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1 Data Structures

1.1 Bitmasks

1.2 Union-Find Disjoint Sets

```
struct DisjointSets{
   void addelements(int num){
     while (num--)
        s.push_back(-1);
   int find(int elem) {
     return s[elem] < 0 ? elem : s[elem] = find(s[elem]);</pre>
   void setunion(int a, int b) {
     int root1 = find(a), root2 = find(b);
     int newSize = s[root1] + s[root2];
     if (s[root1] <= s[root2]){</pre>
        s[root2] = root1;
        s[root1] = newSize;
     }
     else{
        s[root1] = root2;
        s[root2] = newSize;
     }}
   vector<int> s;
};
```

1.3 Segment Tree

```
// Segment tree for range sum queries.
struct segment_tree {
   vector<long long> st, lazy;
   const vector<long long> &A;
   size_t n;
   inline int left(int p) { return p << 1;}</pre>
   inline int right(int p) { return (p << 1) + 1; }</pre>
   void propagate(int p, int L, int R) {
       if (lazy[p] != 0) {
          if (L != R) {
              lazy[left(p)] += lazy[p];
              lazy[right(p)] += lazy[p];
          }
          st[p] += (R - L + 1) * lazy[p];
          lazv[p] = 0;
       }}
   void build(int p, int L, int R) {
       if (L == R)
          st[p] = A[L];
       else {
          build(left(p), L, (L + R) / 2);
          build(right(p), (L + R) / 2 + 1, R);
          st[p] = st[left(p)] + st[right(p)];
   long long update(int p, int L, int R, int i, int j, long
       long val) {
       propagate(p, L, R);
       if (L > j || R < i)
          return st[p];
       if (L >= i && R <= j) {
          lazv[p] = val;
          propagate(p, L, R);
          return st[p];
       return st[p] = update(left(p), L, (L + R) / 2, i, j,
           val) +
                    update(right(p), (L + R) / 2 + 1, R, i, j,
                        val);
```

```
long long query(int p, int L, int R, int i, int j) {
   if (L > j || R < i)
       return 0;
   propagate(p, L, R);
   if (L >= i && R <= j)
       return st[p];
   return query(left(p), L, (L + R) / 2, i, j) +
         query(right(p), (L + R) / 2 + 1, R, i, j);
segment_tree(const vector<long long> &_A): A(_A) {
   n = A.size();
   st.assign(n * 4, 0);
   lazy.assign(n * 4, 0);
   build(1, 0, n - 1);
void update(int i, int j, long long val) {
   update(1, 0, n - 1, i, j, val);
long long query(int i, int j) {
   return query(1, 0, n - 1, i, j);
}};
```

1.4 Fenwick Tree

```
#define LSOne(S) (S & (-S))
class FenwickTree {
private:
 vi ft;
public:
 FenwickTree() {}
 // initialization: n + 1 zeroes, ignore index 0
 FenwickTree(int n) { ft.assign(n + 1, 0); }
 int rsq(int b) {
                                               // returns
     RSQ(1, b)
   int sum = 0; for (; b; b -= LSOne(b)) sum += ft[b];
   return sum; }
 int rsq(int a, int b) {
                                               // returns
      RSQ(a, b)
```

1.5 Treap

```
template<typename T>
struct treap{
   treap(){
      srand(time(0));
      root = nullptr;
   void insert(const T& elem){
      insert(root, elem);
   void remove(const T& elem){
      remove(root, elem);
   struct node_t{
      T elem;
      shared_ptr<node_t> left, right;
      int priority;
   };
   shared_ptr<node_t> root;
   shared_ptr<node_t> rotateLeft(shared_ptr<node_t> node){
      shared_ptr<node_t> right = node->right, rightLeft =
           right->left;
      right->left = node;
      node->right = rightLeft;
      return right;
   }
   shared_ptr<node_t> rotateRight(shared_ptr<node_t> node){
      shared_ptr<node_t> left = node->left, leftRight =
```

```
left->right;
   left->right = node;
   node->left = leftRight;
   return left;
}
void insert(shared_ptr<node_t>& node, const T& elem){
   if (node == nullptr){
       node = make_shared<node_t>();
       node->elem = elem;
       node->left = node->right = nullptr;
       node->priority = rand();
       return;
   // We do not allow multiple keys with the same value
   if (node->elem == elem)
       return;
   if (node->elem > elem){
       insert(node->left, elem);
       if (node->priority < node->left->priority)
          node = rotateRight(node);
   }else{
       insert(node->right, elem);
       if (node->priority < node->right->priority)
          node = rotateLeft(node);
   }}
void remove(shared_ptr<node_t>& node, const T& elem){
   if (node == nullptr)
       return;
   if (node->elem == elem){
       if (!node->left && !node->right)
          node = nullptr;
       // Keep rotating until the node to be deleted becomes
           a leaf node.
       else if (!node->left || (node->left && node->right &&
          node->left->priority < node->right->priority)){
          node = rotateLeft(node);
          remove(node->left, elem);
       }
       else{
```

```
node = rotateRight(node);
    remove(node->right, elem);
}
else if (node->elem > elem)
    remove(node->left, elem);
else
    remove(node->right, elem);
};
```

1.6 Splay

```
const int maxNodeCnt = 111111;
int nodeCnt, root, type[maxNodeCnt], parent[maxNodeCnt],
    childs[maxNodeCnt][2],
   size[maxNodeCnt], stack[maxNodeCnt], reversed[maxNodeCnt];
// ...
void clear() {
   root = 0;
   size[0] = 0;
   nodeCnt = 1;
int malloc() {
   type[nodeCnt] = 2;
   childs[nodeCnt][0] = childs[nodeCnt][1] = 0;
   size[nodeCnt] = 1;
   reversed[nodeCnt] = 0;
   return nodeCnt ++;
void update(int x) {
   size[x] = size[childs[x][0]] + 1 + size[childs[x][1]];
   // ...
}
void pass(int x) {
   // NOTICE: childs[x][i] == 0
   if (reversed[x]) {
       swap(childs[x][0], childs[x][1]);
       type[childs[x][0]] = 0;
       reversed[childs[x][0]] ^= 1;
```

```
type[childs[x][1]] = 1;
       107reversed[childs[x][1]] ^= 1;
      reversed[x] = 0;
   }
   // ...
}
void rotate(int x) {
   int t = type[x],
   y = parent[x],
   z = childs[x][1 - t];
   type[x] = type[y];
   parent[x] = parent[y];
   if (type[x] != 2) {
       childs[parent[x]][type[x]] = x;
   type[y] = 1 - t;
   parent[y] = x;
   childs[x][1 - t] = y;
   if (z) {
      type[z] = t;
      parent[z] = y;
   childs[y][t] = z;
   update(y);
void splay(int x) {
   int stackCnt = 0;
   stack[stackCnt ++] = x;
   for (int i = x; type[i] != 2; i = parent[i]) {
       stack[stackCnt ++] = parent[i];
   for (int i = stackCnt - 1; i > -1; -- i) {
       pass(stack[i]);
   while (type[x] != 2) {
      int y = parent[x];
      if (type[x] == type[y]) {
          rotate(y);
      } else {
          rotate(x);
```

```
if (type[x] == 2) {
          break;
          108}
       rotate(x);
   }
   update(x);
}
int find(int x, int rank) {
   while (true) {
       pass(x);
       if (size[childs[x][0]] + 1 == rank) {
          break;
       }
       if (rank <= size[childs[x][0]]) {</pre>
          x = childs[x][0];
       } else {
          rank -= size[childs[x][0]] + 1;
          x = childs[x][1];
       }
   }
   return x;
void split(int &x, int &y, int a) {
   // NOTICE: x, y != 0
   y = find(x, a + 1);
   splay(y);
   x = childs[y][0];
   type[x] = 2;
   childs[y][0] = 0;
   update(y);
void split3(int &x, int &y, int &z, int a, int b) {
   split(x, z, b);
   split(x, y, a - 1);
void join(int &x, int y) {
   // NOTICE x, y != 0
   x = find(x, size[x]);
   splay(x);
```

```
childs[x][1] = v;
   type[y] = 1;
   parent[y] = x;
   109update(x);
void join3(int &x, int y, int z) {
   join(y, z);
   join(x, y);
int getRank(int x) {
   splay(x);
   root = x;
   return size[childs[x][0]];
void reverse(int a, int b) {
   int x, y;
   split3(root, x, y, a + 1, b + 1);
   reversed[x] ^= 1;
   join3(root, x, y);
```

