

Autoencoders - an Introduction

What they are and what you can do with them

Umberto Michelucci¹

¹ Presenting author, umberto.michelucci@hslu.ch

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Lucerne University of
Applied Sciences and Arts

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- ## Anomaly Detection

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You can find a complete discussion at [1]
<https://arxiv.org/pdf/2201.03898.pdf>

GitHub:
<https://github.com/toelt-llc/ETH-ZURICH-GDSC-WORKSHOPS-2022>

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 y_i indicate the expected value or label.

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Now suppose we have only unlabelled observations. We have only a training dataset S_T with M observations:

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 y_i indicate the expected value or label.

$$S_T = \{\mathbf{x}_i \mid i = 1, \dots, M\} \quad \text{with } \mathbf{x}_i \in \mathbb{R}^n$$

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If you have problems imagining what that means, think of having a dataset made of images. An autoencoder would be an algorithm that can give as output an image that is as similar as possible to the input one.

¹https://web.stanford.edu/class/psych209a/ReadingsByDate/02_06/PDPVolIChapter8.pdf

We humans do not certainly learn to write by filling pixels with gray values.

Structure of an autoencoder

The structure of an autoencoder looks typically like this

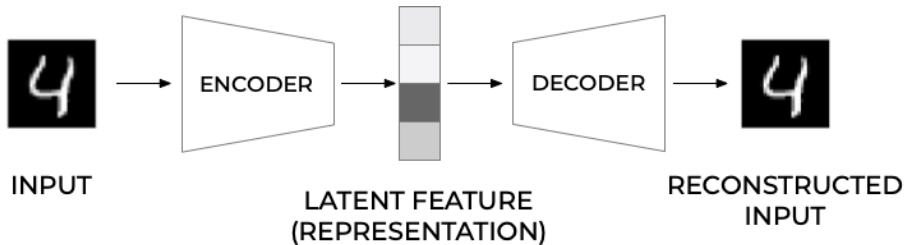


Figure: The typical structure of an autoencoder.

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- 1 To enforce \mathbf{h}_i to be useful, we impose that it must be of lower dimension than \mathbf{x}_i ;
- 2 The fact that the dimension of \mathbf{h}_i is lower than that of \mathbf{x}_i is called a **bottleneck**.

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Example of bottleneck

A diagram of a bottleneck with Feed Forward Neural Networks is the following

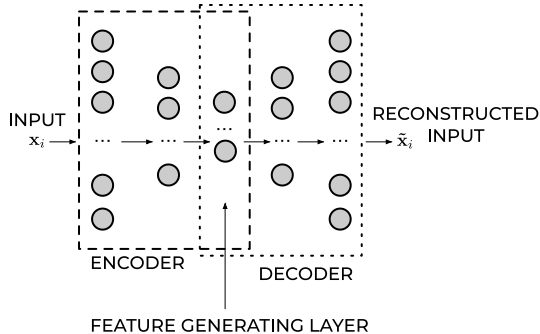


Figure: A typical architecture of a Feed-Forward Autoencoder. The number of neurons in the layers at first goes down as we move through the network until it reaches the middle and then starts to grow again until the last layer has the same number of neurons as the input dimensions.

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The encoder can reduce the number of dimensions of the input observation (n) and create a learned representation (\mathbf{h}_i) of the input that has a smaller dimension $q < n$. This learned representation is enough for the decoder to reconstruct the input accurately (if the autoencoder training was successful as intended).

Loss Functions

For autoencoders one can use both typical loss functions:

- 1 MSE
- 2 Cross-entropy

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$$\text{RE} = \text{MSE} = \frac{1}{M} \sum_{i=1}^M |\mathbf{x}_i - \tilde{\mathbf{x}}_i|^2 \quad (3)$$

Reconstruction Error - an example

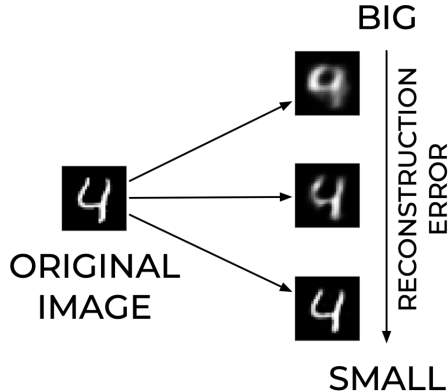


Figure: An example of big and small reconstruction error when an autoencoder tries to reconstruct an image.

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Table: the different in accuracy and running time when applying the kNN algorithm to the original 784 features or the 8 latent features for the MNIST dataset.

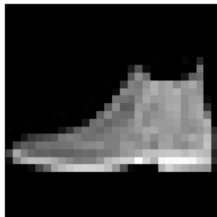
Table: the difference in accuracy and running time when applying the kNN algorithm to the original 784 features with a FFA with 8 neurons and with a FFA with 16 neurons for the Fashion MNIST dataset.

Anomaly Detection

- 1 We consider an autoencoder with only three layers with 784 neurons in the first, 64 in the latent feature generation layer, and again 784 neurons in the output layer;
- 2 We will train it with the MNIST dataset and in particular with the 60000 training portion of it;
- 3 Let us choose an image of a shoe from this dataset and add it to the testing portion of the MNIST dataset (that now will have 10001 images).

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Anomaly Detection - how the autoencoder reconstruct the shoe

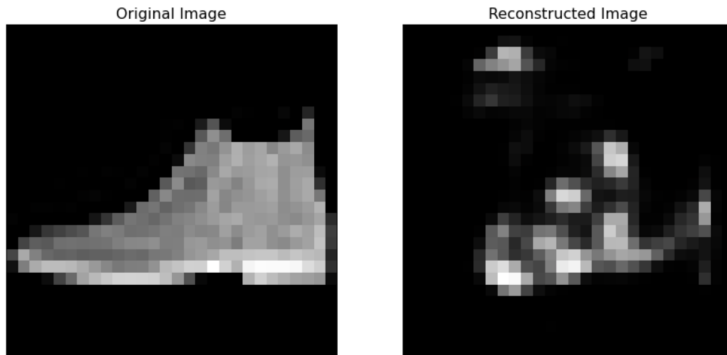


Figure: The shoe and the autoencoder's reconstruction trained on the 60000 hand-written images of the MNIST dataset. This image has the biggest RE in the entire 10001 test dataset we built with a value of 0.062.

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