

# IMPUTATION OF MISSING DATA WITH BAYESIAN ADDITIVE REGRESSION TREES

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# INTRODUCTION TO THE PROBLEM OF MISSING DATA

- ▶ Historically, **missingness** assumed accidental and thus the process that caused it was ignored.<sup>1</sup>
- ▶ **Donald Rubin** formalised the analysis of missing data allowing considerations for **imputing** the data.
- ▶ **Multiple Imputation** proposed to capture the uncertainty caused by the missing data.<sup>2</sup>

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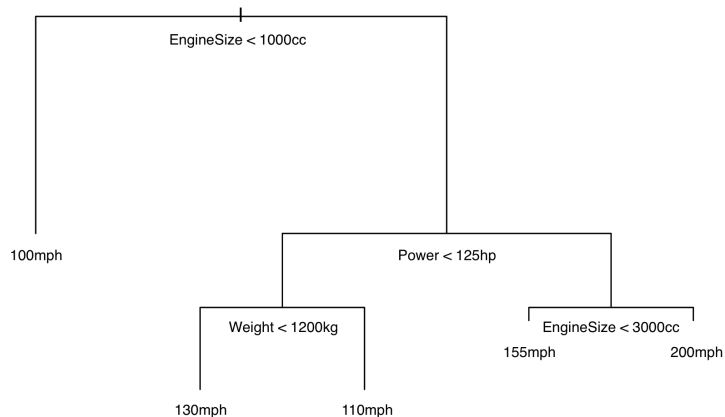
<sup>1</sup>Rubin, 1976

<sup>2</sup>Rubin, 1978

# TREE BASED REGRESSION

## CLASSIFICATION AND REGRESSION TREES <sup>3</sup>

- ▶ Statistical **classification** or **regression** which partitions the predictor space into subgroups.
- ▶ Once built, **predicts** a response given a set of covariates.
- ▶ **Non-parametric** and can model high level **interactions** and **non-linearities**.



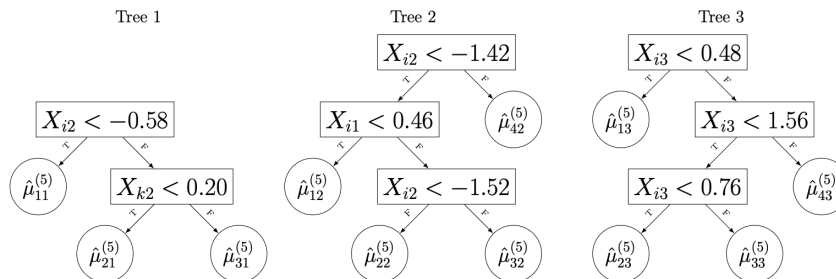
**Figure.** A simple regression tree to predict the top speed of a vehicle, given the engine size, power and weight.

<sup>3</sup>Formalised by Breiman et al., 1984

# BAYESIAN ADDITIVE REGRESSION TREES

## AN INTRODUCTION TO BART <sup>4</sup>

- ▶ BART utilises a **sum-of-trees** structure,  $Y = \sum_{j=1}^m g(\mathbf{X}; T_j, M_j) + \epsilon$ , where for tree  $j$ 
  - ▶  $T_j$  is the **tree structure**.
  - ▶  $M_j = \{\mu_{1j}, \mu_{2j}, \dots, \mu_{b_jj}\}$  is the set of  $b_j$  **terminal parameters**.
- ▶ Trees built via a **Bayesian Backfitting** algorithm.
- ▶ Can form the basis of an **imputation** model.



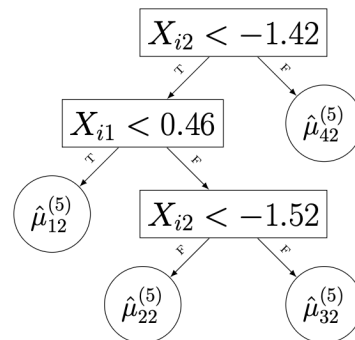
**Figure.** A sum-of-trees structure. Extracted from **Tan and Roy, 2019**

# THE BART PROCESS

## THE PRIORS

- Strong influential **regularising** priors guide the tree building process, tailoring the fit.