1.7 Trie

```
const int maxnode = 4000 * 100 + 10;
const int sigma_size = 26;

// This template use unnecessary large memory.
// should replace ch[maxnode][sigma_size] by vector<node>.
struct Trie {
  int ch[maxnode][sigma_size];
  int val[maxnode];
  int sz; // the number of node
  void clear() { sz = 1; memset(ch[0], 0, sizeof(ch[0])); }
  int idx(char c) { return c - 'a'; }

// insert string s, with additional information v
  // v has to be non-zero, zero means "this node is not word node"
  void insert(const char *s, int v) {
```

```
int u = 0, n = strlen(s);
for(int i = 0; i < n; i++) {
  int c = idx(s[i]);
  if(!ch[u][c]) { // the node not exist
    memset(ch[sz], 0, sizeof(ch[sz]));
  val[sz] = 0;
  ch[u][c] = sz++;
  }
  u = ch[u][c]; // going down
}
val[u] = v;
}};</pre>
```

1.8 Kth Element

```
const int D = 18;
const int N = 100000;
int n, value[N], rank[N], order[D][N], pos[D][N];
long long sum[D][N];
pair <int, int> backup[N];
void build (int d, int l, int r) {
   if (r - 1 > 1) {
       int m = (1 + r) >> 1,
          curLeft = 1,
          curRight = m;
      for (int i = 1; i < r; ++ i) {
          if (rank[order[d][i]] < m) {</pre>
              order[d + 1][curLeft ++] = order[d][i];
          }else{
              order[d + 1][curRight ++] = order[d][i];
          }
          pos[d][i] = curLeft;
       build(d + 1, 1, m);
       build(d + 1, m, r);
   sum[d][r-1] = value[order[d][r-1]];
   for (int i = r - 2; i \ge 1; -- i) {
       sum[d][i] = value[order[d][i]] + sum[d][i + 1];
```

```
}
// [1, r) [a, b) k-th sum
long long query (int d, int l, int r, int a, int b, int k) {
   if (k) {
       if (r - 1 == 1) {
          return sum[d][a];
       }
       int m = (1 + r) >> 1,
          posBegin = pos[d][a];
       if (rank[order[d][a]] < m) {</pre>
          posBegin -= 1;
       int posEnd = pos[d][b - 1],
       posCnt = posEnd - posBegin;
       if (k < posCnt) {</pre>
          return query(d + 1, 1, m, posBegin, pos[d][b - 1], k);
#define RIGHT(i) m + i + 1 - pos[d][i]
       int rightBegin = RIGHT(a);
       if (rank[order[d][a]] >= m) {
          rightBegin -= 1;
       }
       long long result = (posBegin < m? sum[d + 1][posBegin]:</pre>
           0) - (posEnd <
              m? sum[d + 1][posEnd]: 0);
       result += query(d + 1, m, r, rightBegin, RIGHT(b - 1), k
           - posCnt);
#undef RIGHT
       return result;
   }
   return 0;
}
void clear () {
   for (int i = 0; i < n; ++ i) {
       order[0][i] = i;
   build(0, 0, n);
int main(){
```

```
std::ios::sync with stdio(false);
int testCount;
scanf("%d", &testCount);
for(int t = 1; t <= testCount; ++ t){</pre>
   std::cout << "Case #" << t << ":\n";
   scanf("%d", &n);
   for(int i = 0; i < n; ++ i){
       scanf("%d", value + i);
       backup[i] = std::make_pair(value[i], i);
   std::sort(backup, backup + n);
   for(int i = 0; i < n; ++ i){
       rank[backup[i].second] = i;
   }
   int m;
   scanf("%d", &m);
   while(m --){
       int a, b;
       scanf("%d%d", &a, &b);
       b ++:
       int length = b - a;
       long long result = sum[0][a] - (b < n? sum[0][b]: 0);
       result -= query(0, 0, n, a, b, (length + 1) >> 1);
       result -= query(0, 0, n, a, b, length >> 1);
       std::cout << result << "\n";</pre>
   }
   std::cout << "\n";
}
return 0;
```

2 Graph Theory

2.1 Articulation Points and Bridges

```
vi dfs_low;    // additional information for articulation
    points/bridges/SCCs
vi articulation_vertex;
int dfsNumberCounter, dfsRoot, rootChildren;
int DFS_WHITE = -1; // unvisited
```

}

```
void articulationPointAndBridge(int u) {
 dfs_low[u] = dfs_num[u] = dfsNumberCounter++; // dfs_low[u]
      <= dfs num[u]
 for (int j = 0; j < (int)AdjList[u].size(); j++) {</pre>
   ii v = AdjList[u][j];
   if (dfs_num[v.first] == DFS_WHITE) {
                                                         // a
        tree edge
     dfs_parent[v.first] = u;
     if (u == dfsRoot) rootChildren++; // special case, count
         children of root
     articulationPointAndBridge(v.first);
                                                // for
     if (dfs_low[v.first] >= dfs_num[u])
         articulation point
       articulation vertex[u] = true;
                                           // store this
           information first
     if (dfs_low[v.first] > dfs_num[u])
                                                          // for
         bridge
       printf(" Edge (%d, %d) is a bridge\n", u, v.first);
     dfs_low[u] = min(dfs_low[u], dfs_low[v.first]); // update
         dfs low[u]
   else if (v.first != dfs_parent[u]) // a back edge and not
        direct cycle
     dfs_low[u] = min(dfs_low[u], dfs_num[v.first]); // update
         dfs_low[u]
} }
//inside int main()
 printThis("Articulation Points & Bridges (the input graph
      must be UNDIRECTED)");
 dfsNumberCounter = 0; dfs_num.assign(V, DFS_WHITE);
      dfs low.assign(V, 0);
  dfs_parent.assign(V, -1); articulation_vertex.assign(V, 0);
 printf("Bridges:\n");
 for (int i = 0; i < V; i++)
   if (dfs_num[i] == DFS_WHITE) {
     dfsRoot = i; rootChildren = 0;
```

2.2 Tarjan's Algorithm

```
vi S, visited;
                                           // additional global
    variables
int numSCC;
void tarjanSCC(int u) {
 dfs low[u] = dfs num[u] = dfsNumberCounter++; // dfs low[u]
      <= dfs num[u]
 S.push_back(u);
                        // stores u in a vector based on order
     of visitation
 visited[u] = 1:
 for (int j = 0; j < (int)AdjList[u].size(); j++) {</pre>
   ii v = AdjList[u][j];
   if (dfs_num[v.first] == DFS_WHITE)
     tarjanSCC(v.first);
   if (visited[v.first])
                                                  // condition
       for update
     dfs_low[u] = min(dfs_low[u], dfs_low[v.first]);
 }
 if (dfs_low[u] == dfs_num[u]) { // if this is a root
      (start) of an SCC
   printf("SCC %d:", ++numSCC);
                                      // this part is done
       after recursion
   while (1) {
     int v = S.back(); S.pop_back(); visited[v] = 0;
     printf(" %d", v);
     if (u == v) break;
   printf("\n");
```

2.3 Bipartite Graph Check

```
queue<int> q; q.push(s);
vi color(V, INF); color[s] = 0;
bool isBipartite = true;
while (!q.empty() & isBipartite){
  int u = q.front(); q.pop();
  for (int j = 0; j < (int)AdjList[u].size(); j++){
    ii v = AdjList[u][j];
    if (color[v.first] == INF){
      color[v.first] = 1 - color[u];
      q.push(v.first);}
  else if (color[v.first] == color[u]){
    isBipartite = false; break;}}</pre>
```

2.4 Kruskal's Algorithm

```
sort(EdgeList.begin(), EdgeList.end()); // sort by edge
    weight O(E log E)
                 // note: pair object has built-in comparison
                     function
int mst cost = 0;
UnionFind UF(V):
                                // all V are disjoint sets
    initially
for (int i = 0; i < E; i++) {
                                           // for each edge,
  pair<int, ii> front = EdgeList[i];
  if (!UF.isSameSet(front.second.first, front.second.second))
      { // check
   mst_cost += front.first;
                                      // add the weight of e
        to MST
   UF.unionSet(front.second.first, front.second.second); //
        link them
} }
                      // note: the runtime cost of UFDS is
    very light
// note: the number of disjoint sets must eventually be 1 for
    a valid MST
printf("MST cost = %d (Kruskal's)\n", mst_cost);
```

