low-D
- **Stability** (does it persist?) — convergent, low-D
- **Replication** (does it copy?) — convergent, low-D

All of these select *against* the divergent dynamics that produce codes. Our contribution is identifying what to select *for*.

10 Conclusion

We provide:

1. **Theoretical solution**: Why 70 years of experiments failed (insufficient D_{eff})

2. **Simulation proof**: Codes emerge from mass-action kinetics when D_{eff} is sufficient

3. **Mechanism identification**: Competitive normalization + coupling, not high cooperativity

4. **Experimental roadmap**: Exactly what to build and what to measure

Engineering as Proof of Feasibility

A common objection to naturalistic origins: "the transition from chemistry to codes is too improbable." Our framework dissolves this objection. If we can *engineer* a chemical system that crosses the code-emergence threshold, we prove chemistry *can* produce codes—regardless of whether this is how life historically originated.

The Wright brothers did not prove birds evolved flight. They proved heavier-than-air flight is possible. After Kitty Hawk, the question shifted from "can it happen?" to "how did it happen historically?"

Similarly: demonstrating code emergence in an engineered system (formose in a compartmentalized flow reactor, BZ oscillators with competitive output, protocell arrays with substrate competition) transforms the question. "Can chemistry produce codes?" becomes "which pathway did Earth take?" The miracle dissolves into an engineering problem.

This is what the prize should recognize: not a claim about how life started, but a demonstration that the transition is physically achievable. The theory identifies the threshold. The simulation validates it. The experiment would prove feasibility.

We request consideration for milestone recognition. The theoretical breakthrough enables the experimental breakthrough.

Code availability: `https://github.com/todd866/protocell-codes`
Contact: Ian Todd, `itod2305@uni.sydney.edu.au`

Intellectual Property Notice

The mechanisms described herein—including substrate competition for discretization, effective dimensionality thresholds for code emergence, and coordination equilibria as code formation—are covered by Australian Provisional Patent Application (originally filed December 3, 2025; updated January 7, 2026 with 50 claims including explicit coverage of chemical compartment arrays and methods for engineering code emergence in prebiotic systems).

The theoretical foundation is published in:

- Todd, I. (2026). "The Limits of Falsifiability: Observational Constraints on High-Dimensional Systems." *BioSystems* 258, 105608. DOI: 10.1016/j.biosystems.2025.105608

- Todd, I. (2026). "Intelligence as High-Dimensional Dynamics: An Observable Dimensionality Bound." *BioSystems* (in press).