- **The Tree Prior** –  $p(T_j)$ .
- **The Terminal Parameter Prior** –  $p(\mu_{ij} \mid T_j)$ .
- **The Error Variance Prior** –  $p(\sigma)$ .



**Figure.** A single tree. Extracted from **Tan and Roy, 2019**

# THE BART PROCESS

## TREE BUILDING

- ▶ The **backfitting** algorithm draws each tree  $(T_j, M_j)$  conditional on  $[(T_{(j)}, M_{(j)}), \sigma]$ .
- ▶ The conditional distribution of the  $j^{\text{th}}$  tree depends only on the other trees and the training data via,

$$R_j \equiv y - \sum_{k \neq j} g(\mathbf{x}; T_k, M_k).$$

- ▶ Tree design proposed iteratively by a **stochastic search** procedure that repeatedly perturbs the trees in one of four ways.

▶ **Grow**

▶ **Prune**

▶ **Change**

▶ **Swap**

## MISSBART IMPUTATION METHOD

- Based on the popular **missForest** method of **Stekhoven and Bühlmann, 2012**.

### missBART Algorithm

**Require:**  $\mathbf{X}$  an  $n \times p$  matrix, stopping criterion  $\gamma$

- 1: Initialise the missing values with a simple mean imputation
- 2:  $\mathbf{k} \leftarrow$  vector of the indices of the columns in  $\mathbf{X}$  in order of increasing missingness
- 3: **while** not  $\gamma$  **do**
- 4:    $\mathbf{X}_{\text{old}}^{\text{imp}} \leftarrow$  current imputed matrix
- 5:   **for** each column,  $c$  in  $\mathbf{k}$  **do**
- 6:     Fit a **BART** model:  $\mathbf{y}_{\text{obs}}^{(c)} \sim \mathbf{x}_{\text{obs}}^{(c)}$
- 7:     Predict  $\mathbf{y}_{\text{mis}}^{(c)}$  using  $\mathbf{x}_{\text{mis}}^{(c)}$
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**Table.** Data based on the Theoph dataset [R Core Team, 2024].

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70.5	4.53	7.07	—	—
86.4	3.10	—	4.24	—
—	—	6.98	5.25	74
70.5	4.53	7.15	4.73	85
—	4.40	12.00	3.01	—
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70.5	4.53	0.98	7.31	81
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## DISCUSSION AND RESEARCH

### IMPUTATION MODELS

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<sup>5</sup>van Buuren, 2018

# DISCUSSION AND RESEARCH

## IMPUTATION MODELS

- ▶ **missForest/BART** produces a single complete dataset.
- ▶ Is this a disadvantage?
- ▶ Yes – not multiple imputation! <sup>6</sup>
- ▶ Bootstrap the data and produce multiple complete datasets.
- ▶ Compare missForest vs missBART vs both bootstrapped.
- ▶ Utilise BART's intrinsic **Bayesian probability model** to generate multiple imputations from **posterior predictive** draws and combine via **Rubin's rules**.

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<sup>6</sup>van Buuren, 2018

# DISCUSSION AND RESEARCH

## IMPUTATION METRICS








- ▶ Evaluating accuracy alone **fails** to detect **variability** issues.
  - ▶ Record the **bias**.
  - ▶ Calculate the **coverage**.
- 
- ▶ **Imputation is not prediction.**<sup>7</sup>

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<sup>7</sup>van Buuren, 2018