2.5 Prim's Algorithm

```
// inside int main() --- assume the graph is stored in AdjList,
    pq is empty
 taken.assign(V, 0);
                                // no vertex is taken at the
     beginning
 process(0); // take vertex 0 and process all edges incident
      to vertex 0
 mst cost = 0:
 while (!pq.empty()) { // repeat until V vertices (E=V-1
      edges) are taken
   ii front = pq.top(); pq.pop();
   u = -front.second, w = -front.first; // negate the id and
       weight again
   if (!taken[u])
                              // we have not connected this
       vertex vet
     mst_cost += w, process(u); // take u, process all edges
         incident to u
 }
                                     // each edge is in pg only
      once!
 printf("MST cost = %d (Prim's)\n", mst_cost);
```

2.6 Dijkstra's Algorithm

```
// Dijkstra routine
vi dist(V, INF); dist[s] = 0;
                                           // INF = 1B to
    avoid overflow
priority_queue< ii, vector<ii>, greater<ii> > pq;
    pq.push(ii(0, s));
                       // ^to sort the pairs by increasing
                            distance from s
                                                          11
while (!pq.empty()) {
    main loop
 ii front = pq.top(); pq.pop(); // greedy: pick shortest
      unvisited vertex
 int d = front.first, u = front.second;
 if (d > dist[u]) continue; // this check is important, see
      the explanation
 for (int j = 0; j < (int)AdjList[u].size(); j++) {</pre>
   ii v = AdjList[u][j];
                                          // all outgoing
       edges from u
```

2.7 Bellman Ford's Algorithm

```
// Bellman Ford routine
vi dist(V, INF); dist[s] = 0;
for (int i = 0; i < V - 1; i++) // relax all E edges V-1
    times, overall O(VE)
for (int u = 0; u < V; u++) // these two
    loops = O(E)
  for (int j = 0; j < (int)AdjList[u].size(); j++) {
    ii v = AdjList[u][j]; // we can record SP spanning
        here if needed
    dist[v.first] = min(dist[v.first], dist[u] + v.second);
        // relax
}</pre>
```

2.8 Floyd Warshall's Algorithm

```
for (int k = 0; k < V; k++) // common error: remember that
    loop order is k->i->j
for (int i = 0; i < V; i++)
    for (int j = 0; j < V; j++)
    AdjMatrix[i][j] = min(AdjMatrix[i][j], AdjMatrix[i][k] +
        AdjMatrix[k][j]);</pre>
```

2.9 Shortest Path Faster Algorithm

```
// SPFA from source S
// initially, only S has dist = 0 and in the queue
vi dist(n, INF); dist[S] = 0;
queue<int> q; q.push(S);
vi in_queue(n, 0); in_queue[S] = 1;
```

```
while (!q.empty()) {
  int u = q.front(); q.pop(); in_queue[u] = 0;
  for (j = 0; j < (int)AdjList[u].size(); j++) { // all
    outgoing edges from u
  int v = AdjList[u][j].first, weight_u_v =
        AdjList[u][j].second;
  if (dist[u] + weight_u_v < dist[v]) { // if can relax
        dist[v] = dist[u] + weight_u_v; // relax
        if (!in_queue[v]) { // add to the queue only if it's
            not in the queue
        q.push(v);
        in_queue[v] = 1;
    }}}</pre>
```

2.10 Network Flow

```
void augment(int v, int min_edge){
   if (v == s){
      flow = min_edge;
      return;
   else if (parent[v] != -1){
      int u = parent[v];
       augment(u, min(min_edge, residue[u][v]));
      residue[u][v] -= flow;
      residue[v][u] += flow;
   }}
void Dinic(){
   max_flow = 0;
   while (true){
      parent.assign(V, -1);
      vector<bool> visited(V, false);
       queue<int> q;
      q.push(s);
      visited[s] = true;
       while (!q.empty()){
          int u = q.front();
          q.pop();
```

```
if (u == t)
          break;
       for (int v : adjList[u])
          if (!visited[v] && residue[u][v] > 0){
              parent[v] = u;
              visited[v] = true;
              q.push(v);
          }}
   int new flow = 0;
   for (int u : adjList[t]){
       if (residue[u][t] <= 0)</pre>
          continue:
       flow = 0:
       augment(u, residue[u][t]);
       residue[u][t] -= flow;
       residue[t][u] += flow;
       new flow += flow;
   }
   if (new_flow == 0)
       break:
   max_flow += new_flow;
}}
```

2.11 Euler Tour

2.12 Max Cardinality Bipartite Matching

```
int N, M, P, limit;
#define MAXN 50500
#define MAXE 150500
int pair_left[MAXN], pair_right[MAXN], dist_left[MAXN],
    dist right[MAXN];
bool visited[MAXN];
int adjlist[MAXN];
int node[MAXE];
int link[MAXE];
bool BFS() {
   queue<int> q;
   memset(dist_right, -1, sizeof dist_right);
   memset(dist_left, -1, sizeof dist_left);
   for (int i = 0; i < N; i++) {
      if (pair left[i] == -1) {
          dist left[i] = 0;
          q.push(i);
      }}
   limit = INT_MAX;
   while (!q.empty()) {
      int u = q.front();
      q.pop();
      if (dist left[u] > limit)
      for (int i = adjlist[u]; i != -1; i = link[i]) {
          int v = node[i];
          if (dist_right[v] == -1) {
              dist_right[v] = dist_left[u] + 1;
              if (pair_right[v] == -1)
                 limit = dist_right[v];
              else {
                 dist_left[pair_right[v]] = dist_right[v] + 1;
                 q.push(pair_right[v]);
              }}}}
   return limit != INT_MAX;
}
bool DFS(int u) {
```

```
for (int i = adjlist[u]; i != -1; i = link[i]) {
      int v = node[i];
      if (!visited[v] && dist_right[v] == dist_left[u] + 1) {
          visited[v] = true;
          if (pair_right[v] != -1 && dist_right[v] == limit)
             continue:
          if (pair_right[v] == -1 || DFS(pair_right[v])) {
             pair_right[v] = u;
             pair left[u] = v;
             return true;
          }}}
   return false;
int main() {
   scanf("%d %d %d", &N, &M, &P);
   memset(pair_left, -1, sizeof pair_left);
   memset(pair_right, -1, sizeof pair_right);
   memset(link, -1, sizeof link);
   memset(adjlist, -1, sizeof adjlist);
   for (int i = 0; i < P; i++) {
      int u, v;
      scanf("%d %d", &u, &v);
      node[i] = v - 1;
      link[i] = adjlist[u - 1];
      adjlist[u - 1] = i;
   int matching = 0;
   while (BFS()) {
      memset(visited, 0, sizeof visited);
      for (int i = 0; i < N; i++)
          if (pair_left[i] == -1)
             if (DFS(i))
                 matching++;
   printf("%d\n", matching);
   return 0;
```

