

1. Bo invested \$15000, part at $9\frac{1}{4}\%$ simple interest and the remaining part at $11\frac{1}{2}\%$ simple interest. After one year the total interest earned was \$1623.75. How many dollars were invested at 9.25%?

- a) 4400 b) 4500 c) 4600 d) 4700 e) None of these

2. Burger Barn sells 3 drinks for every 2 burgers. Drinks are \$.70 and burgers are \$1.30. If Burger Barn wants to take in as close to \$200 as possible, how many drinks must be sold? Assume the number of drinks and burgers sold must be positive integers.

- a) 120 b) 123 c) 126 d) 129 e) None of these

3. Find the ratio of 10 kilometers to 4 miles. Assume 1 inch = 2.54 cm. Round the final answer to the nearest 0.0001.

- a) 1.5531 b) 1.5532 c) 1.5533 d) 1.5534 e) None of these

4. You mix 30% acid solution with 50% acid solution to make 100 pints of 43% acid solution. How many pints of the 30% acid solution are needed?

- a) 35 b) 45 c) 55 d) 65 e) None of these

5. Find $y - x$ whenever $\frac{2}{x} + \frac{3}{y} = 4$ and $\frac{5}{x} + \frac{6}{y} = 5$.

- a) $\frac{11}{30}$ b) $\frac{13}{30}$ c) $\frac{17}{30}$ d) $\frac{19}{30}$ e) None of these

6. One plane leaves the airport at noon heading east at x mph. Another plane leaves the same airport heading west 30 minutes later at y mph. At 3 p.m., the two planes are 1800 miles apart. At 5 p.m., the two planes are 3100 miles apart. Find $x - y$.

- a) 48 b) 49 c) 50 d) 51 e) None of these

7. All of the outside surfaces of a cylindrical tank are to be painted. The tank is 10 meters tall and the circular bases have a diameter of 15 meters. How many quarts of paint are needed if one quart will cover 10 m^2 . Round answers to the nearest 0.001.

- a) 82.468 b) 82.467 c) 82.466 d) 82.465 e) None of these

8. Each exterior angle of a regular 50-gon is x° . Each exterior angle of a regular 40-gon is y° . A regular 30-gon has d distinct diagonals. Find $10x + 10y + d$.

- a) 567 b) 568 c) 569 d) 570 e) None of these

9. Given: $f(x) = \frac{x+8}{x}$, $g(x) = x^3 + 5$, and $g(f(-5)) = \frac{a}{b}$, where a and b are relatively prime positive integers. Find $a - b$.

- a) 471 b) 472 c) 473 d) 474 e) None of these

10. A crew of 80 men can do a job in 24 days. If the contractor increases the work force by $\frac{1}{2}$ and productivity is unchanged, how many days will be saved by adding the additional workers?

- a) 7.8 b) 8.0 c) 8.2 d) 8.4 e) None of these

11. There are red, white, and blue marbles in a jar. The ratio of white to blue is 4:5. The ratio of red to white is 2:3. If the red and blue total 322, how many marbles are in the jar?

- a) 490 b) 488 c) 486 d) 484 e) None of these

12. Find the volume of the sphere inscribed in a regular tetrahedron with total surface area $36\sqrt{3}$. Round to the nearest 0.0001 cubic unit.

- a) 7.6952 b) 7.6953 c) 7.6954 d) 7.6955 e) None of these

13. If A men can do B jobs in C days, how long should it take D fewer men to do E jobs. Assume $A > D$.

- a) $AB^{-1}CE(A-D)^{-1}$ days b) $ABCE^{-1}(A-D)^{-1}$ days
c) $A^{-1}BC^{-1}E(A-D)^{-1}$ days d) $AB^{-1}C^{-1}E(A-D)^{-1}$ days e) None of these

14. Find $12(m+b)$ where $y = mx + b$ is the equation of the line tangent to $(x-3)^2 + (y+8)^2 = 169$ at the point $(8, -20)$.

- a) -273 b) -274 c) -275 d) -276 e) None of these

15. The hyperbola $16x^2 = 36y^2 + 1$ has asymptote $y = \pm mx$ and foci $\left(\pm\sqrt{\frac{a}{b}}, 0\right)$ where a and b are relatively prime positive integers and $m > 0$. Find $b - 10a + 12m$.

- a) 22 b) 23 c) 24 d) 25 e) None of these

16. $\cos\left(\text{Arc tan } \frac{15}{8} - \text{Arc sin } \frac{7}{25}\right) = \frac{a}{b}$, where a and b are relatively prime positive integers. Find $b - a$.

- a) 127 b) 128 c) 129 d) 130 e) None of these

17. The product of the 3 solutions of $2\sin x = 1 + \csc x$ on $0 \leq x < 2\pi$ is $\frac{a}{b}\pi^3$ where a and b are relatively prime positive integers. Find $a + b$.

- a) 146 b) 147 c) 148 d) 149 e) None of these

18. All of the points on the graph of $y = 2x + 3$ are rotated 90° counter clockwise with the origin as the center of each rotation. $y = mx + b$ is the equation of the new graph formed. Find $m + b$.

- a) -5 b) -4 c) -3 d) -2 e) None of these

19. Find the area enclosed by $r = \cos 3\theta$.

- a) $.2\pi$ b) $.25\pi$ c) $.3\pi$ d) $.\bar{3}\pi$ e) None of these

20. Find the length of the arc of $4x = y^2$ between the y-axis and the line containing the latus rectum. Round to the nearest .0001.

- a) 4.5912 b) 4.5913 c) 4.5914 d) 4.5915 e) None of these

21. $\frac{d}{dx} \int_{x^2}^{17} \sqrt{\cos \theta} d\theta$

- a) $2x\sqrt{\cos x}$ b) $2x\sqrt{\cos x^2}$ c) $-2x\sqrt{\cos x}$ d) $-2x\sqrt{\cos x^2}$ e) None of these

22. Find the area of the ellipse $\begin{cases} x = 5 \cos \theta \\ y = 6 \sin \theta \end{cases}$

- a) 26π b) 27π c) 28π d) 29π e) None of these

23. Find the average value of $\cos x$ for $\frac{\pi}{3} \leq x \leq \frac{\pi}{2}$.

- a) $\frac{1}{\pi}$ b) $\frac{1}{4}$
c) $3\pi^{-1}(2 - \sqrt{3})$ d) $\frac{2}{3\pi}$ e) None of these

24. Find the area between the curve $y = (x^2 - 1)(x^2 + 1)^{-1}$ and its horizontal asymptote.

- a) π b) 1.5π c) 2π d) 2.5π e) None of these

Solutions

1. B
2. D
3. D
4. A
5. D
6. C
7. B
8. A
9. C
10. B
11. A
12. B
13. A
14. C
15. A
16. B
17. D
18. D
19. B
20. A
21. D
22. E
23. C
24. C