## REFERENCES AND QUESTIONS

THANK YOU FOR LISTENING, ANY QUESTIONS? <sup>8</sup>

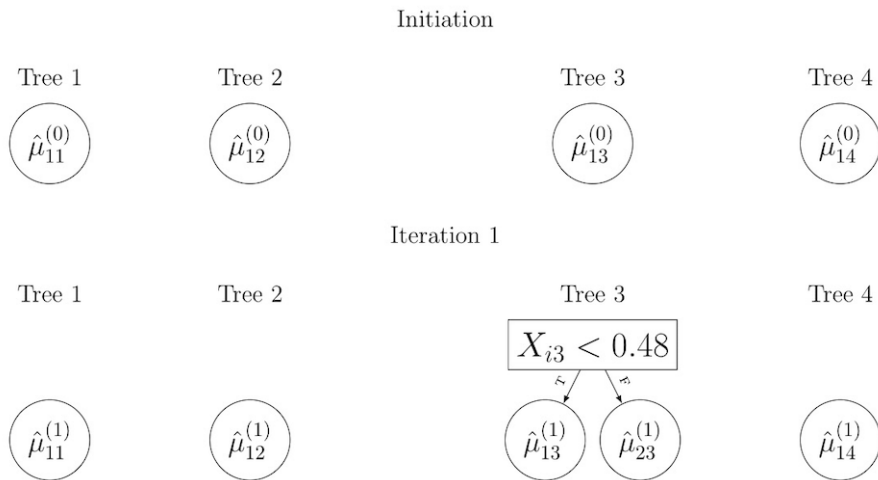
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<sup>8</sup><https://github.com/toddburrows>

## APPENDIX

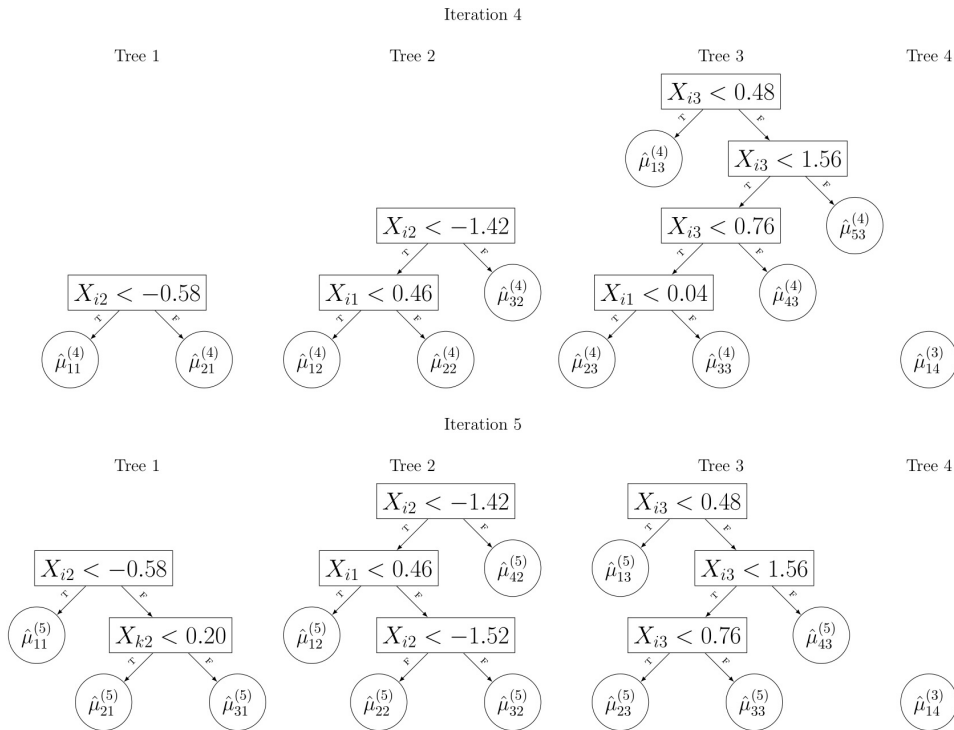
### APPENDIX A: THE BART MCMC CYCLE



**Figure.** Initialisation and Iteration 1 of a BART model. Extracted from [Tan and Roy, 2019](#)

# APPENDIX

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**Figure.** Iteration 4 and 5 of a BART model. Extracted from [Tan and Roy, 2019](#)