2.13 Min-Cost Flow

```
const int inf = 1000000000;
int s, t, node, totalCost;
vector<int> head, dist, vtx, next, c, cost;
vector<bool> vis:
void resize(vector<T> &a, int size, T init) //设大小、初始值
void init(int source, int target, int nodeCount)
    //初始化,记得清空
void add(int a, int b, int cc, int cst) //双向加边
void spfa() {
  resize(vis, node, false); resize(dist, node, -inf);
  queue<int> q; q.push(t); vis[t]=true; dist[t]=0;
  while (q.size()) {
     int u = q.front(); q.pop();
     vis[u] = false;
     for (int p = head[u]; p != -1; p = next[p]) {
       if (c[p ^ 1] && dist[u] + cost[p ^ 1] > dist[vtx[p]]) {
          dist[vtx[p]] = dist[u] + cost[p ^ 1];
          if (!vis[vtx[p]]) {
            vis[vtx[p]] = true; q.push(vtx[p]);
             if (dist[q.back()] < dist[q.front()]) {</pre>
               swap(q.front(), q.back());
}}}}}
int dfs(int u, int limit) {
  if (u == t) {
     totalCost += limit * dist[s];
     return limit;
  int current = 0;
  vis[u] = true;
  for (int p = head[u]; p != -1; p = next[p]) {
     if (c[p] && !vis[vtx[p]] && dist[vtx[p]] + cost[p] ==
         dist[u]) {
       int delta = dfs(vtx[p], min(limit - current, c[p]));
       c[p] = delta; c[p ^ 1] += delta;
       current += delta;
```

```
if (current == limit) {
          break;
       }
     }
  }
  return current;
inline bool adjust() {
  int maxi = -inf;
  for (int i = 0; i < node; ++ i) {
     if (vis[i]) {
       for (int p = head[i]; p != -1; p = next[p]) {
          if (c[p] && !vis[vtx[p]]) {
             assert(dist[vtx[p]] + cost[p] != dist[i]);
             maxi = max(maxi, dist[vtx[p]] + cost[p] - dist[i]);
          }
       }
     }
  if (maxi == -inf) {
     return false;
  for (int i = 0; i < node; ++ i) {
     if (vis[i]) {
       dist[i] += maxi;
     }
  }
  return true;
int maxCostFlow() {
  spfa();
  totalCost = 0;
  do{
       resize(vis, node, false);
     }while (dfs(s, inf));
  }while (adjust());
  return totalCost;
```

3 Math

3.1 Sieve of Eratosthenes

```
#define BOUND 1000000
bitset<BOUND> bs;
vector<long long> primes;
void sieve() {
   bs.set();
   bs[0] = bs[1] = 0;
   for (long long i = 2; i <= BOUND; i++) {
      if (bs[i]) {
         for (long long j=i*i;j<=BOUND;j+=i) bs[j] = 0;
         primes.push_back(i);}
}}</pre>
```

3.2 Euler Phi function

```
int euler_phi(int n){
 int m = (int) sqrt(n+0.5);
 int ans = n;
 for(int i=2;i<=m;i++)</pre>
   if(n%i==0){
     ans = ans/i*(i-1);
     while(n\%i==0) n /= i;
  if (n>1) ans = ans/n*(n-1);
 return ans;}
void euler_phi_table(int n, int *phi){
 for(int i=2;i<=n;i++) phi[i] = 0;
  phi[1] = 1;
 for(int i=2;i<=n;i++)
   if(!phi[i])
     for(int j=i; j<=n; j+=i){</pre>
       if(!phi[j]) phi[j] = j;
       phi[j] = phi[j]/i*(i-1);
}}
```

3.3 GCD mod related (CRT)

```
//ax+by=gcd(a,b),min abs(x)+abs(y) x,y may be negative
void gcd(LL a, LL b, LL & d, LL & x, LL & y) {
 if(!b) { d = a; x = 1; y = 0; }
 else { gcd(b,a\%b,d,y,x); y=x*(a/b);}}
// calculate inv(a) mod n. If not exist, return -1
LL inv(LL a, LL n) {
 LL d, x, y; gcd(a, n, d, x, y);
 return d == 1 ? (x+n)%n : -1; }
// n functions: x=a[i] (mod m[i]) m[i] co-prime
LL CRT(int n, int * a, int * m) {
 LL M = 1, d, y, x = 0;
 for(int i=0;i<n;i++) M *= m[i];</pre>
 for(int i=0:i<n:i++) {</pre>
   LL w = M / m[i];
   gcd(m[i], w, d, d, y);
   x = (x + y*w*a[i]) % M;
 }
 return (x+M)%M;}
// solve a^x=b mod n. n prime. If no solution, return -1
int log_mod(int a, int b, int n) {
 int m, v, e = 1;
 m = (int) sqrt(n+0.5);
 v = inv(pow_mod(a, m, n), n);
 map<int, int> x; x[1] = 0;
 for(int i=1;i<m;i++) {</pre>
   e = mul_mod(e, a, n);
   if(!x.count(e)) x[e] = i;
 for(int i=0;i<m;i++) {</pre>
   if(x.count(b)) return i*m + x[b];
   b = mul_mod(b, v, n);
 return -1;}
```

3.4 Enumerate Combination

```
const int maxn = 1000;
int com[maxn];
```

```
bool next_Com(int num, int k){ //0,1...num-1 choose k
   if(k == 0) return false;
   if(com[k-1]!=num-1){ com[k-1]++; return true;}
   int i;
   for(i=k-1;i>=0;i--)
        if(com[i]!=num-k+i) break;
   if(i==-1) return false;
   com[i]++;
   for(int j=i+1;j<k;j++)
        com[j] = com[i]+(j-i);
   return true; }
void makeFirstCom(int k){
   for(int i=0;i<k;i++) com[i] = i;
}</pre>
```

3.5 Gauss Elimination

```
const int maxn = 110;
typedef double Matrix[maxn][maxn];
// require matrix A invertible
// A is augmented matrix, A[i][n] = bi
// After execution, A[i][n] is the value of i-th variable
void gauss_elimination(Matrix A, int n) {
 int i, j, k, r;
 for (i=0; i<n; i++) {
   r = i;
   for (j=i+1; j<n; j++) {
     if (fabs(A[j][i]) > fabs(A[r][i])) r = j;
   if (r != i)
    for (j=0; j<=n; j++)
       swap(A[r][j], A[i][j]);
   for (j=n; j>=i; j--)
    for (k=i+1; k<n; ++k)
      A[k][j] -= A[k][i] / A[i][i] * A[i][j];
 for (i=n-1; i>=0; i--) {
   for (j=i+1; j<n; j++)
     A[i][n] -= A[j][n] * A[i][j];
```

```
A[i][n] /= A[i][i];
}}
```

3.6 FFT

```
const long double PI = acos(0.0) * 2.0;
typedef complex<double> CD;
inline void FFT(vector<CD> &a. bool inverse) {
 int n = a.size();
 for(int i = 0, j = 0; i < n; i++) {
   if(j > i) swap(a[i], a[j]);
   int k = n;
   while(j & (k >>= 1)) j &= ~k;
   j \mid = k;
 double pi = inverse ? -PI : PI;
 for(int step = 1; step < n; step <<= 1) {</pre>
   double alpha = pi / step;
   for(int k = 0; k < step; k++) {
     CD omegak = exp(CD(0, alpha*k));
     for(int Ek = k; Ek < n; Ek += step << 1) {</pre>
       int Ok = Ek + step;
       CD t = omegak * a[0k];
       a[0k] = a[Ek] - t;
       a[Ek] += t;
     }
   }
 if(inverse)
   for(int i = 0; i < n; i++) a[i] /= n;
inline vector<double> operator * (const vector<double>& v1,
    const vector<double>& v2) {
 int s1 = v1.size(), s2 = v2.size(), S = 2;
 while(S < s1 + s2) S <<= 1;
 vector<CD> a(S,0), b(S,0);
 for(int i = 0; i < s1; i++) a[i] = v1[i];
 FFT(a, false);
 for(int i = 0; i < s2; i++) b[i] = v2[i];
```

```
FFT(b, false);
for(int i = 0; i < S; i++) a[i] *= b[i];
FFT(a, true);
vector<double> res(s1 + s2 - 1);
for(int i = 0; i < s1 + s2 - 1; i++) res[i] = a[i].real();
return res;
} // 用FFT实现的快速多项式乘法
```

3.7 Simplex

```
//输入矩阵a描述线性规划的标准形式。a为m+1行n+1列,其中行0~m-1为不等式
//行m为目标函数(最大化),列0~n-1为变量0~n-1的系数,列n为常数项
//第i个约束为a[i][0]*x[0] + a[i][1]*x[1] + ... <= a[i][n]
//目标为max(a[m][0]*x[0] + a[m][1]*x[1] + ... +
                                                                 this->n = n;
    a[m][n-1]*x[n-1] - a[m][n])
                                                                 this->m = m;
//注意: 变量均有非负约束x[i] >= 0
const int maxm = 500; // 约束数目上限
const int maxn = 500; // 变量数目上限
const double INF = 1e100;
                                                                 for(;;) {
const double eps = 1e-10;
                                                                   int r, c;
struct Simplex {
                                                                   double p = 0;
 int n; // 变量个数
 int m; // 约束个数
                                                                   if(p < eps) {
 double a [maxm] [maxn]; // 输入矩阵
 int B[maxm], N[maxn]; // 算法辅助变量
 void pivot(int r, int c) {
                                                                        a[i][n]:
   swap(N[c], B[r]);
   a[r][c] = 1 / a[r][c];
                                                                    return 1;
   for(int j = 0; j \le n; j++) if(j != c) a[r][j] *= a[r][c];
                                                                   }
   for(int i = 0; i \le m; i++) if(i != r) {
                                                                   p = INF;
    for(int j = 0; j \le n; j++) if(j != c) a[i][j] -= a[i][c]
        * a[r][i];
    a[i][c] = -a[i][c] * a[r][c];
   }
 }
 bool feasible() {
                                                                   pivot(r, c);
   for(;;) {
                                                                 }}
    int r. c:
                                                              };
    double p = INF;
```

```
if(p > -eps) return true;
   p = 0;
   for(int i = 0; i < n; i++) if(a[r][i] < p) p = a[r][c = i];
   if(p > -eps) return false;
   p = a[r][n] / a[r][c];
   for(int i = r+1; i < m; i++) if(a[i][c] > eps) {
     double v = a[i][n] / a[i][c];
     if(v < p) \{ r = i; p = v; \}
   pivot(r, c);
//解有界返回1, 无解返回0, 无界返回-1。b[i]为x[i]的值, ret为目标函数的值
int simplex(int n, int m, double x[maxn], double& ret) {
 for(int i = 0; i < n; i++) N[i] = i;
 for(int i = 0; i < m; i++) B[i] = n+i;</pre>
 if(!feasible()) return 0;
   for(int i = 0; i < n; i++) if(a[m][i] > p) p = a[m][c = i];
     for(int i = 0; i < n; i++) if(N[i] < n) x[N[i]] = 0;
     for(int i = 0; i < m; i++) if(B[i] < n) x[B[i]] =
     ret = -a[m][n];
   for(int i = 0; i < m; i++) if(a[i][c] > eps) {
     double v = a[i][n] / a[i][c];
     if(v < p) \{ r = i; p = v; \}
   if(p == INF) return -1;
```

for(int i = 0; i < m; i++) if(a[i][n] < p) p = a[r = i][n];

3.8 Pell Function

```
//求x^2-ny^2=1的最小正整数根,n不是完全平方数
p[1]=1;p[0]=0; q[1]=0;q[0]=1; a[2]=(int)(floor(sqrt(n)+1e-7));
g[1]=0;h[1]=1;
for (int i=2;i;++i) {
  g[i]=-g[i-1]+a[i]*h[i-1]; h[i]=(n-sqr(g[i]))/h[i-1];
  a[i+1]=(g[i]+a[2])/h[i]; p[i]=a[i]*p[i-1]+p[i-2];
  q[i]=a[i]*q[i-1]+q[i-2]; 检查p[i],q[i]是否为解,如果是,则退出
}
```

3.9 二次剩余

```
/*a*x^2+b*x+c==0 (mod P) 求0..P-1的根 */
int pDiv2,P,a,b,c,Pb,d;
inline int calc(int x,int Time){
   if (!Time) return 1; int tmp=calc(x,Time/2);
   tmp=(long long)tmp*tmp%P;
   if (Time&1) tmp=(long long)tmp*x%P; return tmp;
inline int rev(int x){ if (!x) return 0; return calc(x,P-2);}
inline void Compute(){
   while (1) { b=rand()\%(P-2)+2; if (calc(b,pDiv2)+1==P)
        return; }
}
int main(){
   srand(time(0)^312314); int T;
   for (scanf("%d",&T);T;--T) {
       scanf("%d%d%d%d",&a,&b,&c,&P);
       if (P==2) {
          int cnt=0; for (int i=0; i<2; ++i) if
               ((a*i*i+b*i+c)%P==0) ++cnt;
          printf("%d",cnt);
          for (int i=0; i<2; ++i) if ((a*i*i+b*i+c)%P==0)
               printf(" %d",i);
          puts(""):
      }else {
```

```
int delta=(long long)b*rev(a)*rev(2)%P;
         a=(long long)c*rev(a)%P-sqr((long long)delta)%P;
         a\%=P; a+=P; a\%=P; a=P-a; a\%=P; pDiv2=P/2;
         if (calc(a,pDiv2)+1==P) puts("0");
         else {
            int t=0,h=pDiv2; while (!(h\%2)) ++t,h/=2;
            int root=calc(a,h/2);
            if (t>0) { Compute(); Pb=calc(b,h); }
            for (int i=1;i<=t;++i) {
                d=(long long)root*root*a%P;
                for (int j=1; j <=t-i; ++j) d=(long long) d*d%P;
                if (d+1==P) root=(long long)root*Pb%P;
                Pb=(long long)Pb*Pb%P;
            }
            root=(long long)a*root%P;
            int root1=P-root; root-=delta;
            root%=P; if (root<0) root+=P;</pre>
            root1-=delta; root1%=P; if (root1<0) root1+=P;</pre>
            if (root>root1) { t=root;root=root1;root1=t; }
            if (root==root1) printf("1 %d\n",root);
            else printf("2 %d %d\n",root,root1);
}}return 0; }
```

3.10 Schröder-Hipparchus Number

$$S(n) = \frac{1}{n}((6n-9)S(n-1) - (n-3)S(n-2))$$

3.11 Catalan Numbers

$$Cat(n) = \frac{2n!}{n! \times n! \times (n+1)}$$
$$Cat(n+1) = \frac{(2n+2) \times (2n+1)}{(n+2) \times (n+1)} \times Cat(n)$$

4 Computational Geometry

```
struct Point{
  double x, y;
  Point(double x=0, double y=0):x(x), y(y){}
};
typedef Point Vector;
// Vector + Vector = Vector / Point + Vector = Point
Vector operator + (Vector A, Vector B){
```

```
Point GetLineIntersection(Point P, Vector v, Point Q, Vector w){
 return Vector(A.x + B.x, A.y + B.y);}
// Point - Point = Vector
                                                                      Vector u = P-Q;
Vector operator - (Point A, Point B){
                                                                      double t = Cross(w,u)/Cross(v,w);
 return Vector(A.x - B.x, A.y - B.y);}
                                                                      return P+v*t;}
Vector operator * (Vector A, double p){
                                                                    // distance from P to line AB
 return Vector(A.x * p, A.y * p);}
                                                                    double DistanceToLine(Point P, Point A, Point B){
Vector operator / (Vector A, double p){
                                                                      Vector v1 = B-A, v2 = P-A;
                                                                      return fabs(Cross(v1,v2))/Length(v1);}
 return Vector(A.x / p, A.y / p);}
const double eps = 1e-10;
                                                                    // distance from P to segment AB
int dcmp(double x){
                                                                    double DistanceToSegment(Point P, Point A, Point B){
 if(fabs(x) < eps) return 0;</pre>
                                                                      if(A == B) return Length(P-A);
 return x < 0 ? -1 : 1; }
                                                                      Vector v1 = B-A, v2 = P-A, v3 = P-B;
bool operator < (const Point& a, const Point& b){</pre>
                                                                      if(dcmp(Dot(v1,v2))<0) return Length(v2);</pre>
                                                                      if(dcmp(Dot(v1,v3))>0) return Length(v3);
 return dcmp(a.x - b.x) < 0 \mid \mid (dcmp(a.x-b.x)==0 \&\& dcmp(a.y - b.x))
      b.y) < 0); }
                                                                      return fabs(Cross(v1,v2))/Length(v1);}
bool operator == (const Point& a, const Point &b){
                                                                    Point GetLineProjection(Point P, Point A, Point B){
 return dcmp(a.x-b.x) == 0 && dcmp(a.y-b.y) == 0;}
                                                                      Vector v = B-A;
double Dot(Vector A, Vector B){
                                                                      return A+v*(Dot(v,P-A) / Dot(v,v)); }
 return A.x*B.x + A.y*B.y; }
                                                                    // determine segment a1a2 and b1b2 normal intersection (only
double Length(Vector A){
                                                                        one intersection, not endpoint)
 return sqrt(Dot(A,A)); }
                                                                    // if allowing intersecting on endpoints:
                                                                    // 1) c1 = c2 = 0: on the same line, probably intersecting
// polar angle theta is the counterclockwise angle from the
                                                                    // 2) otherwise, one endpoint on the other segment (Use
    x-axis at which a point in the xy-plane lies
// (-pi, pi]
                                                                        OnSegment() method)
double angle(Vector v) {
                                                                    bool segmentProperIntersection(Point a1, Point a2, Point b1,
 return atan2(v.y, v.x); }
                                                                        Point b2){
// counterclockwise angle from A to B [0, pi]
                                                                      double c1 = Cross(a2-a1,b1-a1);
double Angle(Vector A, Vector B){
                                                                      double c2 = Cross(a2-a1,b2-a1);
 return acos(Dot(A,B)/Length(A)/Length(B)); }
                                                                      double c3 = Cross(b2-b1,a1-b1);
double Cross(Vector A, Vector B){
                                                                      double c4 = Cross(b2-b1,a2-b1);
 return A.x*B.y - A.y*B.x; }
                                                                      return dcmp(c1)*dcmp(c2)<0 && dcmp(c3)*dcmp(c4)<0;}
// counterclockwisely rotate A for rad
                                                                    // determine P on segment a1a2 (endpoint excluded)
Vector Rotate(Vector A, double rad){
                                                                    bool OnSegment(Point p, Point a1, Point a2) {
 return Vector(A.x*cos(rad)-A.y*sin(rad),
                                                                      return dcmp(Cross(a1-p,a2-p))==0 && dcmp(Dot(a1-p,a2-p))<0;}
      A.x*sin(rad)+A.y*cos(rad)); }
                                                                    // calulate the direct area for polygon (not necessarily
// unit normal vector for A (left rotate pi/2) A != 0
                                                                        convex)
Vector Normal(Vector A){
                                                                    double PolygonArea(Point* p, int n) {
 double L = Length(A);
                                                                      double area = 0;
 return Vector(-A.y/L, A.x/L);}
                                                                      for(int i=1;i<n-1;i++)
// P+tv,Q+tw should have only one intersection,iff Cross(v,w)!=0
                                                                        area += Cross(p[i]-p[0],p[i+1]-p[0]);
```

```
return area/2;}
                                                                    // return value: (-2, vertex) (-1, edges) (0, outside) (1,
// convex hull: n points in array p, ch array for output,
                                                                        inside)
    return the number of points on hull
                                                                    // determine if point on the left side of all edges (vertex
// no duplicate points in input; the order of input points is
                                                                        already counterclock ordered)
    not preserved
                                                                    int isPointInPolygon(Point p, Point* poly, int n){
// if want input points on edges of hull, change two <= to <
                                                                     int wn = 0;
                                                                      for(int i=0;i<n;i++){</pre>
int ConvexHull(Point* p, int n, Point* ch) {
  sort(p,p+n); int m = 0;
                                                                       if(p == poly[i]) return -2;
 for(int i=0;i<n;i++){
                                                                       if(OnSegment(p, poly[i], poly[(i+1)%n])) return -1;
   while (m>1 && dcmp(Cross(ch[m-1]-ch[m-2], p[i]-ch[m-2])) <= 0)
                                                                       int k = dcmp(Cross(poly[(i+1)%n]-poly[i], p-poly[i]));
                                                                       int d1 = dcmp(poly[i].y - p.y);
   ch[m++] = p[i];
                                                                       int d2 = dcmp(poly[(i+1)\%n].y - p.y);
 int k = m;
                                                                       if(k>0 && d1<=0 && d2>0) wn++;
 for(int i=n-2; i>=0; i--){
                                                                       if(k<0 && d2<=0 && d1>0) wn--;
   while (m>k \&\& dcmp(Cross(ch[m-1]-ch[m-2], p[i]-ch[m-2])) \le 0)
                                                                     if(wn != 0) return 1;
   ch[m++] = p[i];
                                                                     return 0;
 if(n>1) m--;
 return m;}
                                                                    struct Line{
// return the diameter of set of points (Rotating Calipers
                                                                      Point p; Vector v;
    Algorithm)
                                                                     Line(Point p, Vector v):p(p),v(v){}
// ch: already convex hull (no three points in a line) n: the
                                                                     Point point(double t) {return p + v*t;}
    number of points
                                                                     Line move(double d) {return Line(p + Normal(v)*d, v);}
double diameter(Point* ch, int n) {
                                                                    };
                                                                    struct Circle{
 if(n == 1) return 0;
 if(n == 2) return Length(ch[0] - ch[1]);
                                                                     Point c;
 ch[n] = ch[0];
                                                                     double r;
 double ans = 0;
                                                                      Circle(Point c, double r):c(c),r(r){}
 for(int u = 0, v = 1; u < n; u++) {
                                                                     Point point(double a) {return Point(c.x + cos(a)*r, c.y +
   for(;;) {
                                                                          sin(a)*r):
     double diff = Cross(ch[u+1]-ch[u], ch[v+1]-ch[v]);
                                                                    };
                                                                    // return number of intersection, sol has all intersection
     if(dcmp(diff) <= 0) {</pre>
                                                                    // intersection P = A + t(B-A), simplify to et^2+ft+g = 0
       ans = max(ans, Length(ch[u]-ch[v]));
      if(dcmp(diff) == 0)
                                                                    int getLineCircleIntersection(Line L, Circle C, double& t1,
                                                                        double& t2, vector<Point>& sol){
        ans = \max(ans, Length(ch[u]-ch[v+1]));
                                                                      double a = L.v.x, b = L.p.x - C.c.x, c = L.v.y, d = L.p.y -
       break:
     v = (v + 1) \% n;
                                                                          C.c.v;
   }}
                                                                     double e = a*a + c*c, f = 2*(a*b+c*d), g = b*b + d*d -
 return ans;}
                                                                          C.r*C.r;
// poly: polygon n: the number of points
                                                                     double delta = f*f - 4*e*g;
```

```
if(dcmp(delta) < 0) return 0;</pre>
                                                                       v[0] = Rotate(u, -ang); v[1] = Rotate(u, +ang);
 if(dcmp(delta) == 0){
                                                                       return 2:
   t1 = t2 = -f / (2*e);
                                                                     }}
   sol.push_back(L.point(t1));
                                                                    // return the number of tangents, -1 means inf
   return 1; }
                                                                    // a[i], b[i]: point of tangency with i-th tangent on A, B;
 t1 = (-f - sqrt(delta)) / (2*e);
                                                                        same when internally or externally tangent
                                                                    int getTangents(Circle A, Circle B, Point* a, Point* b) {
 sol.push_back(L.point(t1));
 t2 = (-f + sqrt(delta)) / (2*e);
                                                                      int cnt = 0:
 sol.push back(L.point(t2));
                                                                     if(A.r < B.r) \{ swap(A, B); swap(a, b); \}
 return 2;}
                                                                      double d2 = (A.c.x-B.c.x)*(A.c.x-B.c.x) +
// return the number of intersection
                                                                          (A.c.y-B.c.y)*(A.c.y-B.c.y);
// if two circle identical, then return -1
                                                                      double rdiff = A.r - B.r;
int getCircleCircleIntersection(Circle C1, Circle C2,
                                                                      double rsum = A.r + B.r;
    vector<Point>& sol){
                                                                      if(dcmp(d2 - rdiff*rdiff) < 0) // containing</pre>
 double d = Length(C1.c-C2.c);
                                                                       return 0:
 if(dcmp(d) == 0){
                                                                      double base = atan2(B.c.y-A.c.y, B.c.x-A.c.x);
   if(dcmp(C1.r-C2.r) == 0) return -1;
                                                                      if(dcmp(d2)==0 && dcmp(A.r-B.r)==0) // infinite tangents
   return 0;
                                                                       return -1;
                                                                      if(dcmp(d2-rdiff*rdiff) == 0){ // inscribe, one tangent
 if(dcmp(C1.r+C2.r-d) < 0) return 0;
                                                                       a[cnt] = A.point(base); b[cnt] = B.point(base);
 if(dcmp(fabs(C1.r-C2.r) - d) > 0) return 0;
                                                                       cnt++; return 1;
 double a = angle(C2.c-C1.c);
 double da = acos((C1.r*C1.r + d*d - C2.r*C2.r) / (2*C1.r*d));
                                                                      double ang = acos((A.r-B.r)/sqrt(d2)); // two external common
      // angle from C1C2 to C1P1
                                                                          tangents
                                                                      a[cnt] = A.point(base + ang);
 Point p1 = C1.point(a-da), p2 = C1.point(a+da);
 sol.push_back(p1);
                                                                      b[cnt] = B.point(base + ang); cnt++;
 if(p1 == p2) return 1;
                                                                      a[cnt] = A.point(base - ang);
 sol.push_back(p2);
                                                                      b[cnt] = B.point(base - ang); cnt++;
 return 2;}
                                                                      if(dcmp(d2-rsum*rsum) == 0){
// tangent lines from P to C
                                                                       a[cnt] = A.point(base);
// v[i]: i-th tangent lines, return the number of tangent lines
                                                                       b[cnt] = B.point(PI + base); cnt++;
int getTangents(Point p, Circle C, Vector* v){
                                                                      else if(dcmp(d2 - rsum*rsum) > 0){ // two internal common
 Vector u = C.c - p;
 double dist = Length(u);
                                                                          tangents
 if(dist < C.r) return 0;</pre>
                                                                       double ang = acos((A.r+B.r) / sqrt(d2));
 else if(dcmp(dist-C.r)==0){
                                                                       a[cnt] = A.point(base+ang);
   v[0] = Rotate(u,PI/2);
                                                                       b[cnt] = B.point(PI+base+ang); cnt++;
   return 1;
                                                                       a[cnt] = A.point(base-ang);
 } else {
                                                                       b[cnt] = B.point(PI+base-ang); cnt++;
                                                                     }
   double ang = asin(C.r / dist);
```

```
return cnt;}
                                                                    double a, b, c, B, C, sinB, cosB, sinC, cosC, S, h, theta;
                                                                    a = pb.len(); b = pa.len(); c = (pb-pa).len();
void CircleCenter(point p0 , point p1 , point p2 , point &cp ){
                                                                    cosB=dot(pb,pb-pa)/a/c; sinB=fabs(det(pb,pb-pa)/a/c);
    double a1=p1.x-p0.x , b1=p1.y-p0.y , c1=(sqr(a1)+sqr(b1)) /
                                                                    cosC=dot(pa, pb) / a / b; sinC=fabs(det(pa,pb)/a/b);
        2:
                                                                    B=atan2(sinB , cosB); C=atan2(sinC, cosC);
    double a2=p2.x-p0.x, b2=p2.y-p0.y, c2=(sqr(a2)+sqr(b2)) /
                                                                    if (a > r) { S = C/2*r*r; h = a*b*sinC/c;
                                                                     if (h < r \&\& B < PI/2) S = (acos(h/r)*r*r -
    double d = a1*b2 - a2*b1;
                                                                         h*sqrt(r*r-h*h));
    cp.x = p0.x + (c1*b2 - c2*b1) / d;
    cp.y = p0.y + (a1*c2 - a2*c1) / d;
                                                                    else if (b > r) { theta = PI - B - asin(sinB/r*a);
double Incenter(point A, point B, point C, point &cp ){
                                                                     S = .5*a*r*sin(theta) + (C-theta)/2*r*r; }
 double s , p , r , a , b , c ;
                                                                    else S = .5*sinC*a*b; return S; }// a, b, c, r fixed
 a = dis(B, C), b = dis(C, A), c = dis(A, B); p = (a + b + c)
                                                                  double area(const point &o) {
                                                                    double S = 0; point oa = a-o, ob = b-o, oc = c-o;
 s = sqrt (p * (p-a) * (p-b) * (p-c)); r = s / p;
                                                                    S += area2(oa, ob) * sign(det(oa, ob));
 cp.x = (a*A.x + b*B. x + c*C.x) / (a + b + c);
                                                                   S += area2(ob, oc) * sign(det(ob, oc));
 cp.y = (a*A.y + b*B. y + c*C.y) / (a + b + c);
                                                                   S += area2(oc, oa) * sign(det(oc, oa)); return abs(S);
 return r ;}
                                                                      //====多边形和圆相交的面积用有向面积,划分成一个三角形和圆的面积的交
void Orthocenter(point A, point B, point C, point &cp ){
 CircleCenter(A, B, C, cp );
 cp.x = A.x + B.x + C.x - 2 * cp.x ; cp.y = A.y + B.y + C.y - 2
                                                                  随机增量最小覆盖圆
      * cp.y ;}
                                                                  const double eps=1e-7;
                                                                  const int maxn=100000;
double twoCircleAreaUnion(point a, point b , double r1, double
    r2){
                                                                  class circle{
 if (r1+r2<=(a-b).dist()) return 0;</pre>
                                                                     point o;
                                                                     double r;
 if (r1+(a-b).dist()<=r2) return pi*r1*r1;</pre>
 if (r2+(a-b).dist()<=r1) return pi*r2*r2;</pre>
 double c1, c2, ans=0;
                                                                  point a[maxn];
 c1=(r1*r1-r2*r2+(a-b).dis())/(a-b).dist()/r1/2.0;
                                                                  int n;
 c2=(r2*r2-r1*r1+(a-b).dis())/(a-b).dist()/r2/2.0;
                                                                  circle ans;
                                                                  double area(point a, point b, point c){
 double s1,s2; s1=acos(c1); s2=acos(c2);
                                                                     return ((b.x-a.x)*(c.y-a.y)-(b.y-a.y)*(c.x-a.x));
 ans+=s1*r1*r1-r1*r1*sin(s1)*cos(s1);
 ans+=s2*r2*r2-r2*r2*sin(s2)*cos(s2);
                                                                  double dis(point a, point b){
 return ans;
                                                                     return (a.x-b.x)*(a.x-b.x) + (a.y-b.y)*(a.y-b.y);
}//===两园面积交 dist=是距离, dis是平方
                                                                  }
double area2(point pa, point pb) {
                                                                  void init(){
 if (pa.len() < pb.len()) swap(pa, pb); if (pb.len() < eps)</pre>
                                                                     int i,j,k;
                                                                     scanf("%d",&n);
      return 0;
```

```
rep(i,n) scanf("%lf%lf",&a[i].x,&a[i].y);
}
bool check(const point &a){
   return sqr(a.x-ans.o.x) + sqr(a.y-ans.o.y) <= ans.r + zero;</pre>
}
void Mincircle(){
   int i,j,k;
   ans.r=0; ans.x=0; ans.y=0;
   rep(i,n) if (!check(a[i])) {
       ans.o=a[i]; ans.r=0;
      rep(j,i) if (!check(a[j])) {
          CircleCenter(a[i],a[j],ans.o);
          ans.r=dis(ans.o,a[i]);
          rep(k,j) if (!check(a[k])) {
              CircleCenter(a[i],a[j],a[k],ans.o);
              ans.r=dis(ans.o,a[i]);
          }
      }
   printf("%.4lf\n",sqrt(ans.r));
半平面交 n^2
```

```
半平面交 n^2
const int maxn=200;
const double eps=1e-8;
const int infinite=10000;
struct point{
    double x,y;
    void input(){
        scanf("%lf%lf",&x,&y);
    }
} sol[maxn],tmp[maxn];
struct Tline{
    point a,b;
} line[maxn];
int n,m;
void rebuild(point a, point b){
    int i,t;
    double k1,k2;
```

```
sol[m]=sol[0]; t=0;
   foru(i,1,m){
       k1=area(a,b,sol[i]);
       k2=area(a,b,sol[i-1]);
       if (cmp(k1)*cmp(k2)<0){
          tmp[t].x=(sol[i].x*k2-sol[i-1].x*k1) / (k2-k1);
          tmp[t].y=(sol[i].y*k2-sol[i-1].y*k1) / (k2-k1);
       if (cmp(area(a,b,sol[i])) >=0){
          tmp[t]=sol[i];
          t++;
       }
   }
   m=t:
   rep(i,m) sol[i]=tmp[i];
void work(){
   int i,j,k;
   double ans;
   point o;
   sol[0].x = 0; sol[0].y = 0;
   sol[1].x = infinite; sol[1].y = 0;
   sol[2].x = infinite; sol[2].y = infinite;
   sol[3].x = 0; sol[3].y = infinite;
   m=4;
   rep(i,n) rebuild(line[i].a,line[i].b);
   // 保留直线line[i].a,line[i+1].b
   左边的点
       if (m>0) printf("1\n");
       else printf("0\n");
}
```

5 String Processing

5.1 KMP

```
#define MAX_N 100010
char T[MAX_N], P[MAX_N]; // T = text, P = pattern
```

```
int b[MAX N], n, m; // b = back table, n = length of T, m =
    length of P
void kmpPreprocess() { // call this before calling kmpSearch()
  int i = 0, j = -1; b[0] = -1; // starting values
 while (i < m) { // pre-process the pattern string P
   while (j \ge 0 \&\& P[i] != P[j]) j = b[j]; // if different,
        reset j using b
   i++; j++; // if same, advance both pointers
   b[i] = j; // observe i = 8, 9, 10, 11, 12 with j = 0, 1, 2,
        3, 4
} }
            // in the example of P = "SEVENTY SEVEN" above
void kmpSearch() { // this is similar as kmpPreprocess(), but
    on string T
 int i = 0, j = 0; // starting values
 while (i < n) { // search through string T
   while (j \ge 0 \&\& T[i] != P[j]) j = b[j]; // if different,
        reset j using b
   i++; j++; // if same, advance both pointers
   if (j == m) \{ // \text{ a match found when } j == m \}
     printf("P is found at index %d in T\n", i - j);
     j = b[j]; // prepare j for the next possible match
} } }
```

5.2 Suffix Array

```
// for computing longest common prefix
int Phi[MAX N];
int PLCP[MAX_N];
int LCP[MAX_N]; // LCP[i] stores the LCP between previous
    suffix T+SA[i-1]
                                        // and current suffix
                                            T+SA[i]
bool cmp(int a, int b) { return strcmp(T + a, T + b) < 0; } //</pre>
    compare
void constructSA_slow() {
                                  // cannot go beyond 1000
    characters
 for (int i = 0; i < n; i++) SA[i] = i; // initial SA: {0, 1,
      2, \ldots, n-1
 sort(SA, SA + n, cmp); // sort: O(n log n) * compare: O(n) =
      O(n^2 \log n)
}
                                                           11
void countingSort(int k) {
    O(n)
 int i, sum, maxi = max(300, n); // up to 255 ASCII chars or
     length of n
                                            // clear frequency
 memset(c, 0, sizeof c);
      table
 for (i = 0; i < n; i++) // count the frequency of each
      integer rank
   c[i + k < n ? RA[i + k] : 0]++;
 for (i = sum = 0; i < maxi; i++) {
   int t = c[i]; c[i] = sum; sum += t;
 }
 for (i = 0; i < n; i++)
                              // shuffle the suffix array if
      necessary
   tempSA[c[SA[i]+k < n ? RA[SA[i]+k] : 0]++] = SA[i];
 for (i = 0; i < n; i++)
                                     // update the suffix
      array SA
   SA[i] = tempSA[i];
void constructSA() {
                         // this version can go up to 100000
    characters
```

```
int i, k, r;
 for (i = 0; i < n; i++) RA[i] = T[i];
                                              // initial
      rankings
 for (i = 0; i < n; i++) SA[i] = i; // initial SA: {0, 1, 2, }
 for (k = 1; k < n; k <<= 1) { // repeat sorting process log n</pre>
   countingSort(k); // actually radix sort: sort based on the
        second item
   countingSort(0);
                         // then (stable) sort based on the
       first item
   tempRA[SA[0]] = r = 0;
                               // re-ranking; start from rank
       r = 0
   for (i = 1; i < n; i++)
                                        // compare adjacent
        suffixes
     tempRA[SA[i]] = // if same pair => same rank r; otherwise,
     (RA[SA[i]] == RA[SA[i-1]] &\& RA[SA[i]+k] == RA[SA[i-1]+k])
         ? r : ++r;
   for (i = 0; i < n; i++)
                                         // update the rank
       array RA
     RA[i] = tempRA[i];
                                         // nice optimization
   if (RA[SA[n-1]] == n-1) break;
        trick
} }
void computeLCP_slow() {
 LCP[0] = 0:
                                            // default value
 for (int i = 1; i < n; i++) { // compute LCP by definition</pre>
   int L = 0:
                                        // always reset L to 0
   while (T[SA[i] + L] == T[SA[i-1] + L]) L++; // same L-th
        char, L++
   LCP[i] = L;
ነ ነ
void computeLCP() {
 int i, L;
 Phi[SA[0]] = -1;
                    // default value
 for (i = 1; i < n; i++) // compute Phi in O(n)
   Phi[SA[i]] = SA[i-1]; // remember which suffix is behind
```

```
this suffix
 for (i = L = 0; i < n; i++) { // compute Permuted LCP in O(n)
   if (Phi[i] == -1) { PLCP[i] = 0; continue; } // special case
   while (T[i + L] == T[Phi[i] + L]) L++; // L increased max n
       times
   PLCP[i] = L;
   L = max(L-1, 0):
                             // L decreased max n times
 }
 for (i = 0; i < n; i++) // compute LCP in O(n)
   LCP[i] = PLCP[SA[i]]; // put the permuted LCP to the correct
       position
ii stringMatching() {    // string matching in O(m log n)
 int lo = 0, hi = n-1, mid = lo; // valid matching = [0..n-1]
 while (lo < hi) {
                                // find lower bound
   mid = (lo + hi) / 2;
                              // this is round down
   int res = strncmp(T + SA[mid], P, m); // try to find P in
       suffix 'mid'
   if (res >= 0) hi = mid; // prune upper half (notice the
       >= sign)
               lo = mid + 1; // prune lower half including mid
   else
                        // observe '=' in "res >= 0" above
 if (strncmp(T + SA[lo], P, m) != 0) return ii(-1, -1); // if
      not found
 ii ans; ans.first = lo;
 lo = 0; hi = n - 1; mid = lo;
  while (lo < hi) { // if lower bound is found, find upper
      bound
   mid = (lo + hi) / 2;
   int res = strncmp(T + SA[mid], P, m);
   if (res > 0) hi = mid;
                              // prune upper half
   else
              lo = mid + 1;  // prune lower half including
        // (notice the selected branch when res == 0)
 if (strncmp(T + SA[hi], P, m) != 0) hi--; // special case
 ans.second = hi;
 return ans:
} // return lower/upperbound as first/second item of the pair,
    respectively
```

```
ii LRS() {
              // returns a pair (the LRS length and its index)
 int i, idx = 0, maxLCP = -1;
 for (i = 1; i < n; i++) // O(n), start from i = 1
   if (LCP[i] > maxLCP)
     maxLCP = LCP[i], idx = i;
 return ii(maxLCP, idx);
}
int owner(int idx) { return (idx < n-m-1) ? 1 : 2; }</pre>
ii LCS() {
              // returns a pair (the LCS length and its index)
 int i, idx = 0, maxLCP = -1;
 for (i = 1; i < n; i++)
                              // O(n), start from i = 1
   if (owner(SA[i]) != owner(SA[i-1]) && LCP[i] > maxLCP)
     maxLCP = LCP[i], idx = i;
 return ii(maxLCP, idx);
```

6 Sundry

6.1 Day of some Date

6.2 Java

```
import java.io.*;
import java.util.*;
import java.math.*;
import static java.lang.Math.*;
public class main{
   public static StringTokenizer st;
   public static DataInputStream in;
   public static PrintStream out;
   private static int nextInt() throws Exception{
       for (;st.countTokens()==0;) st=new
           StringTokenizer(in.readLine());
       return Integer.valueOf(st.nextToken());
   }
   public static BigInteger getsqrt(BigInteger n){
       if (n.compareTo(BigInteger.ZERO)<=0) return n;</pre>
       BigInteger x,xx,txx;
       xx=x=BigInteger.ZERO;
       for (int t=n.bitLength()/2;t>=0;t--){
          txx=xx.add(x.shiftLeft(t+1)).add(BigInteger.ONE.shiftLeft(t+t));
          if (txx.compareTo(n)<=0){</pre>
              x=x.add(BigInteger.ONE.shiftLeft(t));
             xx=txx;
          }
       }
       return x;
   public static void main(String args[]) throws Exception{
       in=new DataInputStream(System.in);
       out=new PrintStream(new
           BufferedOutputStream(System.out));
       st=new StringTokenizer(in.readLine());
       out.close();
   }
```